

1. (a)

$$\begin{aligned}h_1 &= g (w_{h1x1} \times x_1 + w_{h1x2} \times x_2 + w_{h1b}) \\&= g (2.5 \times 0 + 1 \times 1 + 1.5) \\&= g (2.5) \\&= 1 / (1 + e^{(-2.5)}) \\&= 0.9241\end{aligned}$$

$$\begin{aligned}h_2 &= g (w_{h2x1} \times x_1 + w_{h2x2} \times x_2 + w_{h2b}) \\&= g (-1.5 \times 0 + (-3) \times 1 + 2) \\&= g (-1) \\&= 1 / (1 + e^{(1)}) \\&= 0.2689\end{aligned}$$

$$\begin{aligned}\text{output } y &= g (w_{yh1} \times h_1 + w_{yh2} \times h_2 + w_{yb}) \\&= g (1 \times 0.9241 + 0.5 \times 0.2689 + (-1)) \\&= g (0.0586) \\&= 1 / (1 + e^{(-0.0586)}) \\&= 0.5146\end{aligned}$$

(b)

$$\begin{aligned}\Delta w_{yh1} &= \alpha h_1 \times (y - O) \times O \times (1 - O) \\&= 0.1 \times 0.9241 \times (1 - 0.5146) \times 0.5146 \times (1 - 0.5146) \\&= 0.0112\end{aligned}$$

$$\begin{aligned}\text{update : } w_{yh1} &= w_{yh1} + \Delta w_{yh1} \\&= 1 + 0.0112 \\&= 1.0112\end{aligned}$$

$$\begin{aligned}\Delta w_{yh2} &= \alpha h_2 \times (y - O) \times O \times (1 - O) \\&= 0.1 \times 0.2689 \times (1 - 0.5146) \times 0.5146 \times (1 - 0.5146) \\&= 0.0033\end{aligned}$$

$$\begin{aligned}\text{update : } w_{yh2} &= w_{yh2} + \Delta w_{yh2} \\&= 0.5 + 0.0033 \\&= 0.5003\end{aligned}$$

$$\begin{aligned}\Delta w_{yb} &= \alpha b \times (y - O) \times O \times (1 - O) \\&= 0.1 \times 1 \times (1 - 0.5146) \times 0.5146 \times (1 - 0.5146) \\&= 0.0121\end{aligned}$$

$$\begin{aligned}\text{update : } w_{yb} &= w_{yb} + \Delta w_{yb} \\&= -1 + 0.0121 \\&= -0.9879\end{aligned}$$

$$\begin{aligned}\Delta w_{h1x1} &= \alpha \times h1x1 \times (1 - h1) \times w_{h1y} \times (y - O) \times O \times (1 - O) \\ &= 0.1 \times 0 \times 0.9241 \times (1 - 0.9241) \times 1 \times (1 - 0.5146) \times 0.5146 \times (1 - 0.5146) \\ &= 0\end{aligned}$$

$$\begin{aligned}\text{update : } w_{h1x1} &= w_{h1x1} + \Delta w_{h1x1} \\ &= 2.5 + 0 \\ &= 2.5\end{aligned}$$

$$\begin{aligned}\Delta w_{h1x2} &= \alpha \times h1x2 \times (1 - h1) \times w_{h1y} \times (y - O) \times O \times (1 - O) \\ &= 0.1 \times 1 \times 0.9241 \times (1 - 0.9241) \times 1 \times (1 - 0.5146) \times 0.5146 \times (1 - 0.5146) \\ &= 0.0112\end{aligned}$$

$$\begin{aligned}\text{update : } w_{h1x2} &= w_{h1x2} + \Delta w_{h1x2} \\ &= 1 + 0.0008 \\ &= 1.0008\end{aligned}$$

$$\begin{aligned}\Delta w_{h1b} &= \alpha \times h1b \times (1 - h1) \times w_{h1y} \times (y - O) \times O \times (1 - O) \\ &= 0.1 \times 1 \times 0.9241 \times (1 - 0.9241) \times 1 \times (1 - 0.5146) \times 0.5146 \times (1 - 0.5146) \\ &= 0.0112\end{aligned}$$

$$\begin{aligned}\text{update : } w_{h1b} &= w_{h1b} + \Delta w_{h1b} \\ &= 1.5 + 0.0008 \\ &= 1.5008\end{aligned}$$

$$\begin{aligned}\Delta w_{h2x1} &= \alpha \times h2x1 \times (1 - h2) \times w_{h2y} \times (y - O) \times O \times (1 - O) \\ &= 0.1 \times 0 \times 0.2689 \times (1 - 0.2689) \times 0.5 \times (1 - 0.5146) \times 0.5146 \times (1 - 0.5146) \\ &= 0\end{aligned}$$

$$\begin{aligned}\text{update : } w_{h2x1} &= w_{h2x1} + \Delta w_{h2x1} \\ &= -1.5 + 0 \\ &= -1.5\end{aligned}$$

$$\begin{aligned}
\Delta w_{h2x2} &= \alpha \times h_{2x1} \times (1 - h_2) \times w_{h2y} \times (y - O) \times O \times (1 - O) \\
&= 0.1 \times 1 \times 0.2689 \times (1 - 0.2689) \times 0.5 \times (1 - 0.5146) \times 0.5146 \times (1 - 0.5146) \\
&= 0.0012 \\
\text{update : } w_{h2x2} &= w_{h2x2} + \Delta w_{h2x2} \\
&= -3 + 0.0012 \\
&= -2.9988
\end{aligned}$$

$$\begin{aligned}
\Delta w_{h2b} &= \alpha \times h_{2b} \times (1 - h_2) \times w_{h2y} \times (y - O) \times O \times (1 - O) \\
&= 0.1 \times 1 \times 0.2689 \times (1 - 0.2689) \times 0.5 \times (1 - 0.5146) \times 0.5146 \times (1 - 0.5146) \\
&= 0.0012 \\
\text{update : } w_{h2b} &= w_{h2b} + \Delta w_{h2b} \\
&= 2 + 0.0012 \\
&= 2.0012
\end{aligned}$$