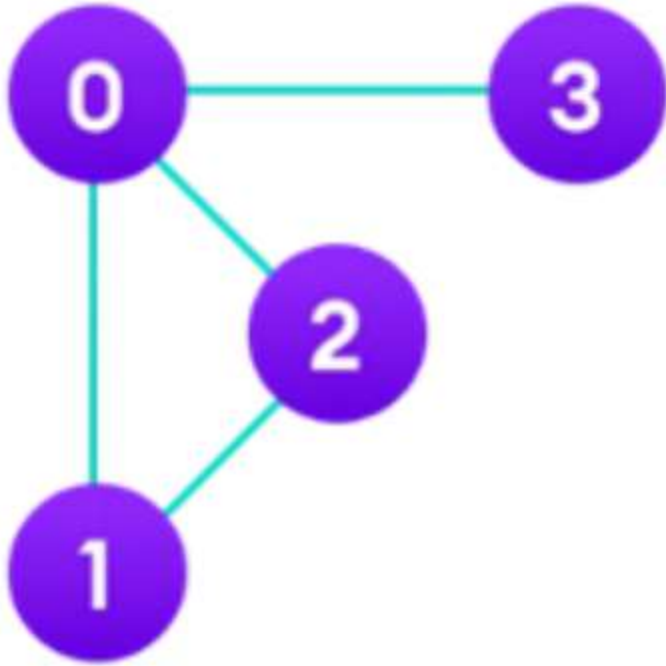


Graph

- *Non-Linear Data Structure*
- *Collection of vertices that have data and are connected to other vertices*
- **Example 1 – Social Media**
 - *Users on social networking sites such as **Facebook, WhatsApp, Messenger, Twitter, Google+, LinkedIn, etc.** are linked through a large graph*
 - *Here, people or users are represented by the **vertices** and any connection between the users, such as followers, friendships, likes, or subscriptions, is represented by the **edges***
- **Example 2 – Graphs used in connecting people through viral videos**
 - *Each user is a **vertex** in this case, and when users connect, they form an **edge**. When a video reaches a certain number of connections/views, it is said to be viral.*
- **Example 3 – Google Maps**
 - *In Google Maps, various locations are represented as **vertices** and the roads are represented as **edges**.*
 - *Graph theory is used to **find the shortest path in road or a network***

Few more examples for Graph

- *Web Page Searching,*
- *City Planning,*
- *Traffic Control,*
- *Transportation & Navigation,*
- *Travelling Salesman Problem,*
- *GSM mobile phone networks, etc.*
- **Graph Theory**
 - *Graph theory can also be used to determine how viruses spread across borders or cities.*
 - *Graph theory is used in biology and medicine to distinguish drug targets, decide the job of proteins, or determine the qualities of vague capacity.*



In the graph,

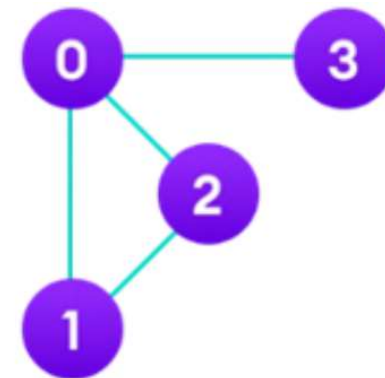
$$V = \{0, 1, 2, 3\}$$

$$E = \{(0,1), (0,2), (0,3), (1,2)\}$$

$$G = \{V, E\}$$

Graph Terminologies

- **Vertex** - It's a fundamental unit from which the graph is formed. It contains data. It is also known as nodes. A vertex is usually represented by a circle with a label.
 - In the above graph, 0, 1, 2 and 3 are the vertices
- **Edge** - It's a link connecting the two vertices. An edge is represented by a line or arrow extending from one vertex to another.
 - In the above, there is edge between vertex 0 and vertex 1
- **Adjacency** - A vertex is said to be adjacent to another vertex if there is an edge connecting them.
 - In the above graph, Vertices 2 and 1 are adjacent because there is an edge between them.
- **Path** - A sequence of edges that allows you to go from vertex A to vertex B is called a path.
 - In the above graph, paths from vertex 0 to vertex 2 are 0 - 1, 1 - 2 and 0 - 2
- **Cycle** - A path that starts from a given vertex and ends at the same vertex is called a cycle
 - In the above graph, there is cycle: 0 - 1 - 2 - 0
- **Degree** - The degree of a vertex of a graph is the number of edges that are incident to the vertex. It is usually represented as Degree (Vertex)
 - The degree of all the vertices in the above graph is
 - Degree (0) = 3
 - Degree (1) = 2
 - Degree (2) = 2
 - Degree (3) = 1

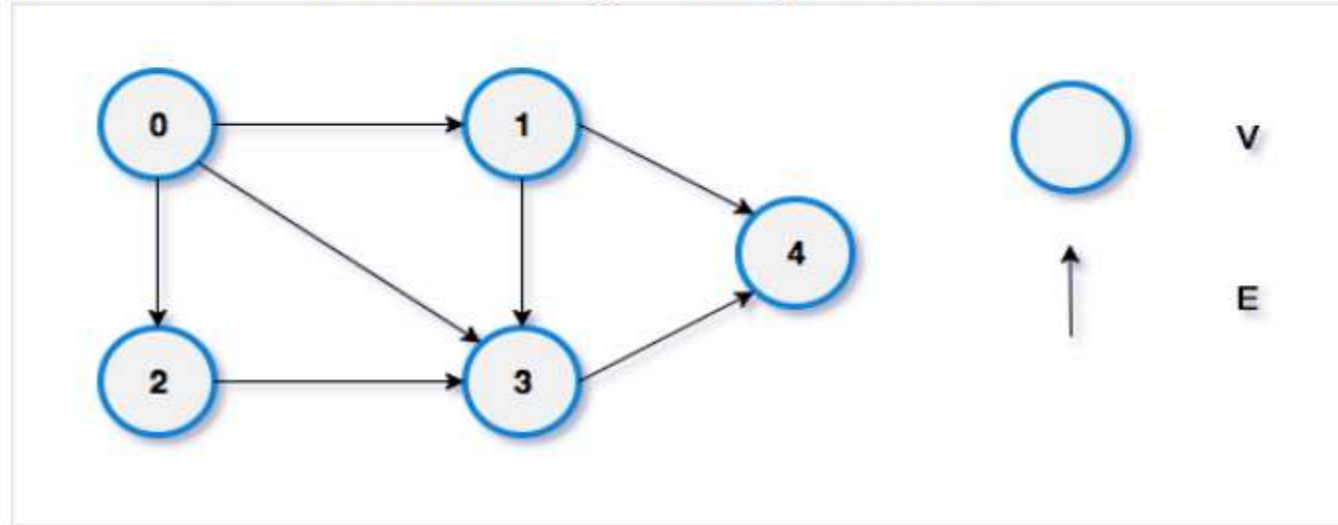


Types of Graph

- *Directed Graph*
- *Undirected Graph*
- *Connected Graph*
- *Disconnected Graph*
- *Complete Graph*
- *Weighted Graph*
- *Cyclic Graph*
- *Acyclic Graph*

Directed Graph

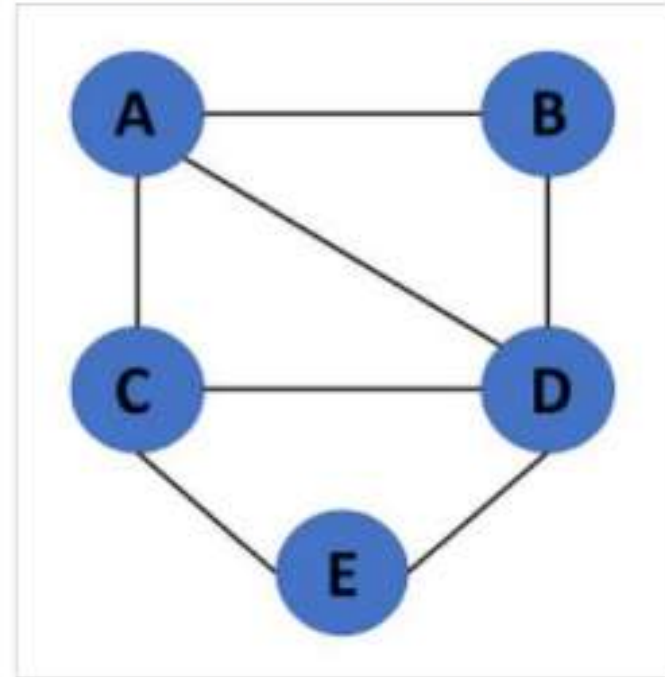
- A directed graph is a graph in which the edges are directed by arrows.
- Directed graphs are also known as digraphs.
- In the directed graph, we have in-degree and out-degree for every vertex.
- In-degree of a vertex is the number of edges coming to the vertex.



- 1) In-degree (0) = 0
 - 2) In-degree (1) = 1
 - 3) In-degree (2) = 1
 - 4) In-degree (3) = 3
 - 5) In-degree (4) = 2
- Out-degree of a vertex is the number edges which are coming out from the vertex.
 - 1) Out-degree (0) = 3
 - 2) Out-degree (1) = 2
 - 3) Out-degree (2) = 1
 - 4) Out-degree (3) = 1
 - 5) Out-degree (4) = 0

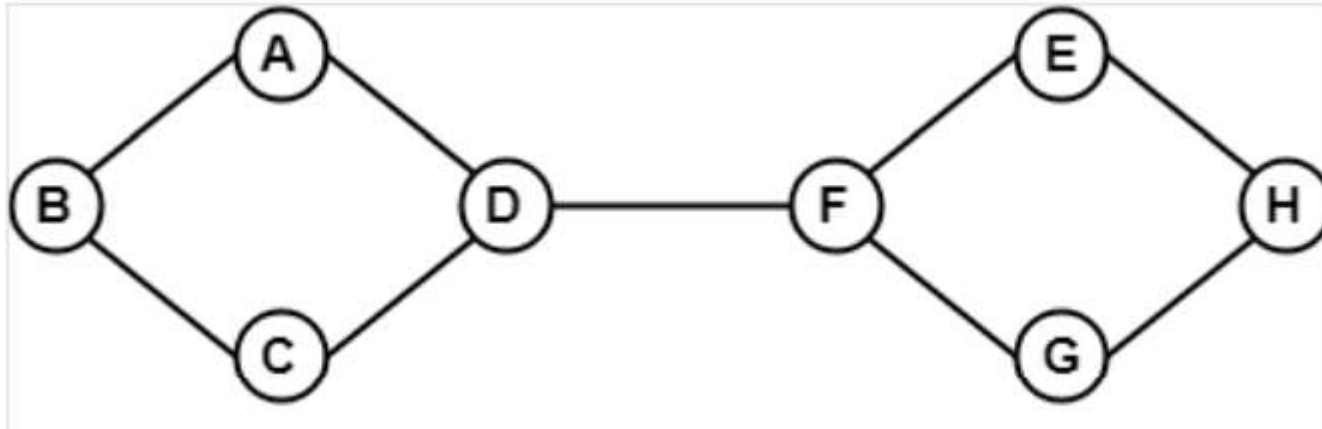
Undirected Graph

- An undirected graph is a graph whose edges are not directed.



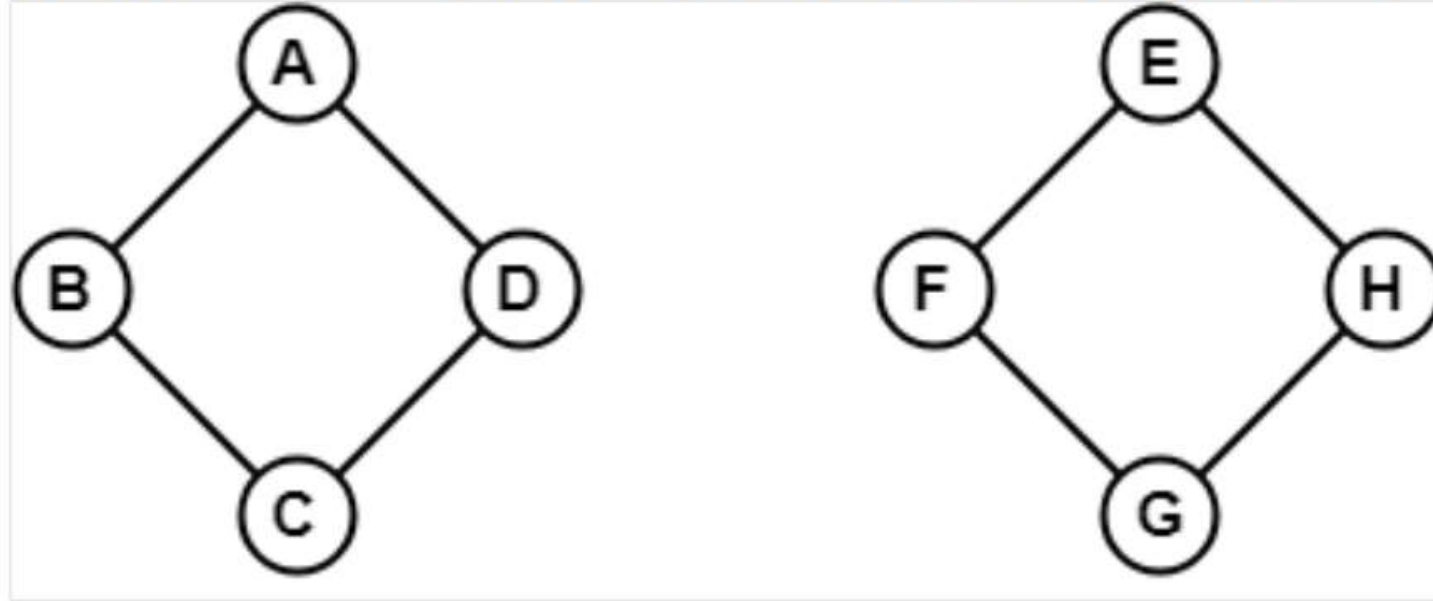
Connected Graph

- A connected graph is a graph in which at least one edge or path exists between every pair of vertices.



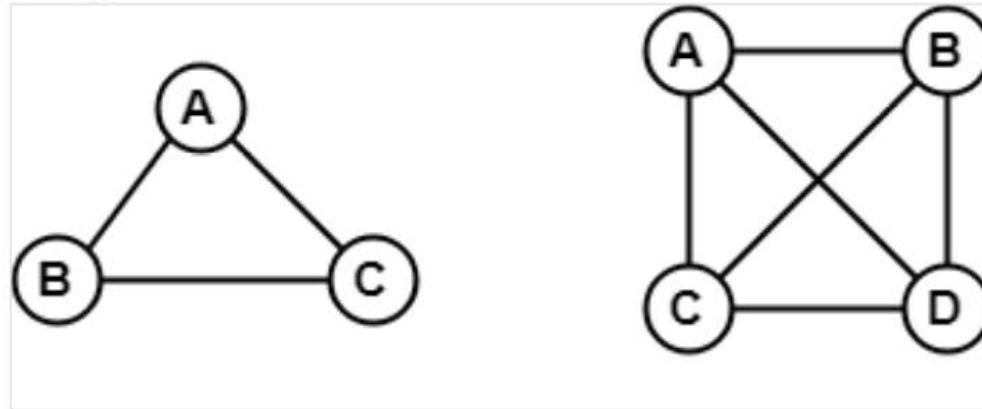
Disconnected Graph

- A disconnected graph is a graph in which any path does not exist between every pair of vertices.



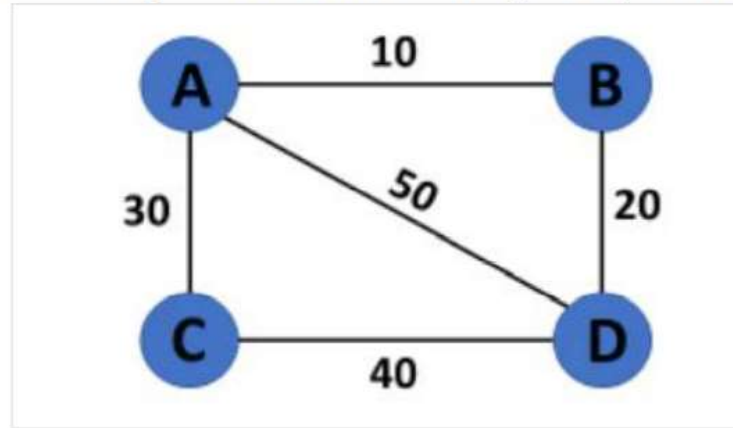
Complete Graph

- A complete graph is a graph in which every pair of vertices is connected by exactly one edge. So, a complete graph on n vertices contains $n(n - 1)/2$ edges



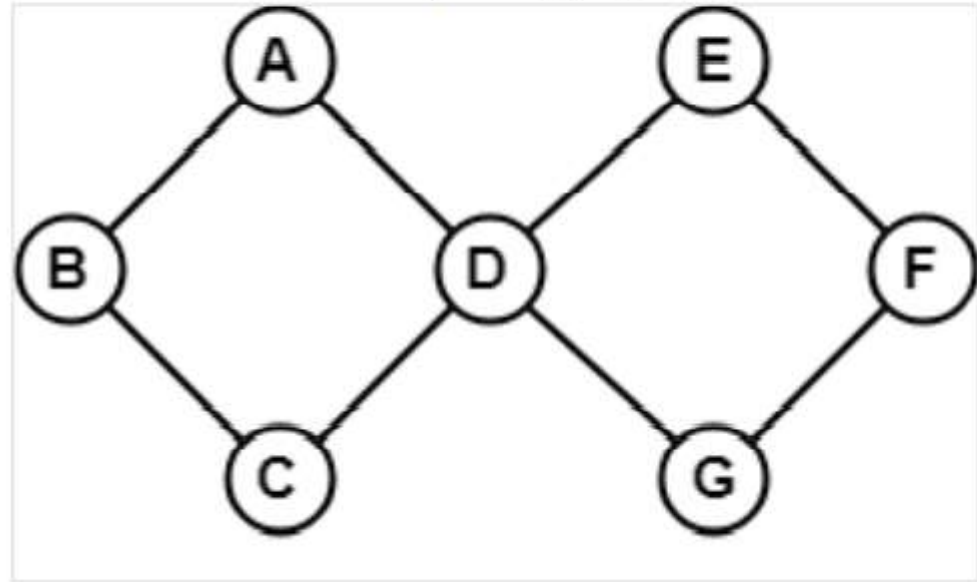
Weighted Graph

- A graph weighted graph in which each edge has a value or weight representing the cost of traversing that edge.



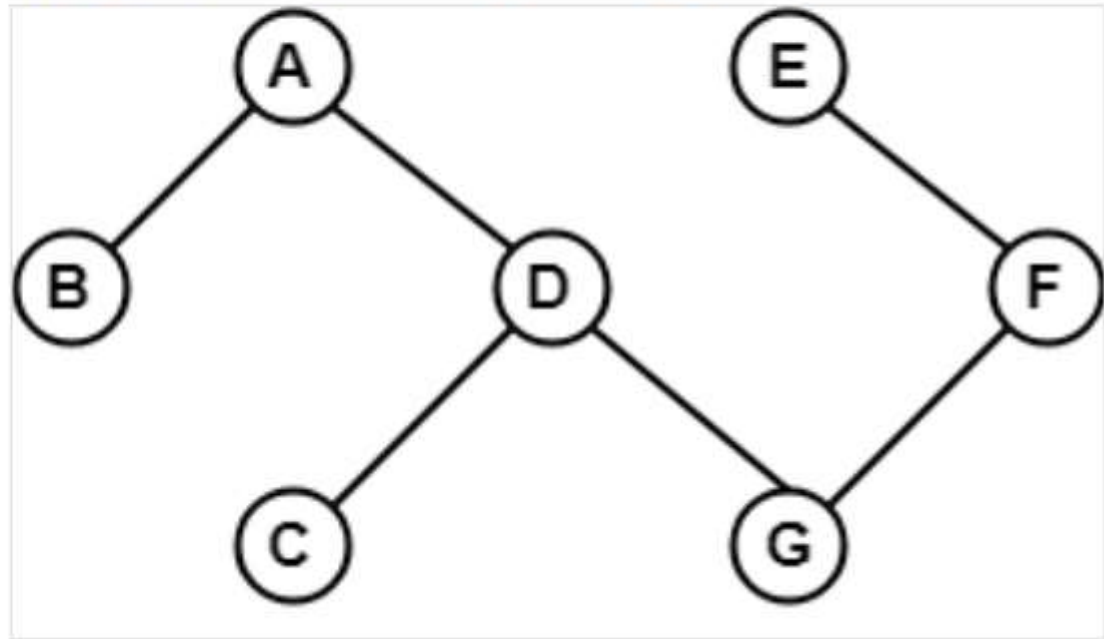
Cyclic Graph

- A graph which contains any cycle in it is called as a cyclic graph.



Acyclic Graph

- A graph which does not contain any cycle in it is called an acyclic graph.



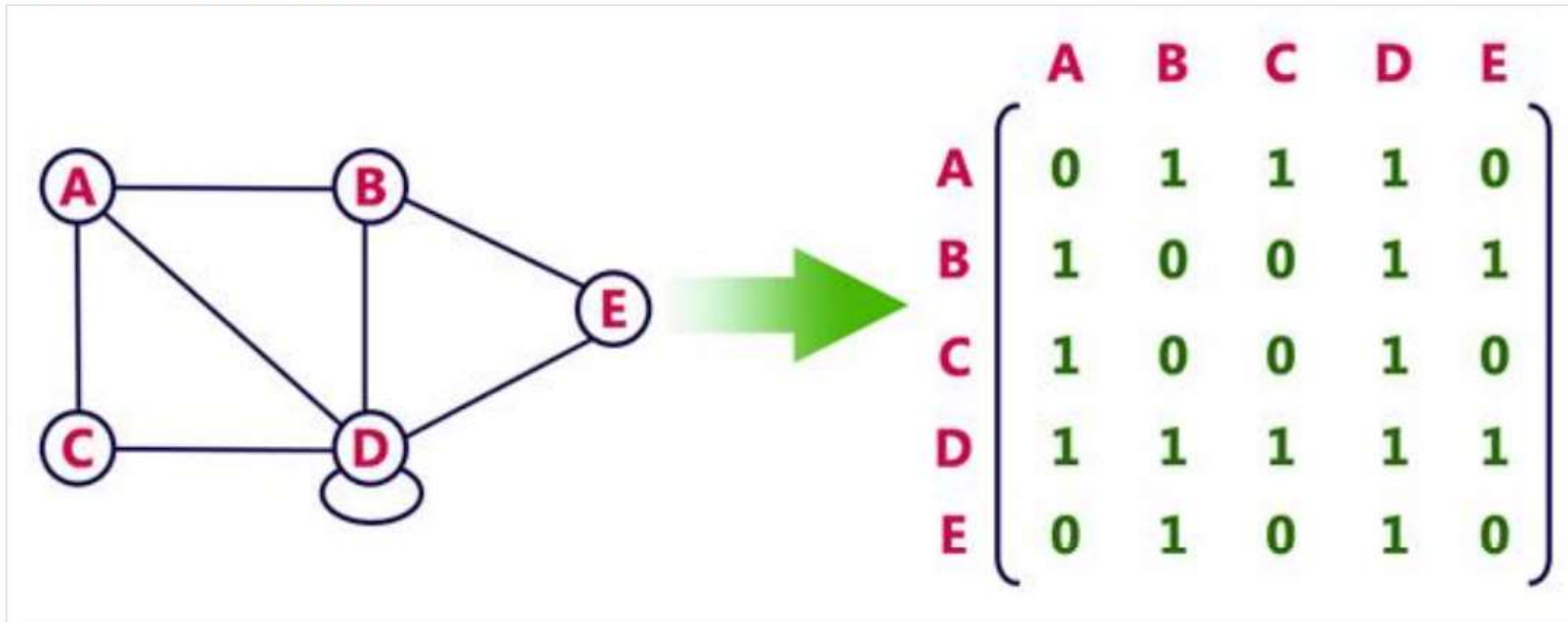
Graph Representation

Graphs are commonly represented in two ways:


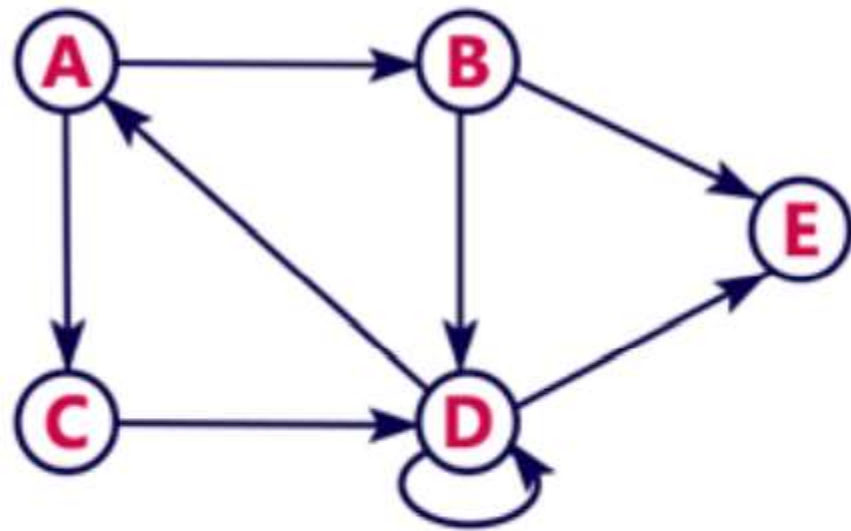
- *Adjacency Matrix*
- *Adjacency Lists*

Adjacency Matrix

- An adjacency matrix is a 2D array of $V \times V$ vertices.
- Each row and column represent a vertex.
- If the value of any element $a[i][j]$ is 1, it represents that there is an edge connecting vertex i and vertex j .
- For undirected graph


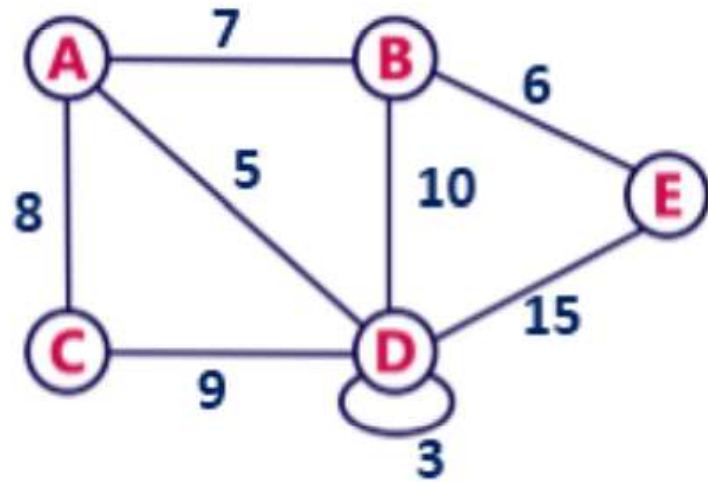


For directed graph,



	A	B	C	D	E
A	0	1	1	0	0
B	0	0	0	1	1
C	0	0	0	1	0
D	1	0	0	1	1
E	0	0	0	0	0

For undirected weighted graph



	A	B	C	D	E
A	0	7	8	5	0
B	7	0	0	10	6
C	8	0	0	9	0
D	5	10	9	3	15
E	0	6	0	15	0

Adjacency Lists

- An adjacency list represents a graph as an array of linked lists.
- The index of the array represents a vertex and each element in its linked list represents the other vertices that form an edge with the vertex.

