REMOVING PROJECTIVE DISTORTION FROM IMAGES

HOMOGRAPHY

The homography (H) can be calculated using point to point correspondence. The calculated homography can be use to remove the projective distortion.

Let,

$$X_{i} = \begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix}$$

$$X_{w} = \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

$$H = \begin{bmatrix} h_{11} & h_{12} & h_{13} \\ h_{21} & h_{22} & h_{23} \\ h_{31} & h_{32} & h_{33} \end{bmatrix}$$

The mapping between an image plane and a world plane is $X_i = HX_w$ where X_i is the coordinates in the image plane and X_w is the coordinates in the world plane. It can also be noted that $h_{33} = 1$. Thus,

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} h_{11} & h_{12} & h_{13} \\ h_{21} & h_{22} & h_{23} \\ h_{31} & h_{32} & h_{33} \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$
$$x'_{i} = x_{i}h_{11} + y_{i}h_{12} + h_{13} - x_{i}'x_{i}h_{31} - x_{i}'y_{i}h_{32}$$
$$y'_{i} = x_{i}h_{21} + y_{i}h_{22} + h_{23} - y_{i}'x_{i}h_{31} - y_{i}'y_{i}h_{32}$$

The matrix form of the above equation is

$$\begin{bmatrix} x_1 & y_1 & 1 & 0 & 0 & 0 & -x_1{'}x_1 & -x_1{'}y_1 \\ 0 & 0 & 0 & x_1 & y_1 & 1 & -y_1{'}x_1 & -y_1{'}y_1 \\ \vdots & & \vdots & & \vdots & & \vdots \\ x_n & y_n & 1 & 0 & 0 & 0 & -x_n{'}x_n & -x_n{'}y_n \\ 0 & 0 & 0 & x_n & y_n & 1 & -y_n{'}x_n & -y_n{'}y_n \end{bmatrix}_{2nx8} \times \begin{bmatrix} h_{11} \\ h_{12} \\ h_{13} \\ h_{21} \\ h_{22} \\ h_{23} \\ h_{31} \\ h_{32} \end{bmatrix}_{8x1} = \begin{bmatrix} x_1{'} \\ y_1{'} \\ \vdots \\ x_n{'} \\ y_n{'} \end{bmatrix}_{2nx1}$$

Note: n is the number of pairs of corresponding points

Let A be the 2nx8 matrix, B be the 2nx1 matrix and h be the 8x1 matrix. Thus, the matrix equation above can be denoted as Ah = B. Using the least square estimate, we can get the value of h.

$$h = (A^T A)^{-1} A^T B$$

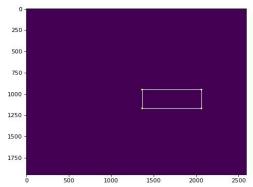
After calculating the homography, we can perform the mapping from the image plane to world plane.

RESULTS:

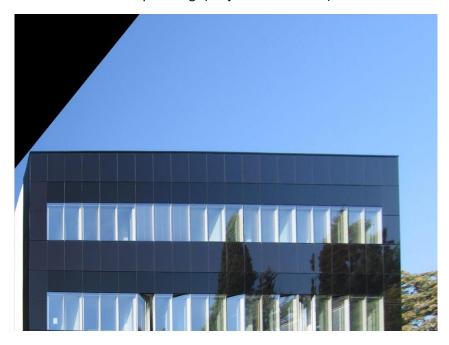
Original Image







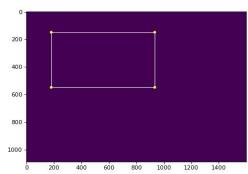
Output Image(Projective Removed)



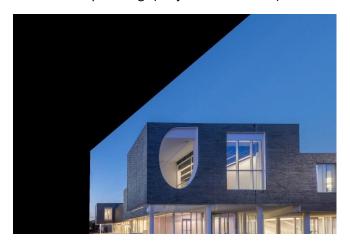
Original Image





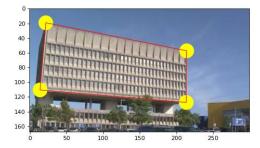


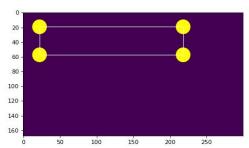
Output Image(Projective Removed)



Original Image







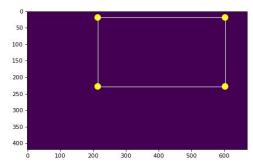
Output Image(Projective Removed)



Original Image







Output Image (Projective Removed)



REFERENCES:

R. Wu, "ECE661 Computer Vision HW 3." [Online] Available: https://engineering.purdue.edu/kak/computervision/ECE661_Fall2016/Homeworks/HW3/2BestSolution s/1.pdf

V. Ravi, "ECE 661 Computer Vision Homework 3." [Online] Available: https://engineering.purdue.edu/RVL/ECE661_2018/Homeworks/HW3/2BestSolutions/2.pdf