



Essential Data Skills for Business Analytics

Lecture 6 : Functions and Parameters

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Reusable codes

calc:

Do the following operations for two numbers and print results:

+, -, *, /

```
def calc(a, b):
    sum = a + b
    subtraction = a - b
    multiply = a * b
    division = a / b
    print ("sum is: ", sum)
    print ("subtraction is: ", subtraction)
    print ("multiplication is: ", multiply)
    print ("division is: ", division)
```

- >>> calc (5,7)
- >>> calc (3.0, 4)
- >>> calc (1.2, 2.5)

Function

- A function is a block of organized, reusable code that is used to perform a group of related actions.
- Functions provide better modularity for your application and a high degree of code reusing.

Python functions

- There are two kinds of functions in Python
 - ❑ **Build-in functions** that are provided as part of Python
 - `input()`, `type()`, `float()`, `int()`, ...
 - ❑ **Functions that we define ourselves** and then use

Build-in functions

- Math functions
 - Python has a math module that provides most of the familiar mathematical functions.
 - Before use all these functions, we have to import them: `>>> import math`
 - To call one of the functions, we have to specify the name of the module and the name of the function, separated by a dot. This format is also called **dot notation**.
 - `>>>decibel = math.log10(17.0)`
 - `>>>angle = 1.5`
 - `>>>height = math.sin(angle)`

Math function examples

```
>>> degrees = 45
```

```
>>> angle = degrees * 2 * math.pi / 360
```

```
>>> math.sin(angle)
```

```
0.707106781187
```

- Combination of functions

```
>>> x = math.exp(math.log(10))
```

Many other math functions

Function name	Description
<code>abs (value)</code>	absolute value
<code>ceil (value)</code>	rounds up
<code>cos (value)</code>	cosine, in radians
<code>degrees (value)</code>	convert radians to degrees
<code>floor (value)</code>	rounds down
<code>log (value, base)</code>	logarithm in any base
<code>log10 (value)</code>	logarithm, base 10
<code>max (value1, value2, ...)</code>	larger of two (or more) values
<code>min (value1, value2, ...)</code>	smaller of two (or more) values
<code>radians (value)</code>	convert degrees to radians
<code>round (value)</code>	nearest whole number
<code>sin (value)</code>	sine, in radians
<code>sqrt (value)</code>	square root
<code>tan (value)</code>	tangent

Constant	Description
<code>e</code>	2.7182818...
<code>pi</code>	3.1415926...

Defining our own functions

- Simple rules to define a function
 1. Function blocks begin with the keyword **def** followed by the function name, parentheses (), and a colon :
 2. Any parameters or arguments should be placed within these parentheses.
 3. The code block within every function is **indented**.

```
def function_name (parameters):  
    statement 1 in the function body  
    statement 2 in the function body  
    ...  
    statement n in the function body
```

Building our own functions

- Defining a function doesn't mean we execute the body of the function
- test.py file:

```
x = 5
print ('Hello')

def print_oks():
    print ('OK 1')
    print ('OZ 2')

print 'Yo'
x = x + 2
print (x)
```

- python test.py

```
Hello
Yo
7
```

Calling a function

- Once we have defined a function, we can **call** (or **invoke**) it as many times as we like
- This is a store and reuse pattern
- test.py file:

```
x = 5                                (1)
print ('Hello')                         (2)

def print_oks():
    print ('OK 1')                      (5)
    print ('OK 2')                      (6)

print ('World')                          (3)
print_oks()                            (4)
x = x + 2                             (8)
print (x)                              (9)
```

- python test.py

```
Hello
World
OK 1
OK 2
7
```

Arguments

- An **argument** is a value we pass into the **function** as its **input** when we call the function
- Sometimes, the function doesn't need input (**no arguments**)
- We use **arguments** so we can direct the **function** to do different kinds of work when we call it at **different** times
- We put the **arguments** in parentheses after the **name** of the function

```
def calc(a, b):  
    sum = a + b  
    subtraction = a - b  
    multiply = a * b  
    division = a / b  
    print ("sum is: ", sum)  
    print ("subtraction is: ", subtraction)  
    print ("multiplication is: ", multiply)  
    print ("division is: ", division)
```

Arguments

```
def calc(a, b):
    sum = a + b
    subtraction = a - b
    multiply = a * b
    division = a / b
    print ("Sum is: ", sum)
    print ("Subtraction is: ", subtraction)
    print ("Multiplication is: ", multiply)
    print ("Division is: ", division)
```

x = 3 (1)

y = 5 (2)

m = 2.0 (3)

n = 7 (4)

i = 2.5 (5)

j = 2.2 (6)

Arguments

calc(x, y) ## or calc(3, 5) (7)

calc(m, n) ## or calc(2.0, 7) (8)

calc(i, j) ## or calc(2.5, 2.2) (9)

Outputs:

Sum is: 8

Subtraction is: -2

Multiplication is: 15

Division is: 0

Sum is: 9.0

Subtraction is: -5.0

Multiplication is: 14.0

Division is: 0.2857142857142857

Sum is: 4.7

Subtraction is: 0.3

Multiplication is: 5.5

Division is: 1.1363636363636362

Parameters

- A **parameter** is a variable which we use in the function definition
- It is a “**handle**” that allows the code in the function to **access the arguments** for a particular **function invocation**

Parameter



```
def greet(lang):  
    if lang == 'es':  
        print ('Hola')  
    elif lang == 'fr':  
        print ('Bonjour')  
    else:  
        print ('Hello')  
  
>>> greet('en')  
Hello  
>>> greet('es')  
Hola  
>>> greet('fr')  
Bonjour  
>>>
```

Back to arguments

- In Python, there are four types of arguments
 - Required arguments
 - Keyword arguments
 - Default arguments
 - Variable-length arguments

Required arguments

- Required arguments are the arguments passed to a function in correct positional order.
- **The number of arguments in the function call should match exactly with the parameters in the function definition.**

```
#!/usr/bin/python

# define a function
def printme( s ):
    print (s)
    return

# call the function
printme()      → printme("I'm KZ")
```

Traceback (most recent call last):
 File "test.py", line 8, in <module>
 printme();
TypeError: printme() takes exactly 1 argument (0 given)

Required argument

Keyword arguments

- Keyword arguments are related to the function calls.
- When you use keyword arguments **in a function call**, the **caller identifies the arguments by the parameter name**.
- This **allows you to skip arguments or place them out of order** because the Python interpreter is able to use the keywords provided to match the values with parameters.

```
#!/usr/bin/python

# Function definition is here
def printinfo( name, age ):
    "This prints a passed info into this function"
    print "Name: ", name
    print "Age ", age
    return;

# Now you can call printinfo function
printinfo( age=50, name="miki" )
```

Keyword arguments

Name: miki
Age: 50

Required arguments:
printinfo("miki", 50)



Printinfo(50, "miki")



Default arguments

- A default argument is an argument that assumes a default value if a value is not provided in the **function call** for that argument.

```
#!/usr/bin/python

# Function definition is here
def printinfo( name, age = 35 ):
    "This prints a passed info into this function"
    print "Name: ", name
    print "Age ", age
    return;

# Now you can call printinfo function
printinfo( age=50, name="miki" ) → Keyword arguments
printinfo( name="miki" ) → Default arguments
```

```
Name: miki
Age 50
Name: miki
Age 35
```

Variable-length arguments

- You may need to process a function for more arguments than you specified while defining the function.
- Variable-length arguments are not named in the function definition.
- Use * before the variable name that holds the values of all other variable arguments **in the definition**.
- This variable remains empty if no additional arguments are specified **during the call**.

```
def functionaame(< formal_args >, *var_args_tuple):  
    statements
```

```
#!/usr/bin/python  
  
# Function definition is here  
def printinfo( arg1, *vartuple ):  
    "This prints a variable passed arguments"  
    print "Output is: "  
    print arg1  
    for var in vartuple:  
        print var  
    return;  
  
# Now you can call printinfo function  
printinfo( 10 )  
printinfo( 70, 60, 50 )
```

```
Output is:  
10  
Output is:  
70  
60  
50
```

Anonymous functions

- Anonymous functions are not declared in the standard manner by using the **def** keyword.
- Use the **lambda** keyword to create small anonymous functions.

```
lambda : expression
lambda arg1, arg2, ..., argN: expression
```

Anonymous function rules (1)

- Lambda forms can take any number of arguments but return just one value in the form of an expression. They can not contain commands or multiple expression.

```
>>>func = lambda : 5+3
>>>func
8

>>>func = lambda a, b: a+b
>>>sum = func(5,3)
>>>print ("sum is: ", sum)
sum is: 8
```

```
>>>func = lambda a,b: a+b; a-b
>>>func(5,3)
8
```



Anonymous function rules (2)

- An anonymous function **can not be a direct call** to print because lambda **requires an expression**.

```
>>>func = lambda : print "hello world"  
>>>func
```



The *return* statement

- Often a function will take its arguments, do some computation, and **return a value** to be used as the **value of the function call** in the **calling expression**.
- The ***return*** keyword is used for this.
- A return statement with no arguments is the same as return none.

```
def greet():
    return "Hello"      (2) (4)
```

```
print greet(), "Glenn"  (1)
print greet(), "Sally"  (3)
```

```
Hello Glenn
Hello Sally
```

The *return* statement

- The *return* statement ends the function execution and “sends back” the result of the function

```
def greet(lang):  
    if lang == 'es':  
        return 'Hola'  
    elif lang == 'fr':  
        return 'Bonjour'  
    else:  
        return 'Hello'  
  
>>> print (greet('en'), 'Glenn')  
Hello Glenn  
>>> print (greet('es'), 'Sally')  
Hola Sally  
>>> print (greet('fr'), 'Michael')  
Bonjour Michael
```

What `greet` does:

- 1) Receives the argument value
- 2) If the lang is es, then return Hola, otherwise,
 - 2.1) If the lang is fr, then return Bonjour, otherwise return Hello

```
#!/usr/bin/python

# Function definition is here
def sum( arg1, arg2 ):
    # Add both the parameters and return them."
    total = arg1 + arg2
    print "Inside the function : ", total
    return total;

# Now you can call sum function
total = sum( 10, 20 );
print "Outside the function : ", total
```

```
Inside the function : 30
Outside the function : 30
```

Arguments, parameters, and results

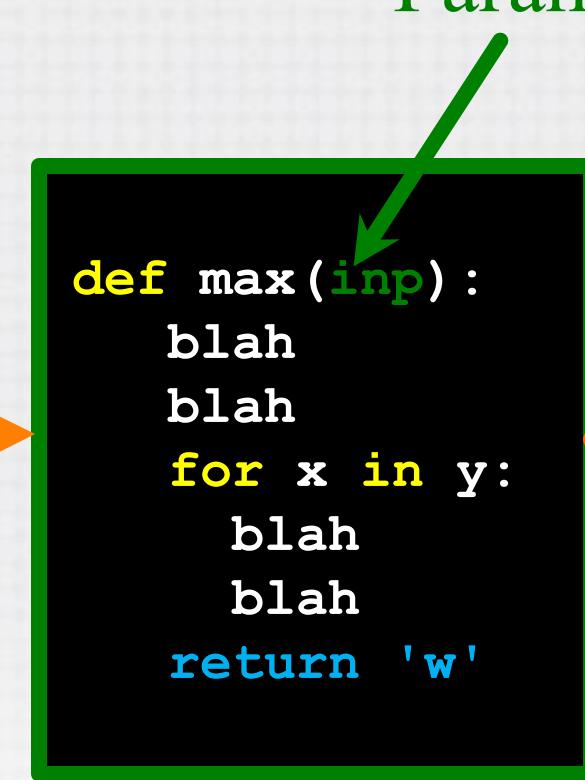
```
>>> big = max('Hello World')
```

```
>>> print big
```

```
w
```

'Hello world'

Argument



Parameter

'w'

Result

Multiple parameters / arguments

- We can define more than one **parameter** in the **function** definition
- We simply add more **arguments** when we call the **function**
- We match the number and the order of arguments and parameters

```
def addtwo(a, b):  
    added = a + b  
    return added
```

```
x = addtwo(3, 5)  
print (x)
```

Void (non-fruitful) functions

- When a function does not return a value, we call it a “void” function
- Functions that return values are “fruitful” functions
- Void functions are “not fruitful”

Program development

- To deal with increasingly complex programs, we are going to suggest a technique called **incremental development**.
- It is to avoid long debugging sessions by adding and testing only a small amount of code at a time.

$$\text{distance} = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

- The first step is to consider what a distance function should look like in Python.

Program development

$$\text{distance} = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

- What are the inputs (parameters) and what is the output (return value)?

```
def distance(x1,y1,x2, y2):  
    return 0.0
```

- To test the function, we call it with sample values

```
>>> distance(1,2,4,6)  
0
```

Program development

- Find the differences $x_2 - x_1$ and $y_2 - y_1$

```
def distance(x1,y1,x2,y2):  
    dx = x2-x1  
    dy = y2-y1  
    print ('dx is: ', dx)  
    print ('dy is: ', dy)  
    return 0.0
```

- To test the function, we call it with sample values

```
>>> distance(1,2,4,6)  
dx is: 3  
dy is: 4  
0
```

Program development

- Compute the sum of squares of dx and dy

```
def distance(x1,y1,x2,y2):  
    dx = x2-x1  
    dy = y2-y1  
    dsquared = dx**2 + dy**2  
    result = math.sqrt(dsquared)  
    return result
```

Recursion

- It is legal for one function to call another.

```
def distance(x1,y1,x2,y2):  
    dx = subtraction(x2,x1)  
    dy = subtraction(y2,y1)  
    dsquared = dx**2 + dy**2  
    result = math.sqrt(dsquared)  
    return result
```

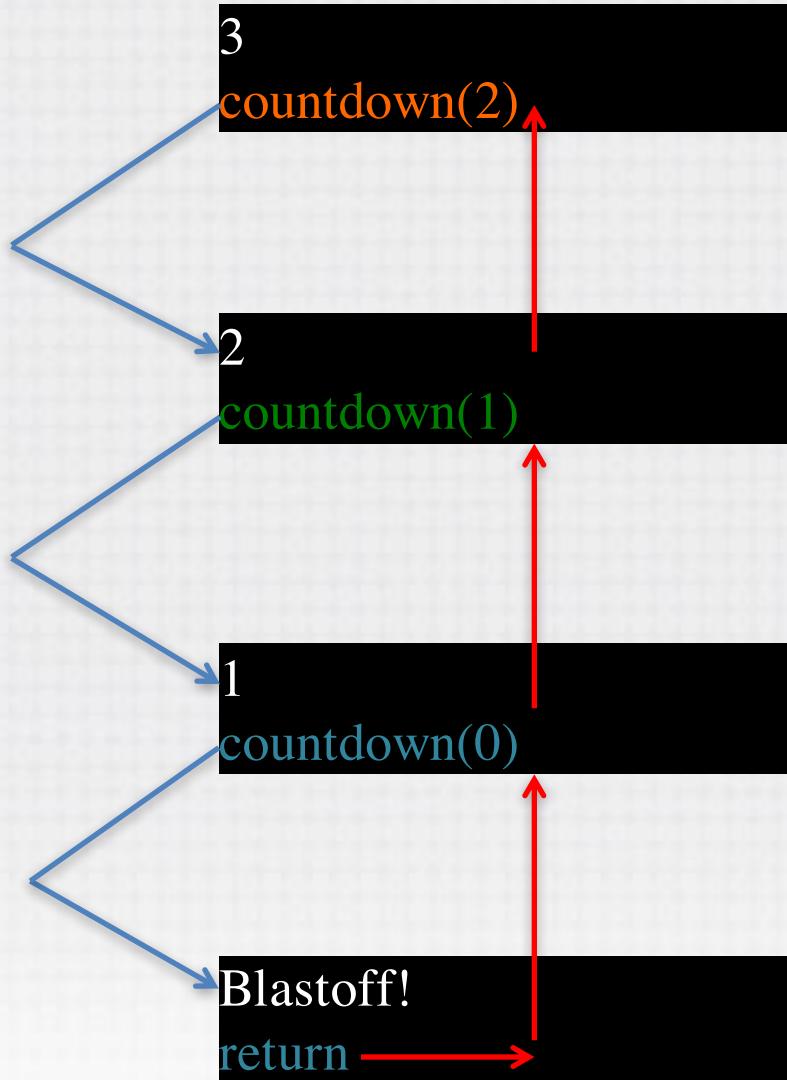
```
def subtraction(a,b):  
    sub = a-b  
    return sub
```

- What about **calling itself?**

Recursion

```
def countdown(n):
    if n == 0:
        print "Blastoff!"
    else:
        print n
        countdown(n-1)
```

```
>>> countdown(3)
```



Examples

```
def factorial(n):
    if n == 0:
        return 1
    else:
        return n * factorial(n-1)
```

```
>>> factorial(4)
```

```
def fibonacci(n):
    if n == 0:
        return 0
    elif n == 1:
        return 1
    else:
        return fibonacci(n-1) + fibonacci(n-2)
```

```
>>> fibonacci(5)
```