## EE5609 Matrix Theory

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Download the python code from

https://github.com/kranthiakssy/ AI20RESCH14002 PhD IITH/tree/master/ EE5609 Matrix Theory/Assignment-2

and latex-file codes from

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## Assignment-2

## Problem

Lines and Planes (81): In each of the following cases, determine the normal to the plane and the distance from the origin.

(a) 
$$\begin{pmatrix} 0 & 0 & 1 \end{pmatrix} \mathbf{x} = 2$$

(b) 
$$(1 \ 1 \ 1) \mathbf{x} = 1$$

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$$(0 \ 0 \ 1) \mathbf{x} = 2$$
  
(b)  $(1 \ 1 \ 1) \mathbf{x} = 1$   
(c)  $(0 \ 5 \ 0) \mathbf{x} = -8$   
(d)  $(2 \ 3 \ -1) \mathbf{x} = 5$ 

(d) 
$$(2 \ 3 \ -1)\mathbf{x} = 5$$

Solution

If ax+by+cz = k is a linear equation representing a plane, then the normal **n** to that plane is the coefficients of the linear equation

$$\mathbf{n} = \begin{pmatrix} a \\ b \\ c \end{pmatrix} \tag{0.0.1}$$

The equation of plane can be written as

$$\mathbf{n}^T \mathbf{x} = c \tag{0.0.2}$$

The shortest distance between the plane (0.0.2) and origin is

$$\frac{|c|}{\|\mathbf{n}\|}\tag{0.0.3}$$

(a) 
$$\begin{pmatrix} 0 & 0 & 1 \end{pmatrix} \mathbf{x} = 2$$

$$\mathbf{n} = \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix} \tag{0.0.4}$$

$$c = 2$$
 (0.0.5)

1

As per (0.0.3), shortest distance from origin =

$$\frac{|2|}{\sqrt{0^2 + 0^2 + 1^2}} = 2 \tag{0.0.6}$$

(b) 
$$(1 \ 1 \ 1) \mathbf{x} = 1$$

$$\mathbf{n} = \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix} \tag{0.0.7}$$

$$c = 1 \tag{0.0.8}$$

As per (0.0.3), shortest distance from origin =

$$\frac{|1|}{\sqrt{1^2 + 1^2 + 1^1}} = \frac{1}{\sqrt{3}} \tag{0.0.9}$$

(c) 
$$(0 \ 5 \ 0) \mathbf{x} = -8$$

$$\mathbf{n} = \begin{pmatrix} 0 \\ 5 \\ 0 \end{pmatrix} \tag{0.0.10}$$

$$c = -8 \tag{0.0.11}$$

As per (0.0.3), shortest distance from origin =

$$\frac{|-8|}{\sqrt{0^2 + 5^2 + 0^2}} = \frac{8}{5} \tag{0.0.12}$$

(0.0.1) (d) 
$$(2 \ 3 \ -1)\mathbf{x} = 5$$

$$\mathbf{n} = \begin{pmatrix} 2\\3\\-1 \end{pmatrix} \tag{0.0.13}$$

$$c = 5$$
 (0.0.14)

As per (0.0.3), shortest distance from origin =

$$\frac{|5|}{\sqrt{2^2 + 3^2 + (-1)^2}} = \frac{5}{\sqrt{14}} \tag{0.0.15}$$