Batch normalization

Issues with training Deep Neural Networks

• There are 2 major issues 1) Internal Covariate shift, 2) Vanishing Gradient

Internal Covariate shift

- The concept of covariate shift pertains to the change that occurs in the distribution of the input to a learning system. In deep networks, this distribution can be influenced by parameters across all input layers. Consequently, even minor changes in the network can have a significant impact on its output. This effect gets magnified as the signal propagates through the network, which can result in a shift in the distribution of the inputs to internal layers. This phenomenon is known as internal covariate shift.
- When inputs are whitened (i.e., have zero mean and unit variance) and are uncorrelated, they tend to converge faster during training. However, internal covariate shift can have the opposite effect, as it introduces changes to the distribution of inputs that can slow down convergence. Therefore, to mitigate this effect, techniques like batch normalization have been developed to normalize the inputs to each layer in the network based on statistics of the current mini-batch.

Vanishing Gradient

- Saturating non-linearities such as sigmoid or tanh are not suitable for deep networks, as the signal tends to get trapped in the saturation region as the network grows deeper. This makes it difficult for the network to learn and can result in slow convergence during training. To overcome this problem we can use the following.
- Non-linearities like ReLU which do not saturate.
- Smaller learning rates

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Careful initializations

What is Normalization?

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Normalization in deep learning refers to the process of transforming the input or output of a layer in a neural network to improve its performance during training. The most common type of normalization used in deep learning is batch normalization, which normalizes the activations of a layer for each mini-batch during training.

What is batch normalization?

• Batch normalization is a technique in deep learning that helps to standardize and normalize the input to each layer of a neural network by adjusting and scaling the activations. The idea behind batch normalization is to normalize the inputs to a layer to have zero mean and unit variance across each mini-batch of the training data.

Steps involved in batch normalization

- During training, for each mini-batch of data, compute the mean and variance of the activations of each layer. This can be done using the following formulas:
- Mean: $\mu_B = \frac{1}{m} \sum_{i=1}^m x_i$
- Variance: $\sigma_B^2 = \frac{1}{m} \sum_{i=1}^m (x_i \mu_B)^2$
- Here, m is the size of the mini-batch, and x_i is the activation of the i-th neuron in the layer.
- 2) Normalize the activations of each layer in the mini-batch using the following formula:
- $\hat{x_i} = \frac{x_i \mu_B}{\sqrt{\sigma_B^2 + \epsilon}}$ Here, ϵ is a small constant added for numerical stability.
- 3) Scale and shift the normalized activations using the learned parameters γ and β , respectively:
- $y_i = \gamma \hat{x_i} + \beta$
- The parameters γ and β are learned during training using backpropagation.

4) During inference, the running mean and variance of each layer are used for normalization instead of the mini-batch statistics. These running statistics are updated using a moving average of the mini-batch statistics during training.

The benefits of batch normalization include:

- Improved training performance: Batch normalization reduces the internal covariate shift, which is the change in the distribution of the activations of each layer due to changes in the distribution of the inputs. This allows the network to converge faster and with more stable gradients.
- Regularization: Batch normalization acts as a form of regularization by adding noise to the activations of each layer, which can help prevent overfitting.

•

Increased robustness: Batch normalization makes the network more robust to changes in the input distribution, which can help improve its generalization performance.

Code example for batch normalization

```
import tensorflow as tf

# Define a fully connected layer
fc_layer = tf.keras.layers.Dense(units=128, activation='relu')

# Add batch normalization to the layer
bn_layer = tf.keras.layers.BatchNormalization()

# Define the model with the layer and batch normalization
model = tf.keras.models.Sequential([fc_layer, bn_layer])

# Compile the model
model.compile(optimizer='adam', loss='categorical_crossentropy')

# Train the model
model.fit(x_train, y_train, batch_size=32, epochs=10)
```

• In the above code, the tf. keras.layers. Batch Normalization() layer is added after the fully connected layer to normalize the output before passing it to the activation function. The model. fit() function is then used to train the model using batch normalization.

Practical discussion of Callback functions:

A callback is a powerful tool to customize the behavior of a Keras model during training, evaluation, or inference. Tensor Board to visualize training progress and results with Tensor Board, or tf. keras. callbacks. Model Checkpoint to periodically save your model during training. This callback reduces the learning rate when a metric you've mentioned during training eg. accuracy or loss has stopped improving. Models often benefit from reducing the learning rate. There are many callback functions,

- · Early Stopping callback
- Model checkpointing callback
- · Tensorboard callback Functions

We will also see how to save a model & load as well.

```
In [1]: # Importing Libraries
    import tensorflow as tf
    import matplotlib.pyplot as plt
    import numpy as np
    import pandas as pd
    import seaborn as sns
    import os
In [2]: # Checking version of Tensorflow and Keras
    print(f"Tensorflow Version {tf.__version__}")
    print(f"Keras Version {tf.keras.__version__}")
```

Tensorflow Version 2.10.0 Keras Version 2.10.0

GPU / CPU Check

```
In [3]: tf.config.list_physical_devices("GPU")
Out[3]: []
In [4]: tf.config.list_physical_devices("CPU")
Out[4]: [PhysicalDevice(name='/physical_device:CPU:0', device_type='CPU')]
```

```
In [5]: check_list = ['GPU','CPU']

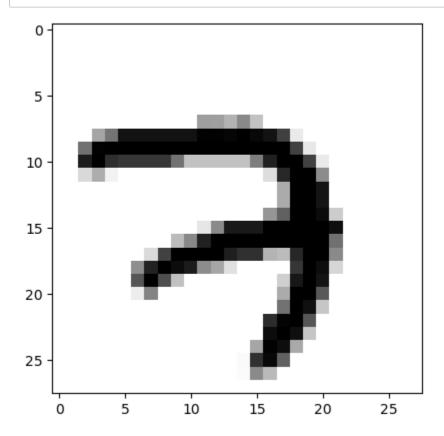
for device in check_list:
    out = tf.config.list_physical_devices(device)
    if len(out) > 0:
        print(f"{device} is available!")
        print(f"Details >> {out}")
    else:
        print(f"{device} isn't available!")

GPU isn't available!
    CPU is available!
    Details >> [PhysicalDevice(name='/physical_device:CPU:0', device_type='CPU')]
```

Creating a simple classifier using keras on MNIST data

```
In [6]: |mnist = tf.keras.datasets.mnist
          (X train full, y train full), (X test, y test) = mnist.load data()
 In [7]: print(f"data type of X_train_full: {X_train_full.dtype},\n shape of X_train_full: {X_train_full.dtype}
          data type of X train full: uint8,
           shape of X train full: (60000, 28, 28)
 In [8]: |X_test.shape
 Out[8]: (10000, 28, 28)
In [9]: len(X_test[1][0])
Out[9]: 28
In [10]: |# create a validation data set from the full training data
         # Scale the data between 0 to 1 by dividing it by 255. as its an unsigned data between 0
         X_valid, X_train = X_train_full[:5000] / 255., X_train_full[5000:] / 255.
         y_valid, y_train = y_train_full[:5000], y_train_full[5000:]
         # scale the test set as well
         X_{\text{test}} = X_{\text{test}} / 255.
In [11]: |len(X_train_full[5000:] )
Out[11]: 55000
```

```
In [12]: # Lets view some data
plt.imshow(X_train[0], cmap="binary")
plt.show()
```



```
In [13]: |plt.figure(figsize=(15,15))
            sns.heatmap(X train[0], annot=True, cmap="binary")
Out[13]: <Axes: >
                                    0
                                       0
                                           0
                                              0
                                                        0
                                                           0
                                                               0
                                                                         0
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                                          0
                                              0
                                                 0 0.38 0.38 0.3 0.46 0.24 0 0
                          0.35 0.54 0.92 0.92 0.92 0.92 0.92 0.92 0.98 0.98 0.97 1 0.96 0.92 0.75 <mark>0.082</mark> 0
                                                                                  0
                      0.55 0.98 1 1 1
                                             1 1 1 1 1 1 1 1 0.74 0.09 0
             o - 0
                   0 0.89 1 0.82 0.78 0.78 0.78 0.78 0.55 0.24 0.24 0.24 0.24 0.24 0.5 0.87 1 1 0.740.082 0
                                                                                                                        - 0.6
                   0 0.15 0.320.051 0
                                                          0 0 0 0.13 0.84 1
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                                             0 0 0.0980.46 0.89 0.89 0.89 0.99 1 1 1
                                                                                  1 0.94
                                       0 0 0.27 0.47 0.86 1 1 1 1 1 1 1
                                                                                     0.56
                                                                                                                        - 0.4
                                   0 0.15 0.73 0.99 1 1 1 0.87 0.81 0.81 0.29 0.27 0.84 1 1 0.46
                                   0.44 0.86 1 0.95 0.89 0.45 0.35 0.12 0 0 0 0 0.78 1 0.95 0.16 0
                                 0 0.66 1 0.69 0.24
                                                                     0 0.19 0.91 1 0.92
                                                           0
                                 0 0.0710.49
                                                        0
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                                                                    0 0.55
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                                                                                                                        - 0.2
                                                                 0 0.82 0.98 1 0.66
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                                                                 0 0.95 1 0.94 0.22 0
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                                                                 0.35 0.98 0.95 0
                                                           0 0.02 0.81 0.96 0.62
                                                           0 0.0160.46 0.27 0
                                                               0
                                                                        0
                                                                                                                        - 0.0
                                                    11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27
                                                 10
          LAYERS = [tf.keras.layers.Flatten(input_shape=[28, 28], name="inputLayer"),
In [14]:
                        tf.keras.layers.Dense(300, activation="relu", name="hiddenLayer1"),
                        tf.keras.layers.Dense(100, activation="relu", name="hiddenLayer2"),
                        tf.keras.layers.Dense(10, activation="softmax", name="outputLayer")]
```

model clf = tf.keras.models.Sequential(LAYERS)

```
In [15]: |model_clf.layers
Out[15]: [<keras.layers.reshaping.flatten.Flatten at 0x19e30cc3460>,
          <keras.layers.core.dense.Dense at 0x19e30cc2bf0>,
          <keras.layers.core.dense.Dense at 0x19e30cc2c80>,
          <keras.layers.core.dense.Dense at 0x19e30cc2cb0>]
In [16]: | model_clf.summary()
         Model: "sequential"
          Layer (type)
                                     Output Shape
                                                              Param #
         ______
          inputLayer (Flatten)
                                     (None, 784)
                                                              0
         hiddenLayer1 (Dense)
                                     (None, 300)
                                                              235500
         hiddenLayer2 (Dense)
                                     (None, 100)
                                                              30100
          outputLayer (Dense)
                                     (None, 10)
                                                              1010
         Total params: 266,610
         Trainable params: 266,610
         Non-trainable params: 0
In [17]: |# first Layer * second Layer + bias
         784*300 + 300, 300*100+100, 100*10+10
Out[17]: (235500, 30100, 1010)
In [18]: # Total parameters to be trained -
         sum((235500, 30100, 1010))
Out[18]: 266610
In [19]: hidden1 = model clf.layers[1]
         hidden1.name
Out[19]: 'hiddenLayer1'
In [20]: |model_clf.get_layer(hidden1.name) is hidden1
Out[20]: True
In [21]: len(hidden1.get_weights()[1])
Out[21]: 300
```

```
In [22]: | hidden1.get_weights()
Out[22]: [array([[-0.00863542, 0.07263291, -0.03879336, ..., 0.00046017,
          0.04086754, -0.00439219],
         [ 0.00946854, -0.05513434, -0.01372449, ..., 0.01021195,
         -0.04177602, 0.05911638],
         [-0.02636152, -0.06728062, -0.04932404, ..., -0.017939 ,
          0.01761802, -0.04399509],
         [ 0.01695059, -0.00667475,
                       0.06896693, ..., -0.02042392,
         -0.02046927, 0.01085705],
         [-0.05604234, -0.04010153, 0.00630041, ..., -0.00471536,
         -0.06079594, -0.07128973],
         [-0.02956304, 0.06041798, -0.05449025, ..., -0.06903378,
          0.0262394 , -0.02772664]], dtype=float32),
     0., 0., 0., 0., 0., 0., 0., 0., 0., 0.], dtype=float32)]
In [23]: |weights, biases = hidden1.get_weights()
In [24]: |print("shape\n",weights.shape, "\n")
    weights
     shape
     (784, 300)
Out[24]: array([[-0.00863542, 0.07263291, -0.03879336, ..., 0.00046017,
         0.04086754, -0.00439219],
        [0.00946854, -0.05513434, -0.01372449, ..., 0.01021195,
         -0.04177602, 0.05911638],
        [-0.02636152, -0.06728062, -0.04932404, ..., -0.017939]
         0.01761802, -0.04399509],
        [0.01695059, -0.00667475, 0.06896693, ..., -0.02042392,
         -0.02046927, 0.01085705],
        [-0.05604234, -0.04010153, 0.00630041, ..., -0.00471536,
         -0.06079594, -0.07128973],
        [-0.02956304, 0.06041798, -0.05449025, ..., -0.06903378,
         0.0262394 , -0.02772664]], dtype=float32)
```

Tensorboard callback Functions

```
In [27]: # Logging
import time

def get_log_path(log_dir="logs/fit"):
    fileName = time.strftime("log_%Y_%m_%d_%H_%M_%S")
    logs_path = os.path.join(log_dir, fileName)
    print(f"Saving logs at {logs_path}")
    return logs_path

log_dir = get_log_path()
    tb_cb = tf.keras.callbacks.TensorBoard(log_dir=log_dir)
```

Saving logs at logs/fit\log_2023_07_26_00_44_20

Early Stopping callback

Model checkpointing callback

```
In [29]: CKPT_path = "Model_ckpt.h5"
    checkpointing_cb = tf.keras.callbacks.ModelCheckpoint(CKPT_path, save_best_only=True)
```

```
Epoch 1/30
476 - val loss: 0.3059 - val accuracy: 0.9170
Epoch 2/30
172 - val_loss: 0.2423 - val_accuracy: 0.9336
321 - val loss: 0.2069 - val accuracy: 0.9420
Epoch 4/30
412 - val loss: 0.1821 - val accuracy: 0.9506
Epoch 5/30
9499 - val loss: 0.1622 - val accuracy: 0.9564
Epoch 6/30
9545 - val_loss: 0.1480 - val_accuracy: 0.9598
Epoch 7/30
9602 - val_loss: 0.1381 - val_accuracy: 0.9626
Epoch 8/30
9631 - val loss: 0.1270 - val accuracy: 0.9644
Epoch 9/30
667 - val_loss: 0.1200 - val_accuracy: 0.9672
Epoch 10/30
9699 - val_loss: 0.1096 - val_accuracy: 0.9714
Epoch 11/30
720 - val_loss: 0.1061 - val_accuracy: 0.9718
Epoch 12/30
746 - val loss: 0.1002 - val accuracy: 0.9704
Epoch 13/30
763 - val_loss: 0.0960 - val_accuracy: 0.9742
Epoch 14/30
783 - val_loss: 0.0928 - val_accuracy: 0.9732
Epoch 15/30
799 - val loss: 0.0907 - val accuracy: 0.9738
Epoch 16/30
820 - val loss: 0.0865 - val accuracy: 0.9754
Epoch 17/30
828 - val_loss: 0.0818 - val_accuracy: 0.9760
Epoch 18/30
841 - val loss: 0.0797 - val accuracy: 0.9774
Epoch 19/30
850 - val_loss: 0.0782 - val_accuracy: 0.9778
Epoch 20/30
```

```
9865 - val_loss: 0.0761 - val_accuracy: 0.9776
Epoch 21/30
874 - val loss: 0.0754 - val accuracy: 0.9764
Epoch 22/30
883 - val loss: 0.0746 - val accuracy: 0.9782
Epoch 23/30
889 - val loss: 0.0727 - val accuracy: 0.9790
Epoch 24/30
899 - val loss: 0.0730 - val accuracy: 0.9784
Epoch 25/30
910 - val loss: 0.0728 - val accuracy: 0.9774
Epoch 26/30
913 - val loss: 0.0709 - val accuracy: 0.9798
Epoch 27/30
9920 - val loss: 0.0702 - val accuracy: 0.9786
Epoch 28/30
928 - val loss: 0.0688 - val accuracy: 0.9786
Epoch 29/30
933 - val loss: 0.0675 - val accuracy: 0.9794
Epoch 30/30
940 - val loss: 0.0689 - val accuracy: 0.9806
```

```
939 - val loss: 0.0670 - val accuracy: 0.9794
Epoch 2/30
944 - val loss: 0.0673 - val accuracy: 0.9794
Epoch 3/30
947 - val loss: 0.0669 - val accuracy: 0.9804
Epoch 4/30
1719/1719 [=================== ] - 6s 3ms/step - loss: 0.0233 - accuracy: 0.9
952 - val loss: 0.0694 - val accuracy: 0.9798
Epoch 5/30
960 - val loss: 0.0681 - val accuracy: 0.9798
Epoch 6/30
962 - val loss: 0.0675 - val accuracy: 0.9808
Epoch 7/30
967 - val loss: 0.0664 - val accuracy: 0.9802
9972 - val_loss: 0.0662 - val_accuracy: 0.9802
Epoch 9/30
9972 - val_loss: 0.0667 - val_accuracy: 0.9798
Epoch 10/30
9973 - val_loss: 0.0698 - val_accuracy: 0.9798
Epoch 11/30
9977 - val_loss: 0.0660 - val_accuracy: 0.9800
Epoch 12/30
9981 - val_loss: 0.0661 - val_accuracy: 0.9806
Epoch 13/30
9982 - val loss: 0.0676 - val accuracy: 0.9804
9983 - val_loss: 0.0666 - val_accuracy: 0.9810
Epoch 15/30
9985 - val_loss: 0.0660 - val_accuracy: 0.9812
Epoch 16/30
9987 - val_loss: 0.0666 - val_accuracy: 0.9810
```

Saving the Model

```
import time
In [32]:
         import os
         def save_model_path(MODEL_dir = "TRAINED_MODEL"):
           os.makedirs(MODEL dir, exist ok= True)
           fileName = time.strftime("Model_%Y_%m_%d_%H_%M_%S_.h5")
           model path = os.path.join(MODEL dir, fileName)
           print(f"Model {fileName} will be saved at {model_path}")
           return model_path
In [33]: |UNIQUE_PATH = save_model_path()
         UNIQUE_PATH
         Model Model_2023_07_26_00_53_52_.h5 will be saved at TRAINED_MODEL\Model_2023_07_26_00_
         53_52_.h5
Out[33]: 'TRAINED MODEL\\Model 2023 07 26 00 53 52 .h5'
In [34]: |tf.keras.models.save_model(model_clf, UNIQUE_PATH)
In [35]: |history.params
Out[35]: {'verbose': 1, 'epochs': 30, 'steps': 1719}
In [36]: # history.history
```

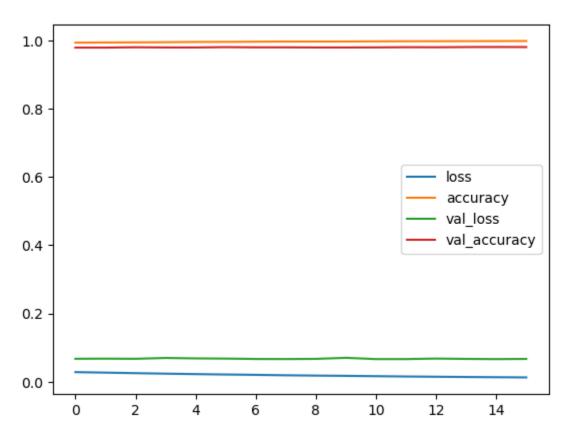
In [37]: pd.DataFrame(history.history)

Out[37]:

| | loss | accuracy | val_loss | val_accuracy |
|----|----------|----------|----------|--------------|
| 0 | 0.027838 | 0.993945 | 0.066974 | 0.9794 |
| 1 | 0.026399 | 0.994364 | 0.067307 | 0.9794 |
| 2 | 0.024844 | 0.994709 | 0.066889 | 0.9804 |
| 3 | 0.023314 | 0.995218 | 0.069436 | 0.9798 |
| 4 | 0.022058 | 0.995982 | 0.068107 | 0.9798 |
| 5 | 0.020838 | 0.996182 | 0.067498 | 0.9808 |
| 6 | 0.019833 | 0.996655 | 0.066364 | 0.9802 |
| 7 | 0.018600 | 0.997200 | 0.066153 | 0.9802 |
| 8 | 0.017650 | 0.997182 | 0.066678 | 0.9798 |
| 9 | 0.016868 | 0.997273 | 0.069837 | 0.9798 |
| 10 | 0.015999 | 0.997709 | 0.066010 | 0.9800 |
| 11 | 0.015030 | 0.998073 | 0.066082 | 0.9806 |
| 12 | 0.014267 | 0.998218 | 0.067568 | 0.9804 |
| 13 | 0.013561 | 0.998345 | 0.066585 | 0.9810 |
| 14 | 0.012970 | 0.998509 | 0.066026 | 0.9812 |
| 15 | 0.012334 | 0.998727 | 0.066566 | 0.9810 |
| | | | | |

In [38]: pd.DataFrame(history.history).plot()

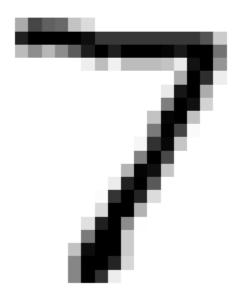
Out[38]: <Axes: >



```
In [39]: |model_clf.evaluate(X_test, y_test)
        Out[39]: [0.06929262727499008, 0.9776999950408936]
In [40]: |x_new = X_test[:3]
        # x_new
In [41]: |actual = y_test[:3]
        actual
Out[41]: array([7, 2, 1], dtype=uint8)
In [42]: |y_prob = model_clf.predict(x_new)
        y_prob.round(3)
        1/1 [======= ] - 0s 302ms/step
Out[42]: array([[0.
                    , 0.
                          , 0. , 0. , 0. , 0. , 1.
               0.
                    ],
                    , 0.
               [0.
                          , 0.999, 0.001, 0. , 0. , 0.
                                                          , 0.
                                                                , 0.
               0.
                    , 0.998, 0. , 0.
                                     , 0. , 0. , 0. , 0.001, 0.001,
               [0.
               0.
                    ]], dtype=float32)
In [43]: y_prob
Out[43]: array([[1.5794069e-06, 7.6853473e-07, 1.0801427e-04, 1.3993130e-04,
                5.5980118e-09, 2.3529131e-07, 2.5731752e-12, 9.9971408e-01,
               9.0249375e-07, 3.4513163e-05],
               [2.5457732e-06, 1.9585187e-04, 9.9901319e-01, 7.7849202e-04,
               1.9284004e-12, 2.7663469e-07, 1.9941704e-06, 1.1564657e-09,
               7.6111187e-06, 3.1541395e-13],
               [2.6645846e-06, 9.9758554e-01, 6.5624081e-05, 3.2423293e-05,
               2.2758909e-04, 8.4465260e-05, 8.3897270e-05, 8.2147971e-04,
               1.0715602e-03, 2.4860985e-05]], dtype=float32)
In [44]: |y_pred = np.argmax(y_prob, axis = -1)
In [45]: |y_pred
Out[45]: array([7, 2, 1], dtype=int64)
In [46]: |actual
Out[46]: array([7, 2, 1], dtype=uint8)
```

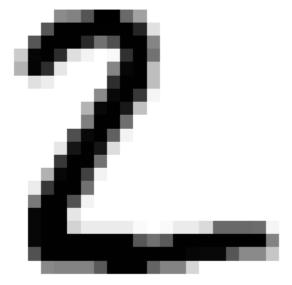
```
In [47]: # plot
for data, pred, actual_data in zip(x_new, y_pred, actual):
    plt.imshow(data, cmap="binary")
    plt.title(f"Predicted {pred} and Actual {actual_data}")
    plt.axis("off")
    plt.show()
    print("##############")
```

Predicted 7 and Actual 7



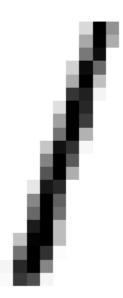
#############################

Predicted 2 and Actual 2



#############################

Predicted 1 and Actual 1



#############################

| In []: | |
|---------|--|
|---------|--|

Assignment Questions

Q1. Explain the concept of batch normalization in the context of Artificial Neural Networks.

Batch normalization is a technique used in Artificial Neural Networks to normalize the inputs of each layer during training. It aims to stabilize and speed up the training process by reducing internal covariate shift. Internal covariate shift refers to the change in the distribution of each layer's inputs during training, which can slow down learning and require more careful tuning of hyperparameters.

Batch normalization addresses this issue by normalizing the inputs of each layer to have zero mean and unit variance. It does this by computing the mean and variance of the inputs within a mini-batch (a small subset of the training data) and then applying a normalization transformation. Additionally, batch normalization introduces learnable parameters, scale, and shift, which allow the network to learn the optimal mean and variance for each layer. These parameters give the model more flexibility to adapt to the data distribution.

Q2. Describe the benefits of using batch normalization during training.

Using batch normalization during training offers several benefits:

- Improved training stability: Batch normalization helps to mitigate the vanishing and exploding gradient problems, making it easier for deep neural networks to converge during training.
- Faster convergence: By reducing internal covariate shift, batch normalization accelerates the training process, leading to faster convergence and fewer training iterations required.
- Reduced sensitivity to initialization: Batch normalization makes neural networks less sensitive to the choice of weight initialization, allowing for a wider range of initialization strategies.
- Regularization effect: Batch normalization acts as a form of regularization, reducing the need for other regularization techniques like dropout.
- Allows for larger learning rates: The improved stability provided by batch normalization allows for the use of larger learning rates, which can speed up training further.

Q3. Discuss the working principle of batch normalization, including the normalization step and the learnable parameters.

The working principle of batch normalization involves two main steps: normalization and learnable parameters.

Normalization Step: For each mini-batch of input data during training, batch normalization computes the mean and variance of the data within that mini-batch. It then normalizes the data by subtracting the mean and dividing by the standard deviation, resulting in inputs with zero mean and unit variance:

```
x normalized = (x - mean) / sqrt(variance + epsilon)
```

where x is the input data, mean and variance are the batch-wise statistics, and epsilon is a small constant added to avoid division by zero.

Learnable Parameters: Batch normalization introduces two learnable parameters for each layer: scale (gamma) and shift (beta). These parameters are applied after normalization and allow the model to learn the optimal scaling and shifting of the normalized inputs. The transformed output is given by:

```
y = gamma * x normalized + beta
```

Impementation

```
In [1]: # Importing Libraries
   import tensorflow as tf
   import matplotlib.pyplot as plt
   import numpy as np
   import pandas as pd
   import seaborn as sns
   import os
```

Creating a simple classifier using keras on MNIST data

```
In [2]: mnist = tf.keras.datasets.mnist
    (X_train_full, y_train_full), (X_test, y_test) = mnist.load_data()

In [3]: print(f"data type of X_train_full: {X_train_full.dtype},\n shape of X_train_full: {X_tra
```

In [6]: X_train_full[0]

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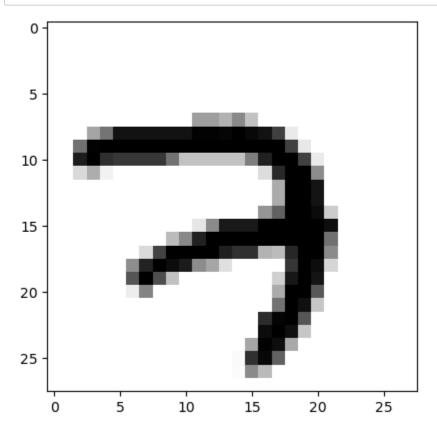
```
In [7]: # create a validation data set from the full training data
# Scale the data between 0 to 1 by dividing it by 255. as its an unsigned data between 0
X_valid, X_train = X_train_full[:5000] / 255., X_train_full[5000:] / 255.
y_valid, y_train = y_train_full[:5000], y_train_full[5000:]

# scale the test set as well
X_test = X_test / 255.
```

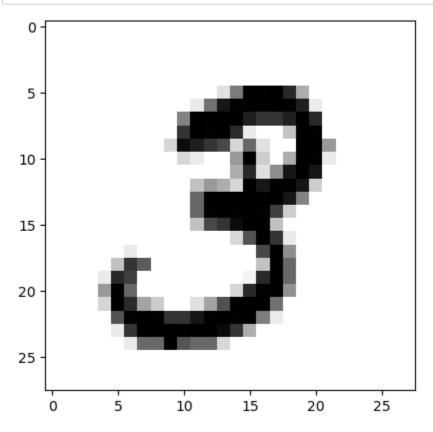
```
In [8]: len(X_train_full[5000:] )
```

Out[8]: 55000

```
In [9]: # Lets view some data
plt.imshow(X_train[0], cmap="binary")
plt.show()
```



In [10]: # Lets view some data
plt.imshow(X_train[1], cmap="binary")
plt.show()



```
In [11]: |plt.figure(figsize=(15,15))
             sns.heatmap(X train[0], annot=True, cmap="binary")
Out[11]: <Axes: >
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In []: SO Input is: 28 * 28 :784 : flattern the input layeers

And we have 10 Output:[0,1,2,3,4,5,6,7,8,9] ## Softmax is used their because it tell pr

11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27

Without Batch Normalization

```
In [12]: |# Creating Layers of ANN
         LAYERS = [tf.keras.layers.Flatten(input_shape=[28, 28], name="inputLayer"),
                   tf.keras.layers.Dense(300, activation="relu", name="hiddenLayer1"),
                   tf.keras.layers.Dense(100, activation="relu", name="hiddenLayer2"),
                   tf.keras.layers.Dense(10, activation="softmax", name="outputLayer")]
         model clf without bn = tf.keras.models.Sequential(LAYERS)
In [13]: |model_clf_without_bn.layers
Out[13]: [<keras.layers.reshaping.flatten.Flatten at 0x21939ca6da0>,
          <keras.layers.core.dense.Dense at 0x21939ca6740>,
          <keras.layers.core.dense.Dense at 0x21939ca6500>,
          <keras.layers.core.dense.Dense at 0x21939ca43a0>]
In [14]: | model_clf_without_bn.summary()
         Model: "sequential"
          Layer (type)
                                       Output Shape
                                                                 Param #
          inputLayer (Flatten)
                                       (None, 784)
                                       (None, 300)
          hiddenLayer1 (Dense)
                                                                 235500
          hiddenLayer2 (Dense)
                                       (None, 100)
                                                                 30100
          outputLayer (Dense)
                                       (None, 10)
                                                                 1010
         Total params: 266,610
         Trainable params: 266,610
         Non-trainable params: 0
In [15]: |# first Layer * second Layer + bias
         784*300 + 300, 300*100+100, 100*10+100
Out[15]: (235500, 30100, 1100)
In [16]: # Total parameters to be trained
         sum((235500, 30100, 1010))
Out[16]: 266610
```

```
In [18]: | # training
       EPOCHS = 10
      VALIDATION SET = (X valid, y valid)
       # Record starting time
       start time = time.time()
      history = model clf without bn.fit(X train, y train, epochs=EPOCHS,
                     validation_data=VALIDATION_SET, batch_size=64)
       # Record ending time
       end time = time.time()
       # Calculate training time
       training time = end time - start time
       print(f"Total training time: {training_time:.2f} seconds")
       Epoch 1/10
       3 - val loss: 0.1005 - val accuracy: 0.9700
       Epoch 2/10
       860/860 [============== ] - 4s 4ms/step - loss: 0.0893 - accuracy: 0.972
       8 - val loss: 0.0895 - val accuracy: 0.9714
       Epoch 3/10
       860/860 [=================== ] - 4s 5ms/step - loss: 0.0595 - accuracy: 0.981
       7 - val loss: 0.0751 - val accuracy: 0.9762
       Epoch 4/10
       1 - val loss: 0.0703 - val accuracy: 0.9814
       860/860 [================== ] - 4s 5ms/step - loss: 0.0313 - accuracy: 0.989
       2 - val_loss: 0.0843 - val_accuracy: 0.9780
       Epoch 6/10
       8 - val_loss: 0.0726 - val_accuracy: 0.9818
       Epoch 7/10
       3 - val_loss: 0.0752 - val_accuracy: 0.9812
       Epoch 8/10
       8 - val_loss: 0.0866 - val_accuracy: 0.9808
       Epoch 9/10
       860/860 [=============== ] - 4s 5ms/step - loss: 0.0155 - accuracy: 0.994
       6 - val_loss: 0.0835 - val_accuracy: 0.9776
       Epoch 10/10
       860/860 [=================== ] - 4s 4ms/step - loss: 0.0135 - accuracy: 0.995
       4 - val loss: 0.0837 - val accuracy: 0.9814
In [19]: | history.params
```

Out[19]: {'verbose': 1, 'epochs': 10, 'steps': 860}

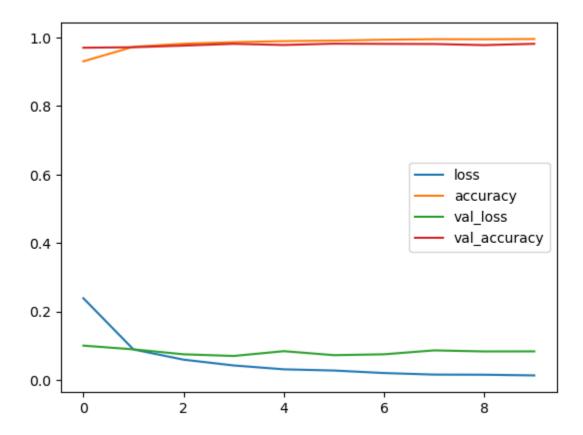
In [20]: pd.DataFrame(history.history)

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| \mathbf{c} | <i>a</i> c | 20 | |

| | loss | accuracy | val_loss | val_accuracy |
|---|----------|----------|----------|--------------|
| 0 | 0.238738 | 0.930345 | 0.100475 | 0.9700 |
| 1 | 0.089264 | 0.972782 | 0.089536 | 0.9714 |
| 2 | 0.059478 | 0.981673 | 0.075137 | 0.9762 |
| 3 | 0.042577 | 0.986127 | 0.070268 | 0.9814 |
| 4 | 0.031306 | 0.989236 | 0.084280 | 0.9780 |
| 5 | 0.027780 | 0.990764 | 0.072608 | 0.9818 |
| 6 | 0.020448 | 0.993327 | 0.075167 | 0.9812 |
| 7 | 0.015920 | 0.994818 | 0.086569 | 0.9808 |
| 8 | 0.015546 | 0.994618 | 0.083470 | 0.9776 |
| 9 | 0.013514 | 0.995400 | 0.083705 | 0.9814 |

In [21]: pd.DataFrame(history.history).plot()

Out[21]: <Axes: >



In [23]: # Evaluate both models on the test dataset
loss_without_bn, accuracy_without_bn = model_clf_without_bn.evaluate(X_test, y_test, ver
 print("Model without Batch Normalization:")
 print(f"Accuracy: {accuracy_without_bn*100:.2f}%, Loss: {loss_without_bn:.4f}")

Model without Batch Normalization: Accuracy: 97.92%, Loss: 0.0877

With Batch Normalization

```
In [24]: | # Define the layers of the model with batch normalization
         LAYERS1 = [tf.keras.layers.Flatten(input_shape=[28, 28], name="inputLayer"),
                   tf.keras.layers.Dense(300, activation="relu", name="hiddenLayer1"),
                   tf.keras.layers.BatchNormalization(name="batchNorm1"),
                   tf.keras.layers.Dense(100, activation="relu", name="hiddenLayer2"),
                   tf.keras.layers.BatchNormalization(name="batchNorm2"),
                   tf.keras.layers.Dense(10, activation="softmax", name="outputLayer")]
         model clf with bn = tf.keras.models.Sequential(LAYERS1)
```

In [25]: |model_clf_with_bn.summary()

Model: "sequential 1"

| Layer (type) | Output Shape | Param # |
|---|--------------|---------|
| inputLayer (Flatten) | (None, 784) | 0 |
| hiddenLayer1 (Dense) | (None, 300) | 235500 |
| <pre>batchNorm1 (BatchNormalizat ion)</pre> | (None, 300) | 1200 |
| hiddenLayer2 (Dense) | (None, 100) | 30100 |
| <pre>batchNorm2 (BatchNormalizat ion)</pre> | (None, 100) | 400 |
| outputLayer (Dense) | (None, 10) | 1010 |

Total params: 268,210 Trainable params: 267,410 Non-trainable params: 800

```
In [26]: LOSS_FUNCTION = "sparse_categorical_crossentropy" # use => tf.losses.sparse_categorical_
         OPTIMIZER = "ADAM" # or use with custom learning rate=> tf.keras.optimizers.SGD(0.02)
         METRICS = ["accuracy"]
         model clf with bn.compile(loss=LOSS FUNCTION,
                       optimizer=OPTIMIZER,
                       metrics=METRICS)
```

```
In [28]: | # training
     import time
     EPOCHS = 10
     VALIDATION_SET = (X_valid, y_valid)
     # Record starting time
     start time = time.time()
     history = model_clf_with_bn.fit(X_train, y_train, epochs=EPOCHS,
                validation_data=VALIDATION_SET, batch_size=64)
     # Record ending time
     end time = time.time()
     # Calculate training time
     training_time = end_time - start_time
     print(f"Total training time: {training time:.2f} seconds")
     Epoch 1/10
     860/860 [================== ] - 8s 7ms/step - loss: 0.2105 - accuracy: 0.937
     2 - val_loss: 0.0989 - val_accuracy: 0.9702
     Epoch 2/10
     2 - val_loss: 0.0835 - val_accuracy: 0.9756
     Epoch 3/10
     1 - val loss: 0.0852 - val accuracy: 0.9726
     Epoch 4/10
     3 - val loss: 0.0738 - val accuracy: 0.9774
     Epoch 5/10
     8 - val loss: 0.0756 - val accuracy: 0.9786
     Epoch 6/10
     0 - val_loss: 0.0636 - val_accuracy: 0.9800
     Epoch 7/10
     2 - val_loss: 0.0733 - val_accuracy: 0.9802
     Epoch 8/10
     2 - val loss: 0.0687 - val accuracy: 0.9802
     Epoch 9/10
     2 - val loss: 0.0764 - val accuracy: 0.9810
     Epoch 10/10
     0 - val loss: 0.0688 - val accuracy: 0.9802
```

Total training time: 49.95 seconds

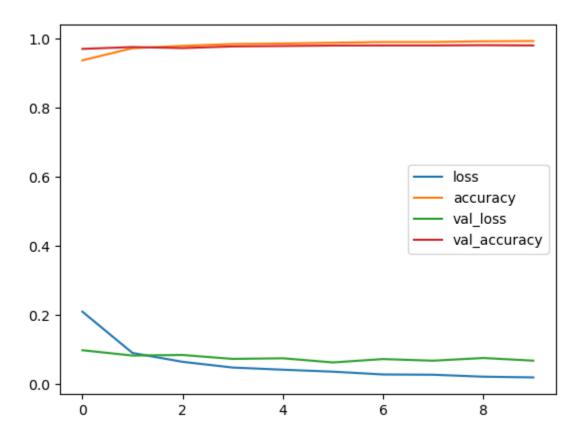
In [31]: |pd.DataFrame(history.history)

| | loss | accuracy | val_loss | val_accuracy |
|---|----------|----------|----------|--------------|
| 0 | 0.210480 | 0.937218 | 0.098913 | 0.9702 |
| 1 | 0.090966 | 0.972236 | 0.083534 | 0.9756 |
| 2 | 0.065417 | 0.979055 | 0.085216 | 0.9726 |
| 3 | 0.048829 | 0.984273 | 0.073797 | 0.9774 |
| 4 | 0.042590 | 0.985800 | 0.075644 | 0.9786 |
| 5 | 0.036925 | 0.988018 | 0.063586 | 0.9800 |
| 6 | 0.028844 | 0.990164 | 0.073334 | 0.9802 |
| 7 | 0.028057 | 0.990236 | 0.068650 | 0.9802 |
| 8 | 0.022416 | 0.992218 | 0.076421 | 0.9810 |
| 9 | 0.020310 | 0.993018 | 0.068799 | 0.9802 |

In [32]: pd.DataFrame(history.history).plot()

Out[32]: <Axes: >

Out[31]:



Model with Batch Normalization: Accuracy: 97.96%, Loss: 0.0748

SO the Difference is:

```
In [37]: # Evaluate both models on the test dataset
    loss_without_bn, accuracy_without_bn = model_clf_without_bn.evaluate(X_test, y_test, ver
    loss_with_bn, accuracy_with_bn = model_clf_with_bn.evaluate(X_test, y_test, verbose=0)

    print("Model without Batch Normalization:")
    print(f"Accuracy: {accuracy_without_bn*100:.2f}%, Loss: {loss_without_bn:.4f}")

    print(f"Accuracy: {accuracy_with_bn*100:.2f}%, Loss: {loss_with_bn:.4f}")
```

Model without Batch Normalization: Accuracy: 97.92%, Loss: 0.0877 Model with Batch Normalization: Accuracy: 97.96%, Loss: 0.0748

The provided experiment results show the comparison of two models trained on the same dataset using different batch sizes. The models were trained with and without batch normalization. Let's analyze the effects of different batch sizes on training dynamics and model performance.

Experiment Results:

Model without Batch Normalization:

• Accuracy: 97.92%

Loss: 0.0877

Model with Batch Normalization:

Accuracy: 97.96%

• Loss: 0.0748

Observations:

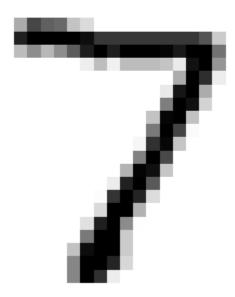
Both models achieve high accuracy, indicating that they are able to effectively learn from the data and make accurate predictions on unseen samples. The model with batch normalization slightly outperforms the model without batch normalization in terms of accuracy and loss. This suggests that batch normalization has provided some improvement in the model's performance.

Testing The Model

```
In [39]: | x_new = X_test[:3]
         x_new
Out[39]: array([[[0., 0., 0., ..., 0., 0., 0.],
                 [0., 0., 0., \ldots, 0., 0., 0.]
                 [0., 0., 0., ..., 0., 0., 0.]
                 [0., 0., 0., \ldots, 0., 0., 0.]
                 [0., 0., 0., \ldots, 0., 0., 0.]
                 [0., 0., 0., \ldots, 0., 0., 0.]
                [[0., 0., 0., ..., 0., 0., 0.],
                 [0., 0., 0., \ldots, 0., 0., 0.]
                 [0., 0., 0., \ldots, 0., 0., 0.]
                 [0., 0., 0., ..., 0., 0., 0.]
                 [0., 0., 0., \ldots, 0., 0., 0.]
                 [0., 0., 0., \ldots, 0., 0., 0.]
                [[0., 0., 0., ..., 0., 0., 0.],
                 [0., 0., 0., \ldots, 0., 0., 0.]
                 [0., 0., 0., ..., 0., 0., 0.]]
In [40]: | actual = y_test[:3]
         actual
Out[40]: array([7, 2, 1], dtype=uint8)
In [41]: | y_prob = model_clf_with_bn.predict(x_new)
         y_prob.round(3)
         1/1 [======= ] - 0s 307ms/step
Out[41]: array([[0.
                      , 0. , 0. , 0. , 0. , 0. , 1.
                                                                      , 0.
                 0.
                      ],
                      , 0.
                            , 1.
                                   , 0. , 0. , 0. , 0.
                                                               , 0.
                [0.
                                                                      , 0.
                 0.
                     ],
                [0.
                      , 0.998, 0. , 0.
                                           , 0. , 0.001, 0.
                                                               , 0.
                 0.
                      ]], dtype=float32)
In [43]: |y_pred = np.argmax(y_prob, axis = -1)
```

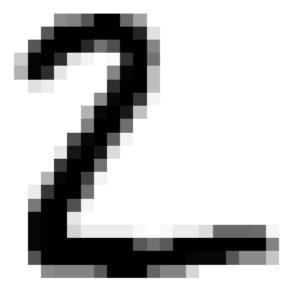
```
In [44]: # plot
for data, pred, actual_data in zip(x_new, y_pred, actual):
    plt.imshow(data, cmap="binary")
    plt.title(f"Predicted {pred} and Actual {actual_data}")
    plt.axis("off")
    plt.show()
    print("###############"")
```

Predicted 7 and Actual 7

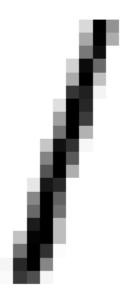


#############################

Predicted 2 and Actual 2



Predicted 1 and Actual 1



| ####################################### | | |
|---|------|--|
| | Done | |

Assignment Questions

```
In [34]: |# Importing Libraries
          import tensorflow as tf
          import matplotlib.pyplot as plt
          import numpy as np
          import pandas as pd
          import seaborn as sns
          import os
          from sklearn.model selection import train test split
          from sklearn.preprocessing import StandardScaler
In [35]: # Checking version of Tensorflow and Keras
          print(f"Tensorflow Version {tf.__version__}}")
          print(f"Keras Version {tf.keras.__version__})")
          Tensorflow Version 2.10.0
          Keras Version 2.10.0
In [36]: |df=pd.read_csv("wine.csv")
In [37]: | df.head()
Out[37]:
                                                          free
                                                                  total
                      volatile
               fixed
                              citric
                                    residual
                                             chlorides
                                                        sulfur
                                                                 sulfur
                                                                       density
                                                                                pH sulphates alcohol quality
              acidity
                      acidity
                               acid
                                      sugar
                                                       dioxide
                                                               dioxide
                                                                        0.9978 3.51
           0
                 7.4
                        0.70
                              0.00
                                                0.076
                                                                  34.0
                                                                                                         bad
                                        1.9
                                                          11.0
                                                                                         0.56
                                                                                                  9.4
           1
                 7.8
                        88.0
                              0.00
                                        2.6
                                                0.098
                                                         25.0
                                                                  67.0
                                                                        0.9968 3.20
                                                                                         0.68
                                                                                                  9.8
                                                                                                         bad
           2
                 7.8
                        0.76
                              0.04
                                        2.3
                                                0.092
                                                         15.0
                                                                  54.0
                                                                        0.9970 3.26
                                                                                         0.65
                                                                                                  9.8
                                                                                                         bad
           3
                11.2
                        0.28
                               0.56
                                        1.9
                                                0.075
                                                         17.0
                                                                  60.0
                                                                        0.9980 3.16
                                                                                         0.58
                                                                                                  9.8
                                                                                                        good
                 7.4
                        0.70
                               0.00
                                        1.9
                                                0.076
                                                          11.0
                                                                  34.0
                                                                        0.9978 3.51
                                                                                         0.56
                                                                                                  9.4
                                                                                                         bad
In [38]: | df.shape
Out[38]: (1599, 12)
In [39]: df.columns
Out[39]: Index(['fixed acidity', 'volatile acidity', 'citric acid', 'residual sugar',
                   'chlorides', 'free sulfur dioxide', 'total sulfur dioxide', 'density',
                   'pH', 'sulphates', 'alcohol', 'quality'],
                 dtype='object')
```

```
In [40]: |# Calculate class distribution
         class_distribution = df['quality'].value_counts()
         # Display the class distribution
         print(class_distribution)
         # Check if the target variable is imbalanced
         if len(class distribution) == 2:
             majority_class_count = max(class_distribution)
             minority_class_count = min(class_distribution)
             class_ratio = majority_class_count / minority_class_count
             if class ratio > 2:
                 print("The target variable is imbalanced.")
             else:
                 print("The target variable is not imbalanced.")
         else:
             print("The target variable is not binary.")
                 855
         good
```

bad 744
Name: quality, dtype: int64
The target variable is not imbalanced.

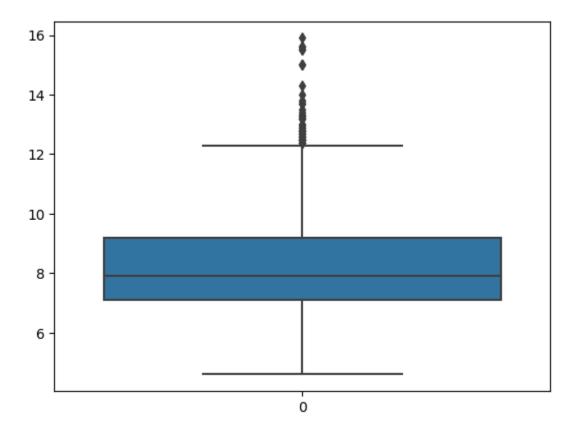
.... ... 800 ... -.....

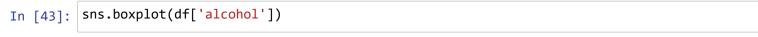
As Our target vaiable is not imbalanced

```
In [41]: print('Checking for Null values in the dataframe:','\n',df.isnull().sum(),'\n')
```

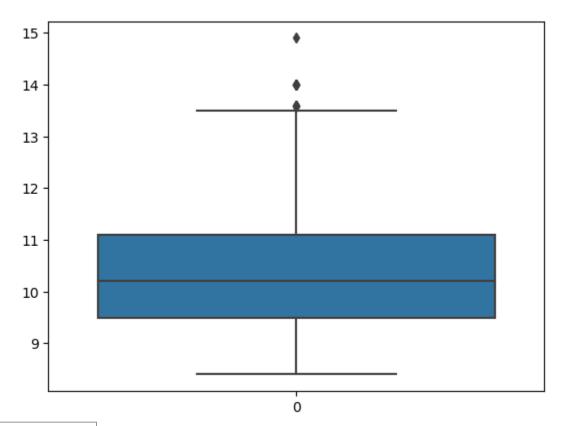
```
Checking for Null values in the dataframe:
fixed acidity
volatile acidity
                         0
citric acid
                         0
residual sugar
                         0
chlorides
                         0
free sulfur dioxide
                         0
total sulfur dioxide
                         0
                         0
density
                         0
pН
sulphates
                         0
                         0
alcohol
quality
dtype: int64
```

```
In [42]: sns.boxplot(df['fixed acidity'])
Out[42]: <Axes: >
```





Out[43]: <Axes: >



As we have some Outliers in data, But we are using Deep Learning Model so dont worry

```
y = df.quality
In [44]:
          X = df.drop(columns = ['quality'])
In [45]: | X. shape
Out[45]: (1599, 11)
          X.head()
In [46]:
Out[46]:
                                                                 free
                                                                           total
                         volatile
                 fixed
                                 citric
                                         residual
                                                  chlorides
                                                               sulfur
                                                                          sulfur
                                                                                density
                                                                                          pH sulphates alcohol
               acidity
                         acidity
                                  acid
                                           sugar
                                                              dioxide
                                                                        dioxide
           0
                  7.4
                           0.70
                                  0.00
                                                     0.076
                                                                 11.0
                                             1.9
                                                                           34.0
                                                                                 0.9978 3.51
                                                                                                   0.56
                                                                                                            9.4
           1
                   7.8
                           88.0
                                  0.00
                                             2.6
                                                     0.098
                                                                 25.0
                                                                           67.0
                                                                                 0.9968
                                                                                        3.20
                                                                                                   0.68
                                                                                                            9.8
           2
                  7.8
                           0.76
                                  0.04
                                             2.3
                                                     0.092
                                                                 15.0
                                                                           54.0
                                                                                 0.9970
                                                                                        3.26
                                                                                                   0.65
                                                                                                            9.8
           3
                  11.2
                           0.28
                                  0.56
                                             1.9
                                                     0.075
                                                                 17.0
                                                                           60.0
                                                                                 0.9980 3.16
                                                                                                   0.58
                                                                                                            9.8
                  7.4
                           0.70
                                  0.00
                                             1.9
                                                     0.076
                                                                 11.0
                                                                           34.0
                                                                                 0.9978 3.51
                                                                                                   0.56
                                                                                                            9.4
In [47]: |y.head()
Out[47]:
          0
                 bad
           1
                 bad
           2
                 bad
           3
                good
                 bad
           Name: quality, dtype: object
          As we have our Target Feature in "Good" or "Bad" so we use Label encoder
In [48]: # Let's perform categorical features encoding:
           from sklearn.preprocessing import LabelEncoder
          LE = LabelEncoder()
         # Target feature Encoding:
In [49]:
          y = LE.fit_transform(y)
In [50]: | y # 0= bad 1=Good
Out[50]: array([0, 0, 0, ..., 1, 0, 1])
In [51]: X_train_full, X_test, y_train_full, y_test = train_test_split(X,y, random_state=42)
          X_train, X_valid, y_train, y_valid = train_test_split(X_train_full,y_train_full, random_
```

```
In [52]: |print(X_train_full.shape)
         print(X test.shape)
         print(X_train.shape)
         print(X valid.shape)
         (1199, 11)
         (400, 11)
         (899, 11)
         (300, 11)
In [53]: |X_train.shape[1:]
Out[53]: (11,)
In [54]: |X_train.shape[1:]
Out[54]: (11,)
In [55]: |y_train.shape[:1]
Out[55]: (899,)
In [56]: # Creating layers of ANN
         LAYERS = [
             tf.keras.layers.Dense(30, activation="relu", name="HiddenLayer1", input_shape=X_trai
             tf.keras.layers.Dense(10, activation="relu", name="HiddenLayer2"),
             tf.keras.layers.Dense(5, activation='relu', name="HiddenLayer3"),
             tf.keras.layers.Dense(1, activation="sigmoid", name="OutputLayer")
         ]
         # Create the model using Sequential API
         model = tf.keras.models.Sequential(LAYERS)
In [57]: # Logging
         import time
         def get_log_path(log_dir="logs/fit"):
           fileName = time.strftime("log_%Y_%m_%d_%H_%M_%S")
           logs path = os.path.join(log dir, fileName)
           print(f"Saving logs at {logs_path}")
           return logs_path
         log_dir = get_log_path()
         tb_cb = tf.keras.callbacks.TensorBoard(log_dir=log_dir)
         Saving logs at logs/fit\log_2023_07_31_21_39_54
In [58]: early_stopping_cb = tf.keras.callbacks.EarlyStopping(patience=5, restore_best_weights=Tr
In [59]: | CKPT_path = "Model_ckpt.h5"
         checkpointing cb = tf.keras.callbacks.ModelCheckpoint(CKPT path, save best only=True)
```

```
In [60]: # Q13. Use binary cross-entropy as the loss function, Adam optimizer, and ['accuracy'] a
loss_function = 'binary_crossentropy'
optimizer = 'adam'
metrics = ['accuracy']

# Q14. Compile the model
model.compile(optimizer=optimizer, loss=loss_function, metrics=metrics)
```

In [61]: # Q12. Print the model summary model.summary()

Model: "sequential 1"

| Layer (type) | Output Shape | Param # |
|----------------------|--------------|---------|
| HiddenLayer1 (Dense) | (None, 30) | 360 |
| HiddenLayer2 (Dense) | (None, 10) | 310 |
| HiddenLayer3 (Dense) | (None, 5) | 55 |
| OutputLayer (Dense) | (None, 1) | 6 |
| | | |

Total params: 731
Trainable params: 731
Non-trainable params: 0

```
In [62]: scaler = StandardScaler()
```

X_train = scaler.fit_transform(X_train)
X_valid = scaler.transform(X_valid)
X_test = scaler.transform(X_test)

```
In [68]: |# Orginal train
    EPOCHS = 40
    VALIDATION SET = (X valid, y valid)
    history = model.fit(X_train, y_train, epochs=EPOCHS,
              validation data=VALIDATION SET, batch size=64, callbacks=[tb cb, ear
    Epoch 1/40
    - val loss: 0.5633 - val accuracy: 0.7333
    Epoch 2/40
    - val loss: 0.5635 - val accuracy: 0.7233
    Epoch 3/40
    - val_loss: 0.5632 - val_accuracy: 0.7233
    Epoch 4/40
    - val loss: 0.5631 - val accuracy: 0.7333
    Epoch 5/40
    - val loss: 0.5643 - val accuracy: 0.7300
    Epoch 6/40
    - val loss: 0.5647 - val accuracy: 0.7200
    Epoch 7/40
    - val loss: 0.5635 - val accuracy: 0.7300
    Epoch 8/40
    - val_loss: 0.5651 - val_accuracy: 0.7267
    Epoch 9/40
    - val_loss: 0.5665 - val_accuracy: 0.7200
    model_params = model.get_weights()
```

```
In [69]: # Q16. Get the model's parameters
         # 017. Store the model's training history as a Pandas DataFrame
         history df = pd.DataFrame(history.history)
```

```
In [70]: # Q18. Plot the model's training history
plt.plot(history_df['accuracy'], label='Train Accuracy')
plt.plot(history_df['val_accuracy'], label='Validation Accuracy')
plt.plot(history_df['loss'], label='Train Loss')
plt.plot(history_df['val_loss'], label='Validation Loss')
plt.legend()
plt.xlabel('Epoch')
plt.ylabel('Metric Value')
plt.title('Training History')
plt.show()

# Q19. Evaluate the model's performance using the test data
test_loss, test_accuracy = model.evaluate(X_test, y_test)
print(f'Test Loss: {test_loss:.4f}, Test Accuracy: {test_accuracy:.4f}')
```



```
In [81]: |model.predict(new.reshape((1,11)))
         1/1 [======] - 0s 64ms/step
Out[81]: array([[0.39237672]], dtype=float32)
In [83]: # Assuming you have already trained the model and loaded the test data (X_test, y_test)
        # Make predictions on the test data using the trained model
        y pred probs = model.predict(X test)
         # Convert the predicted probabilities to class labels (0 or 1)
        y pred labels = (y pred probs > 0.5).astype(int)
        # If you have used the sigmoid activation function in the output layer
         # and want to predict the class with the highest probability directly:
        # y pred labels = np.argmax(y pred probs, axis=1)
         # Evaluate the model's performance
        from sklearn.metrics import accuracy_score, confusion_matrix, classification_report
         # Calculate accuracy
         accuracy = accuracy_score(y_test, y_pred_labels)
         # Create a confusion matrix
         conf_matrix = confusion_matrix(y_test, y_pred_labels)
         # Print the classification report
         class report = classification report(y test, y pred labels)
         print("Accuracy:", accuracy)
         print("Confusion Matrix:")
         print(conf matrix)
         print("Classification Report:")
        print(class report)
         Accuracy: 0.74
         Confusion Matrix:
         [[137 41]
         [ 63 159]]
         Classification Report:
                      precision recall f1-score support
                   0
                                    0.77
                                              0.72
                           0.69
                                                         178
                   1
                           0.80
                                    0.72
                                              0.75
                                                         222
                                              0.74
                                                         400
            accuracy
                           0.74
                                    0.74
                                              0.74
                                                         400
           macro avg
         weighted avg
                           0.75
                                    0.74
                                              0.74
                                                         400
```

```
In [87]: | # Assuming you have already trained the model and loaded the test data (X_test)
         # Make predictions on the test data using the trained model
         y_pred_probs = model.predict(X_test)
         # Verify the shape of the y_pred_probs array
         print("Shape of y_pred_probs:", y_pred_probs.shape)
         # Assuming '0' represents 'Bad' and '1' represents 'Good',
         # you can access the probability of 'Good' wine for the first sample (index 0) as follow
         prob_good = y_pred_probs[0][0]
         print("Probability of Good Wine:", prob_good)
         13/13 [======== ] - 0s 4ms/step
         Shape of y_pred_probs: (400, 1)
         Probability of Good Wine: 0.39237672
```

In []:

Assignment Question

Q1. What is the purpose of forward propagation in a neural network?

Answer: The purpose of forward propagation in a neural network is to compute the output of the network based on given input data. It involves passing the input through the network's layers, applying weights and biases to the data, and activating neurons using specific functions until the final output is generated.

Q2. How is forward propagation implemented mathematically in a single-layer feedforward neural network?

Answer: In a single-layer feedforward neural network, the forward propagation process can be mathematically represented as follows:

Input: The input features are denoted as a vector $x = [x_1, x_2, ..., x_n]$. Weighted Sum: Each input feature is multiplied by its corresponding weight, and the biases are added to the weighted sum. Activation Function: The weighted sum is then passed through an activation function, producing the output of the neuron.

Q3. How are activation functions used during forward propagation?

Answer: Activation functions are applied during forward propagation to introduce non-linearity in the neural network, allowing it to learn complex patterns and make predictions for more diverse datasets. The activation function takes the output of a neuron and transforms it into a new value, which becomes the input for the next layer in the network.

Q4. What is the role of weights and biases in forward propagation?

Answer: The weights and biases are crucial parameters in forward propagation. The weights determine the strength of connections between neurons, controlling how much influence each input has on the neuron's output. Biases, on the other hand, shift the output of the activation function and allow the network to learn from different parts of the data distribution.

Q5. What is the purpose of applying a softmax function in the output layer during forward propagation?

Answer: The softmax function is typically applied in the output layer of a neural network when dealing with multi-class classification problems. It converts the raw output scores (logits) of the network into probabilities. The softmax function ensures that the output probabilities sum up to 1, making it easier to interpret the model's certainty about each class.

Q6. What is the purpose of backward propagation in a neural network?

Answer: The purpose of backward propagation, also known as backpropagation, is to adjust the network's weights and biases based on the computed error during forward propagation. By propagating the error backward through the network, it allows the model to learn and improve its performance through the process of gradient descent.

Q7. How is backward propagation mathematically calculated in a single-layer feedforward neural network?

Answer: In a single-layer feedforward neural network, backward propagation involves calculating the gradients of the loss function with respect to the weights and biases. These gradients indicate how the weights and biases should be adjusted to minimize the error. The chain rule is used to compute these gradients layer-by-layer, starting from the output layer and moving backward towards the input layer.

Q8. Can you explain the concept of the chain rule and its application in backward propagation?

Answer: The chain rule is a fundamental concept in calculus that allows us to find the derivative of a composite function. In the context of neural networks, it enables us to compute the gradients of the loss function with respect to the weights and biases of each layer. During backward propagation, the chain rule is applied to calculate how the changes in the output of a layer affect the error, and these gradients are used to update the parameters of the network through gradient descent.

Q9. What are some common challenges or issues that can occur during backward propagation, and how can they be addressed?

Answer: Some common challenges or issues during backward propagation are:

- Vanishing gradients: When gradients become very small, hindering the learning process. This can be
 mitigated using activation functions that preserve gradients, like ReLU.
- Exploding gradients: When gradients become extremely large, causing instability during learning. Techniques like gradient clipping can be applied to control the magnitude of gradients.
- Overfitting: When the model becomes too complex and performs well on training data but poorly on unseen data. Regularization techniques, such as L1 or L2 regularization, can be used to address this problem.
- Learning rate selection: Choosing an appropriate learning rate is essential for stable and efficient learning. Techniques like learning rate scheduling or adaptive learning rate methods (e.g., Adam) can be used.
- Local minima. The entimization process may get stuck in local minima, localing to subentimal colutions