

HOMEWORK #5 - TRAVELLING SALESMAN PROBLEM

TABLE A : 1 COMPUTER

| Communication Latency Optimization | Workers | Avg. time as seen by the client (Tc milliseconds) | Parallel Efficiency : $T1/C.Tc$ |
|------------------------------------|----------|---|---------------------------------|
| On | Multiple | 13071 (T1) | 1 |
| On | Single | 15224 (T1) | 1 |
| Off | Multiple | 19430 (T1) | 1 |
| Off | Single | 20200 (T1) | 1 |

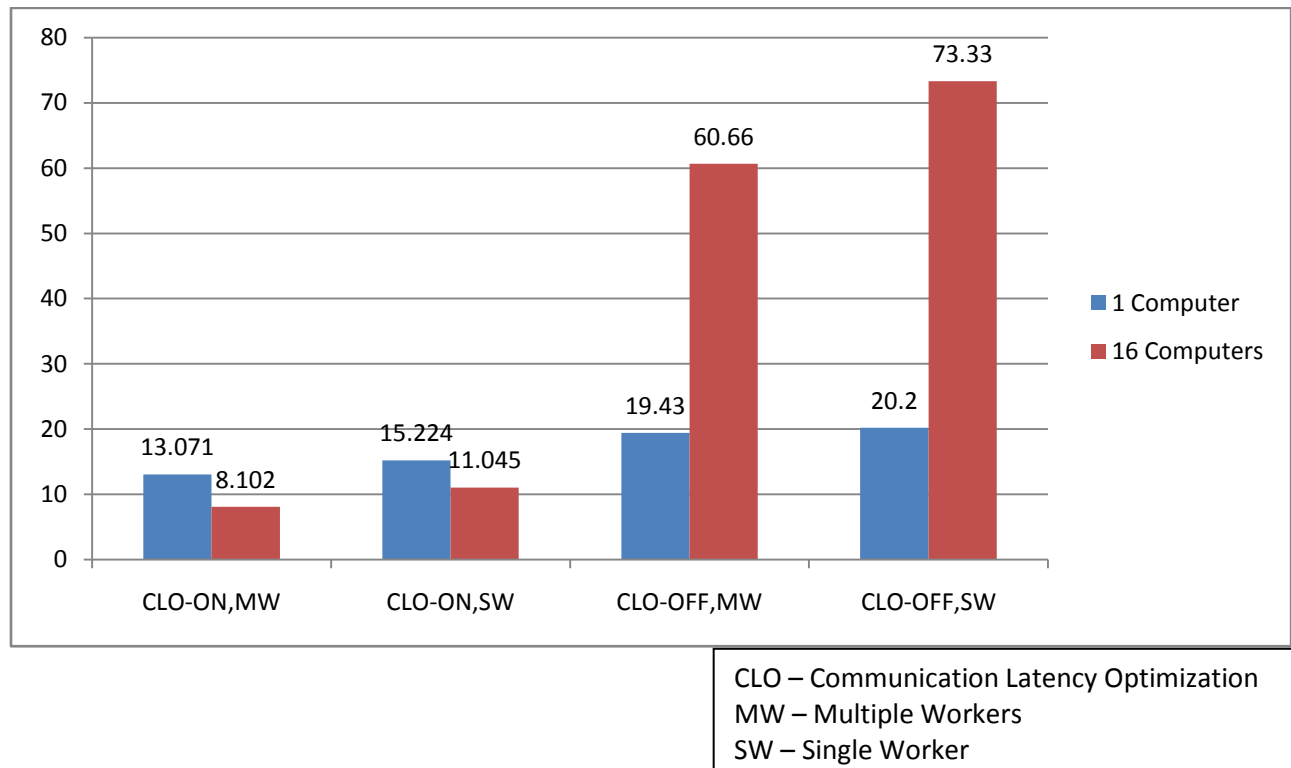
TABLE B : 16 COMPUTERS

| Communication Latency Optimization | Workers | Avg. time as seen by the client (Tc milliseconds) | Parallel Efficiency : $T1/C.Tc$ |
|------------------------------------|----------|---|---------------------------------|
| On | Multiple | 8102 | 0.1008 |
| On | Single | 11045 | 0.0861 |
| Off | Multiple | 60660 | 0.02 |
| Off | Single | 73330 | 0.0172 |

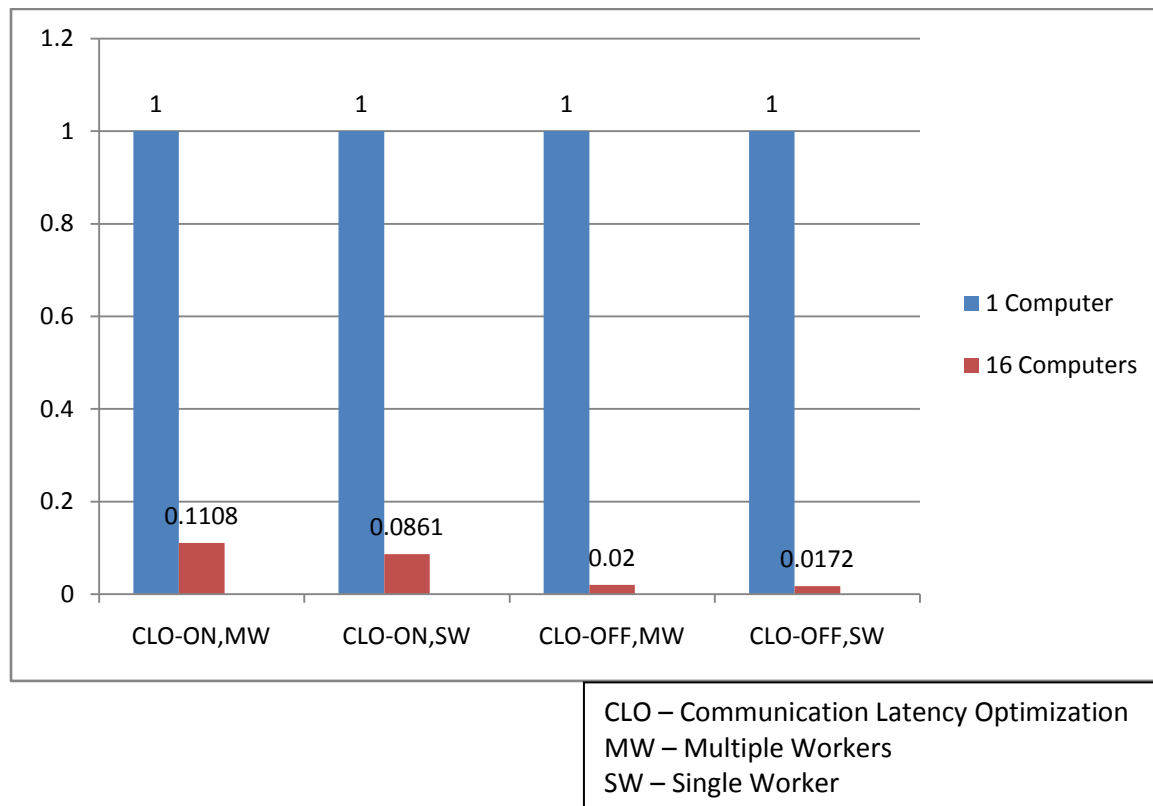
TABLE C : AVERAGE EXECUTION BASED ON LATENCY OPTIMIZATION

| Communication Latency Optimization | Computers | Avg. execution time across different worker types viz. multiple/single (milliseconds) | |
|------------------------------------|-----------|---|-----------------|
| On | 1 | 14147.5 | Diff. = 5.6 s |
| Off | 1 | 19815 | |
| On | 16 | 9573.5 | Diff. = 57.42 s |
| Off | 16 | 66995 | |

GRAPH A - EXECUTION TIMES



GRAPH B - EFFICIENCY PLOT



In the case : $C=16$, it can be seen that the parallel efficiency decreases with increase in number of parallel processors. This suggests that the degree of parallelization keeps decreasing and approaches zero as more parallel computational power is added to the infrastructure. This was an expected result. Not all tasks can achieve perfect parallelization, and this also holds good for the TSP task which we experimented with.

However, we see a clear difference in numbers when compared to homework #4. In the table below, we have considered the best case in homework #5 viz. (Multiple Workers + Communication Latency Optimization) verses the normal case in homework #4.

| No. of computers (C) | Homework #4 Parallel Efficiency | Homework #5 Parallel Efficiency |
|-----------------------|---------------------------------|---------------------------------|
| 1 | 1 | 1 |
| 16 | 0.05 | 0.1008 |

For both homeworks, we used the same input containing 12 cities and the same decomposition depth of 5. After the 5th level of decomposition, each computer used a depth-first search algorithm to systematically traverse all possible paths locally and prune nodes along the way using the branch-and-bound strategy.

As seen in the table above, the parallel efficiency has improved twofold.

- (1) This can be attributed to the decrease in time lost in communication due to the presence of a local queue in each of the 16 computers. From Table C (see above), one can note the drastic difference in times between cases where communication latency optimization was switched on and off. In the absence of any optimization, a massive number of subtasks generated in the 5th level of decomposition increase the time spent in communicating with the compute space and also the idle time of the computers.
- (2) The algorithm implemented by us for homework #4 to compute a tighter lower bound for TSP was computationally intensive with a complexity of $O(N^2)$. This has been replaced with a lighter algorithm discussed in class that has a linear time complexity for tightening the lower bound. This should have also contributed to the improvement in numbers.