

Applying Dijkstra’s Algorithm

1. **Introduction** Dijkstra’s Algorithm is applied to find the shortest path from a source node to all other nodes in a weighted graph. This document presents a step-by-step application of Dijkstra’s Algorithm starting from **Node A**.

2. **Given Graph** The graph consists of the following edges and weights:

- (A, B) -> 4
- (A, C) -> 2
- (B, C) -> 5
- (B, D) -> 10
- (C, E) -> 3
- (E, D) -> 4
- (D, F) -> 11

3. **Initialization** A distance table is maintained where:

- **d(A) = 0** (starting node)
- All other nodes are set to  $\infty$  (unreachable initially)
- A **visited set** is used to keep track of processed nodes

Node	A	B	C	D	E	F
d[]	0	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$

4. **Step-by-Step Execution**

**Step 1:** Select the smallest distance from non-visited vertices → **A** (d = 0)

- Possible vertices A can visit: **B, C**
- Compute new distances:
  - $d(B) = \min(d(B), d(A) + \text{cost}(A, B))$ 
    - $d(B) = \min(\infty, 0 + 4) = 4$
  - $d(C) = \min(d(C), d(A) + \text{cost}(A, C))$ 
    - $d(C) = \min(\infty, 0 + 2) = 2$

Node	A	B	C	D	E	F
d[]	0	4	2	$\infty$	$\infty$	$\infty$

**Step 2:** Select the smallest distance from non-visited vertices → **C** (d = 2)

- Possible vertices C can visit: **B, E**
- Compute new distances:
  - $d(B) = \min(d(B), d(C) + \text{cost}(C, B))$ 
    - $d(B) = \min(4, 2 + 5) = 4$
  - $d(E) = \min(d(E), d(C) + \text{cost}(C, E))$ 
    - $d(E) = \min(\infty, 2 + 3) = 5$

Node	A	B	C	D	E	F
d[]	0	4	2	$\infty$	5	$\infty$

**Step 3:** Select the smallest distance from non-visited vertices → **B** (d = 4)

- Possible vertices B can visit: **D**
- Compute new distances:
  - $d(D) = \min(d(D), d(B) + \text{cost}(B, D))$ 
    - $d(D) = \min(\infty, 4 + 10) = 14$

Node	A	B	C	D	E	F
d[]	0	4	2	14	5	$\infty$

**Step 4:** Select the smallest distance from non-visited vertices → **E** (d = 5)

- Possible vertices E can visit: **D**
- Compute new distances:
  - $d(D) = \min(d(D), d(E) + \text{cost}(E, D))$ 
    - $d(D) = \min(14, 5 + 4) = 9$

Node	A	B	C	D	E	F
d[]	0	4	2	9	5	$\infty$

**Step 5:** Select the smallest distance from non-visited vertices → **D** (d = 9)

- Possible vertices D can visit: **F**
- Compute new distances:
  - $d(F) = \min(d(F), d(D) + \text{cost}(D, F))$ 
    - $d(F) = \min(\infty, 9 + 11) = 20$

Node	A	B	C	D	E	F
d[]	0	4	2	9	5	20

**Step 6:** Select the smallest distance from non-visited vertices → **F** (d = 20)

- No updates, as **F** has no unvisited neighbors.

**5. Final Shortest Distances from Node A**

- A → A = 0
- A → B = 4
- A → C = 2
- A → D = 9
- A → E = 5
- A → F = 20

**6. Conclusion** Dijkstra’s Algorithm successfully computes the shortest path from **Node A** to all other nodes. The computed shortest distances confirm the correctness of the algorithm’s step-by-step execution.