Skeleton Clustering : A Dimension free Density-Aided Clustering

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Traditional Clustering Methods

• k-means clustering:

- Unable to detect non-convex clusters.
- The center of a non-convex cluster falls outside the cluster itself and may come close to observations from a different cluster.
- In high dimension k-means algorithm may assign all the points to a single cluster.

Density Based Clustering:

- To estimate the underlying PDF and detect clusters based on the PDF.
- The rate of convergence for the density estimates is $\mathcal{O}_{\mathbb{P}}(n^{-\frac{1}{d+4}})$
- Hierarchical Clustering:

Skeleton Clustering Framework.

Input: Observations X_1, X_2, \dots, X_N , final number of clusters S.

- **Knot construction**: Perform k—means clustering with a large number k; the centers are the knots.
- **2 Edge construction** : Apply approximate Delaunay triangulation to the knots. Generally we choose $k = |\sqrt{n}|$
- Edge weights construction: Add weights to each edge using either Voronoi density, Face density or Tube density similarity measure.
- Knots segmentation: Use linkage criterion to segment knots into S groups based on the edge weights.
- **Assignment of labels**: Assign a cluster label to each observation based on which knot group the nearest knot belongs to.

Knot construction

- Some knots are constructed to give a concise representation of the data structure.
- In practice we use k-Means to choose $k = \lfloor \sqrt{n} \rfloor$ knots, where n is the number of samples.
- Empirically robustness performance with sufficient number of knots.