Empirical_Distribution

October 18, 2022

1 The Empirical Rule and Distribution

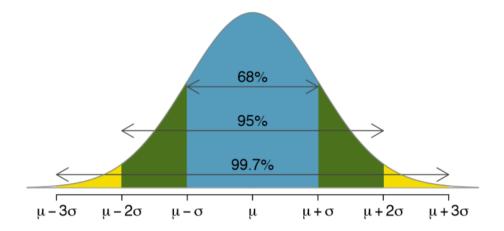
In week 2, we discussed the empirical rule or the 68 - 95 - 99.7 rule, which describes how many observations fall within a certain distance from our mean. This distance from the mean is denoted as sigma, or standard deviation (the average distance an observation is from the mean).

The following image may help refresh your memory:

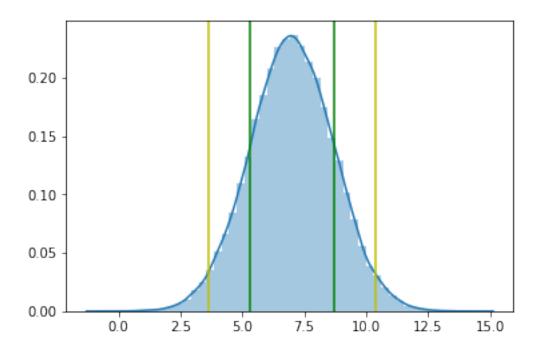
For this tutorial, we will be exploring the number of hours the average college student gets.

The example used in lecture stated there was a mean of 7 and standard deviation of 1.7 for hours of sleep; we will use these same values.

```
In [1]: import warnings
        warnings.filterwarnings('ignore')
        import random
        import numpy as np
        import pandas as pd
        import matplotlib.pyplot as plt
        import seaborn as sns
        random.seed(1738)
In [2]: mu = 7
        sigma = 1.7
        Observations = [random.normalvariate(mu, sigma) for _ in range(100000)]
In [3]: sns.distplot(Observations)
        plt.axvline(np.mean(Observations) + np.std(Observations), color = "g")
        plt.axvline(np.mean(Observations) - np.std(Observations), color = "g")
        plt.axvline(np.mean(Observations) + (np.std(Observations) * 2), color = "v")
        plt.axvline(np.mean(Observations) - (np.std(Observations) * 2), color = "y")
Out[3]: <matplotlib.lines.Line2D at 0x7fb631cc85c0>
```



Three Sigma Rule



In [6]: pd.Series(Observations).describe()

Out[6]:	count	100000.000000
	mean	7.000626
	std	1.693249
	min	-0.754203
	25%	5.865611
	50%	7.003080
	75%	8.144851

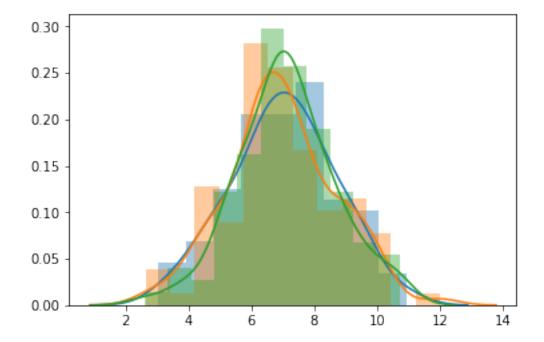
```
max 14.595650
dtype: float64

In [4]: SampleA = random.sample(Observations, 100)
        SampleB = random.sample(Observations, 100)
        SampleC = random.sample(Observations, 100)

In [5]: fig, ax = plt.subplots()

sns.distplot(SampleA, ax = ax)
        sns.distplot(SampleB, ax = ax)
        sns.distplot(SampleC, ax = ax)
```

Out[5]: <matplotlib.axes._subplots.AxesSubplot at 0x7fb631c15be0>



Now that we have covered the 68 - 95 - 99.7 rule, we will take this a step further and discuss the empirical distribution.

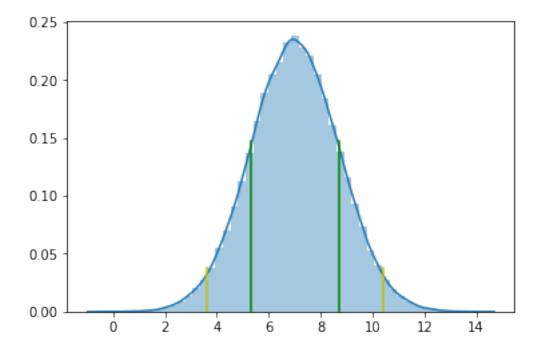
The empirical distribution is a cumulative density function that signifies the proportion of observations that are less than or equal to a certain values.

Lets use the initial image above as an example of this concept:

Now, by using our observations for ours of sleep, we can create an empirical distribution in python that signifies the proportion of observations are observed at a specific number for hours of sleep.

```
Observations = [random.normalvariate(mu, sigma) for _ in range(100000)]
sns.distplot(Observations)
plt.axvline(np.mean(Observations) + np.std(Observations), 0, .59, color = 'g')
plt.axvline(np.mean(Observations) - np.std(Observations), 0, .59, color = 'g')
plt.axvline(np.mean(Observations) + (np.std(Observations) * 2), 0, .15, color = 'y')
plt.axvline(np.mean(Observations) - (np.std(Observations) * 2), 0, .15, color = 'y')
```

Out[7]: <matplotlib.lines.Line2D at 0x7fb633fbbf60>



In [8]: from statsmodels.distributions.empirical_distribution import ECDF
 import matplotlib.pyplot as plt

ecdf = ECDF(Observations)

plt.plot(ecdf.x, ecdf.y)

plt.axhline(y = 0.025, color = 'y', linestyle='-')
 plt.axvline(x = np.mean(Observations) - (2 * np.std(Observations)), color = 'y', linestyle='-')

plt.axhline(y = 0.975, color = 'y', linestyle='-')
 plt.axvline(x = np.mean(Observations) + (2 * np.std(Observations)), color = 'y', linestyle='-')

Out[8]: <matplotlib.lines.Line2D at 0x7fb6318e8ba8>

