

(a)

$$\begin{aligned} &P(\text{Word} = \text{groot}) \\ &= P(\text{Word} = \text{groot} | \text{Document} = 1) + P(\text{Word} = \text{groot} | \text{Document} = 2) + P(\text{Word} = \text{groot} | \text{Document} = 3) \\ &= \frac{1}{3} * \frac{13}{(12+12+1+1+13)} + \frac{1}{3} * \frac{17}{(17+17+17)} + \frac{1}{3} * \frac{15}{(14+14+2+2+15)} \\ &= 0.3286 \end{aligned}$$

(b)

$$\begin{aligned} &P(\text{Document} = 1 | \text{Word} = \text{we}) \\ &= P(\text{Document} = 1, \text{Word} = \text{we}) / P(\text{Word} = \text{we}) \\ &= \frac{1}{3} * \frac{1}{(12+12+1+1+13)} / \left( \frac{1}{3} * \frac{1}{(12+12+1+1+13)} + \frac{1}{3} * \frac{2}{(14+14+2+2+15)} \right) \\ &= 0.376 \end{aligned}$$

(c)

$$\begin{aligned} &P(\text{Document} = 2 | \text{Word} = \text{am or Word} = \text{are}) \\ &= P(\text{Document} = 2, \text{Word} = \text{am or Word} = \text{are}) / P(\text{Word} = \text{am or Word} = \text{are}) \\ &= \frac{1}{3} * \frac{17}{(17+17+17)} / \left( \frac{1}{3} * \frac{(12+1)}{(12+12+1+1+13)} + \frac{1}{3} * \frac{17}{(17+17+17)} + \frac{1}{3} * \frac{(14+2)}{(14+14+2+2+15)} \right) \\ &= 0.3310 \end{aligned}$$

(d)

$$\begin{aligned} &P(\text{Word} = \text{groot}) \\ &= \frac{1}{6} * \frac{13}{(12+12+1+1+13)} + \frac{1}{3} * \frac{17}{(17+17+17)} + \frac{1}{2} * \frac{15}{(14+14+2+2+15)} \\ &= 0.3262 \end{aligned}$$

(e)

$$\begin{aligned} &P(\text{Document} = 1 | \text{Word} = \text{we}) \\ &= P(\text{Document} = 1, \text{Word} = \text{we}) / P(\text{Word} = \text{we}) \\ &= \frac{1}{6} * \frac{1/39}{(1/6 * 1/39 + 1/2 * 2/47)} \\ &= 0.1673 \end{aligned}$$

(f)

$$\begin{aligned} &P(\text{Document} = 2 | \text{Word} = \text{am or Word} = \text{are}) \\ &= P(\text{Document} = 2, \text{Word} = \text{am or Word} = \text{are}) / P(\text{Word} = \text{am or Word} = \text{are}) \\ &= \frac{1}{3} * \frac{17}{(17+17+17)} / \left( \frac{1}{6} * \frac{13}{39} + \frac{1}{3} * \frac{17}{51} + \frac{1}{2} * \frac{16}{47} \right) \\ &= 0.3298 \end{aligned}$$