

The **Two-Pointer Technique** is a powerful and common algorithmic pattern used to solve problems efficiently, often on sorted arrays or linked lists. It involves using two pointers (variables that store an index or memory address) to traverse the data structure.

The efficiency comes from the fact that it often reduces the time complexity from  $O(n^2)$  (like nested loops) to  $O(n)$ , as you examine each element only once or a constant number of times.

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## How the Two-Pointer Technique Works

There are two main variations:

### 1. Pointers Moving Towards Each Other (Opposite Directions)

- **Setup:** One pointer, usually called **left** (or *i*), starts at the beginning (index 0). The other pointer, **right** (or *j*), starts at the end (index  $n-1$ ).
- **Movement:** The pointers move towards the center based on a specific condition.
  - If a condition is met, both pointers might move.
  - If the result is too large, the right pointer moves left.
  - If the result is too small, the left pointer moves right.
- **Best for:** Problems involving **searching for a pair** or an element in a **sorted array** where the order helps determine the next move.
- **Example Problem:** Finding a pair that sums to a target.

### 2. Pointers Moving in the Same Direction

- **Setup:** Both pointers, often called **slow** and **fast**, or *i* and *j*, start at or near the beginning of the structure (e.g., index 0 and index 1).
- **Movement:** They advance based on their role:
  - The **slow** pointer typically keeps track of the position to insert or the start of a valid window.
  - The **fast** pointer explores new elements or finds the end of a valid window.
- **Best for:** Problems involving **maintaining a window** (like a sliding window), **removing duplicates** in-place, or in linked lists (like finding the middle or detecting a cycle).
- **Example Problem:** Removing duplicates from a sorted array.



## Example: Finding a Pair with a Specific Sum (Opposite Directions)

**Problem:** Given a **sorted array** of integers and a target sum  $\$S\$$ , find if there is a pair of numbers in the array that adds up to  $\$S\$$ .

<b>Index</b>	0	1	2	3	4	5
<b>Value</b>	2	7	11	15	20	25
<b>Pointers</b>	\$L\$					\$R\$

Target Sum (\$SS) = 26

### Steps:

1. **Initialize Pointers:**
  - o L (left) = index 0 (value 2)
  - o R (right) = index 5 (value 25)
2. **Iterate (while \$L < R\$):**

Step	L (Value)	R (Value)	Current Sum	S=26	Action
1	2	25	27	Too Large	Move \$R\$ left (\$R \leftarrow R-1\$)
2	2	20	22	Too Small	Move \$L\$ right (\$L \leftarrow L+1\$)
3	7	20	27	Too Large	Move \$R\$ left (\$R \leftarrow R-1\$)
4	7	15	22	Too Small	Move \$L\$ right (\$L \leftarrow L+1\$)
5	11	15	26	<b>MATCH!</b>	<b>Success!</b> (Pair found: 11 and 15)

### Why This is Efficient (\$O(n)\$):

- In each step, you calculate the sum and then **eliminate one number** from the remaining search space by moving *either* the \$L\$ pointer or the \$R\$ pointer.
- Since the total number of elements is \$n\$, and you move a pointer in almost every step, you will find the pair or determine it doesn't exist in a maximum of \$n\$ steps. This is much faster than the \$O(n^2)\$ approach of checking every possible pair with nested loops.