

ECE 214 — Exam #2

Estimated time for completion: ≤ 1.25 hour
26 April 2016

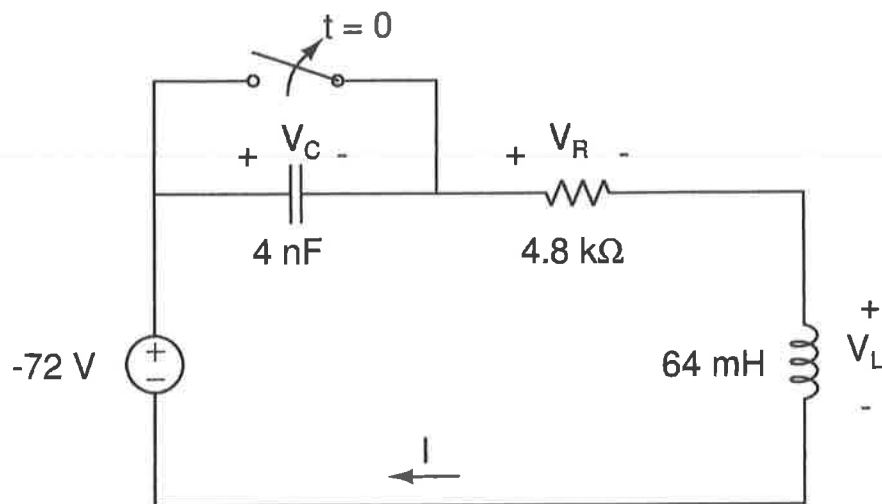
Rules of the Exam

- Rule 1:** The examination period begins at 8:00am on Tuesday 26 April 2016 and ends at 9:15am on Tuesday 26 April 2016.
- Rule 2:** The exam is worth 15% of your grade.
- Rule 3:** To receive credit for the answer make sure to include the units along with the numerical answer and show all work.
- Rule 4:** There is minimal partial credit.
- Rule 5:** The exam is closed book and closed notes. You may use your ECE 214 Laboratory Notebook and a calculator.
- Rule 6:** Do not discuss this exam with anyone until after 1:00pm on Tuesday 26 April 2016.

Answer Key

Name

Problem: Step response for a series RLC circuit. The switch in the circuit below has been closed for 37,321 years and opens at time $t = 0$. Complete the table for the circuit:



	$t = -50\mu\text{s}$	$t = 0^+ \text{ s}$	$t = 50\mu\text{s}$	$t = \infty$
V_C	0 V	0 V	-82.77 V	-72 V
V_R	-72 V	-72 V	3.89 V	0 V
V_L	0 V	0 V	6.88 V	0 V
I	-15 mA	-15 mA	-810.4 μA	0 A

Extra Credit:

At what time after the switch opens is the voltage across the inductor a maximum? 18.55 μs

$$\alpha = \frac{R}{2L} = \frac{4800}{2 \times 64 \times 10^{-3}} = 37,500 \text{ rad/s}$$

$$\omega_0 = \frac{1}{\sqrt{LC}} = \frac{1}{\sqrt{64 \times 10^{-3} \times 4 \times 10^{-9}}} = 62,500 \text{ rad/s}$$

$$\omega_d = (\omega_0^2 - \alpha^2)^{\frac{1}{2}} = 50,000 \text{ rad/s}$$

$$i(t) = A_1 e^{-\alpha t} \cos(50,000 t) + A_2 e^{-\alpha t} \sin(50,000 t) + i(0)$$

$$i(0) = -0.015 = A_1$$

$$A_1 = -0.015 \text{ A}$$

$$L \left. \frac{di(t)}{dt} \right|_{t=0^+} = v_L(0^+) = 0$$

$$\left. \frac{di(t)}{dt} \right|_{t=0^+} = 0$$

$$\left. \frac{di}{dt} \right|_{t=0^+} = A_1(-\alpha) + A_2(50,000) = 0$$

$$A_2 = A_1 \frac{\alpha}{50,000} = 0.75 A_1$$

$$A_2 = 0.75 A_1$$

$$i(t) = -0.015 e^{-37,500 t} \cos(50,000 t) - (0.75)(0.015) e^{-37,500 t} \sin(50,000 t)$$

.001843 - .001033

$$i(50 \mu\text{s}) = 810.4 \mu\text{A}$$

$$v_r = 4800 \times i(50 \mu\text{s}) = 3.89 \text{ V}$$

$$v_L = L \frac{di}{dt} = 64 \times 10^{-3} \frac{di}{dt}$$

$$i(t) = -0.015 e^{-37,500t} \left[\cos(50,000t) + \frac{3}{4} \sin(50,000t) \right]$$

$$\frac{di}{dt} = -0.015 e^{-37,500t} \left[-50,000 \sin(50,000t) + \frac{3}{4} 50,000 \cos(50,000t) \right] \\ + (0.015)(37,500) e^{-37,500t} \left[\cos(50,000t) + \frac{3}{4} \sin(50,000t) \right]$$

$$\frac{di}{dt} = e^{-37,500t} \left[750 \sin(50,000t) + 562.5 \cos(50,000t) \right] \\ + 562.5 \cos(50,000t) + 421.875 \sin(50,000t) \\ = e^{-37,500t} \left[1171.88 \sin(50,000t) \right]$$

$$V_L = L \frac{di}{dt} = 64 \times 10^{-3} \frac{di}{dt}$$

$$V_L(50 \mu s) = 64 \times 10^{-3} e^{-37,500 \times 50 \times 10^{-6}} \left[1171.88 \sin(50,000 \times 50 \times 10^{-6}) \right] \\ = 6.8834 V$$

$$V_C + V_R + V_L + 72 = 0$$

$$V_C = -72 - V_R - V_L = -72 - 3.89 - 6.88 = -82.77$$

Extra Credit

$$V_L(t) = 75 e^{-37,500t} \sin(50,000t)$$

$$\frac{dV_L}{dt} = 75 e^{-37,500t} \cos(50,000t) \times 50,000 - (37,500) e^{-37,500t} \sin(50,000t) = 0$$

$$50,000 \cos(50,000t) = 37,500 \sin(50,000t)$$

$$\cos(50,000t) = 0.75 \sin(50,000t)$$

$$1 = 0.75 \tan(50,000t)$$

$$1 = 0.75 \tan(50,000t)$$

$$50,000 \cos(50,000t) = 37,500 \sin(50,000t)$$

$$\frac{4}{3} = \frac{\sin(50,000t)}{\cos(50,000t)} = \tan(50,000t)$$

$$t = 18.55 \mu s$$

