

Q1:

(1): In 1 mol of ideal gas, there are  $N$  molecules. Therefore, the total internal energy is  $\boxed{\frac{3}{2}NkT}$ .

(2): As  $U = \frac{3}{2}NkT$ , we have  $\Delta U = \frac{3}{2}Nk\Delta T$ .

As the gas is under constant volume, there is no work done.

By the first law of thermodynamics, we have  $Q = \Delta U = \boxed{\frac{3}{2}Nk}$ .

(3): As  $V = \frac{R}{p}T$ , we have  $\Delta V = \frac{R}{p}\Delta T = \frac{R}{p}$ . Therefore, the amount of work done  $= p\Delta V = R = \boxed{Nk}$ .

(4): By  $U = \frac{3}{2}kT$ ,  $U \propto T$ , as the temperature remains fixed, the kinetic energy remains fixed (i.e.  $\boxed{1}$  times greater).

(5): As  $T \propto pV$ , the temperature becomes  $2 \cdot 0.3 = 0.6$  times greater than before. As  $U \propto T$ , the kinetic energy becomes  $\boxed{0.6}$  times greater than before.

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Q2:

(1): By the conservation of momentum, we have

$$m_A v_A = (m_A + m_B)v$$

$$2.0 \cdot 7 = (2.0 + 5.0)v$$

$$v = \boxed{2}$$

(2): The total force acting on A and B is the friction, which has a magnitude of  $-\mu m_B g = -0.2 \cdot 5 \cdot 9.8 = -9.8 \text{ N}$ .

Therefore, we have:

$$\begin{cases} (m_A + m_B)a = 7a = -9.8 \\ -P = m_A a = 2a \end{cases}$$

By solving, we have  $a = \boxed{-1.4} \text{ m/s}^2$  and  $P = 2 \cdot 1.4 = \boxed{2.8} \text{ N}$ .

(3): By  $v^2 - u^2 = 2as$ , we have  $s = \frac{0-2^2}{-2 \cdot 1.4} \approx \boxed{1.4} \text{ m}$

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Q3:

(1): By  $F = ma$ ,  $g = \frac{G \frac{mM}{R^2}}{m} = \boxed{\frac{GM}{R^2}}$ .

(2): Note that the gravitational attraction provides the entire centripetal force, we have

$$\frac{mv^2}{r} = \frac{GmM}{r^2}$$

$$\frac{v^2}{2R} = \frac{GM}{(2R)^2}$$

$$v^2 = \frac{1}{2}gR$$

$$v = \boxed{\sqrt{\frac{gR}{2}}}$$

(3):  $KE + GPE = \frac{1}{2}mv^2 - \frac{GmM}{r}$

$$\begin{aligned}
&= \frac{1}{2}m\left(\sqrt{\frac{gR}{2}}\right)^2 - \frac{GmM}{2R} \\
&= \frac{mgR}{4} - \frac{1}{2}mgR \\
&= \boxed{-\frac{1}{4}mgR}
\end{aligned}$$


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Q4:

(1): Using the distance of the first resonance for the open-end correction, we have  $\frac{\lambda}{2} = 0.151 - 0.045$ , i.e.  $\lambda = \boxed{0.212} \text{ m}$ .

(2): We have  $\frac{\lambda}{4} + e = 0.045$ , i.e.  $e = \frac{0.212}{4} - 0.045 = \boxed{0.008} \text{ m}$ .

(3):  $v = f\lambda = 1620 \cdot 0.212 \approx \boxed{343} \text{ m/s}$ .

(4): By that time, the third resonance occurs at  $0.151 \text{ m}$ , i.e.

$$\frac{5}{4}\lambda = 0.151 + 0.008 \text{ m, i.e. } \lambda = 0.1272 \text{ m}.$$

Then,  $f = \frac{v}{\lambda} \approx \boxed{2696} \text{ Hz}$ .

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Q5:

(1): After  $S$  is closed, immediately, the capacitor does not contain any charges and has zero resistance. Therefore,  $I_2 = \boxed{0} \text{ mA}$  and  $I_3 = I_1$ .

As all the voltage are consumed by  $R_1$ , by Ohm's law, we have  $E = I_1 R_1$ ,

$$\text{i.e. } I_1 = \frac{6.0}{2.0 \times 10^3} = \boxed{3.0} \text{ mA. Then, } I_3 = \boxed{3.0} \text{ mA}.$$

(2): After  $S$  is closed for sufficiently long, the capacitor is fully charged and has infinite resistance. Therefore, the equivalent resistance of  $R_2 - C$  is  $R_2$  and  $I_3 = \boxed{0} \text{ mA}$ .

Moreover,  $I_1 = I_2$  and by Ohm's law  $E = I(R_1 + R_2)$ , i.e.

$$I_1 = I_2 = I = \boxed{1.0} \text{ mA}.$$

(3): After  $S$  is opened again, no current passed through the main circuit, hence  $I_1 = \boxed{0} \text{ mA}$ .

However, the capacitor acted as a battery for the  $R_2 - C$  circuit.

As the voltage across the capacitor during charging was  $\frac{R_2}{R_1 + R_2} E = 4.0 \text{ V}$ , the EMF provided by the capacitor will also be  $4.0 \text{ V}$ .

By Ohm's law,  $V = IR_2$ , we have the current of the circuit  $I = 1.0 \text{ mA}$  and the direction is anti-clockwise.

$$\text{Therefore, } I_2 = \boxed{1.0} \text{ mA and } I_3 = \boxed{-1.0} \text{ mA}.$$

Q6:

$$(1): H = \frac{I}{2\pi r} = \frac{15.7}{2 \cdot 3.14 \cdot 0.20} = \boxed{12.5} \text{ A/m}.$$

$$(2): B = \mu H = \boxed{1.57 \times 10^{-5}} \text{ Wb/m}^2.$$

(3): By right hand grip rule, the magnetic field due to the long wire is pointing

into the paper. To counter the magnetic field, a magnetic field pointing out of the paper is required, which requires the current passing *counter – clockwise*. Moreover, the strength of the magnetic field produced  $= \frac{\mu I}{r}$ .

Solving

$$\frac{\mu I}{0.10} = \frac{\mu \cdot 15.7}{2 \cdot 3.14 \cdot 0.20}$$

$$I = \span style="border: 1px solid black; padding: 0 5px;">1.25$$