

1) CONDITION BASED EVALUATION OF EXPO EXPRESSIONS :

(1) If $2^x \cdot 4^y = 32$ and $\frac{3^x}{9^y} = 3$, then $\frac{5^x}{125^y} =$.

(2) If $\frac{2^x - 2^{-x}}{2^x + 2^{-x}} = \frac{1}{3}$, then $x =$

2. Take a point $P(a, e^{-a})$ ($a > -1$) on the curve $C: y = e^{-x}$. Let $S(a)$ be the area of the triangle surrounded by the tangent line to C at P , the x -axis and the y -axis.

- (1) Let X denote 2^x . Express y in terms of X .
- (2) Calculate the local maximum and minimum of y , and the values of X in (1) at which y attains them.
- (3) Calculate the global maximum and minimum of y in the interval $0 \leq x \leq \log_2 7$, and the values of x at which y attains them.

(1) $y =$

(2) The local maximum is $\textcircled{1}$ at $X = \textcircled{2}$;

the local minimum is ③ at $X =$ ④.

(3) The global maximum is $\boxed{\textcircled{1}}$ at $x = \boxed{\textcircled{2}}$;

the global minimum is ③ at $x =$ ④.

3) EXPO AS EQUATIONS :

(2) The real-number solution to the equation $2^{x+2} - 2^{-x} + 3 = 0$ is

$$x = \boxed{}.$$

LOGARITHMS :

1) EVALUATION OF LOG EXPRESSIONS :

2007 Q1 *

$$(3) \quad 4 \log_2 \sqrt{2} - \frac{1}{2} \log_2 3 + \log_2 \frac{\sqrt{3}}{2} = \boxed{}.$$

2012 Q1 **

$$(1) \text{ If } k = \frac{\log_7 9}{\log_7 4}, \text{ then } 2^{5k} = \boxed{}.$$

2013 Q1 *

$$(5) \text{ If } 3^x = 2^y = 5, \text{ then } \frac{1}{x} + \frac{1}{y} = \log_5 \boxed{}.$$

2015 Q1 *

$$(3) \text{ If } y = \log_2(x + \sqrt{x^2 + 1}), \text{ then } 2^y - 2^{-y} = \boxed{} x.$$

2017 Q1 *

$$(1) \quad \log_{10} \frac{4}{5} + 2 \log_{10} 5\sqrt{5} = \boxed{}.$$

2020 Q1 **

(1) The largest one among natural numbers that are less than

$$\log_2 3 \cdot \log_3 4 \cdot \log_4 5 \cdots \cdots \log_{2019} 2020$$

is .

2) LOGARITHM AND INEQUALITIES :

2008 Q1 *

(3) The solution of the inequality $\log_2(x+1) \leq 3$ is $\{ \text{①} < x \leq \text{②} \}$.

2014 Q1 *

(4) The solution to the inequality $\log_2 x + \log_2(x-2) < 4 \log_{16} 8$, in the set of real numbers, is $\text{①} < x < \text{②}$.

3) LOGARITHMS AND EQUATIONS :

2015 Q1 **

(1) If the equation $\log_{10}(ax) \log_{10}(bx) + 1 = 0$ with $a > 0, b > 0$ constants has a solution $x > 0$, it follows that $\frac{b}{a} \geq \text{①}$
or $\text{②} \geq \frac{b}{a} > \text{③}$.

2016 Q1 *

(1) If $\log_3 6 - \log_9 x = \frac{1}{2}$, then $x =$.

4) LOGARITHMS AS FUNCTIONS :

2010 Q7 *** partial presence only

2015 Q1 **

- (4) The function $f(x) = \log_2(\log_3(\log_2(\log_3(\log_2 x))))$ has the interval $x > \boxed{}$ as its maximum domain on real numbers.

5) FINDING THE NUMBER OF DIGITS AND LEADING DIGIT :

2019 Q1 **

- (6) By $\log_{10} 2 \approx 0.3010$ and $\log_{10} 3 \approx 0.4771$, the number of digits of 6^{100} is $\boxed{\textcircled{1}}$, and its leading digit is $\boxed{\textcircled{2}}$.

6) OTHER TYPES OF LOG EXERCISES :

2020 Q1 **

- (1) The largest one among natural numbers that are less than

$$\log_2 3 \cdot \log_3 4 \cdot \log_4 5 \cdot \dots \cdot \log_{2019} 2020$$

is $\boxed{}$.

Level 1: No unknown variables, straightforward answer, mobilizes one concept at once*

Level 2: Inclusion of unknown variables which calls for more analysis, various conditions, domains rather than specific answers, mobilizes two to three concepts at once **

Level N: When the concept has partial presence***

Logarithms and exponentials have more presence than trigonometry, there was no presence of expo as inequalities, might appear next year,?