

Q: Rumor spreading

There are n people, each in possession of a different rumor. They want to share all the rumors with each other by sending electronic messages. Assume that a sender includes all the rumors he or she knows at the time the message is sent and that a message may only have one addressee.

Design a greedy algorithm that always yields the minimum number of messages they need to send to guarantee that every one of them gets all the rumors.

A: Say people are labeled as P_1, P_2, \dots, P_n

P_1 sends a rumor to P_2 , P_2 sends the same message plus their possessed rumor to P_3 , then from P_3 to P_4 , until P_{n-1} sends all the combined rumors plus their possessed rumor to P_n . Then P_n , which possesses all the rumors at that point, sends them to P_1, P_2, \dots, P_{n-1} .

The minimum number of messages that will be sent is $2n - 1$.