

Q1:

(a) The normal reaction of the object by the ground, R =The weight of the object= $mg = 10 \cdot 9.8 = 98 \text{ N}$. Then, by $f_{max} = \mu R$, we have the maximum kinetic friction= $0.50 \cdot 98 = \boxed{49 \text{ N}}$.

(b) By $F = ma$, the deceleration of the object= $\frac{f_{max}}{m} = \frac{49}{10} = 4.9 \text{ m/s}^2$ (hence the acceleration $a = -4.9 \text{ m/s}^2$). Then, as the object is performing uniform acceleration motion, by $\frac{v-v_0}{t} = a$, the time required for the object to stop= $t = \frac{0-49}{-4.9} = \boxed{10 \text{ s}}$.

(c) The total energy lost=The kinetic energy lost= $\frac{1}{2}mv_0^2 = \frac{1}{2} \cdot 10 \cdot 49^2 = 12005 \text{ J}$. As 70% of it is turned to heat, the amount of heat= $70\% \cdot 12005 = 8403.5 \text{ J} = 8403.5 \cdot \frac{1}{4.2} \text{ cal} = \boxed{\frac{12005}{6} \text{ cal}}$.

Q2:

(a) The required acceleration=The magnitude of the component of the gravitational acceleration in the direction of the motion= $\boxed{g \sin \theta \text{ m/s}^2}$

(b) As the object is stationary relative to the plane, the acceleration of the motion of the object is 0 m/s^2 relative to the plane.

The magnitude of the horizontal component of the acceleration of the motion of the object= $g \sin \theta \cos \theta \text{ m/s}^2$. Hence, the acceleration of the motion of the object relative to the plane= $|g \sin \theta \cos \theta - a| \text{ m/s}^2$. Therefore, we have $|g \sin \theta \cos \theta - a| = 0$, which yields $a = \boxed{g \sin \theta \cos \theta \text{ m/s}^2}$.

Q3:

(a) By $pV = nRT$, T is directly proportional to pV . From the graph, obviously, pV is highest at (3). Hence, T_3 is the highest.

On the other hand, the process (1) \rightarrow (2) is an adiabatic compression, where the temperature increases. Hence, we have $T_1 < T_2$.

Combining the above, we have $T_1 < T_2 < T_3$.

(b) As the process (2) \rightarrow (3) has fixed pressure, we have $\frac{V_2}{T_2} = \frac{V_3}{T_3}$, i.e. $V_3 = \frac{T_3}{T_2} V_2$, where V_2 and V_3 are the volume of the gas at (2) and (3) respectively.

Now, the work done by the gas $= p\Delta V = p_2(V_3 - V_2) = p_2 V_2 (\frac{T_3 - T_2}{T_2})$, where p_2 is the pressure at (2). As $p_2 V_2 = nRT_2 = RT_2$, the work done $= RT_2 \frac{T_3 - T_2}{T_2} =$

$$\boxed{R(T_3 - T_2) \text{ J}}.$$

(c) For an adiabatic process, we have $pV^\gamma = \text{Constant}(C)$, where $\gamma = \frac{5}{3}$ for a monoatomic gas. Then, we have $p = CV^{-\frac{5}{3}}$. The work done by the gas $= \int_{V_1}^{V_2} CV^{-\frac{5}{3}} dV = -\frac{3}{2} CV^{-\frac{2}{3}} \Big|_{V_1}^{V_2} = -\frac{3}{2} C(V_2^{-\frac{2}{3}} - V_1^{-\frac{2}{3}})$, where V_1 and V_2 are the volume of the gas at (1) and (2) respectively. As $C = p_1 V_1^{\frac{5}{3}} = p_2 V_2^{\frac{5}{3}}$, where p_1 and p_2 are the pressure at (1) and (2) respectively, we have the work done by

$$\text{the gas} = -\frac{3}{2} (p_2 V_2^{\frac{5}{3}} V_2^{-\frac{2}{3}} - p_1 V_1^{\frac{5}{3}} V_1^{-\frac{2}{3}}) = -\frac{3}{2} (p_2 V_2 - p_1 V_1) = -\frac{3}{2} (nRT_2 - nRT_1) = \boxed{\frac{3}{2} R(T_1 - T_2) \text{ J}}.$$

Alternative: By $W = \frac{nR}{\gamma-1}(T_1 - T_2)$, where $\gamma = \frac{5}{3}$ for a monoatomic gas, we have the work done by the gas $= \frac{R}{\frac{5}{3}-1}(T_1 - T_2) = \boxed{\frac{3}{2} R(T_1 - T_2) \text{ J}}.$

Q4:

(a) By the definition of the refractive index, $n = \frac{c}{v}$, we have $v_{water} = \frac{1}{n}c$. Hence the speed of light in water is $\boxed{\frac{1}{n}}$ times that in vacuum.

(b) When the angle of incidence is equal to the critical angle, the angle of refraction is equal to 90° . By $n_1 \sin \theta_1 = n_2 \sin \theta_2$, we have $n \sin \theta = 1 \sin 90^\circ$. Hence, $\sin \theta = \boxed{\frac{1}{n}}$.

(c) Let d be the distance between the coin and the point of refraction. Then, by some geometry, we have $\tan(90^\circ - i) = \frac{h}{d}$ and $\tan r = \frac{d}{h'}$. Multiply the two equations together, we have $\frac{h}{h'} = \tan(90^\circ - i) \tan r = \frac{\tan r}{\tan i}$. By small angle approximation, $\frac{\tan r}{\tan i} \approx \frac{\sin r}{\sin i} = \frac{1}{n}$. Therefore, we have $\frac{h'}{h} = \boxed{n}$.

Q5:

(a) By Kirchoff's law, we have $\boxed{I_1 + I_3 = I_2}$.

(b) The voltage across the circuit $= 6 - 5 = 1 \text{ V}$ anti-clockwise. Hence the current flow through R_1 is in the direction $\boxed{\leftarrow}$.

(c) As there became no current flow through R_1 , there is no voltage across R_1 . Hence the voltage of E_1 and E_x cancelled each other, i.e. $E_x = E_1 = \boxed{5 \text{ V}}$.

Q6:

(a) The magnitude of the component of the velocity in the y direction (i.e. the

direction perpendicular to the B-field) $=v \sin \theta$ m/s. By $F = Bqv$, the Lorentz force $=B \cdot e \cdot v \sin \theta = \boxed{Bev \sin \theta \text{ N}}$.

(b) The electron is performing uniform circular motion in the y-z plane. The magnitude of the centripetal force is given by $F_c = \frac{m(v \sin \theta)^2}{r} = \frac{mv^2 \sin^2 \theta}{r}$, where r is the radius of the circular path, i.e. the radius of the helicoid. Note that the centripetal force is provided completely by the Lorentz force. Hence we have

$$\frac{mv^2 \sin^2 \theta}{r} = Bev \sin \theta \text{ and the required radius } r = \boxed{\frac{mv \sin \theta}{Be} m}.$$

(c) The angular velocity of the circular motion $=\omega = \frac{v \sin \theta}{r} = \frac{v \sin \theta}{\frac{mv \sin \theta}{Be}} = \frac{Be}{m}$.

After 1 period, the electron returns to the x-axis. Hence, the required time $=T =$

$$\frac{2\pi}{\omega} = \frac{2\pi}{\frac{Be}{m}} = \boxed{\frac{2\pi m}{Be} \text{ s}}.$$