

Q1:

(1): The component of the weight in the direction of the slope

$$=mg \sin 30^\circ = 19.6 \text{ N}.$$

As the body is at rest, the forces are balance, i.e.  $T = \boxed{19.6} \text{ N}$ .

(2): As calculated in (1), the magnitude of the net force is 19.6 N.

By  $F = ma$ , the magnitude of the acceleration is  $\frac{19.6}{4.0} = \boxed{4.9} \text{ m/s}^2$ .

**Alternative** The acceleration is the gravitational acceleration in the direction of the slope. Therefore, its magnitude is  $g \sin 30^\circ = \boxed{4.9} \text{ m/s}^2$ .

(3): By  $v^2 - u^2 = 2as$ , we have  $v = \sqrt{2 \cdot 4.9 \cdot 5} = \boxed{7} \text{ m/s}$ .

**Alternative** Set the GPE at the initial height be 0. By the conservation of energy: KE+GPE=KE+GPE, we have

$$0 + 0 = \frac{1}{2}mv^2 - mg(5.0 \cdot \sin 30^\circ)$$

$$v = \sqrt{2 \cdot 9.8 \cdot 2.5} = \boxed{7}$$

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Q2:

(1): As the coefficient of restitution is 0.50, we have  $-\frac{v_A - v_B}{10 - (-4.0)} = 0.5$ , i.e.

$$v_A = v_B - 7.$$

By the conservation of momentum, we have  $2.0 \cdot 10 + 4.0 \cdot (-4.0) = 2.0v_A + 4.0v_B$ ,

i.e.  $v_A = 2 - 2v_B$ .

Solving, we have  $v_A = \boxed{-4}$  and  $v_B = \boxed{3}$ .

$$\begin{aligned} (2): & \left( \frac{1}{2} \cdot 2.0 \cdot (10)^2 + \frac{1}{2} \cdot 4.0 \cdot (-4)^2 \right) - \left( \frac{1}{2} \cdot 2.0 \cdot (-4)^2 + \frac{1}{2} \cdot 4.0 \cdot (3)^2 \right) \\ &= \boxed{98} \text{ J} \end{aligned}$$


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Q3:

(1): There is no pressure difference between the confined gas and the atmosphere, i.e. the pressure of the confined gas is  $1.0 \times 10^5 \text{ Pa}$ .

$$\text{By } pV = nRT, V = \frac{nRT}{p} = \frac{0.10 \cdot 8.3 \cdot 300}{1.0 \times 10^5} = \boxed{24.9 \times 10^{-4}} \text{ m}^3.$$

(2): The compression of the spring is the force due to the pressure difference  
( $F = kx = 500 \cdot 0.20 = 100 \text{ N}$ ).

$$\text{Therefore, } (p - p_0)S = (p - 1.0 \times 10^5) \cdot 1.0 \times 10^{-3} = 100, \text{ i.e. } p = \boxed{2.0 \times 10^5} \text{ Pa}.$$

(3):

$$\begin{aligned} \frac{p_1 V_1}{T_1} &= \frac{p_2 V_2}{T_2} \\ \frac{1.0 \times 10^5 \cdot 24.9 \times 10^{-4}}{300} &= \frac{2.0 \times 10^5 \cdot (24.9 \times 10^{-4} + 1.0 \times 10^{-3} \cdot 0.20)}{T_2} \\ T_2 &\approx \boxed{648} \end{aligned}$$

(4): Work done by the atmosphere on the gas

$$= 1.0 \times 10^5 \cdot (-0.20 \cdot 1.0 \times 10^{-3}) = -20 \text{ J}.$$

$$\text{Work done by the spring on the gas} = -\frac{1}{2} kx^2 = -10 \text{ J}.$$

$$\text{Therefore, total work done on the gas} = -30 \text{ J and the work done by the gas} = \boxed{30} \text{ J}.$$

Q4:

$$(1): \text{Refer to the graph, } \lambda = \boxed{4.0} \text{ m}.$$

$$(2): \text{Refer to the graph, the wave travelled by } \frac{3}{4} \text{ period after } 0.30 \text{ s. Therefore, } \frac{3}{4}T = 0.30, \text{ i.e. } T = \boxed{0.40} \text{ s}.$$

$$\text{Moreover, } v = \frac{\lambda}{T} = \boxed{10} \text{ m/s}.$$

(3): The amplitude of the wave is  $1.0 \text{ m}$ . And the medium at  $x = 2.0 \text{ m}$  has a 0 phase.

$$y(t) = A \sin\left(\frac{2\pi}{T}t - \phi\right) = \boxed{\sin(5\pi t)}$$

Q5:

(1): Let  $\theta$  be the angle between the electric force due to the charge at  $x = -4L$  and the y-axis, we have  $\cos \theta = \frac{3}{5}$ .

$$\text{By symmetry, the net electric force} = 2 \cdot k \frac{qQ}{5L^2} \cos \theta = \boxed{\frac{6kqQ}{125L^2}} N.$$

(2): The electric potential due to the charge at  $x = -4L$  is  $k \cdot \frac{Q}{5L}$ .

Similarly for the charge at  $x = 4L$ .

Therefore, the electric potential =  $\boxed{\frac{2kQ}{5L}}$ .

(3): Similar to (2), the electric potential at B =  $\frac{kQ}{4L}$ .

The difference in electric potential =  $\frac{3kQ}{20L}$ .

The difference in electric potential energy =  $\frac{3kqQ}{20L}$ .

By the conservation of energy, we have

$$\Delta KE = \Delta EPE$$

$$\frac{1}{2}mv^2 = \frac{3kqQ}{20L}$$

$$v = \boxed{\sqrt{\frac{3kqQ}{10mL}}}$$

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Q6:

(1): By Ohm's law,  $V = IR$ ,  $I = \frac{V}{R} = \frac{1.5}{5.0} = \boxed{0.3} \text{ A}$ .

(2):  $F = BIL = 3.0 \cdot 0.3 \cdot 0.2 = \boxed{0.18} \text{ N}$ .

(3):  $\Phi = BA = Blx$ .

$$\frac{d\Phi}{dt} = Bl \cdot \frac{dx}{dt} = Blv.$$

By Faraday's law,  $E = \frac{d\Phi}{dt} = 3.0 \cdot 0.20 \cdot 1.5 = \boxed{0.9} \text{ V}$ .

(4): The induced EMF is in clockwise direction by Fleming's right hand rule.

Therefore, the equilibrium voltage across the circuit  $= 1.5 - 0.9 = 0.6 \text{ V}$ .

By Ohm's law,  $V = IR$ ,  $I = \frac{V}{R} = \frac{0.6}{5.0} = \boxed{0.12} \text{ A}$ .