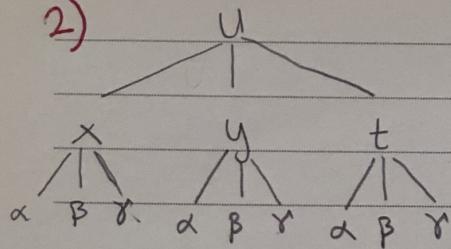


2)



When  $\alpha = -1, \beta = 2$  and  $\gamma = 1$ , we have  $x = 2, y = 4$  and  $t = -1$ .

With the help of this tree diagram, we have

$$\frac{\partial u}{\partial \alpha} = \frac{\partial u}{\partial x} \cdot \frac{\partial x}{\partial \alpha} + \frac{\partial u}{\partial y} \cdot \frac{\partial y}{\partial \alpha} + \frac{\partial u}{\partial t} \cdot \frac{\partial t}{\partial \alpha} = e^{ty}(2\alpha\beta) + x + te^{ty} \cdot 0 + xy e^{ty} \cdot \gamma^2$$

So, when  $(\alpha, \beta, \gamma) = (-1, 2, 1)$ , we have  $\frac{\partial u}{\partial \alpha} = e^{-4} \cdot 2(-1) \cdot 2 + 0 + 2 \cdot 4 e^{-4} \cdot 1^2$

$\frac{\partial u}{\partial \beta}$  and  $\frac{\partial u}{\partial \gamma}$  can be obtained in a similar manner.

$$= 4e^{-4}$$

Warning!!

don't write such things

3) Clearly, the profit function of  $x$  and  $y$  is

$$P(x, y) = R(x, y) - C(x, y) = 20x + 4y - 5x^2 - 2y^2 - 2xy - 4$$

To find which values of  $x$  and  $y$  maximize the profit, we need to find all critical points and determine which one gives us the absolute maximum.

$$P_x(x, y) = 20 - 10x - 2y = 0 \Rightarrow 10x + 2y = 20 \quad \left. \begin{array}{l} \\ \end{array} \right\} \Rightarrow x = 2 \text{ and}$$

$$P_y(x, y) = 4 - 4y - 2x = 0 \Rightarrow 2x + 4y = 4 \quad \left. \begin{array}{l} \\ \end{array} \right\} \quad y = 0$$

So we have a single critical point  $(2, 0)$ . Now.

$$P_{xx} = -10, P_{yy} = -4, P_{xy} = -2. \text{ So } D = P_{xx} P_{yy} - (P_{xy})^2 = (-10)(-4) - (-2)^2 = 40 - 4 = 36 > 0$$

and  $P_{xx} = -10 < 0$ .

Thus  $(2, 0)$  is the location of a maximum. Therefore, the profit is maximized when  $x = 2$  and  $y = 0$ . Moreover the maximum profit is

$$P(2, 0) = 16 \text{ thousand dollars.}$$