Q:

a. Outline an algorithm for deleting a key from a binary search tree. Would you classify this algorithm as a variable-size-decrease algorithm?
b. What is the time efficiency class of your algorithm in the worst case?

A:

a. When deleting a key from a binary search tree, three possibilities can happen:

Case 1: *The key's node is a leaf*
What to do: **Remove node from tree**

Case 2: *The key's node has one child*
What to do: **Copy the child node, delete the key's node, replace it with the child node**

Case 3: *The key's node has two children*
What to do: **Find either the minimum in the right subtree of the key's node or the maximum in the left subtree, *M*, copy *M* to the key's node, and delete the duplicate *M* from the subtree.**

Note: deleting the duplicate *M* may perform the 3rd case in every iteration until it reaches either the 1st or 2nd case.

With this, deleting a key from a binary search tree can be classified as a variable-size-decrease algorithm since the size-reduction pattern varies on the number of children of each node, and the key of each node.

b. The time efficiency of the algorithm in the worst case is $O(h)$ where h is the height of the tree.