

Q1(1):

Consider the whole system and each object respectively, we have:

$$\begin{cases} F = 6ma \\ F - T_1 - T_2 = 3ma \\ T_2 - T_1 = 2ma \\ T_1 = ma \end{cases}$$

Therefore, $T_1 = \frac{1}{6}F$ and $T_2 = \frac{1}{3}F + T_1 = \frac{1}{2}F$. $\boxed{(d)}$

Q1(2):

Let u_A, u_B, v_A and v_B be the velocity of A and B before and after collision respectively. Note that $u_B = v_A = 0$.

By the conservation of momentum, we have $mu_A + 3m(0) = m(0) + 3mv_B$, i.e.

$$v_B = \frac{1}{3}u_A.$$

$$\text{Therefore, the coefficient of restitution} = -\frac{v_A - v_B}{u_A - u_B} = -\frac{-\frac{1}{3}u_A}{u_A} = \boxed{\frac{1}{3}}.$$

Note: The information h is misleading.

Q1(3):

We have the initial capacitance of the capacitor $C = \frac{\epsilon_0 S}{d}$ and the capacitance after the action $C' = \frac{\epsilon_0 S}{d + \Delta d}$.

Moreover, the number of charges stored in the capacitor $= CV = \frac{\epsilon_0 SV}{d}$.

As the internal energy U is given by $\frac{Q^2}{2C}$, for constant Q , we have

$$W = \Delta U = \frac{Q^2}{2} \Delta \frac{1}{C}.$$

$$\text{As } \Delta \frac{1}{C} = \frac{d+\Delta d}{\epsilon_0 S} - \frac{d}{\epsilon_0 S} = \frac{\Delta d}{\epsilon_0 S}, \text{ we have } W = \frac{(\frac{\epsilon_0 S V}{d})^2}{2} \left(\frac{\Delta d}{\epsilon_0 S} \right) = \boxed{\frac{\epsilon_0 S V^2}{2 d^2} \Delta d}.$$

Q1(4):

When $t = 2 \text{ s}$, the wave has travelled $0.3 \cdot 2 = 0.6 \text{ m}$. Therefore, the 0.30 m-0.60 m section has reflected and the 0 m-0.3 m section has been travelled to 0.6 m-0.9 m.

For the reflected wave, it is up-side-down. Therefore, superposition happens and the amplitude of the section becomes twice. Therefore, the graph is \boxed{d} .

Q1(5):

The work done by the gas = The area bounded = $\frac{1}{2}(2P_0 - P_0)(2V_0 - V_0) = \frac{1}{2}P_0V_0$.

As the gas goes back to the initial state after the whole process, by the first law of thermodynamics, the net thermal energy added = the work done by the gas = $\boxed{\frac{1}{2}P_0V_0}$.

Q2:

(1): The electric field by the charge at A on $C = \frac{kq}{2a^2}$ ($N45^\circ E$).

The electric field by the charge at B on $C = \frac{kq}{2a^2}$ ($N45^\circ W$).

Consider the vector sum, as the angle between two vectors = 90° , the net electric

$$\text{field} = \sqrt{\left(\frac{kq}{2a^2}\right)^2 + \left(\frac{kq}{2a^2}\right)^2} = \boxed{\frac{kq}{\sqrt{2}a^2}}.$$

(2): The electric potential by the charge at A at $C = \frac{kq}{\sqrt{2}a}$.

The electric field by the charge at B at $C = \frac{kq}{\sqrt{2}a}$.

Therefore, the electric potential at $C = \boxed{\frac{\sqrt{2}kq}{a}}$.

(3): By (1), the electric field strength of the electric field produced by the two charges $= \frac{kq}{\sqrt{2}a^2}$.

Therefore, by $F = qE$, we have $F = \boxed{\frac{kq^2}{\sqrt{2}a^2}}$.

(4): By (2), the electric potential at $C = \frac{\sqrt{2}kq}{a}$. Therefore, the electric potential energy of the charge at $C = -\frac{\sqrt{2}kq^2}{a}$.

Moreover, similarly, the electric potential energy of the charge at $O = -\frac{2kq^2}{a}$.

Consider the conservation of energy: KE+EPE=KE+EPE

$$0 - \frac{\sqrt{2}kq^2}{a} = \frac{1}{2}mv^2 - \frac{2kq^2}{a}$$

$$v = \boxed{\sqrt{\frac{2(2 - \sqrt{2})kq^2}{ma}}}$$

(5): Similar to (4), consider the conservation of energy, we have

$$\frac{1}{2}mv_0^2 - \frac{\sqrt{2}kq^2}{a} = 0 + 0$$

$$v_0 = \boxed{\sqrt{\frac{2\sqrt{2}kq^2}{ma}}}$$

Q3:

(1): Consider the conservation of momentum, we have $mv = mv_a + 3mv_b$, i.e.

$$v_a + 3v_b = v \dots (1).$$

Moreover, as the collision is elastic, the coefficient of restitution $= \frac{v_b - v_a}{v} = 1$, i.e.

$$v_b - v_a = v \dots (2).$$

(1)+(2): $4v_b = 2v$, i.e. $v_b = \frac{v}{2}$.

Therefore, $v_a = \boxed{-\frac{v}{2}}$.

Note: The second equation can also be replaced by the conservation of kinetic energy, i.e. $\frac{1}{2}mv^2 = \frac{1}{2}mv_a^2 + \frac{1}{2}mv_b^2$, but the solving will be a bit clumsy.

(2): By the calculation in (1), $v_b = \boxed{\frac{v}{2}}$.

(3): Consider the conservation of energy: KE+EPE=KE+EPE

$$\frac{1}{2}(3m)\left(\frac{v}{2}\right)^2 + 0 = 0 + \frac{1}{2}kl^2$$

$$l = \boxed{\sqrt{\frac{3mv^2}{4k}}}$$

(4): By (3), the amplitude of the SHM $= \sqrt{\frac{3mv^2}{4k}}$.

As the maximum velocity $= A\omega = \frac{v}{2}$, we have $\omega = \sqrt{\frac{k}{3m}}$.

Therefore, as $\omega = \frac{2\pi}{Period}$, we have $Period = 2\pi\sqrt{\frac{3m}{k}}$.

Hence, $T = \frac{Period}{4} = \boxed{\frac{\pi}{2}\sqrt{\frac{3m}{k}}}$.

(5): We have $x = A \sin \omega t = l \sin \frac{\pi}{2T}t$.

When $t = \frac{T}{2}$, $x = l \sin \frac{\pi}{4} = \boxed{\frac{l}{\sqrt{2}}}$.

Q4:

(1): By $PV = nRT$, we have $P = \frac{\rho}{m}RT$. Therefore, $\rho = \boxed{\frac{mP}{RT}}$.

(2): By Archimedes' principle, we have $F = \rho Vg = \boxed{\frac{PVmg}{RT_0}}$.

(3): The balloon starts rising when the buoyancy balance the weight of the balloon (including the air inside), i.e.

$$\frac{PVmg}{RT_0} = \frac{PVmg}{RT_1} + Mg$$

$$T_1 = \boxed{\frac{mPVT_0}{mPV - MRT_0}}$$

(4): By (3), $T_1 = \frac{2.9 \times 10^{-2} \cdot 1.0 \times 10^5 \cdot 3.0 \times 10^3 \cdot 3.0 \times 10^2}{2.9 \times 10^{-2} \cdot 1.0 \times 10^5 \cdot 3.0 \times 10^3 - 5.0 \times 10^2 \cdot 8.3 \cdot 3.0 \times 10^2}$
 $\approx \boxed{3.5 \times 10^2}$.

Note: As a range of error is allowed, we can compute the power of 10 first and calculate the numerical digits by do approximations like $2.9 = 3$, $R = 8$, etc.

Q5:

(1): The path difference= $|d_1 - d_2|$.

As a maximum intensity is heard, the first constructive interference occurs, i.e.

$$|d_1 - d_2| = \lambda.$$

Therefore, $f = \frac{v}{\lambda} = \boxed{\frac{v}{|d_1 - d_2|}}.$

(2): The general form of Doppler effect is given by $f_{observed} = \frac{V - v_{observer}}{V - v_{source}} f.$

As the source is moving in the direction opposite to the propagation of wave,

we have $f_{observed} = \boxed{\frac{v}{v + u} f}.$

(3): The frequency of beat is given by $|f_1 - f_2| = \frac{u}{v + u} f$

Therefore, the period of beat $= \frac{1}{f} = \boxed{\frac{v + u}{uf}}.$

(4): Consider the cosine ratio, we have $\cos \angle S_1 O S_2 = \frac{d_1}{d_2}.$ Therefore, the velocity of S_2 in the direction opposite to the propagation of wave $= u \cos \angle S_1 O S_2 = \frac{ud_1}{d_2}.$

The observed frequency of $S_2 = \frac{v}{v + \frac{ud_1}{d_2}} f = \frac{d_2 f}{ud_1 + vd_2}.$

Therefore, the frequency of beat $= \left| \frac{d_2 f}{ud_1 + vd_2} - \frac{v}{v + u} f \right| = \boxed{\frac{(d_2 - d_1)uvf}{(u + v)(d_2v + d_1u)}}.$