

Module 12

Machine Learning

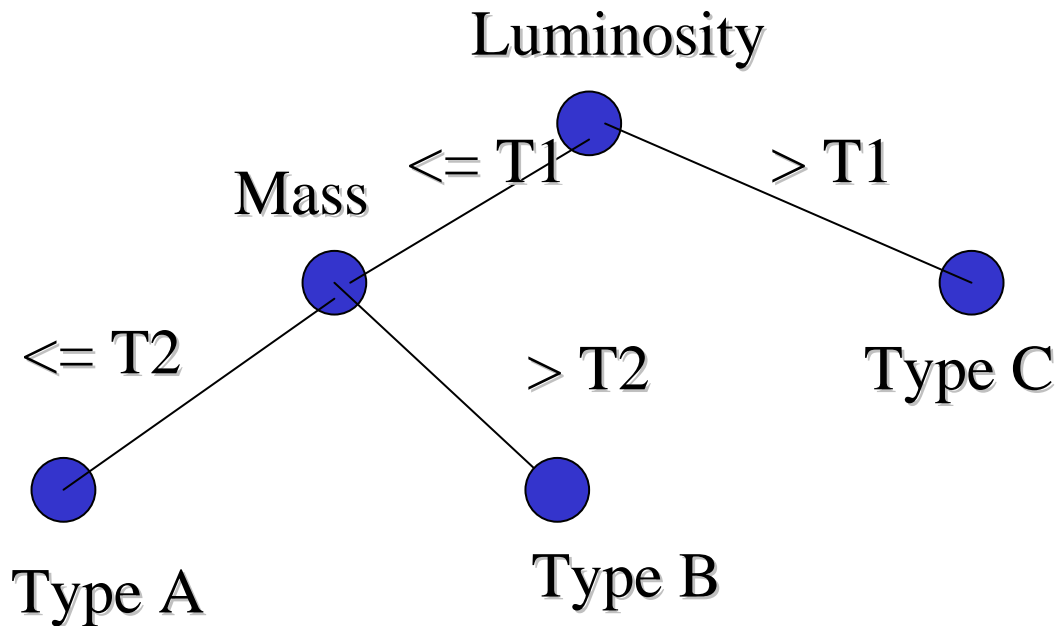
Version 2 CSE IIT, Kharagpur

Lesson 35

Rule Induction and Decision Tree - I

12.3 Decision Trees

Decision trees are a class of learning models that are more robust to noise as well as more powerful as compared to concept learning. Consider the problem of classifying a star based on some astronomical measurements. It can naturally be represented by the following set of decisions on each measurement arranged in a tree like fashion.



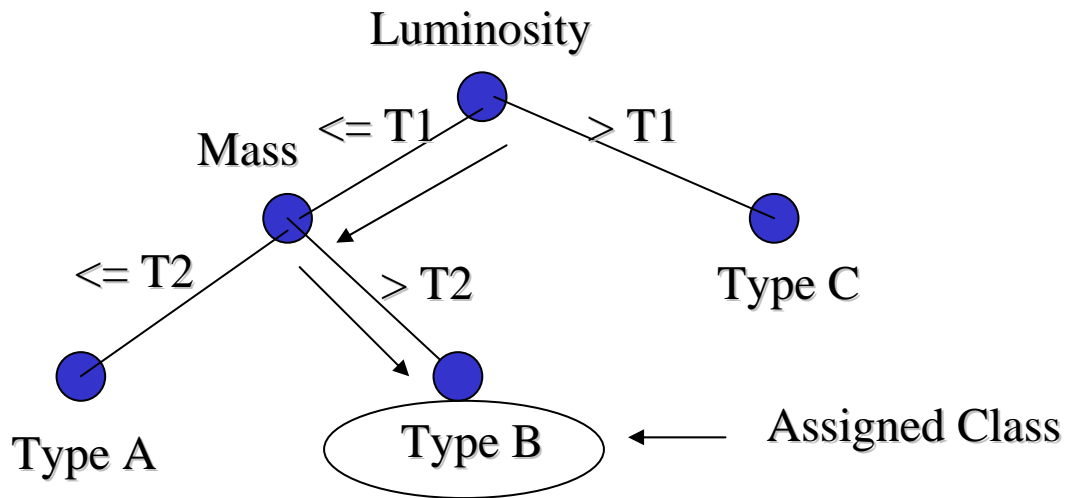
12.3.1 Decision Tree: Definition

- A decision-tree learning algorithm approximates a target concept using a tree representation, where each internal node corresponds to an attribute, and every terminal node corresponds to a class.
- There are two types of nodes:
 - Internal node.- Splits into different branches according to the different values the corresponding attribute can take. Example: luminosity $\leq T1$ or luminosity $> T1$.
 - Terminal Node.- Decides the class assigned to the example.

12.3.2 Classifying Examples Using Decision Tree

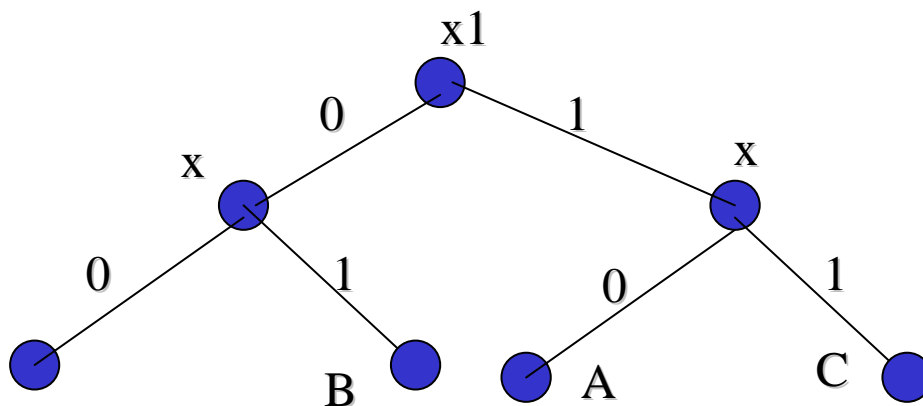
To classify an example X we start at the root of the tree, and check the value of that attribute on X . We follow the branch corresponding to that value and jump to the next node. We continue until we reach a terminal node and take that class as our best prediction.

$$X = (\text{Luminosity} \leq T1, \text{Mass} > T2)$$



Decision trees adopt a DNF (Disjunctive Normal Form) representation. For a fixed class, every branch from the root of the tree to a terminal node with that class is a conjunction of attribute values; different branches ending in that class form a disjunction.

In the following example, the rules for class A are: $(\sim X1 \ \& \ \sim x2)$ OR $(X1 \ \& \ \sim x3)$



12.3.3 Decision Tree Construction

There are different ways to construct trees from data. We will concentrate on the top-down, greedy search approach:

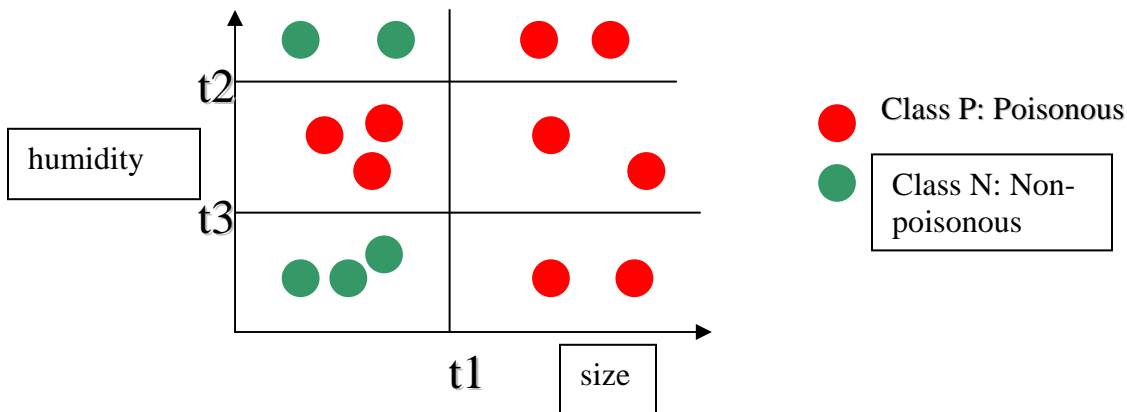
Basic idea:

1. Choose the best attribute a^* to place at the root of the tree.

2. Separate training set D into subsets $\{D_1, D_2, \dots, D_k\}$ where each subset D_i contains examples having the same value for a^*

3. Recursively apply the algorithm on each new subset until examples have the same class or there are few of them.

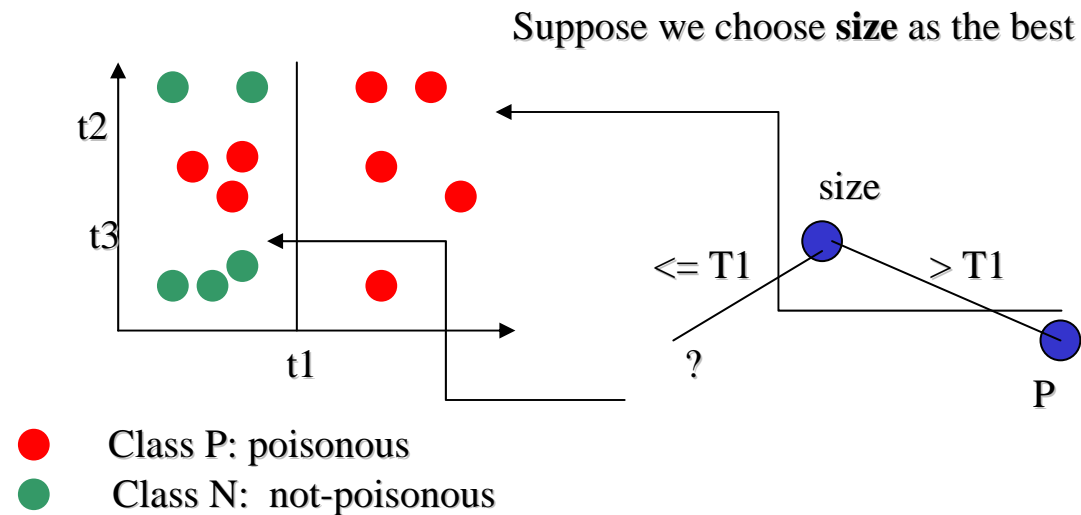
Illustration:



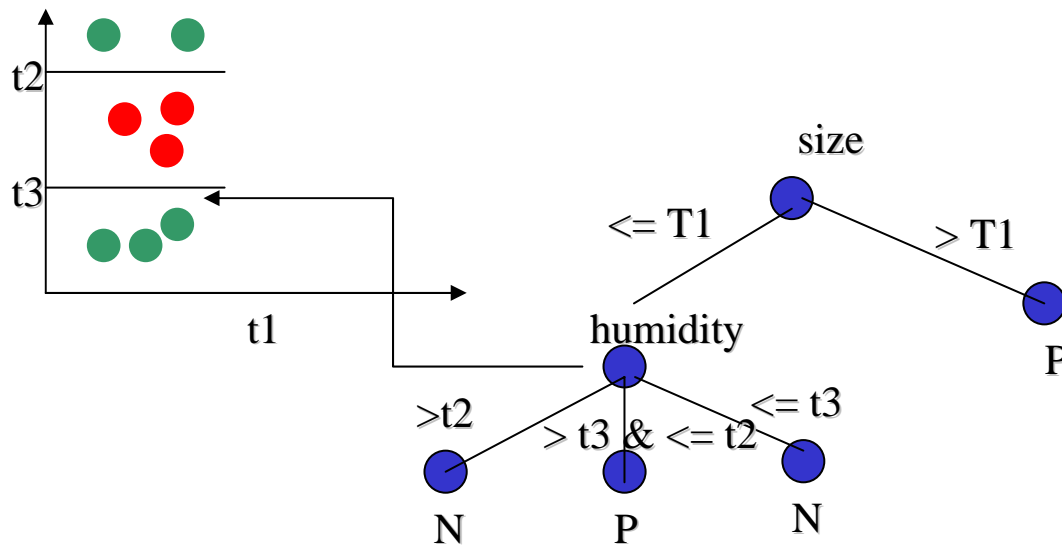
Attributes: size and humidity.

Size has two values: $> t_1$ or $\leq t_1$

Humidity has three values: $> t_2$, ($> t_3$ and $\leq t_2$), $\leq t_3$



Suppose we choose **humidity** as the next best



Steps:

- Create a root for the tree
- If all examples are of the same class or the number of examples is below a threshold return that class
- If no attributes available return majority class
- Let a^* be the best attribute
- For each possible value v of a^*
 - Add a branch below a^* labeled " $a = v$ "
 - Let S_v be the subsets of example where attribute $a^* = v$
 - Recursively apply the algorithm to S_v