2) Nysikm 1. $A = \|\cos\theta - i\sin\theta\|$ | $i\sin\theta - \cos\theta\|$ (1) e.g.: det (A - \(\lambda I \rangle = 0 \) $\begin{vmatrix} \omega s \theta - \lambda & -i \sin \theta \\ -i \sin \theta & -\cos \theta - \lambda \end{vmatrix} = (\cos \theta - \lambda)(-\cos \theta - \lambda) - (-i \sin \theta)(i \sin \theta) =$ $= -\left(\cos^2\theta - \lambda^{\lambda}\right) + i^2 f_{ih}^2 \theta = -\cos^2\theta + \lambda^2 - f_{ih}^2 \theta = \lambda^2 - 1 = 0 = \begin{cases} \lambda_1 = 1 & \text{cootenben-}\\ \lambda_2 = -1 & \text{ventry} \end{cases}$ The cootenber of the parameter of the cootenber of the coote 1) $\lambda_1 = 1$: $\begin{vmatrix} \cos \theta - 1 & -i \sin \theta \\ i \sin \theta & -\cos \theta - 1 \end{vmatrix} = \begin{vmatrix} \psi_1^1 \\ \psi_2^2 \end{vmatrix} = \begin{vmatrix} \psi_1^2 \\ \psi_1^2 \end{vmatrix}$ $(\omega \theta - 1) \psi_1^1 - i \sin \theta \psi_1^2 = 0.$ 1 Nymb $\psi_1^1 = 1 \Rightarrow \cos\theta - 1 = i\sin\theta \psi_1^2 \Rightarrow \psi_1^2 = \frac{\cos\theta - 4}{i\sin\theta} = i\frac{(1 - \cos\theta)}{\sin\theta}$ $|\vec{\psi}_1| = |\vec{\psi}_1| = |\vec{\psi}_1| = |\vec{\psi}_2| = |\vec{\psi}_1| = |\vec{\psi}_1|$ $= \sqrt{1 + \frac{1 - 2 \cos \theta + 1 - \sin^2 \theta}{\sinh^2 \theta}} = \sqrt{1 + \frac{2}{\sinh^2 \theta}} - \frac{2 \cos \theta}{\sinh^2 \theta} \left(\frac{\sinh^2 \theta}{\sinh^2 \theta} \right) = \sqrt{\frac{2(1 - \cos \theta)}{\sin^2 \theta}}$ Таким огразом, отмеримрованный Уз имеет вид: $|\psi_{1}| = \frac{\sinh \theta}{\sqrt{2(1-\cos \theta)}} \cdot || \frac{1}{i \frac{(1-\cos \theta)}{\sin \theta}} || = || \frac{\sinh \theta}{\sqrt{2(1-\cos \theta)}} ||$

2)
$$\lambda_{2} = -4$$
 $\|\cos\theta + 4\| - i\sin\theta - \cos\theta + 4\| \|\psi_{2}^{4}\| = 0$
 $|\cos\theta + 1| \psi_{2}^{4} = 1 = 7 \quad \cos\theta + 4 = i\sin\theta \cdot \psi_{2}^{2} = 0$
 $|\cos\theta + 1| \psi_{2}^{4} = 1 = 7 \quad \cos\theta + 4 = i\sin\theta \cdot \psi_{2}^{2} = 7 \quad \psi_{2}^{2} = \frac{\cos\theta + 1}{\sin^{2}\theta}$
 $|\psi_{2}| = \left\| \frac{1}{\sin^{2}\theta} + \frac{\cos^{2}\theta}{\sin^{2}\theta} + \frac{(2\cos\theta + 4)}{\sin^{2}\theta} - \frac{1}{\sin^{2}\theta} + \frac{2\cos\theta}{\sin^{2}\theta} + \frac{1}{\sin^{2}\theta} + \frac$

3uganul 1 Myukm 2.
$$e^{i\omega A} - 2 d \in \mathbb{R}$$

$$e^{3} = I + \frac{\hat{S}}{4!} + \frac{\hat{S}^{2}}{2!} + \dots, \quad A = \begin{vmatrix} \cos\theta & -i\sin\theta \\ \sin\theta & -\cos\theta \end{vmatrix}$$

$$A^{2} = \begin{vmatrix} \cos\theta & -i\sin\theta \\ i\sin\theta & -\cos\theta \end{vmatrix} = \begin{vmatrix} \cos\theta & -i\sin\theta \\ i\sin\theta & -\cos\theta \end{vmatrix} = \begin{vmatrix} \cos^{2}\theta - i^{2}\sin\theta \cdot \cos\theta \\ -i\sin\theta \cdot \cos\theta + i\sin\theta \cdot \cos\theta \end{vmatrix} = \begin{vmatrix} 10 \\ 0 \end{bmatrix}$$

$$= \begin{vmatrix} \sin\theta \cdot \cos\theta - i\sin\theta \cdot \cos\theta \\ 0 \end{vmatrix} = \begin{vmatrix} 10 \\ 0 \end{vmatrix}$$

$$A^{3} = A \cdot A^{2} = A \cdot I = A$$
Taxuu whazou, luguu, and $A^{2} = I$, $A^{2} = A$

$$= I \cdot (1 + id)^{2} \cdot \frac{A}{2!} + (id)^{2} \cdot \frac{A^{2}}{4!} + \dots + A \cdot \left(\frac{id}{3!} + \frac{(id)^{3}}{3!} + \frac{(id)^{3}}{5!} + \dots \right) = I \cdot (1 - d^{2}\frac{1}{2!} + d^{2}\frac{1}{4!} - d^{2}\frac{1}{6!} + \dots + iA \cdot \left(\frac{d}{3!} - \frac{d^{3}}{3!} + \frac{d^{5}}{5!} - \dots \right) = I \cdot \cos d + iA \cdot \sin d$$

3agajul 2.
$$A = \frac{1}{\sqrt{2}} \begin{vmatrix} 0 & -i & 0 \\ i & 0 & -i \\ 0 & i & 0 \end{vmatrix}$$

1. Haugen (.3. A. det $(A - \lambda E) = 0$: $\begin{vmatrix} -\lambda & -i \sqrt{2} & 0 \\ i \sqrt{2} & -\lambda & -i \sqrt{2} \end{vmatrix} = \frac{1}{\sqrt{2}} \begin{vmatrix} -\lambda & -i \sqrt{2} & 0 \\ i \sqrt{2} & -\lambda & -i \sqrt{2} \end{vmatrix} = \frac{1}{\sqrt{2}} \begin{vmatrix} -\lambda & -i \sqrt{2} & 0 \\ -\lambda & -i \sqrt{2} & -\lambda & -i \sqrt{2} \end{vmatrix} = \frac{1}{\sqrt{2}} \begin{vmatrix} -\lambda & -i \sqrt{2} & 0 \\ -\lambda & -i \sqrt{2} & -\lambda & -i \sqrt{2} \end{vmatrix} + \frac{\lambda}{2} = -\lambda^{3} + \frac{\lambda}{2} + \frac{\lambda}{2} = 0$

$$= -\lambda \left[\lambda^{2} + \frac{i2}{2} \right] + \frac{i}{\sqrt{2}} \cdot \frac{-i\lambda}{\sqrt{2}} = -\lambda \left(\lambda^{2} - \frac{i}{2} \right] + \frac{\lambda}{2} = -\lambda^{3} + \frac{\lambda}{2} + \frac{\lambda}{2} = 0$$

$$= -\lambda \left[\lambda^{2} + \frac{i2}{2} \right] + \frac{i}{\sqrt{2}} \cdot \frac{-i\lambda}{\sqrt{2}} = 0 \Rightarrow \lambda \left(\lambda^{2} - \frac{i}{2} \right) + \frac{\lambda}{2} = -\lambda^{3} + \frac{\lambda}{2} + \frac{\lambda}{2} = 0$$

$$= -\lambda \left[\lambda^{2} + \frac{i2}{2} \right] + \frac{i}{\sqrt{2}} \cdot \frac{-i\lambda}{\sqrt{2}} = 0 \Rightarrow \lambda \left(\lambda^{2} - \frac{i}{2} \right) + \frac{\lambda}{2} = -\lambda^{3} + \frac{\lambda}{2} + \frac{\lambda}{2} = 0$$

$$= -\lambda \left[\lambda^{2} + \frac{i2}{2} \right] + \frac{i}{\sqrt{2}} \cdot \frac{-i\lambda}{\sqrt{2}} = 0 \Rightarrow \lambda \left(\lambda^{2} - \frac{i}{2} \right) + \frac{\lambda}{2} = -\lambda^{3} + \frac{\lambda}{2} + \frac{\lambda}{2} = 0$$

$$= -\lambda \left[\lambda^{2} + \frac{i2}{2} \right] + \frac{i}{\sqrt{2}} \cdot \frac{-i\lambda}{\sqrt{2}} = 0 \Rightarrow \lambda^{3} = 0$$

$$= -\lambda \left[\lambda^{2} + \frac{i}{\sqrt{2}} + \frac{\lambda}{2} + \frac{\lambda}{2} + 0 \right] + 0 \Rightarrow \lambda^{3} = 0$$

$$= -\lambda \left[\lambda^{2} + \frac{\lambda}{2} + \frac{\lambda}{2} + \frac{\lambda}{2} + 0 \right] + 0 \Rightarrow \lambda^{3} = 0$$

$$= -\lambda \left[\lambda^{2} + \frac{\lambda}{2} + \frac{\lambda}{2} + \frac{\lambda}{2} + 0 \right] + 0 \Rightarrow \lambda^{3} = 0$$

$$= -\lambda \left[\lambda^{2} + \frac{\lambda}{2} + \frac{\lambda}{2} + \frac{\lambda}{2} + 0 \right] + 0 \Rightarrow \lambda^{3} = 0$$

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$$= -\lambda \left[\lambda^{2} + \frac{\lambda}{2} + \frac{\lambda}{2} + \frac{\lambda}{2} + 0 \right] + 0 \Rightarrow \lambda^{3} = 0$$

$$= -\lambda \left[\lambda^{2} + \frac{\lambda}{2} + \frac{\lambda}{2} + \frac{\lambda}{2} + \frac{\lambda}{2} + 0 \right] + 0 \Rightarrow \lambda^{3} = 0$$

$$= -\lambda \left[\lambda^{2} + \frac{\lambda}{2} + \frac{\lambda}{2} + \frac{\lambda}{2} + 0 \right] + 0 \Rightarrow \lambda^{3} = 0$$

$$= -\lambda \left[\lambda^{2} + \frac{\lambda}{2} + \frac{\lambda}{2} + \frac{\lambda}{2} + \frac{\lambda}{2} + 0 \right] + 0 \Rightarrow \lambda^{3} = 0$$

$$= -\lambda \left[\lambda^{2} + \frac{\lambda}{2} + \frac{\lambda}$$

Проверии ортого наинисть

$$\langle \vec{\psi}_{0} | \vec{\psi}_{1} \rangle = \| \vec{0} \|^{\frac{1}{2}} \| \vec{0}_{1} \|^{\frac{1}{2}} \| = \| \vec{1}_{1} \vec{0}_{1} \|^{\frac{1}{2}} \| \vec{0}_{1} \|^{\frac{1}{2}} \| = \frac{1}{52} + \frac{1}{52} = 0.$$

$$(\sqrt{10})\sqrt{10} = \|101\|$$
 $(1/\sqrt{2}) = \frac{1}{\sqrt{2}} - \frac{1}{\sqrt{2}} = 0$

$$= -\frac{1}{2} + 4 - \frac{1}{2} = 0.$$

Попарные скашерные произведения = 0 => в-ра ортогонашьно,

Pazioniume
$$|\psi\rangle = \|\frac{1}{0}\|$$
 & Saziui (.6. A)

 $|\psi\rangle = \frac{1}{12}\|\frac{1}{12}\|$; $|\psi\rangle = \frac{1$

$$\frac{1}{2} = 3aganue 2 nynum 2.$$

$$= 7 (Raimu e^{i\Theta A}), A = \begin{vmatrix} 0 & -i/52 & 0 \\ -i/52 & 0 & -i/52 \end{vmatrix}$$

$$= 7 (Raimu e^{i\Theta A}), A = \begin{vmatrix} 0 & -i/52 & 0 \\ -i/52 & 0 & -i/52 \end{vmatrix}$$

$$= 7 (Raimu e^{i\Theta A}), A = \begin{vmatrix} 0 & -i & 0 \\ 0 & 0 & -i \end{vmatrix} = \frac{1}{2} \begin{vmatrix} 1 & 0 & -i \\ 0 & 2 & 0 \end{vmatrix}$$

$$= \frac{1}{2} \begin{vmatrix} 1 & 0 & -i & 0 \\ 0 & 0 & 0 \end{vmatrix} = \frac{1}{2} \begin{vmatrix} 1 & 0 & -i \\ 0 & 2 & 0 \end{vmatrix}$$

$$= \frac{1}{2} \begin{vmatrix} 0 & -i & 0 \\ 0 & 0 & -i \end{vmatrix} = A$$

$$= \frac{1}{2} \begin{vmatrix} 0 & -i & 0 \\ 0 & 0 & -i \end{vmatrix} = A$$

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$$= \frac{1}{2} \begin{vmatrix} 0 & -i & 0 \\ 0 & 0 & -i \end{vmatrix} = A$$

$$= \frac{1}{2} \begin{vmatrix} 0 & -i & 0 \\ 0 & 0 & -i \end{vmatrix} = A$$

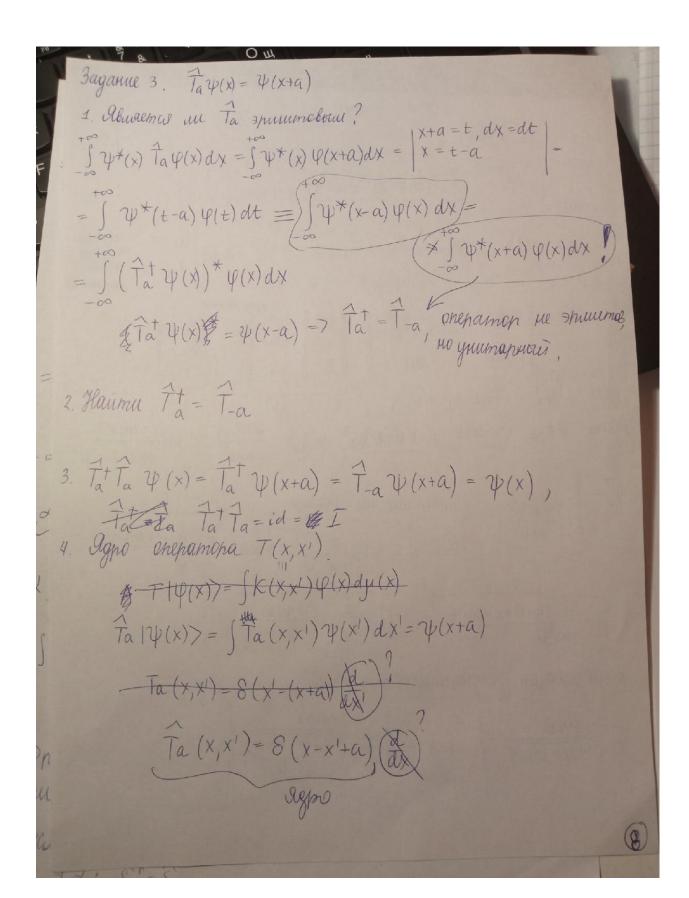
$$= \frac{1}{2} \begin{vmatrix} 0 & -i & 0 \\ 0 & 0 & -i \end{vmatrix} = A$$

$$= \frac{1}{2} \begin{vmatrix} 0 & -i & 0 \\ 0 & 0 & -i \end{vmatrix} = A$$

$$= \frac{1}{2} \begin{vmatrix} 0 & -i & 0 \\ 0 & 0 & -i \end{vmatrix} = A$$

$$= \frac{1}{2} \begin{vmatrix} 0 & -i & 0 \\ 0 & 0 & -i \end{vmatrix} = A$$

$$= \frac{1}{2} \begin{vmatrix} 0 & -i & 0 \\ 0 & 0 & -i$$



Baganue 4. $\hat{S} = \alpha \left(x^2 \frac{d}{dx} - \frac{d}{dx} x^2 \right)$ < 415 47 = (STUNE) (\$ 4 147 $\langle \Psi | \overline{S} \psi \rangle = \int \psi^*(x) \lambda \left(x^2 \frac{d}{dx} - \frac{d}{dx} x^2 \right) \psi(x) dx =$ $z = d \int \varphi(x) \left(x^2 \frac{d \varphi(x)}{dx} - d \left[x^2 \psi(x) \right] \right) dx = \int_{-\infty}^{\infty} \frac{d \psi(x)}{dx} + \psi(x) \cdot 2x dx$ $= \angle \int \psi^*(x) x^2 \frac{d \left[\psi(x) \right]}{dx} dx - \angle \int \psi^*(x) \frac{d \left[x^2 \psi(x) \right]}{dx} dx = -$ = 2 Sy*(x) x2 d[\p(x)] dx -2 Sy*(x) x2 d[\p(x)] dx dx dx dx dx dx $\Theta \times \int \varphi^*(x) \cdot \psi(x) \cdot 2x dx = -\chi \int \varphi^*(x) \cdot 2x \psi(x) dx =$ $= \left[\int d^* dx \cdot \psi(x) \right]^* \psi(x) dx$ 3+14(x)> = -2.2x.4(x) => (3+=-22x), lepto VI Эриштов оператор (шетрого - самосоры тельной) eull 5x=5, m.e. -dx = -xx*, m.e. x = x*x* elun XER mo L= L* u LER m. e. 3 d; 51 = 3

Haumu agno onenamona S(x,x') $\widehat{S}(x,x') \psi(x) = -2dx \psi(x) = \widehat{S}(x,x') \psi(x) dx' =$ $= \int (-2dx) 8(-x+x') \psi(x') dx'$ По изти, дия не равенства нумо х донтно дость павнох! Tonga egno ((-2 xx) 8 (-x + x) (2) ?

B=B¹=
$$\frac{1}{ad-bc}$$
 || $\frac{a}{c}$ $\frac{b}{d}$ || $\frac{d}{d}$ - $\frac{b}{d}$ || $\frac{1}{ad-bc}$ - $\frac{1}{ad-bc}$ || $\frac{1}{ad-bc}$ ||

3aganue 6. <41Â4>=<Â+414> Dakazamb: (AB) += B+A+ \triangle 1) $\langle \psi | \hat{A} \hat{B} \psi \rangle = \langle \hat{A}^{\dagger} \psi | \hat{B} \psi \rangle = \langle \hat{B}^{\dagger} \hat{A}^{\dagger} \psi | \psi \rangle$ У-фиксируей фиксируей 2) $\langle \varphi \mid \hat{A}\hat{B} \mid \psi \rangle = \langle \hat{A}\hat{B} \rangle^{\dagger} \varphi \mid \psi \rangle$ => $(\hat{A}\hat{B})^{\dagger} = \hat{B}^{\dagger}\hat{A}^{\dagger}$ upull Baganue 4. Â-hou.orp., enur VIV> (41A4>20. herazams: Y & mun. op E+C-new. onp. $\Delta \left(\hat{c} \hat{c}^{\dagger} \right)^{\dagger} = \left(\hat{c}^{\dagger} \right)^{\dagger} \hat{c}^{\dagger} = \hat{c} \hat{c}^{\dagger}$ Eun yeV-e.B. CC+, 2+0, 2ER-C.3., woml v, mo $\lambda = \frac{\langle \lambda \varphi | \varphi \rangle}{\langle \varphi | \varphi \rangle} = \frac{\langle \hat{c} \hat{c}^{\dagger} \varphi | \varphi \rangle}{\langle \varphi | \varphi \rangle} = \frac{\langle \hat{c}^{\dagger} \varphi | \hat{c}^{\dagger} \varphi \rangle}{\langle \varphi | \varphi \rangle} = \frac{\| \hat{c}^{\dagger} \varphi \|^2}{\| \varphi \|^2} > 0$

Задание 8. $A(x,x') = \frac{1}{(x-i)(x'+i)}$ \widehat{A} на \mathbb{R}^4 1. е.з; 2) с.в. в координативи описании. $\widehat{A} \psi(x) = \int_{-\infty}^{\infty} \frac{1}{(x-i)(x'+i)} \psi(x) dx' = \lambda \psi(x)$ $\frac{1}{x-i} \int_{-\infty}^{\infty} \frac{1\cdot (x'-i)}{(x'-i)(x'+i)} \psi(x) dx' = \lambda \psi(x)$ $\psi(x) = \frac{1}{x-i}$, поисыку вле от x' $\psi(x) = \frac{1}{x-i}$, поисыку $\psi(x) = \frac{1}{x-i}$ $\psi($