

Transform to Standard Form:

Objective: total profit: $\max z = 200x_1 + 300x_2$

Subject to: Stock Levels: $0.5x_1 + 0.3x_2 \leq 1000$

$$0.2x_1 + 0.25x_2 \leq 500$$

$$0.25x_1 + 0.5x_2 \leq 800$$

non-negative: $x_1, x_2 \geq 0$

$$\Rightarrow \begin{cases} \text{maximize} & z = 200x_1 + 300x_2 \\ \text{Subject to} & 0.5x_1 + 0.3x_2 + s_1 = 1000 \\ & 0.2x_1 + 0.25x_2 + s_2 = 500 \\ & 0.25x_1 + 0.5x_2 + s_3 = 800 \\ & x_1, x_2, s_1, s_2 \geq 0 \end{cases}$$

Simpler Table

Cj	Basic Variable	200	300	0	0	0	0	
		x_1	x_2	s_1	s_2	s_3	b_i	b_i/a_{ij}
0	s_1	0.5	0.3	1	0	0	1000	$1000/0.3 \approx 3333.3$
0	s_2	0.2	0.25	0	1	0	500	2000
0	s_3	0.25	0.5	0	0	1	800	1600
	z_j	0	0					
	$C_j - z_j$	200	300					

select s_1, s_2, s_3 as basic variables

max

min

first value

Cj	Basic Variable	200	300	0	0	0	0	
		x_1	x_2	s_1	s_2	s_3	b_i	b_i/a_{ij}
0	s_1	7/20	0	1	0	-0.6	520	1458.7
0	s_2	3/40	0	0	1	-0.5	100	1333.3
3	x_2	0.5	1	0	0	2	1600	3200
	z_j	150	300	0	0	600		
	$C_j - z_j$	50	0	0	0	-600		

max

min

Select s_1, s_2, s_3 as basic variables, set 1 to pivot, set 0 to all cells of the other rows of pivot column

Replace s_3 with x_2 as basic variables, set 1 to pivot, set 0 to all cells of the other rows of pivot column

$c_j - z_j \geq 0$, the coefficients of x_1, x_2 are positive \Rightarrow not the optimal solution \Rightarrow repeat above steps

Cj	Basic Variable	200	300	0	0	0	0	
		x_1	x_2	s_1	s_2	s_3	b_i	b_i/a_{ij}
0	s_1	0	0	1	-14/3	26/15	164/3	
2	x_1	1	0	0	40/3	-20/3	4000/3	
3	x_2	0	1	0	-10/3	16/3	2800/3	
	z_j	200	300	0	2000/3	800/3	1640000/3	$= 546666.7$
	$C_j - z_j$	0	0	0	-2000/3	-800/3		

≤ 0

Replace s_2 with x_1 as basic variables, set 1 to pivot, set 0 to all cells of the other rows of pivot column

all $c_j - z_j \leq 0 \Rightarrow$ find the optimal solution

The optimal solution: $(z, x_1, x_2, s_1, s_2, s_3) = \left(\frac{1640000}{3}, \frac{4000}{3}, \frac{2800}{3}, \frac{160}{3}, 0, 0\right)$

$$z = \frac{1640000}{3} - \frac{2000}{3}s_2 - \frac{800}{3}s_3$$

The optimal value $z = \frac{1640000}{3} \approx 546666.7$

The shadow price of material2 is $\frac{2000}{3} \text{ ¥/g}$, and the shadow price of material3 is $\frac{800}{3} \text{ ¥/g}$, which means 1g material2 is bought, $\frac{2000}{3} \text{ ¥}$ optimal value will be increased and 1g material3 is bought, $\frac{800}{3} \text{ ¥}$ optimal value will be increased