Package 'tempted'

May 4, 2023

J 1	6.
Title	TEMPTED: Temporal Tensor Decomposition, a Dimensionality Reduction Tool for Longitudi
	nal Multivaraite Data

Version 0.1.0

Type Package

Depends R, np, ggplot2 **Imports** np, ggplot2 **Author** Pixu Shi

Maintainer Pixu Shi <pixu.shi@duke.edu>

Description TEMPTED is a dimension reduction method for multivariate longitudinal data. It format the data into a temporal tensor, with three modes representing subject, feature, and continuous time, respectively. The tensor is then decomposed into a summation of low-dimensional components, each consisting of a subject loading vector, a feature loading vector, and a temporal loading function. These loadings provide low-dimensional representation of subjects or samples, and can be used to identify features associated with clusters of subjects or samples. TEMPTED provides the flexibility of allowing subjects to have different temporal sampling, so time points do not need to be binned and missing time points do not need to be imputed.

License GPL-3 Encoding UTF-8 LazyData true RoxygenNote 7.2.3

R topics documented:

aggregate_feature	2
bernoulli_kernel	3
count_table	4
est_test_subject	4
format_tempted	5
freg_rkhs	6
meta_table	7
plot_feature_summary	7
plot_metafeature	8
plot_time_loading	9
processed_table	10
ratio_feature	10
svd_centralize	12

2 aggregate_feature

aggre	egate_fea	ture	<u>,</u>		Ag	gr	ego	ate	fe	eat	tur	es	us	ing	; fe	eai	tur	e i	loc	adi	ing	zs.						
Index																												19
	tempted_	all .											•			•								•				 15
	tempted																											 13
	tdenoise																											 13

Description

This function aggregate the features into "meta features" by calculating a weighted summation of the features using feature loading of each component as weights. It can also aggregate features by using the combination of multiple components by ranking the features by a linear combination of feature loadings from multiple components.

Usage

```
aggregate_feature(
  res_tempted,
  mean_svd = NULL,
  datlist,
  pct = 1,
  contrast = NULL,
  get_contrast = NULL)
```

Arguments

res_tempted	Output of tempted.
mean_svd	Output of svd_centralize.
datlist	$Output \ of \ {\tt format_tempted}, the \ original \ temporal \ tensor \ that \ will \ be \ aggregated.$
pct	The percent of features to aggregate, features ranked by absolute value of the feature loading of each component. Default is 1, which means 100% of features are aggregated. Setting pct=0.01 means top 1% of features is aggregated, where features are ranked in absolute value of feature loading of each component.
contrast	A matrix choosing how components are combined, each column is a contrast of length r and used to calculate the linear combination of the feature loadings of r components.
get_contrast	A vector denoting which components to use to construct a contrast and combine. A vector of $c(1,1,0)$ means the first two of three components are used to find the contrast to combine.

Value

A list of results.

```
metafeature.aggregate
```

The meta feature obtained by aggregating the observed temporal tensor. It is a data.frame with four columns: "value" for the meta feature values, "subID" for the subject ID, "timepoint" for the time points, and "PC" indicating which component was used to construct the meta feature.

bernoulli_kernel 3

metafeature.aggregate.est

The meta feature obtained by aggregating the denoised temporal tensor. It has

the same structure as metafeature.aggregate.

contrast The contrast used to linearly combine the components. It is either from the input

parameter contrast or calculated by setting get_contrast.

toppct A matrix of TRUE/FALSE indicating which features are aggregated in each

component and contrast.

Examples

```
datlist <- format_tempted(count_table,</pre>
                            meta_table$day_of_life,
                            meta_table$studyid,
                            pseudo_count=0.5,
                            transform="clr")
mean_svd <- svd_centralize(datlist, r=1)</pre>
res_tempted <- tempted(mean_svd$datlist, r=3, smooth=1e-5)</pre>
datlist_raw <- format_tempted(count_table,</pre>
                                meta_table$day_of_life,
                                meta_table$studyid,
                                transform="none")
contrast <- cbind(c(1/2,1,0), c(1/2,-1,0))
res_aggregate <- aggregate_feature(res_tempted,</pre>
                                     mean_svd,
                                     datlist,
                                     pct=1,
                                     contrast=contrast)
group <- unique(meta_table[, c("studyid", "delivery")])</pre>
plot_metafeature(res_aggregate$metafeature.aggregate, group, bws=30)
```

bernoulli_kernel

Caculate the Bernoulli kernel

Description

This function is used to calculate the kernel matrix for the RKHS regression that iteratively updates the temporal loading function.

Usage

```
bernoulli_kernel(x, y)
```

Arguments

x,y

Two values between which the Bernoulli kernel is calculated.

4 est_test_subject

Value

The calculated kernel between x and y.

count_table

OTU read count table from the ECAM data

Description

OTU read count table from the ECAM data

Usage

count_table

Format

A data.frame with rows matching with data.frame meta_table and columns representing microbial features (i.e. OTUs). Each entry is a read count.

Source

Bokulich, Nicholas A., et al. "Antibiotics, birth mode, and diet shape microbiome maturation during early life." Science translational medicine 8.343 (2016): 343ra82-343ra82.

est_test_subject

Estimate subject loading of testing data

Description

This function estimates the subject loading of the testing data based on feature and temporal loading from training data, so that both the testing data and training data have the same dimensionality reduction.

Usage

```
est_test_subject(datlist, res_tempted, mean_svd = NULL)
```

Arguments

datlist Testing data formatted into datlist in the same fashion as the training data. The

same transformation needs to be used for both training and testing data.

res_tempted Result from tempted ran on the training data.

mean_svd Result from svd_centralize ran on the training data.

Value

estimated subject loading of testing data

format_tempted 5

Examples

```
# split the example data into training and testing
id_test <- meta_table$studyid=="1"</pre>
count_train <- count_table[!id_test,]</pre>
meta_train <- meta_table[!id_test,]</pre>
count_test <- count_table[id_test,]</pre>
meta_test <- meta_table[id_test,]</pre>
# run tempted on training data
datlist_train <- format_tempted(count_train,</pre>
                                  meta_train$day_of_life,
                                  meta_train$studyid,
                                   threshold=0.95,
                                   pseudo_count=0.5,
                                   transform="clr")
mean_svd_train <- svd_centralize(datlist_train, r=1)</pre>
res_tempted_train <- tempted(mean_svd_train$datlist,</pre>
r=3, smooth=1e-5)
# get the overlapping features
count_test <- count_test[,rownames(datlist_train[[1]])[-1]]</pre>
datlist_test <- format_tempted(count_test,</pre>
                                 meta_test$day_of_life,
                                 meta_test$studyid,
                                 threshold=1,
                                 pseudo_count=0.5,
                                 transform="clr")
# estimate the subject loading of the testing subject
sub_test <- est_test_subject(datlist_test, res_tempted_train, mean_svd_train)</pre>
```

 ${\tt format_tempted}$

Format data table into the input of tempted

Description

This function applies a variety of transformations to the read counts and format the sample by feature table and meta data into a data list that can be used as the input of tempted and svd_centralize. For data that are not read counts, or data that are not microbiome data, the user can apply their desired transformation to the data before formatting into list.

```
format_tempted(
  feature_table,
```

6 freg_rkhs

```
time_point,
subjectID,
threshold = 0.95,
pseudo_count = NULL,
transform = "clr"
)
```

Arguments

feature_table A sample by feature matrix.

time_point The time stamp of each sample, matched with the rows of feature_table.

subjectID The subject ID of each sample, matched with the rows of feature_table.

threshold A threshold for feature filtering for microbiome data. Features with zero value

percentage > threshold will be excluded. Default is 0.95.

pseudo_count A small number to add to all the counts before normalizing into proportions and

log transformation. Default is 1/2 of the smallest non-zero value that is specific for each sample. This pseudo count is added for transform=c("log_comp",

"clr", "logit").

transform The transformation applied to the data. "log_comp" for log of compositions.

"comp" for compositions. "ast" for arcsine squared transformation. "clr" for central log ratio transformation. "logit" for logit transformation. "none" for no transformation. Default transform="clr" is recommended for microbiome

data. For data that are already transformed, use transform="none".

Value

A length n list of matrices as the input of tempted and svd_centralize. Each matrix represents a subject, with columns representing samples from this subject, the first row representing the sampling time points, and the following rows representing the feature values.

See Also

Examples can be found in tempted.

freg_rkhs

RKHS regression to update the temporal loading function.

Description

This function is an internal function that performs the RKHS regression. It is applied iteratively in tempted to update the temporal loading function.

```
freg_rkhs(Ly, a.hat, ind_vec, Kmat, Kmat_output, smooth = 1e-08)
```

meta_table 7

meta_table

Meta data table from the ECAM data

Description

Meta data table from the ECAM data

Usage

```
meta_table
```

Format

A data.frame with rows matching with data.frame count_table and processed_table and three variables:

studyid character denoting the subject ID of the infants.

delivery character denoting the delivery mode of the infants.

day_of_life character denoting the age of infants measured in days when microbiome sample was taken.

Source

Bokulich, Nicholas A., et al. "Antibiotics, birth mode, and diet shape microbiome maturation during early life." Science translational medicine 8.343 (2016): 343ra82-343ra82.

plot_feature_summary

Plot nonparametric smoothed mean and error bands of features versus time

Description

This is a handy function to plot the smoothed mean and error bands for multiple features.

```
plot_feature_summary(
  feature_mat,
  time_vec,
  group_vec,
  coverage = 0.95,
  bws = NULL,
  nrow = 1
)
```

8 plot_metafeature

Arguments

feature_mat A sample by feature matrix. Each feature will be plotted separately as a facet.

The features can be original features, meta features, log ratios, or any variables

of interest.

time_vec A vector of time points matched to the rows of feature_mat.

group_vec A vector of factor variable indicating the group membership of samples matched

to the rows of feature_mat.

coverage The coverage rate for the error band. Default is 0.95.

bws The smoothness parameter for the smoothing lines and error bands. A larger

value means a smoother line. Default is NULL and calculated by function

np::npreg().

nrow The number of rows to plot the features used in function ggplot2::facet_wrap().

Value

A ggplot2 object.

Examples

plot_metafeature

Plot nonparametric smoothed mean and error bands of meta features

versus time

Description

This function plot the smoothed mean and error band of meta features grouped by a factor variable provided by the user.

Usage

```
plot_metafeature(metafeature, group, coverage = 0.95, bws = NULL, nrow = 1)
```

Arguments

metafeature It can be metafeature.ratio from the output of ratio_feature and tempted_all(),

metafeature.aggregate from the output of ratio_feature and tempted_all(),

or metafeature.aggregate.est from the output of ratio_feature.

group A subject by 2 data.frame with the first column for subject ID and second column

for group membership.

plot_time_loading 9

coverage The coverage rate for the error band. Default is 0.95.

bws The smoothness parameter for the smoothing lines and error bands. A larger

value means a smoother line. Default is NULL and calculated by function

np::npreg().

nrow The number of rows to plot the features used in function ggplot2::facet_wrap().

Value

A ggplot2 object.

See Also

Examples can be found in tempted_all, ratio_feature and aggregate_feature.

Description

This function uses ggplot2::geom_line() in ggplot2 to plot the temporal loading functions from tempted.

Usage

```
plot_time_loading(res, r = NULL, ...)
```

Arguments

res Output of function tempted.

The number of components to plot. By default all the components estimated by

tempted will be plotted.

... Arguments to put in ggplot2::geom_line(aes(...)).

Value

An ggplot2 object.

See Also

Examples can be found in tempted_all and tempted.

10 ratio_feature

processed_table

Central-log-ratio (clr) transformed OTU table from the ECAM data

Description

Central-log-ratio (clr) transformed OTU table from the ECAM data

Usage

```
processed_table
```

Format

A data.frame with rows matching with data.frame meta_table and columns representing microbial features (i.e. OTUs). Entries do not need to be transformed, and will be directly used by tempted. This data.frame is used to illustrate how tempted can be used for general form of multivariate longitudinal data already preprocessed by user.

Source

Bokulich, Nicholas A., et al. "Antibiotics, birth mode, and diet shape microbiome maturation during early life." Science translational medicine 8.343 (2016): 343ra82-343ra82.

ratio_feature

Take log ratio of the abundance of top features over bottom features

Description

Top and bottom ranking features are picked based on feature loadings (and their contrasts). The log ratio abundance of the top ranking features over the bottom ranking features is produced as the main result. This function and its result is designed for longitudinal microbiome data, and may not be meaningful for other type of temporal data.

```
ratio_feature(
  res_tempted,
  datlist,
  pct = 0.05,
  absolute = FALSE,
  contrast = NULL
)
```

ratio_feature 11

Arguments

res_tempted Output of tempted.

datlist Output of format_tempted(, transform="none"), the temporal tensor that in-

clude the raw read counts.

pct The percent of features to sum up. Default is 0.05, i.e. 5%.

absolute absolute = TRUE means features are ranked by the absolute value of feature

loadings, and the top pct percent of features are picked. absolute = FALSE means features are ranked by the original value of feature loadings, and the top and bottom pct percent of features are picked. Then ratio is taken as the abundance of the features with positive loading over the abundance of the features

with negative loading.

contrast A matrix choosing how components are combined, each column is a contrast of

length r and used to calculate the linear combination of the feature loadings of r

components.

get_contrast A vector denoting which components to use to construct a contrast and combine.

A vector of c(1,1,0) means the first two of three components are used to find

the contrast to combine.

Value

A list of results.

metafeature.ratio

The log ratio abundance of the top over bottom ranking features. It is a data.frame with five columns: "value" for the log ratio values, "subID" for the subject ID, and "timepoint" for the time points, and "PC" indicating which component was

used to construct the meta feature.

contrast The contrast used to linearly combine the components. It is either from the input

parameter contrast or calculated by setting get_contrast.

toppct A matrix of TRUE/FALSE indicating which features are ranked top in each

component (and contrast) and used as the numerator of the log ratio.

bottompct A matrix of TRUE/FALSE indicating which features are ranked bottom in each

component (and contrast) and used as the denominator of the log ratio.

Examples

12 svd_centralize

```
absolute=FALSE, contrast=contrast)
group <- unique(meta_table[, c("studyid", "delivery")])
plot_metafeature(res_ratio$metafeature.ratio, group, bws=30)</pre>
```

svd_centralize

Remove the mean structure of the temporal tensor

Description

This function first average the feature value of all time points for each subject to form a subject by feature matrix. Next, it performs a singular value decomposition of this matrix and construct the matrix's rank-r approximation. Then, it subtracts this rank-r subject by feature matrix from the temporal tensor.

Usage

```
svd_centralize(datlist, r = 1)
```

Arguments

datlist A length n list of matrices. Each matrix represents a subject, with columns

representing samples from this subject, the first row representing the sampling

time points, and the following rows representing the feature values.

The number of ranks in the mean structure. Default is 1.

Value

A list of results.

datlist The new temporal tensor after mean structure is removed

A. tilde The subject singular vector of the mean structure, a subject by r matrix.

B. tilde The feature singular vector of the mean structure, a feature by r matrix.

 $lambda.\,tilde \qquad The \ singular \ value \ of \ the \ mean \ structure, \ a \ length \ r \ vector.$

See Also

Examples can be found in tempted.

tdenoise 13

tdenoise

Calculate the de-noised temporal tensor

Description

This function constructs a de-noised version of the temporal tensor using the low-rank components obtained by svd_centralize tempted and uses the loadings to

Usage

```
tdenoise(res_tempted, mean_svd = NULL)
```

Arguments

```
res_tempted Output of tempted
mean_svd Output of svd_centralize
```

Value

The de-noised functional tensor

tempted

Decomposition of temporal tensor

Description

This is the main function of tempted.

Usage

```
tempted(
  datlist,
  r = 3,
  smooth = 1e-06,
  interval = NULL,
  resolution = 101,
  maxiter = 20,
  epsilon = 1e-04
)
```

Arguments

datlist

A length n list of matrices. Each matrix represents a subject, with columns representing samples from this subject, the first row representing the sampling time points, and the following rows representing the feature values.

r

Number of components to decompose into, i.e. rank of the CP type decomposition. Default is set to 3.

14 tempted

Smoothing parameter for RKHS norm. Larger means smoother temporal loading functions. Default is set to be 1e-8. Value can be adjusted depending on the dataset by checking the smoothness of the estimated temporal loading function in plot.

The range of time points to ran the decomposition for. Default is set to be the range of all observed time points. User can set it to be a shorter interval than the observed range.

resolution Number of time points to evaluate the value of the temporal loading function.

Default is set to 101. It does not affect the subject or feature loadings.

maxiter Maximum number of iteration. Default is 20.

epsilon Convergence criteria for difference between iterations. Default is 1e-4.

Value

The estimations of the loadings.

A. hat Subject loading, a subject by r matrix.B. hat Feature loading, a feature by r matrix.

Phi.hat Temporal loading function, a resolution by r matrix.

time.Phi The time points where the temporal loading function is evaluted.

Lambda Eigen value, a length r vector.

r.square Variance explained by each component. This is the R-squared of the linear re-

gression of the vectorized temporal tensor against the vectorized low-rank re-

construction using individual components.

accum.r.square Variance explained by the first few components accumulated. This is the R-

squared of the linear regression of the vectorized temporal tensor against the

vectorized low-rank reconstruction using the first few components.

Examples

```
res_tempted <- tempted(mean_svd$datlist, r=3, smooth=1e-5)
# plot the temporal loading
plot_time_loading(res_tempted, r=2)</pre>
```

tempted_all

Run all major functions of tempted

Description

This function wraps format_tempted, svd_centralize, tempted, ratio_feature, and aggregate_feature.

Usage

```
tempted_all(
  feature_table,
  time_point,
  subjectID,
  threshold = 0.95,
  pseudo_count = NULL,
  transform = "clr",
  r = 3,
  smooth = 1e-06,
  interval = NULL,
  resolution = 51,
  maxiter = 20,
  epsilon = 1e-04,
  r.svd = 1,
  pct.ratio = 0.05,
  absolute = FALSE,
  pct.aggregate = 1,
  contrast = NULL
)
```

Arguments

feature_table	A sample by feature matrix. Input for format_tempted.
time_point	The time stamp of each sample, matched with the rows of feature_table. Input for format_tempted.
subjectID	The subject ID of each sample, matched with the rows of feature_table. Input for format_tempted.
threshold	A threshold for feature filtering for microbiome data. Features with zero value percentage >= threshold will be excluded. Default is 0.95. Input for format_tempted.
pseudo_count	A small number to add to all the counts before normalizing into proportions and log transformation. Default is 1/2 of the smallest non-zero value that is specific for each sample. This pseudo count is added for transform=c("log_comp", "clr", "logit"). Input for format_tempted.

transform The transformation applied to the data. "log_comp" for log of compositions. "comp" for compositions. "ast" for arcsine squared transformation. "clr" for

central log ratio transformation. "logit" for logit transformation. "none" for no transformation. Default transform="clr" is recommended for microbiome data. For data that are already transformed, use transform="none". Input for

format_tempted.

Number of components to decompose into, i.e. rank of the CP type decomposi-

tion. Default is set to 3. Input for tempted.

smooth Smoothing parameter for RKHS norm. Larger means smoother temporal load-

ing functions. Default is set to be 1e-8. Value can be adjusted depending on the dataset by checking the smoothness of the estimated temporal loading function

in plot. Input for tempted.

interval The range of time points to ran the decomposition for. Default is set to be the

range of all observed time points. User can set it to be a shorter interval than the

observed range. Input for tempted.

resolution Number of time points to evaluate the value of the temporal loading function.

Default is set to 101. It does not affect the subject or feature loadings. Input for

tempted.

maxiter Maximum number of iteration. Default is 20. Input for tempted.

epsilon Convergence criteria for difference between iterations. Default is 1e-4. Input

for tempted.

r.svd The number of ranks in the mean structure. Default is 1. Input for svd_centraliz

pct.ratio The percent of features to sum up. Default is 0.05, i.e. 5%. Input for ratio_feature.

absolute = TRUE means features are ranked by the absolute value of feature

loadings, and the top pct.ratio percent of features are picked. absolute = FALSE means features are ranked by the original value of feature loadings, and the top and bottom pct.ratio percent of features are picked. Then ratio is taken as the abundance of the features with positive loading over the abundance of the

features with negative loading. Input for ratio_feature.

pct.aggregate The percent of features to aggregate, features ranked by absolute value of the

feature loading of each component. Default is 1, which means 100% of features are aggregated. Setting pct.aggregate=0.01 means top 1% of features is aggregated, where features are ranked in absolute value of feature loading of each

component. Input for aggregate_feature.

contrast A matrix choosing how components are combined, each column is a contrast of

length r and used to calculate the linear combination of the feature loadings of r components. Input for ratio_feature and Input for aggregate_feature.

Value

A list including all the input and output of functions format_tempted, svd_centralize(), tempted, ratio_feature, and aggregate_feature.

input All the input options of function tempted_all().

datlist_raw
datlist

mean_svd

A.hat Subject loading, a subject by r matrix.

B. hat Feature loading, a feature by r matrix.

Phi.hat Temporal loading function, a resolution by r matrix.

time.Phi The time points where the temporal loading function is evaluted.

Lambda Eigen value, a length r vector.

r.square Variance explained by each component. This is the R-squared of the linear re-

gression of the vectorized temporal tensor against the vectorized low-rank re-

construction using individual components.

accum.r.square Variance explained by the first few components accumulated. This is the R-

squared of the linear regression of the vectorized temporal tensor against the

vectorized low-rank reconstruction using the first few components.

metafeature.ratio

The log ratio abundance of the top over bottom ranking features. It is a data.frame with five columns: "value" for the log ratio values, "subID" for the subject ID, and "timepoint" for the time points, and "PC" indicating which component was

used to construct the meta feature.

toppct.ratio A matrix of TRUE/FALSE indicating which features are ranked top in each

component (and contrast) and used as the numerator of the log ratio.

bottompct.ratio

A matrix of TRUE/FALSE indicating which features are ranked bottom in each component (and contrast) and used as the denominator of the log ratio.

#'

metafeature.aggregate

The meta feature obtained by aggregating the observed temporal tensor. It is a data.frame with four columns: "value" for the meta feature values, "subID" for the subject ID, "timepoint" for the time points, and "PC" indicating which component was used to construct the meta feature.

toppct.aggregate

A matrix of TRUE/FALSE indicating which features are aggregated in each component and contrast.

component and contrast.

parameter contrast.

Examples

```
# for preprocessed data that do not need to be transformed
```

for count data that will have pseudo_count added and clr transformed

```
transform="clr",
                          pseudo_count=0.5,
                          r=2,
                          smooth=1e-5)
\# for proportional data that will have pseudo_count added and clr transformed
res_proportion <- tempted_all(count_table/rowSums(count_table),</pre>
                                meta_table$day_of_life,
                                meta_table$studyid,
                                threshold=0.95,
                                transform="clr",
                                pseudo_count=NULL,
                                r=2,
                                smooth=1e-5)
\ensuremath{\text{\#}} plot the temporal loading and subject trajectories grouped by delivery mode
plot_time_loading(res_proportion, r=2)
group <- unique(meta_table[,c("studyid", "delivery")])</pre>
plot_metafeature(res_proportion$metafeature.aggregate, group, bws=30)
```

Index

```
* datasets
    count_table, 4
    meta_table, 7
    processed_table, 10
aggregate_feature, 2, 9, 15, 16
bernoulli_kernel, 3
count_table, 4
\verb"est_test_subject", 4"
format_tempted, 2, 5, 15, 16
freg_rkhs, 6
meta\_table, 7
plot_feature_summary, 7
plot_metafeature, 8
\verb|plot_time_loading|, 9
processed_table, 10
ratio_feature, 8, 9, 10, 15, 16
svd_centralize, 2, 4-6, 12, 13, 15
tdenoise, 13
tempted, 2, 4-6, 9, 11-13, 13, 15, 16
tempted_all, 9, 15
```