

4 a) Hallar una aproximación $\sqrt{3}$ con una tolerancia 10^{-4} usando el algoritmo bisección

Escriba las primeras 5 iteraciones del método

$$\text{Sea } a_0 = 1 \text{ y } b_0 = 2 \quad f(a) = 1^2 - 3 = -2 \quad \Rightarrow \quad a_1 = m = 1.5^2 \\ \Rightarrow m = 1 + \frac{2-1}{2} = 1.5 \quad \Rightarrow \quad f(m) = (1.5)^2 - 3 = -0.75 \quad \Rightarrow \quad b_1 = 2$$

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$$\Rightarrow m = 1.5 + \frac{2-1.5}{2} = 1.75 \quad \Rightarrow f(a_1) = (1.5)^2 - 3 = -0.75 \quad \Rightarrow b_2 = m = 1.75 \\ f(m_1) = (1.75)^2 - 3 = 0.0625 \quad a_2 = 1.5$$

$$\Rightarrow m = 1.5 + \frac{1.75-1.5}{2} = 1.625 \quad f(m) = (1.625)^2 - 3 = -0.359375 \quad \Rightarrow m = a_3 = 1.625 \\ \Rightarrow f(a_2) = -0.75 \quad b = 1.75$$

$$\Rightarrow m = 1.625 + \frac{1.75-1.625}{2} = 1.6875 \quad \Rightarrow f(m) = (1.6875)^2 - 3 = -0.15234375 \\ f(a_3) = -0.359375 \quad \Rightarrow m = a = 1.6875 \\ b = 1.75$$

$$\Rightarrow m = 1.6875 + \frac{1.75-1.6875}{2} = 1.71875$$

$$f(a) = (1.6875)^2 - 3 = -0.15234375$$

$$f(m) = (1.71875)^2 - 3 = -0.0458984375$$