## Homework 01: Text Classification

## CS 6501-005 Natural Language Processing

Updated on: September 13, 2019

1. Suppose you have a single feature x, with the following conditional distribution:

$$p(x \mid y) = \begin{cases} \alpha & X = 0, Y = 0\\ 1 - \alpha & X = 1, Y = 0\\ 1 - \beta & X = 0, Y = 1\\ \beta & X = 1, Y = 1 \end{cases}$$
(1)

Further suppose that the prior distribution is uniform, P(Y=0) = P(Y=1) = 0.5, and that both  $\alpha > \frac{1}{2}$  and  $\beta > \frac{1}{2}$ . Given a Naive Bayes classifier with accurate parameters, what is the probability of making an error?

- 2. Suppose you have two labeled datasets  $D_1$  and  $D_2$ , with the same feature set and labels
  - Let  $\theta^{(1)}$  be the unregularized logistic regression (LR) coefficients from training on dataset  $D_1$ ,
  - Let  $\theta^{(2)}$  be the unregularized logistic regression (LR) coefficients from training on dataset  $D_2$ ,
  - Let  $\theta^*$  be the unregularized logistic regression (LR) coefficients from training on dataset  $D_1 \cup D_2$ .

Under these conditions, prove that for any feature j,

$$\min(\theta_j^{(1)}, \theta_j^{(2)}) \le \theta_j^* \le \max(\theta_j^{(1)}, \theta_j^{(2)})$$

- 3. Let  $\hat{\boldsymbol{\theta}}$  be the solution to an unregularized logistic regression problem, and let  $\boldsymbol{\theta}^*$  be the solution to the same problem, with  $L_2$  regularization. Prove that  $\|\boldsymbol{\theta}^*\|_2^2 \leq \|\hat{\boldsymbol{\theta}}\|_2^2$ .
- 4. Prove that F-measure is never greater than the arithmetic mean of precision and recall,  $\frac{p+r}{2}$ . Your solution should also show that F-measure is equal to  $\frac{p+r}{2}$  if and only if p=r. [Hint: "if and only if" means that you need to prove the statement in both directions. In other words, your solution needs to show, with the definition of F-measure, both (1)  $p=r \Rightarrow F=\frac{p+r}{2}$  and (2)  $F=\frac{p+r}{2} \Rightarrow p=r$  hold.]
- 5. In this assignment, you will be asked to build a logistic regression classifier for sentiment classification with the following files
  - trn-reviews.txt: the Yelp reviews in the training set
  - trn-labels.txt: the corresponding labels of the Yelp reviews in the training set
  - dev-reviews.txt: the Yelp reviews in the development set
  - dev-labels.txt: the corresponding labels of the Yelp reviews in the development set

The starting point of building a classifier is from the IPython notebook **demo.ipynb**. The first section of this notebook provides a simple code to load the training and development set. Your work starts from the *second* section.

- In the second section, you can implement the CountVectorizer function with different parameter settings, as shown in the two examples in this section.
- In the third section, try to pick different values of the parameters within function LogisticRegression

The task is to find the parameter setting used for both CountVectorizer and LogisticRegression, which can give the **best** accuracy on the development set. The baseline accuracy is 61.4% with uni-gram features and your results should be better than this number.

Your homework submission should include the IPython notebook with the name [Your-ComputingID].ipynb. Please keep the best parameter setting only in the notebook, so we can easily reproduce the results.