

Problems on Complexity Analysis

Find the Time Complexities of the following snippets of code:

(A)

```
/* Assume that rand() takes constant amount of time */
int a = 0, b = 0;
for (int i = 0; i < N; i++) {
    a = a + rand();
}
for (int j = 0; j < M; ++j) {
    b = b + rand();
}
```

(B)

```
int a = 0, b = 0;
for (int i = 0; i < N; i++) {
    for (int j = 0; j < N; j++) {
        a = a + j;
    }
}
for (int k = 0; k < N; k++) {
    b = b + k;
}
```

(C)

```
int a = 0;
for (int i = 0; i < N; i++) {
    for (int j = N; j > i; --j) {
        a = a + i + j;
    }
}
```

(D)

```
int a = 0, i = N;
while (i > 0) {
    a += i;
    i /= 2;
}
```

(E)

```
void fun(int N, int K) {  
    for(int i = 1; i <= N; i++) {  
        /* Assume that pow() takes constant amount of time */  
        int P = pow(i, K);  
        for (int j = 1; j <= P; ++j) {  
            /* Some constant amount of computation */  
        }  
    }  
}
```

(F)

```
int count = 0;  
for(int i = N; i > 0; i /= 2) {  
    for(int j = 0; j < i; j++) {  
        count += 1;  
    }  
}
```

(G)

```
int k = 0;  
for(int i = N/2; i <= N; ++i) {  
    for (int j = 2; j <= N; j = j * 2) {  
        k = k + N/2;  
    }  
}
```

(H)

```
int j = 0;  
for(int i = 0; i < N; ++i) {  
    while(j < N && arr[i] <= arr[j]) {  
        j++;  
    }  
}
```

Match the following Time Complexities:

(1) Linear

(2) Logarithmic

(3) Exponential

(4) Polynomial

(5) Log Linear

(6) Quadratic

(A) N^{K+G}

(B) $5^{N \times 2}$

(C) $\frac{N}{4} \log_2 \left(\frac{N}{4000} \right)$

(D) $3^{20}N + 10^5$

(E) $10N + 9 \frac{N}{100} + 340N^2$

(F) $10^3 \log_2(N+3N)$

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