

Q1(1):

The distance travelled=The area under the $v - t$ graph

$$\begin{aligned} &= \frac{1}{2}v_1t_1 + \frac{(v_2+v_1)(t_2-t_1)}{2} \\ &= \boxed{\frac{v_1t_2 - v_2t_1 + v_2t_2}{2}}. \end{aligned}$$

Q1(2):

The change in internal energy= $\frac{3}{2}P(V_2 - V_1)$.

The work done= $P(V_2 - V_1)$.

By the first law of thermodynamics, we have the heat required

$$= \frac{3}{2}P(V_2 - V_1) + P(V_2 - V_1) = \boxed{\frac{5}{2}P(V_2 - V_1)}.$$

Alternative The molar heat capacitor of monoatomic ideal gas under constant pressure is given by $\frac{5}{2}R$.

As $T \propto V$ under constant pressure, we have $\Delta T = T_0(\frac{V_2}{V_1} - 1)$.

Moreover, by $pV = nRT$, we have $T_0 = \frac{pV_1}{R}$.

$$\text{Given the above, } Q = (\frac{5}{2}R)(\frac{pV_1}{R})(\frac{V_2}{V_1} - 1) = \boxed{\frac{5}{2}P(V_2 - V_1)}.$$

Q1(3):

When $t = 0$, the acceleration of the block is maximum with the direction opposite to the stretch.

After the speed reaches the maximum $v = \omega d$, it starts to move in the positive

direction and so on.

Therefore, the correct graph is $\boxed{(b)}$.

Q1(4):

Consider the balance of force: The compression of the spring=The electric force.

$$kd = \frac{1}{4\pi\epsilon_0} \frac{qQ}{(l+d)^2}$$

$$Q = \frac{4\pi\epsilon_0}{q} kd(l+d^2)$$

Q1(5):

The angle of infraction= $90^\circ - \theta$. By considering the trigonometric ratio, we have $\sin(90^\circ - \theta) = \frac{d}{\sqrt{h^2+d^2}}$.

Let ϕ be the angle of refractive, by considering the trigonometric ratio, we have

$$\sin \phi = \frac{d-x}{\sqrt{h^2+(d-x)^2}}.$$

By Snells' law, we have $\frac{d}{\sqrt{h^2+d^2}} = n(\frac{d-x}{\sqrt{h^2+(d-x)^2}})$, i.e. $n = \boxed{\frac{d}{d-x} \sqrt{\frac{h^2+(d-x)^2}{h^2+d^2}}}$.

Q2:

(1): By the defination of capacitance, we have $Q = \boxed{CV}$.

(2): The electric field strength is given by $E = \boxed{\frac{V}{d}}$.

(3): We have $C = \frac{\epsilon_r S}{d}$. As $C = \frac{(1)S}{d}$, we have the surface area of the plate $S = Cd$.

Therefore, we have $C_1 = \frac{\epsilon(Cd)}{\frac{d}{2}} = \boxed{2\epsilon C}$.

(4): Similar to (3), the capacitance $C_2 = 2C$.

Therefore, the equivalent capacitance $= \frac{1}{\frac{1}{2\epsilon C} + \frac{1}{2C}} = \boxed{\frac{2\epsilon}{\epsilon + 1} C}$.

(5): Similar to what we did above, we split the capacitor into two capacitors in parallel.

Then, the capacitances of the two capacitors are $\frac{\epsilon_1 \frac{S}{2}}{d} = \frac{1}{2}\epsilon_1 C$ and $\frac{\epsilon_2 \frac{S}{2}}{d} = \frac{1}{2}\epsilon_2 C$ respectively.

Then, the equivalent capacitance $= \frac{1}{2}\epsilon_1 C + \frac{1}{2}\epsilon_2 C = \boxed{\frac{\epsilon_1 + \epsilon_2}{2} C}$.

Q3:

(1): Set the GPE as 0 at the height of point A.

The height at the position $= R \cos \theta$. Therefore, the GPE at the position $= -mgR(1 - \cos \theta)$.

Consider the conservation of energy: KE+GPE=KE+GPE

$$0 + 0 = \frac{1}{2}mv^2 - mgR(1 - \cos \theta)$$

$$v = \boxed{\sqrt{2gR(1 - \cos \theta)}}$$

(2): The component of the weight in the direction perpendicular to the motion= $\boxed{mg \cos \theta}$.

As the ball is performing circular motion, we have the balance of force: Centripetal force=(The component)-(Normal force)

$$\frac{mv^2}{r} = mg \cos \theta - N$$

$$N = mg \cos \theta - \frac{m(\sqrt{2gR(1 - \cos \theta)})^2}{R} = \cos \theta = \boxed{mg(3 \cos \theta - 2)}$$

(3): The ball leaves the hemisphere when the normal force=0, i.e.

$$mg(3 \cos \theta_B - 2) = 0$$

$$\cos \theta_B = \boxed{\frac{2}{3}}$$

(4): Consider the conservation of energy: KE+GPE=KE+GPE

$$0 + 0 = \frac{1}{2}mv^2 - mgR$$

$$v = \boxed{\sqrt{2gR}}$$

(5): By (1) and (3), the speed of the ball at the point B

$$= \sqrt{2gR(1 - \frac{2}{3})} = \sqrt{\frac{2}{3}gR}.$$

$$\text{The horizontal component} = \sqrt{\frac{2}{3}gR} \cos \theta_B = \sqrt{\frac{2}{3}gR} \frac{2}{3} = \sqrt{\frac{8}{27}gR}.$$

After the ball left the hemi-sphere, it undergoes a projectile motion, where the horizontal acceleration is 0.

$$\text{Therefore, the horizontal velocity at C=That at B} = \boxed{\sqrt{\frac{8}{27}gR}}.$$

Q4:

(1): As T is directly proportional to pV under constant number of moles, we

have $T_A = \boxed{\frac{1}{3}T_0}$.

(2): The change in internal energy in the process

$$\Delta U = \frac{3}{2}(3p_0)(V_0) - \frac{3}{2}p_0V_0 = 3p_0V_0 = RT_0.$$

As the volume remains constant, there is no work done by the gas.

Therefore, by the first law of thermodynamics, we have $Q = \Delta U + W_{gas} = \boxed{RT_0}$.

Alternative The molar heat capacity for fixed volume is given by $\frac{3}{2}R$. There-

fore, the heat absorbed $= \frac{3}{2}R(T_0 - \frac{1}{3}T_0) = \boxed{RT_0}$.

(3): As the change in internal energy during the process $= 0$, by the first law

of thermodynamics, we have $W_{gas} = Q - \Delta U = \boxed{Q_0}$.

(4): The work done by the gas = The signed area under the $p - V$ graph

$$= p_0(V_0 - 3V_0)$$

$$= -2p_0V_0$$

$$= \boxed{-\frac{2}{3}T_0}.$$

(5): As the gas back to its initial state after the whole process, the net change

in internal energy $= 0$.

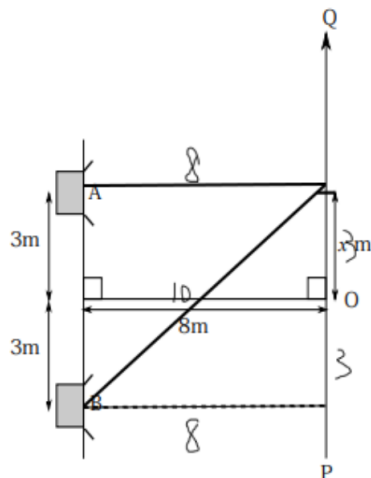
As the net work done by gas is given by the signed area bounded in the $p - V$ graph, where is greater than 0 in this process, we have $W > 0$.

Now, by the first law of thermodynamics, we have $Q = W > 0$.

Therefore, $\boxed{W > 0, Q > 0}$.

Q5:

(1): Refer to the graph:



A minimum sound is heard at 3 m, which implies a destructive interference occurs there.

Therefore, we have the path difference $= \frac{1}{2}\lambda$, i.e. $10 - 8 = \frac{1}{2}\lambda$, i.e. $\lambda = \boxed{4 \text{ m}}$.

(2): By $v = f\lambda$, we have $f = \frac{v}{\lambda} = \frac{3.4 \times 10^2}{4} = \boxed{8.5 \times 10^1 \text{ Hz}}$.

(3): When f increases, λ decrease as the speed of wave is constant.

As the observer heard the minimum again, the second destructive interference occur at $x = 3 \text{ m}$.

Therefore, we have $2 = \frac{3}{2}\lambda$, $\lambda = \frac{4}{3} \text{ m}$, i.e. $f = \frac{3.4 \times 10^2}{\frac{4}{3}} \approx \boxed{2.6 \times 10^2 \text{ Hz}}$.

(4): As temperature increases, the density of the air increases. As sound waves spread via the vibration of air particles, the speed of the sound wave is hence increased. Therefore, λ is also increased as f is fixed.

Then, the path difference required for destructive interference to occur will be increased and hence the value of x will also increase.