1

(0.0.7)

EE5609 Matrix Theory

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Download the latex-file codes from

https://github.com/kranthiakssy/
AI20RESCH14002_PhD_IITH/tree/master/
EE5609 Matrix Theory/Assignment-5

Assignment-5 Geolin

Problem:

Triangle Exercises (1.19): D is a point on side BC of $\triangle ABC$ such that AD = AC. Show that AB > AD

Solution:

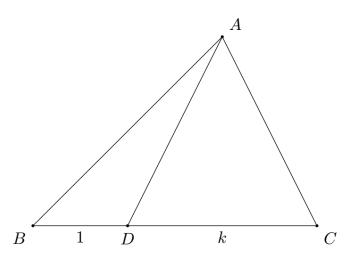


Fig. 0: Triangle generated using LaTeX tikz

The above Fig. 0 shows that, point D placed on side BC of $\triangle ABC$ such that

$$\|\mathbf{D} - \mathbf{A}\| = \|\mathbf{C} - \mathbf{A}\| \tag{0.0.1}$$

Let Point D bisecting the side BC at 1:k ratio and Direction vectors of AB,AD & AC are

 $\mathbf{B} - \mathbf{A}, \mathbf{D} - \mathbf{A} & \mathbf{C} - \mathbf{A}$ respectively.

By applying the section formula for bisecting the line internally

$$(\mathbf{D} - \mathbf{A}) = \frac{k.(\mathbf{B} - \mathbf{A}) + 1.(\mathbf{C} - \mathbf{A})}{1 + k}$$
(0.0.2)

$$\implies \|\mathbf{D} - \mathbf{A}\|^2 = \frac{k^2 \|\mathbf{B} - \mathbf{A}\|^2 + \|\mathbf{C} - \mathbf{A}\|^2}{(1+k)^2} \quad (0.0.3)$$

substituting (0.0.1)

$$\|\mathbf{D} - \mathbf{A}\|^2 = \frac{k^2 \|\mathbf{B} - \mathbf{A}\|^2}{(1+k)^2} + \frac{\|\mathbf{D} - \mathbf{A}\|^2}{(1+k)^2}$$

$$(0.0.4)$$

$$\implies \|\mathbf{D} - \mathbf{A}\|^2 \left(1 - \frac{1}{(1+k)^2}\right) = \frac{k^2 \|\mathbf{B} - \mathbf{A}\|^2}{(1+k)^2}$$

$$(0.0.5)$$

$$\implies \|\mathbf{D} - \mathbf{A}\|^2 \left(1 + \frac{2}{k}\right) = \|\mathbf{B} - \mathbf{A}\|^2$$

$$(0.0.6)$$

$$\therefore AB > AD$$

for k > 0Hence Proved.