ECE 214 - Lab #1 — Test Equipment Loading

30 January 2018

Introduction In this lab you are to determine the voltage ratio, V_{OUT}/V_{IN} , produced by the voltage divider with resistors R_a and R_b shown in Figure 1.

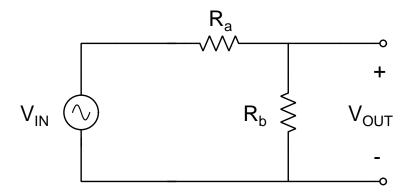


Figure 1: The circuit under test (CUT) is an ideal resistor divider circuit.

This lab illustrates that the actual values of the components, and the impedances associated with the test equipment and cables, must be considered when determining the actual value of the voltage across a circuit element. All voltage sources, including batteries, have a finite source impedance. All measurement equipment, including oscilloscopes and digital volt meters (DVMs), have a non-infinite input impedance that presents a load to the circuit. Cables that connect the circuit to the test equipment introduce additional impedances in the circuit. The schematic showing the circuit under test (CUT) connected to a function generator and oscilloscope is shown in Figure 2.

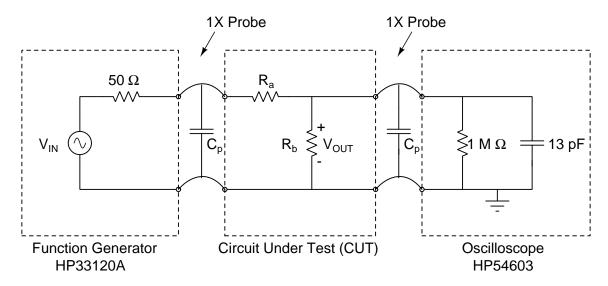


Figure 2: Measurement set—up for the resistor divider circuit.

Lab Procedure

Part A

- 1. Configure the HP33120A Function Generator (FG) to generate a 1kHz sinusoidal signal with an output voltage of 1 V peak.
- 2. Connect the output of the FG directly to the input of the HP54603 Oscilloscope (scope) and measure the FG output voltage and frequency. Verify that the FG is producing a 1V peak signal with a frequency of 1kHz. Make sure you understand the relationship between the voltage displayed on the FG panel and the value of the output voltage. Record this relationship in our notebook and try to remember this relationship in the future when you use the FG.

Part B

- 1. Use the Tenma 72-1025 LCR Meter to measure the capacitance of your 1X probes at a frequency of 1kHz. Make sure the capacitance meter is set to measure capacitance with series resistance. Also measure the Dissipation Factor (DF) of the probes at a frequency of 1kHz. Record these values in your notebook.
- 2. Calculate the ESR of the probes at a frequency of 1kHz. Do your probes represent a high quality capacitor at a frequency of 1kHz?
- 3. Obtain two resistors with each of the following values: 10Ω , $10k\Omega$, and $1M\Omega$. Measure the resistance of each resistor using your digital volt meter (DVM). Record these values in your notebook.
- 4. For each of the three pairs of resistors, place two resistors with the same value on the breadboard to make a series circuit as shown in Figure 1. If the resistors have slightly different values, make sure you keep track of which resistor is which.
- 5. Assuming that the resistors had the ideal values, calculate the ratio of V_{OUT}/V_{IN} assuming an ideal world where the voltage source is ideal (with zero source resistance), the probes are perfect connectors (with zero resistance, capacitance, and inductance), and V_{OUT} is measured with an ideal scope (with infinite input impedance). Record the values in your notebook in the form of a table like Table 1 in a column labeled "Ideal Components."
- 6. Using the measured values of the resistors, calculate the expected ratio of V_{OUT}/V_{IN} assuming an ideal world where the voltage source is ideal (with zero source resistance), the probes are perfect connectors (with zero resistance), and V_{OUT} is measured with an ideal scope (with infinite input impedance). Record the values in your notebook in a table like Table 1 in a column labeled "Real Components."
- 7. Calculate the %Error caused by the tolerance in the resistor values. The %Error is defined by:

$$\% \text{Error} = 100 * \frac{\left| \frac{V_{OUT}}{V_{IN}} (\text{Ideal Components}) - \frac{V_{OUT}}{V_{IN}} (\text{Real Components}) \right|}{\frac{V_{OUT}}{V_{IN}} (\text{Ideal Components})}$$
(1)

Record the values in your notebook in a table as like Table 1 in a column labeled "% Error (R Tolerance)."

R_a	R_b	$ m V_{OUT}$ / $ m V_{IN}$			
		Ideal Components	Real Components	%Error (R Tolerance)	
10Ω	10Ω				
$10 \mathrm{k}\Omega$	$10 \mathrm{k}\Omega$				
$1 \mathrm{M}\Omega$	$1 \mathrm{M}\Omega$				

Table 1: Measurement error due to tolerance in the resistor values.

- 8. Using the measured values of the resistors, the measured capacitance of the 1X probes, the output resistance of the FG and the input impedance of the scope, calculate the expected ratio of V_{OUT}/V_{IN} for the three values of resistors. Show all calculations in your notebook. Record the calculated values in Table 2 in a column labeled "Calculated" and place the table in your notebook.
- 9. Set the FG to generate a 1kHz sinusoidal signal with peak voltage $V_{IN} = 1V$. Verify both the frequency and peak voltage using the scope then connect the FG and scope to the resistors as shown in Figure 2.
- 10. Use the scope to measure the peak value of the output voltage (V_{OUT}) across resistor R_b for the pairs of resistors. Record the value of V_{OUT} in Table 2 in a column labeled "Measured" and place the table in your notebook.
- 11. Calculate the %Calculated-Measured (%CM) Error for the three pairs of resistors. The %CM Error is defined by:

$$\% \text{CM Error} = 100 * \frac{\left| \frac{V_{OUT}}{V_{IN}} (\text{Calculated}) - \frac{V_{OUT}}{V_{IN}} (\text{Measured}) \right|}{\frac{V_{OUT}}{V_{IN}} (\text{Calculated})}$$
(2)

Record the values in Table 2 in a column labeled "%CM Error" and place the table in your notebook. Your %CM Error should be on the order of 1% or less. If the error is greater than 2%, there is either a mistake in your calculation or an inaccuracy in your measurement. Try and obtain values such that the %CM Error is less than 1.5% for all three resistor pairs. Explain in your notebook any discrepancy between the measured and calculated values. Indicate possible sources of the error.

12. Calculate the %Total Error for the three resistor pairs. The %Total Error is defined by:

$$\% \text{Total Error} = 100 * \frac{\left| \frac{V_{OUT}}{V_{IN}} (\text{Ideal}) - \frac{V_{OUT}}{V_{IN}} (\text{Measured}) \right|}{\frac{V_{OUT}}{V_{IN}} (\text{Ideal})}$$
(3)

Record the values in Table 2 in a column labeled "%Total Error" and place the table in your notebook.

R_a	R_b	$ m V_{OUT} \ / \ m V_{IN}$				
		Calculated	Measured	% C-M Error	% Total Error	
10Ω	10Ω					
$10 \mathrm{k}\Omega$	$10 \mathrm{k}\Omega$					
$1 \mathrm{M}\Omega$	$1M\Omega$					

Table 2: Measurement error introduced by the measurement equipment and 1X probes.

13. For which resistor values does the measurement equipment have a minimal effect on the circuit under test?

Part C

- 1. Change the FG output to a square wave with a 1V peak amplitude. Keep the frequency at 1kHz.
- 2. For the $10k\Omega$ resistors, record in your notebook the shape of the rising edge of the signal as observed on the oscilloscope. Make sure to expand the time scale to see the details of the rising edge of the signal. It is not just a vertical line. The signal should appear similar to the response of a first order RC system studied in ECE 210.
- 3. What is the approximate mathematical equation which can be used to describe this waveform? Record the equation in your notebook.
- 4. Measure and record in your notebook both the rise time and the time constant of the signals at $V_{\rm OUT}$.

Post-Lab

Part A

For the voltage divider circuit, an estimate of the error introduced by the measurement apparatus can be obtained by comparing the values of V_{OUT} from an analysis of the circuit in Figure 1 with the values of V_{OUT} from an analysis of the circuit in Figure 2.

Assume that $V_{IN} = 1.0 \text{ Vp}$, f = 1 kHz, and $R_a = R_b = R$.

- 1. Derive an equation $V_{OUT1}(R)$ expressing the output voltage V_{OUT} as a function of the resistance R for the circuit of Figure 1. Do <u>not</u> include in the calculation the capacitance of the 1X probes, the output resistance of the FG and the input impedance of the scope.
- 2. Derive an equation $V_{OUT\,2}(R)$ expressing the output voltage V_{OUT} as a function of the resistance R for the circuit of Figure 2. Include in the calculation the capacitance of the 1X probes, the output resistance of the FG and the input impedance of the scope.

Record these equations in your notebook.

Use Matlab® to plot $V_{OUT1}(R)$ and $V_{OUT2}(R)$ when the value of R is varied from 10Ω to $10M\Omega$. Plot the data on a semi-log graph with the x-axis (resistance value) as the logarithmic scale. On the same graph, plot the three measured values of V_{OUT} , appropriately scaled, from the Table on page 3. Place a copy of the graph in your notebook and place an entry to this graph in the table of contents. Make sure the axes and the data are correctly labeled using Matlab® . A Matlab® template file is available on the course website at http://web.eece.maine.edu/kotecki/ECE214/docs/Matlab/ECE214_2018_Lab1_A.m.

Part B

Use NGspice to simulate the expected output voltage V_{OUT} as a function of the resistance R for the circuit of Figure 2. Include in the simulation the capacitance of the 1X probes, the output resistance of the FG and the input impedance of the scope. A Matlab® template file (http://web.eece.maine.edu/kotecki/ECE214/docs/Matlab/ECE214_2018_Lab1_B.m) and an hspc simulation file (http://web.eece.maine.edu/kotecki/ECE214/docs/ngspice/ECE214_2018_Lab1.hspc) are available on the course website.

Part C

In your notebook provide a summary of the major results and conclusions from this lab. Compare the measured results with the calculated and simulated results. What is the most important piece of information you learned in this laboratory? Make an entry of the location of this information in the table of contents.