## Problem Set 4, Problem 3

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This problem set is due Tuesday, November 5 at 11:59PM.

This solution template should be turned in through our submission site. <sup>1</sup>

For written questions, full credit will be given only to correct solutions that are described clearly and concisely.

 $<sup>^{1}</sup>$ Register an account, if you haven't done so. Then go to Homework, Problem Set 4, and upload your files.

## Problem 4-3. [25 points] Joan of Arcsin

(a) [10 points] Explain how you would implement the arcsin function using Newton's Method, and the given library. It must work correctly and efficiently for all y in the given range, including the endpoints. You may assume that the given library is correct and of great accuracy.

We start with the equation  $x = \arcsin(y)$ . Since we can only use mathematical functions in our library with  $\sin$ ,  $\cos$ , and  $\tan$ , we change this equation to  $y = \sin(x)$ . Then we subtract from both sides to get  $\sin(x) - y = 0$ . Thus, we let  $f(x) = \sin(x) - y$  and find that  $f'(x) = \cos(x)$ . We can use the tangent line approximation to get  $x_{i+1} = x_i - \frac{f(x_i)}{f'(x_i)}$ .

(b) [10 points] Explain why one iteration of Newton's Method definitely improves your approximation to the correct answer (assuming that it is not already exactly the correct answer).

(c) [5 points] Explain why your iterative procedure doesn't take you outside the range  $[0, \frac{\pi}{2}]$ , inclusive.

Write something here!