

Input

- n : The size of the chessboard (in this case, 12 for a 12x12 board).
- $(r1, c1)$ and $(r2, c2)$: Coordinates of two cells that are removed from the board

Variable Representation:

- Each cell (i, j) on the board is represented by four variables:
- $X_{i,j,1}$ (a): Indicates the cell is covered by the left side of a horizontally placed domino.
- $X_{i,j,-1}$ (b): Indicates the cell is covered by the right side of a horizontally placed domino.
- $X_{i,j,2}$ (c): Indicates the cell is covered by the top side of a vertically placed domino.
- $X_{i,j,-2}$ (d): Indicates the cell is covered by the bottom side of a vertically placed domino.
- The variable counter keeps track of these four variables for each cell.

Single Domino Coverage:

Each cell must be covered by exactly one domino. The code enforces this by creating clauses:

- $\{a, b, c, d\}$ ensures that one of these options must be true (at least one direction covers the cell).
- $\{-a, -b\}$, $\{-a, -c\}$, $\{-a, -d\}$, $\{-b, -c\}$, $\{-b, -d\}$, and $\{-c, -d\}$ ensure that no two directions simultaneously cover the cell

Neighbor to the Right :

- $\text{newcolumn} = \text{column} + 1$: Sets the potential right neighbor's column.

Boundary Check:

- $\text{if}(\text{newcolumn} > n \ || \ \text{newrow} > n \ || \ (\text{newrow} == r1 \ \&\& \ \text{newcolumn} == c1) \ || \ (\text{newrow} == r2 \ \&\& \ \text{newcolumn} == c2))$: Checks if this right neighbor is outside the board bounds or one of the removed cells.
- If true, $\text{clauses.push_back}(\{-a\})$ adds a clause $\{-a\}$, indicating that if cell (i, j) has a (left side of a horizontal domino) set, it cannot find a valid right neighbor to pair with.

Valid Right Neighbor:

- If a valid neighbor exists, `clauses.push_back({-a, a+5})` links `a` to its neighboring variable `a + 5`, enforcing that if the current cell is covered by the left side of a horizontal domino, the right neighbor must be covered by the right side of the same domino.

Neighbor to the Left :

- Set Left Neighbor:
- `newcolumn = column - 1` sets the potential left neighbor's column index by moving one cell to the left.

Boundary Check:

- The condition `if (newcolumn < 1 || newrow < 1 || (newrow == r1 && newcolumn == c1) || (newrow == r2 && newcolumn == c2))` checks if this left neighbor is outside the grid bounds (i.e., `newcolumn < 1`) or is one of the removed cells at `(r1, c1)` or `(r2, c2)`.
- If true, `clauses.push_back({-b})` adds a clause `{-b}`, indicating that if cell `(i, j)` has `b` (right side of a horizontal domino) set, it cannot find a valid left neighbor to pair with.

Valid Left Neighbor:

- If a valid left neighbor exists, `clauses.push_back({-b, b-5})` links `b` (right side of the domino) to

the neighboring variable `b - 5`, representing the left side of the horizontal domino.

Neighbor Below :

- `newrow = row + 1`: Sets the potential lower neighbor's row

Boundary Check:

- `if(newrow > n || (newrow == r1 && newcolumn == c1) || (newrow == r2 && newcolumn == c2))`: Ensures the potential lower neighbor is within bounds and not a removed cell.
- If true, `clauses.push_back({-c})` adds a clause `{-c}`, meaning if cell `(i, j)` has `c` (top side of a vertical domino) set, there is no valid bottom neighbor to pair with.

Valid Lower Neighbor:

- If a valid lower neighbor exists, `clauses.push_back({-c, c + 1 + tobeadded})` links `c` to the adjusted neighbor variable, enforcing the pairing.

Calculating tobeadded

- Since each row contains `n` cells, and each cell has four variables:

One row of cells has $n * 4$ variables.

Thus:

`tobeadded = n * 4` ensures that we jump to the correct variable index for the row below.

Adjustments to tobeadded for Removed Cells

- If there are removed cells in certain positions (relative to the current cell), they might affect the continuity of variable indexing. For instance:
- If a cell is removed to the left or above the current cell, it affects how we count variables in the row below.
- To correct for this, the code decreases `tobeadded` by 4 whenever such a removed cell exists.

Neighbor Above :

`newrow = row - 1`: Sets the potential upper neighbor.

Boundary Check:

- If the upper neighbor is out of bounds or a removed cell, `clauses.push_back({-d})` adds a clause `{-d}`, indicating that the current cell cannot be covered by the bottom side of a vertical domino.

Valid Upper Neighbor:

- If a valid neighbor exists, `clauses.push_back({-d, d - 1 - tobesubtracted})` links `d` to the corresponding neighbor, ensuring the domino covers both cells.

Calculating tobesubtracted

- To ensure we reach the correct variable index of the upper neighbor, `tobesubtracted` is set to:
- `tobesubtracted = n * 4`, which shifts the variable index back by one row.

Adjustments to `tobesubtracted` for Removed Cells:

- If removed cells are near the current cell, they can affect variable indexing for the row above. To address this, `tobesubtracted` is decreased by 4 (the number of variables per cell) when:
- A cell is removed to the right or below the current cell.
- A cell is removed to the left or above the cell directly above.