

Equation (19) of the article <https://link.springer.com/article/10.1007/s11071-020-06010-w>

$$\mathbf{J} \cdot \boldsymbol{\omega} + \left(\sum_{i=1}^n m_i \mathbf{r}_i \times (\boldsymbol{\omega} \times \mathbf{r}_i) \right) \cdot \boldsymbol{\omega} + M\mu \mathbf{r} \times (\boldsymbol{\omega} \times \mathbf{r} + \dot{\mathbf{r}}) = 0.$$

Using the «BAC – CAB» rule

$$\mathbf{r} \times (\boldsymbol{\omega} \times \mathbf{r}) = \langle \mathbf{r}, \mathbf{r} \rangle \boldsymbol{\omega} - \langle \mathbf{r}, \boldsymbol{\omega} \rangle \mathbf{r} = |\mathbf{r}|^2 \boldsymbol{\omega} - \mathbf{r} \otimes \mathbf{r} \cdot \boldsymbol{\omega} = (|\mathbf{r}|^2 \mathbf{I}_3 - \mathbf{r} \otimes \mathbf{r}) \cdot \boldsymbol{\omega},$$

we can get the following linear system

$$\left[\mathbf{J} + \left(\sum_{i=1}^n m_i |\mathbf{r}_i|^2 \right) \mathbf{I}_3 - \sum_{i=1}^n m_i \cdot \mathbf{r}_i \otimes \mathbf{r}_i + M\mu |\mathbf{r}|^2 \mathbf{I}_3 - M\mu \cdot \mathbf{r} \otimes \mathbf{r} \right] \boldsymbol{\omega} = -M\mu \cdot \mathbf{r} \times \dot{\mathbf{r}}.$$

This is a linear version of the basic equation which allows to find the angular velocity vector from the known parameters of the mechanical system. This version is used in the `fiction-mass.py`.