# 1 Description of the algorithm

### 1.1 Assumptions

- 1. Goal of the algorithm: minimizing the number of pallet load units.
- 2. The basis for planning is the PRODUCT\_ID set in the order, the number of which is smaller than the standard number.
- 3. The number of PRODUCT\_ID units in a shipment (WMS) is not subject to division.
- 4. Adding subsequent PRODUCT\_ID layers to the mix takes into account:
  - height (H) of the layer,
  - degree of layer filling (fw),
  - fragility (stackability) class parameter (CL),
  - weight (W).

## 1.2 Input data

- order (ORDER\_ID)
- place of shipment (DB)
- $\bullet$  product name (PRODUCT\_ID)
- $\bullet$  of product units in the order (BU\_QUANTITY)
- number of product units per standard volume (Quantity\_Max)
- $\bullet\,$  number of layers in the normative pjl (Layers\_Norm)
- product's fragility class (CAPACITY\_LOAD\_CLASS)

## 1.3 Output

- pallet loading unit number (LOADUNIT\_ID)
- $\bullet$  weight of pallet loading unit (WEIGHT) with carrier [mm]
- height of pallet loading unit (HEIGHT) with carrier [kg]
- type of pallet loading unit (TOP or BASE) due to the possibility of creating sandwich pallets (SNDW)

## 1.4 Brief description of the algorithm

The algorithm works for a set of orders that come from at least one contractor. Products are assigned to pallet loading units separately for each order. The following steps are performed for subsequent orders from the set:

- 1. For each assortment (Product\_ID), the number of full layers and the number of residual layers are determined. For the non-full layers, it determines the value of the layer filling factor fw.
- 2. Full layers are placed on pallets while maintaining the permissible pallet weight and pallet height. First, homogeneous pallets. Next, mixed pallets. In both cases taking into account the fragility class of the goods. Pallets that have reached the permissible values of weight or height parameters (W<sup>max</sup>, H<sup>max</sup> respectively) are BASE pallets. The remaining pallets will be used to arrange the non-full layers. If all goods from a given order have been assigned to pallet loading units, go to the next order.
- 3. Non-full layers are then considered:
  - They are tried to be selected so that the difference in the height of the two or three assortments that are potentially to constitute it does not exceed 10 [mm] and the total fill factor of the layer created from them is less than 1.0. Then they are added to the remaining pallet created in step 1, taking into account the weight and maximum height values. If there are no longer pallet loading units with full layers, we create new mixed pallet loading units, taking into account the fragility class of the goods and the weight and height of the pallet. The pallet loading units created in this way are of the BASE type.
  - If there are no goods whose height difference does not exceed 10 [mm], they are combined to form a layer whose total fill factor is not greater than 1.0 and added as the highest layer of the pallet loading unit, taking into account the weight and maximum height of the pallet. The created pallet loading unit is of the TOP type.
- 4. We combine the remaining products (Product\_ID) into layers whose total fill factor does not exceed 1.0. We create a new pallet loading unit and add a layer to it, taking into account the weight and maximum height values. The created pallet loading unit is of the TOP type.
- 5. When all Product\_IDs from the current order have been assigned to pallet load units, the degree of weight and height balance of the created mix type pallet load units is checked. If satisfied, the algorithm terminates for the current order. If they are not, the values of the  $W^{max}$  and  $H^{max}$  parameters are decremented and the algorithm returns to step 2. In the pseudocode below, the parameter values are decremented to 0.99 of their current value.

#### 1.5 Indexes

- i product included in the order, where  $i=1,2,\ldots n,\ldots I$
- $\bullet$  j pallet mix type loading unit
- w layer on a pallet mix loading unit
- z client's order

### 1.6 Parameters

- $CL_i$  fragility class of the *ith* product (according to the standard)
- $CL_j$  fragility class of the jth pallet loading unit determined as the highest CLi value of the PRODUCT\_ID items included in the jth pallet loading unit mix
- fw layer filling degree; parameter subject to control fw = < 0.7; 1 >
- $fW_{top}$  the degree of filling of the highest pallet layer of a load unit
- $H_i$  unit height of the *ith* product (according to the standard)
- $H_j$  height of the jth pallet load unit mix
- Hmax maximum height of a pallet load unit mix (system parameter)
- $H^{diff}$  difference between the maximum height of the pallet loading unit mix Hmax and the height of the jth pallet loading unit mix  $H_j$
- $LP_i$  number of units of the *ith* product in the order
- $LP_i^{nor}$  number of units of the *ith* product on a standard pallet loading unit
- $LW_i^{nor}$  number of layers of the *ith* product in a standard pallet loading unit
- $S_j$  status of the j-th pallet loading unit mix due to the possibility of being included in the planning of the construction of the SNDW T pallet loading unit TOP, i.e. it can only be placed on the top of the SNDW; B BASE pallet loading unit, i.e. can be placed as a base or intermediate layer
- $w_i$  number of layers of the *ith* product in the order, where  $w_i = w_i^{INT} + w_i^R$
- $\bullet$   $w_i^{INT}$  total value of the number of layers of the *ith* product in the order
- $w_i^R$  non-integer value of the number of layers of the *ith* product in the order
- $W_i$  weight of the *ith* product in the order
- $W_i^{norm}$  standard weight of a pallet loading unit with the *ith* product
- $W_j$  weight of the jth pallet load unit mix
- $W_j^{zpk}$  the difference in the weight of the standard pallet loading unit with the *ith* Winorm product and the weight of the *jth* mix pallet loading unit, determined when breaking the fragility class parameter
- W a set of single layers opened with 2 or 3 Product\_ID. Each layer can be supplemented with another Product\_ID and added as the highest layer in the palette

- $W_n$  weight of n products in the order
- $W^{max}$  maximum weight of a pallet load unit mix (system parameter)
- $W^{diff}$  difference between the maximum weight of the pallet loading unit mix  $W^{max}$  and the weight of the jth pallet loading unit mix  $W_j$
- $\bullet$  ZP a set of products for planning a pallet load unit mix

## 1.7 Suggested parameter values

- $H^{max} = 1700[mm]$
- $\bullet \ W^{max} = 700[kg]$
- $f_w \in [0.7 \ 1.0]$

## 1.8 Operators

- U Adding the product layer or Product\_ID to the top layer of the palette that is currently being built. Updates the palette parameters. The goods are marked as assigned to the pallet they become planned. The algorithm stores information about the Product\_ID state in the Added\_i array.
- $\sqcup$  Binary operator. Returns true if the  $Product JD_i$  and  $Product JD_{i+n}$  items were combined in one layer. False otherwise.
- $\mbox{$\uplus$}$  Adding a layer or Product\_ID to the palette that is currently being built taking into account the fragility class. Updates the palette parameters. The goods are marked as assigned to the pallet they become planned.
- \ Removing the last added layer or Product\_ID from the palette that is currently being built. Updates the palette parameters. The goods return to the pool of goods from the current order to be planned they become unplanned. The algorithm stores information about the Product\_ID state in the Added\_i array.
- $\bullet$   $\cap$  Determining the value os layer filling factor for at least two Product\_IDs included in the layer.

## 2 Algorithm

### Algorithm 1 Palet Stacking algorithm

```
Input: z, CL(i), ZP, H^{max}, W^{max}, f_{wmin}, f_{wmax}, h_{diff}
                                                                       Output: SetSofpalletlabeledas, TOP"or, BASE"
 1: i \leftarrow 0
 2: S \leftarrow \emptyset
 3: for each z \in \mathbb{Z} do
                                                                                                                                                      ▶ Execute for each order in the set of orders
         for each Product\_ID \in z do
            \begin{split} l_i^{INT} &\leftarrow int(\frac{LP_i}{LP_i^{NOR}*LW_i^{NOR}}) \\ l_i^R &\leftarrow \frac{LP_i}{LP_i^{NOR}*LW_i^{NOR}} - l_i^{INT} \\ l_i^{Planned}(1:l_i^{INT}+l_i^R) &\leftarrow false \end{split}
 6:
 7:
             Added_i \leftarrow false
                                                                                                          ▶ Each Product_ID in the order has not been assigned to a pallet loading unit
 8:
            \begin{aligned} &l_i = l_i^{INT} + l_i^R \\ &fw_i^{INT} \leftarrow 0 \\ &fw_i^R \leftarrow 1 - l_i^R \end{aligned}
 9:
                                                                                                                                       ▶ The fill factor of the full layer for a given Product_ID
10:
                                                                                                                                 ▶ The fill factor of the non-full layer for a given Product_ID
11:
         end for each
12:
         for each i \in \mathbf{z} do
13:
             if fw_i^{INT} = 0 and fw_i^R = 0 then
14:
                 S \leftarrow S \cup Make\_full\_layers\_pallet(i, CL(i), H^{max}, W^{max}, j)
                                                                                                                                                   ▷ Creating pallet loading units from full layers
15:
                 Added_i = true
16:
                 go to 22
17:
             else
18:
                 go to 22
19:
             end if
20:
         end for each
21:
22:
         for each i \in \mathbf{z} do
             sort(i, CL(i), 1)
                                                                      ▶ Product_IDs that have not been assigned to a pallet loading unit are sorted ascending by fragility class
23:
             sort(i, CL(i), w_i, -1)
                                            > Within each fragility class we sort in descending order by the number of layers that have not been assigned to a pallet unit
24:
    load
         end for each
25:
26:
         for each i \in \mathbf{z} do
             if \exists i: l_i^{Planned}(:) = false \& l_i^{Planned}(:) = true then \triangleright Are there any items on the pallet load unit to which Product_ID has not been attempted?
27:
28:
             else
29:
                 if \exists_i: l_i^{Planned}(1:) = false then \triangleright Are there Product_IDs in the order that have not been attempted to be added to the Product_IDs that make
30:
    up the mix type pallet unit load?
```

```
go to 74
31:
                else
32:
                     for each j \in S do
33:
                        if |W_i - W_{\neq i}| < W^{diff} \& |H_i - H_{\neq i}| < H^{diff} then
                                                                                                              ▷ Check the degree of weight and height balance of pallet load units
34:
                            go to 751
35:
                         else
36:
                             W^{max} \leftarrow 0.99 * W^{max}
                                                                                      \triangleright Changing the values of the W^{max} and H^{max} parameters to achieve improved balance
37:
                             H^{max} \leftarrow 0.99 * H^{max}
38:
                            go to 13
39:
                         end if
40:
                     end for each
41:
                end if
42:
            end if
43:
            for each j \in S do
                                                                                                ▶ Is it possible to add new Product_ID to already created pallet loading units?
44:
            W_{j}^{mix} \leftarrow \frac{\sum_{j=1}^{J} W_{j}}{W_{max}}
H_{j}^{mix} \leftarrow \frac{\sum_{j=1}^{J} H_{j}}{H_{max}}
end for each
                                                                                    \triangleright Calculate the weight coefficient W_{mix} and the height H_{mix} of a pallet mix loading unit.
45:
46:
47:
            W^{max} \leftarrow max_i(W_i^{mix})
                                                                                                                               ▷ Choose a pallet with the maximum weight or height
48:
            H^{max} \leftarrow max_i(H_i^{mix})
49:
            for each j \in S do
50:
                W_i^{diff} \leftarrow W^{max} - W_i
                                                \triangleright Calculate the difference in the maximum weight and height of the pallet loading unit j and the maximum weight and
51:
   height, respectively H_j^{diff} \leftarrow H^{max} - H_j
52:
            end for each
53:
            for each i \in \mathbf{z} do
                                                                              ▷ Select Product_ID with a weight or height not greater than the differences calculated above
54:
                if W_i \le W^{diff} || H_i \le H^{diff} then
55:
                    go to 62
56:
57:
                else
                    S_i \leftarrow, BASE''
                                                                                                                                        ▶ The BASE type pallet loading unit was built
58:
                    go to 26
59:
                end if
60:
            end for each
61:
            for each j \in S do
                                         \triangleright For a pallet loading unit, calculate the difference between its weight W_i or height H_i and the maximum weight W^{max} and
62:
   height H^{max}, respectively
                H_j^{diff} = H^{max} - H_j
63:
                W_i^{diff} = W^{max} - W_i
64:
```

```
\triangleright Are there Product_IDs in the order whose height or weight is less than the difference calculated above (H_{diff}, W_{diff})
65:
                for each i \in \mathbb{Z} do
    respectively)
                    if H_i \le H_{diff} ||W_i \le W_{diff}| then
66:
                        go to 236
67:
                     else
68:
                        S_j \leftarrow, BASE''
                                                                                                                                               ▶ The BASE pallet load unit is builded
69:
                        go to 26
70:
                     end if
71:
                end for each
72:
            end for each
73:
            for each i \in \mathbf{z} do
                                                             \triangleright Are there any Product_ID items that have not been combined yet and have full layers, i.e. fw \in [0.7; 1.0]?
74:
                if Added_i = false \& fw_i \in [0.7; 1.0] then
75:
                     go to 82
76:
                else
77:
78:
                     go to 175
                end if
79:
            end for each
80:
            count \leftarrow 0
                                                                                  \triangleright Are there at least two Product_ID items in the order that have full tiers (fw \in [0.7; 1.0])
81:
            for each i \in \mathbf{z} do
82:
                if fw_i \in [0.7:1.0] then
83:
                     count \leftarrow count + 1
84:
                end if
85:
            end for each
86:
            if count >= 2 then
87:
                go to 92
88:
            else
89:
                go to 143
90:
            end if
91:
            for each i \in z \& f w_i \in [0.7:1.0] do \triangleright Is it possible to combine two Product_IDs into a layer? The difference in their heights ||H_i - H_{i+n}|| <= 10 [mm]
92:
                                                                    \triangleright Will adding the combined Product_ID to a pallet unit load not exceed the value of W^{max} or H^{max}?
                if \exists_n : ||H_i - H_{i+n}|| \le 10 then
93:
                    if \sum_{k=1}^{I} W_k > W^{max} \| \sum_{k=1}^{I} H_k > H^{max} then go to 74
94:
                                                                                                                                \triangleright The values of W^{max} or H^{max} have been exceeded
95:
                     end if
96:
                    if \sum_{K=1}^{I} W_k \leq W^{max} \& \sum_{k=1}^{I} H_k <= H^{max} then if fw_i + fw_{i+n} > 1.0 then
97:
                                                                                                                                       ▶ Checking the fill factor of the common layer
98:
                            go to 74
99:
                         else
100:
```

```
if \exists_i : planned_i = false then
                                                                                      ▶ Is there a Product_ID in the order that is not assigned to a pallet loading unit?
101:
                               for each j \in S do
102:
                                   if W_j + W_i \ge W_{max} ||W_j + W_i \ge W_{max} ||CL_i \ge CL_j then \triangleright Possibility of adding to an existing mix pallet loading unit due to
103:
    values of W^{max}, H^{max} and fragility class
                                      if fw_i + fw_i \leq 1 then
104:
                                          S_i \cup Product\_ID(S_i, i)
105:
                                          if fw_i + fw_{i+n} < 0.7 then \triangleright If the total fw of a layer; 0.7, split the pre-connected Product_IDs that constitute this
106:
    layer
                                              i \setminus i + n
107:
                                              go to 74
108:
                                           else
109:
                                              S_i = BASE
                                                                                                         ▶ A pallet loading unit has been created. It is of the BASE type
110:
                                              go to 30
111:
                                           end if
112:
113:
                                       else
                                          if fw_i + fw_{i+n} < 0.7 then \triangleright If the total fw of a layer; 0.7, split the pre-connected Product IDs that constitute this
114:
    layer
                                              i \setminus i + n
115:
                                              go to 74
116:
                                           end if
117:
                                          if fw_i + fw_{i+n} \in [0.7; 1.0] then
                                                                                                        ▶ A pallet loading unit has been created. It is of the BASE type
118:
                                              S_i = BASE
119:
                                              go to 30
120:
                                           end if
121:
                                      end if
122:
                                   else
123:
                                      if fw_i + fw_{i+n} < 0.7 then \triangleright If the total fw of a layer i 0.7, split the pre-connected Product_IDs that constitute this layer
124:
                                          i \setminus i + n
125:
                                          go to 74
126:
127:
                                      _{
m else}
                                          if fw_i + fw_{i+n} \in [0.7; 1.0] then
                                                                                                           ▶ A pallet loading unit has been created. It is the BASE type
128:
                                              S_i = BASE
129:
                                              go to 30
130:
                                           end if
131:
                                       end if
132:
                                   end if
133:
                               end for each
134:
```

```
else
135:
                            end if
136:
                        end if
137:
                    end if
138:
                else
139:
                    go to 30
                                                                                                                       \triangleright If the height difference ||H_i - H_{i+n}|| exceeds 10 [\text{mm}].
140:
                end if
141:
             end for each
142:
            if i: fw_i \in [0.7; 1.0] \& \exists_n CL_i < CL_{i+n} then \triangleright Can further items from the order be placed on the full-layer i Product_ID item due to the fragility
143:
    class (CL_i \leq CL_{i+n})
                if fw_i + fw_{i+n} \le 1 then
144:
                    if \sum_{i=1}^{I} W_i < W^{max} \& \sum_{i=1}^{I} H_i < H^{max} then \triangleright If the weight and height of the pallet loading unit do not exceed the maximum values after
145:
    entering Product_IDs, add Product_IDs
                        if fw < 0.7 then
                                                                                                                                  ▶ Check the layer feeling degree of top layer
146:
                            S_j \cup Product\_ID(S_j, i)
147:
                            S_i = TOP
148:
                            go to 30
149:
                        end if
150:
                        if fw \in [0.7; 1.0] then
151:
                            S_i \cup Product\_ID(S_i, i)
152:
                            if Try_Pillars(S_i) = true then
153:
                                S_i \leftarrow TOP
154:
                                go to 30
155:
156:
                            else
                                S_i \leftarrow BASE
157:
                                go to 30
158:
                            end if
159:
                        end if
160:
                    end if
161:
                end if
162:
                                                               \triangleright If you cannot Product ID with the full layer fw \in [0.7; 1.0] creates a new mix type pallet loading unit
163:
             else
                Make\_new\_Pallet(Product\_ID_i)
164:
                j \leftarrow j + 1
165:
                if fw_i < 0.7 then
                                                                                                                                  ▶ Check the layer feeling degree of top layer
166:
                    S_i = TOP
167:
                    go to 30
168:
                end if
169:
```

```
if fw_i \in [0.7; 1.0] then
170:
                   S_i = base
171:
                    go to 30
172:
                end if
173:
            end if
174:
            for each i \in z do
                                                                                                  ▷ Check if there are Product_IDs in the order that can create a layer
175:
               if \exists_n : ||H_i - H_{i+n}|| \le 10 then
                                                            ▷ Condition for combining two Product_IDs items into a layer in order to be added to a pallet load unit
176:
                   go to 182
177:
178:
               else
179:
                    go to 30
                end if
180:
            end for each
181:
            W^{sum} \leftarrow 0
                             by Check whether the weight of the pallet loading unit after adding the Product_IDs items that can be combined does not exceed the
182:
    maximum W^{max}
            top\_layer \leftarrow \emptyset
183:
            fw_{top\_layer} \leftarrow 0
184:
            for each i \in z do
185:
               if ||H_i - H_{i+n}|; 10 then
                                                                                                                                                 ▶ If combining is possible
186:
                   top\_layer \leftarrow top\_layer \cup i + n
187:
                   W^{sum} \leftarrow W^{sum} + W_{i+n}
188:
                   fw_{top\_layer} \leftarrow fw_{top\_layer} + fw_{i+w}
189:
               end if
190:
            end for each
191:
            if W^{sum} + W_i < W^{max} then
                                                                                                                      ▶ If it does not exceed, add combined Product_IDs
192:
               if fw_{top\_layer} < 1\&H_j + H_{i+n} < H^{max} then
193:
                   Create_Pillars()
                                                                                                                                                194:
                end if
195:
               if fw_{top\_layer} < 0.7 then
196:
                   S_i \cup top\_layer
197:
                   S_i = TOP
198:
199:
                    go to 175
                end if
200:
                if fw \in [0.7; 1.0] then
201:
                    S_i \cup top\_layer
202:
                   if try\_pillars(S_i) = true then
                                                                                                                                 ▶ Are there any pillars in the top layer?
203:
                       S_i = TOP
204:
                       go to 175
205:
```

```
else
206:
                        S_i = BASE
207:
                        go to 175
208:
                    end if
209:
                end if
210:
             else
211:
                while W^{sum} + W_i > W^{max} do
                                                                  \triangleright If it exceeds, we remove items from the added Product IDs until the weight does not exceed W^{max}
212:
                    top\_layer \leftarrow top\_layer \setminus i + n
213:
                    W^{sum} \leftarrow W^{sum} - W_{i+n}
214:
                    fw_{top\_layer} \leftarrow fw_{top\_layer} - fw_{i+w}
215:
                end while
216:
                if fw_{top\_layer} < 1\&H_i + H_{i+n} < H^{max} then \triangleright Check whether the filling factor of the top layer is not greater than 1 and whether the maximum
217:
    height H^{max} has not been exceeded
                    Create_Pillars()
                                                                                                                                                      ▷ Consider building pillars
218:
                end if
219:
                if fw_{top\_layer} < 0.7 then
                                                                                                                                      ▶ Check the filling factor of the top layer
220:
                    S_i \cup top\_layer
221:
                    S_i \leftarrow TOP
222:
                    go to 175
223:
                end if
224:
                if fw \in [0.7; 1.0] then
225:
                    S_i \cup top\_layer
226:
                    if try\_pillars(S_i) = true then
                                                                                                                                        ▶ Are there any pillars in the top layer?
227:
                        S_i \leftarrow TOP
228:
                        go to 175
229:
                    else
230:
                        S_i \leftarrow BASE
231:
                        go to 175
232:
                    end if
233:
                end if
234:
             end if
235:
             CL_i \leftarrow 0
                                                                                                                              ▶ Check the fragility class of the pre-built pallet
236:
             for each Product\_ID \in S_i do
237:
                if CL_i > CL_i then
238:
                    CL_i \leftarrow CL_i
239:
                end if
240:
             end for each
241:
```

```
end for each
242:
        if Product\_ID \in LP_i = 0 then
                                                                                                             \triangleright How many Product_ID LP_i are left in the current order
243:
            go to 26
244:
        end if
245:
        if Product\_ID \in LP_i = 1 then
246:
            go to 252
247:
        end if
248:
        if Product\_ID \in LP_i > 1 then
249:
            go to 267
250:
        end if
251:
        if CL_i < CL_i then
                                                                \triangleright Compare the fragility class of CL_i Product_ID with the fragility class of the pallet unit load CL_i
252:
            if \exists_i : Considered_i = false then
                                                               > Whether a mix type pallet loading unit was built to which adding Product IDs was not considered
253:
               S_i = BASE
254:
               Considered_i = true
255:
256:
                go to 50
            else
257:
               S_i = BASE
258:
               j \leftarrow j + 1
259:
               S_i \cup Product\_ID
260:
               go to 74
261:
262:
            end if
        else
263:
            S_i \cup Product_ID
264:
265:
            go to 26
        end if
266:
        if CL_1 = CL_2 = CL_n = CL_i \& CL_i < CL_i then
                                                                                                  \triangleright Check the fragility class CL_i of the Product_ID item in the order
267:
            go to 282
268:
        end if
269:
        if CL_1 = CL_2 = CL_n = CL_i \& CL_i \ge CL_i then
270:
            go to 431
271:
        end if
272:
        if CL_1 \neq CL_2 \neq CL_n \neq CL_i \& CL_i < CL_j then
273:
274:
            go to 282
        end if
275:
        if CL_1 \neq CL_2 \neq CL_n \neq CL_i \& CL_i \ge CL_j then
276:
277:
            go to 431
278:
        end if
```

```
if CL_1 \neq CL_2 \neq CL_n \neq CL_i \& CL_i \ge CL_i \& CL_n < CL_i then
279:
            go to 743
280:
         end if
281:
        if \exists_i : fw_i \in [0.7; 1.0] then
                                                                                               \triangleright Are there full-tier Product_IDs (fw \in [0.7; 1.0]) among the order items?
282:
            go to 299
283:
         else
284:
            if LP_i = 1 then
                                                                                                  ▷ Calculate the number of Product_ID items with full tiers in the order
285:
                if fw < 0.7 then
286:
                    go to 26
287:
                end if
288:
                if fw \in [0.7; 1.0] then
289:
                    S_i \cup LP_i
                                                                                   \triangleright Add Product_IDs to the pallet load unit taking into account the fragility class CL_i
290:
                    go to 26
291:
                end if
292:
293:
            else
                if LP_i > 1 then
294:
                    go to 359
295:
                end if
296:
            end if
297:
         end if
298:
        if \exists_{i,...,i+n:n>1}: Product_ID_i \cup Product_ID_i + n\&fw_i, fw_{i+n} \in [0.7; 1.0] then \triangleright There are two or more Product_IDs in the order that have not been
299:
    combied before
            go to 304
300:
         \mathbf{else}
301:
302:
            go to 330
         end if
303:
        if fw_i, fw_{i+n} \in [0.7; 1.0] then
                                                                                                        ▶ Is it possible to combine two Product_ID items with full layers?
304:
            if ||H_i - H_{i+n}|| \le 10 then
305:
                if fw_i + fw_{i+n} < 0.7 then
                                                                                                                  ▷ Checking the possibility of combining 3-rd Product_ID
306:
                    if ||H_i - H_{i+m}|| \le 10 \& ||H_{i+n} - H_{i+n}|| \le 10 \& f w_{i+m} < 0.7 then
307:
                       Li \cup Product\_ID_{i+m}
308:
                                                                                                                              ▶ Add the product to the layer that is created
                        go to 305
309:
                    else
310:
                       go to 305
311:
                    end if
312:
313:
                else
                    if fw \in [0.7; 1.0] then
314:
```

```
if then
315:
                           go to 299
316:
                       else
317:
                          S_i \setminus (Product\_IDi, Product\_IDi + n, Product\_IDi + m)
                                                                                                                                       ▶ Discard previously added items
318:
                          go to 299
319:
                       end if
320:
                   end if
321:
                   if fw > 1 then
322:
                       go to 299
323:
324:
                   end if
               end if
325:
            else
326:
               go to 299
327:
            end if
328:
        end if
329:
                                                                                                                > Are there Product_ID items that were not combined
        if \exists_{i,i+n} : Product_ID_i \cup Product_ID_i + n then
330:
            if ||H_i - H_{i+n}|| \le 10 then
331:
               if fw < 0.7 then
332:
                   go to 330
333:
               end if
334:
               if fw \in [0.7; 1.0] then
335:
                   W \leftarrow Product\_ID_i \cup Product\_ID_{i+n}
                                                                                                                                                   ▶ A new layer is built
336:
                                                                                                  ▶ We add a layer to the pallet taking into account the fragility class
337:
                   if \sum_{i}^{I} W_{i} > W^{max} \& \sum_{i}^{I} H_{i} > H^{max} then
338:
339:
                       go to 330
340:
                   else
341:
                       if \exists n : Product\_ID_n \in z then
                                                                                                                                ▶ Are there any items left in the order?
342:
                          go to 330
343:
                       else
344:
                          S_i = BASE
345:
                          go to 26
346:
                       end if
347:
                   end if
348:
               end if
349:
               if fw > 1 then
350:
                   go to 330
351:
```

```
end if
352:
            else
353:
                go to 330
354:
            end if
355:
         \mathbf{else}
356:
            go to 26
357:
         end if
358:
        if \exists_{i,n} : Product_ID_i \cup Product\_IDn then
359:
            if ||H_i - H_n| < 10 then
360:
                if fw_i \cap fw_n < 0.7 then
361:
                    if \exists_i : i+1 \neq n \$ Produc_I D_i \in z then
362:
                        if ||H_i - H_{i+1}| < 10|| \& ||H_n - H_{i+1}| < 10|| then
363:
                           if fw_i \cap fw_n \cap fw_i + 1 < 0.7 then
364:
                               go to 361
365:
                           end if
366:
                           if fw_i \cap fw_n \cap fw_i + 1 \in [0.7; 1.0] then
367:
                               go to 391
368:
                           end if
369:
                           if fw_i \cap fw_n \cap fw_i + 1 > 1.0 then
370:
                               W \cup Product\_id_{i||i+1||n} where fw_i, fw_i, fw_i < 1.0
371:
                               if fW < 0.7 then
372:
                                   go to 361
373:
                                end if
374:
                               if fW \in [0.7; 1.0] then
375:
                                   go to 391
376:
                               end if
377:
                            end if
378:
                        else
379:
                            go to 361
380:
                        end if
381:
382:
                    else
                        if fW_{top} \in [0.7; 1.0] \& H_{top}^{diff} < 10 then
383:
                            S_i = BASE
384:
                        else
385:
                            S_i = TOP
386:
                        end if
387:
                        go to 26
388:
```

▷ If there are items (Product\_IDs) that were not combined into a layer

▶ Is it possible to add another Product\_ID from the order?

```
end if
389:
                 end if
390:
                 if fw_i \cap fw_n \in [0.7; 1.0] then
391:
                     S_i \cup Product\_ID_i \cup Product\_ID_n
392:
                     if \sum_{i=1}^{I} W_i > W^{max} \| \sum_{i=1}^{I} H_i > H^{max} then
393:
                         go to 359
394:
                     else
395:
                         if \exists n : Product\_ID_n \in z then
396:
                             go to 359
397:
                         else
398:
                             S_i = BASE
399:
                             go to 26
400:
                         end if
401:
                     end if
402:
                 end if
403:
                 if fw_i > 1.0 then
404:
                     go to 359
405:
406:
                 end if
             else
407:
                 go to 359
408:
             end if
409:
410:
             if \exists_{i,n} : Product\_ID_i \cup Product\_ID_n then
411:
                 fW \leftarrow \cap fw_i
412:
                 if fW > 1 then
413:
                     S_i \cup Product\_ID_i \forall_i : \sum \_ifw_i \leq 1
414:
                     415:
416:
                     W_i^{zpk} = W^{norm} - W_j
417:
                     if W_n \leq 0.7 * W_j^{zpk} then S_j \cup Product\_ID_i \forall_i
418:
419:
                         S_i = TOP
420:
                         go to 26
421:
                     end if
422:
                     if W_n > 0.7 * W_i^{zpk} then
423:
                         S_j \cup Product\_ID_i \forall_i : W_n \le 0.7 * W_j^{zpk}
S_j = TOP
424:
425:
```

▶ Are there any items left in the order?

▶ There are no items (Product\_IDs) that were not combined in one layer

▶ The weight of the items to be added▶ Current weight of the pallet

```
go to 26
426:
                       end if
427:
                  end if
428:
              end if
429:
          end if
430:
          if \exists_{i,\dots,i+n;n>1}: Product_ID_i \cup Product_ID_i + n\&fw_i, fw_{i+n} \in [0.7; 1.0] then
                                                                                                                         ▶ Are in the order any items (Product_IDs) that have not been
431:
    combined and have full layers?
              go to 436
432:
          \mathbf{else}
433:
434:
              go to 625
          end if
435:
          if \exists_{i,...,i+n:n>1}: Product_ID_i \cup Product_ID_i + n\&fw_i, fw_{i+n} \in [0.7; 1.0] then \triangleright Are in the order at least two items that have not been combined and
436:
    have full layers?
              go to 441
437:
438:
          else
439:
              go to 481
          end if
440:
          if \exists_{i,i+n} ||H_i - H_{i+n}|| < 10 then
441:
              if fw_i \cap fw_{i+n} < 0.7 then
                                                                                                                            \triangleright Product\_ID_i and Product\_ID_{i+n} common layer fill factor
442:
                  if \exists Product\_ID_{i,...}\&fw_{i,...} < 0.7 then
                                                                                                                         ▶ Are there any items in the order that do not have full layers?
443:
                       if \forall_{m:m\neq i,m\neq i+n} ||H_m - H_i|| < 10 \& ||H_m - H_i|| < 10 then
444:
                           W \cup Product\_Id_i
                                                                                                                                                   \triangleright Create a new layer from Product\_ID_{i...}
445:
                           Si \cup W
446:
                           if fW < 0.7 then
447:
448:
                               go to 436
                           end if
449:
                          \begin{array}{ll} \textbf{if} & fW \in [0.7; 1.0] & \textbf{then} \\ & \textbf{if} & \sum_{i=1}^{I} W_i \leq W^{max} \| \sum_{i=1}^{I} H_i \leq H^{max} & \textbf{then} \\ & \textbf{go to ??} \end{array}
450:
451:
452:
                               else
453:
                                   S_i setminusW
                                                                                                                                     ▶ Remove from the palette the previously added layer
454:
                                    go to 436
455:
                               end if
456:
457:
                           end if
                           if fW > 1 then
458:
                               go to 436
459:
                           end if
460:
```

```
else
461:
                         go to 436
462:
                     end if
463:
                 end if
464:
             end if
465:
             if fw_i \cap fw_{i+n} \in [0.7; 1.0] then
466:
                 S_i \cup (Product\_ID_i, Product\_ID_{i+n})
467:
                 if \sum_{i=1}^{I} W_i \leq W^{max} \& \sum_{i=1}^{I} H_i \leq H^{max} then
468:
                     go to 436
469:
                 else
470:
                     S_i \setminus (Product\_ID_i, Product\_ID_{i+n})
471:
                     go to 436
472:
                 end if
473:
             end if
474:
             if fw_i \cap fw_{i+n} > 1.0 then
475:
                 go to 436
476:
             end if
477:
         else
478:
             go to 436
479:
         end if
480:
         if \exists_{i,i+n} ||H_i - H_{i+n}|| < 10 then
481:
             W \leftarrow \emptyset
482:
             W \cup (Product\_ID_i, Product\_ID_{i+n})
483:
             if fW < 0.7 then
484:
                 if \exists Product\_ID_{i...}\&fw_{i...} < 0.7 then
485:
                     go to 481
486:
                 else
487:
                     if \exists_{i,...,i+n;n} : Product_ID_i \cup Product_ID_i + n then
488:
                         if ||H_i - H_{i+n}| < 10 then
489:
                             W \cup (Product_ID_i, Product_ID_i + n)
490:
                             if fW < 0.7 then
491:
                                 if \exists_{i,\dots,i+n;n>1}: Product_ID_i \cup Product_ID_i + n then
492:
493:
                                      go to 489
                                  else
494:
                                     H_{cmax} \leftarrow 0
495:
                                     for each dom \in W
496:
                                          j_{add} \leftarrow -1
497:
```

▶ Add both items to the palette

▷ Are there any items in the order that do not have full layers?

 $\triangleright$  Are there any other items that have not been linked together?

 $\triangleright$  The filling degree of the layer cannot exceed 1.0

▶ Are in order other items that were not combined?

```
for each j \in S_i do
498:
                                             S_j \cup W_m
499:
                                            if H_i \leq H^{max} \& W_i \leq W^{max} then
500:
                                                if H_j > H_{cmax} then
501:
                                                    H_{cmax} \leftarrow H_j
502:
                                                    j_{add} \leftarrow j
503:
                                                else
504:
                                                    S_j \setminus W_m
505:
                                                    j_{add} \leftarrow -1
506:
                                                end if
507:
                                             else
508:
                                                S_i \setminus W_m
509:
                                                j_{add} \leftarrow -1
510:
                                             end if
511:
                                        end for each
512:
                                        if j_{add} \neq -1 then
513:
                                            if \exists_i : Product JD_i \in z \& W_j + W_i \leq W^{max} \& H_j - H_m + H_i then \triangleright Can we add Product ID from the order to the top
514:
    layer?
                                                S_i \cup Product\_ID_i
515:
                                            end if
516:
                                             S_i \leftarrow TOP
517:
                                             go to 26
518:
                                        end if
519:
                                    end for each
520:
                                     for each m \in W do
521:
                                        W \setminus Product JD_i \in W \& H_i = max
                                                                                                      ▶ From each set we remove the Product_ID whose height is the highest
522:
                                         go to 495
523:
                                    end for each
524:
                                 end if
525:
                            end if
526:
                            if fw \in [0.7; 1.0] then
527:
                                 W \cup (Product_ID_i, Product_ID_i + n)
528:
                                if W_i \leq W^{max} then
529:
                                    \S_i \leftarrow BASE
530:
                                    go to 26
531:
532:
                                 else
                                    while W_i + W_{Product\_Idi} \leq W^{max} do \triangleright Add additional Product_id items that do not exceed the maximum weight limit W^{max}
533:
```

```
S_i \cup Product\_ID_i
534:
                                        end while
535:
                                        if fw < 0.7 then
536:
                                            go to 481
537:
                                        end if
538:
                                        if fw \in [0.7; 1.0] then
539:
                                            S_i \leftarrow BASE
540:
                                            go to 26
541:
                                        end if
542:
                                    end if
543:
                               end if
544:
                           else
545:
                               for each m \in W do
                                                                                         \triangleright Add Product_ID to the linked items so as not to exceed the fill factor value 1(fw \le 1)
546:
                                    while fw_i + fW < 1.0 do
547:
                                       W_m \cup Product\_ID_i
548:
                                    end while
549:
                                   \begin{array}{ll} S_j \cup W_m \\ \text{if} & \sum_{i=1}^I W_i \leq W^{max} \& \sum_{i=1}^I H_i \leq H^{max} & \text{then} \\ & S_j \leftarrow TOP \end{array}
550:
551:
552:
                                        go to 26
553:
554:
                                        while \sum_{i=1}^{I} W_i > W^{max} \& \sum_{i=1}^{I} H_i > H^{max} do
                                                                                                        \triangleright Remove the added Product_id until the W^{max} and H^{max} values of the
555:
     pallet are not exceeded
                                            S_i \setminus Product\_ID_i
556:
                                        end while
557:
                                         S_j \leftarrow TOP
558:
                                        go to 26
559:
                                    end if
560:
                               end for each
561:
                           end if
562:
                                                                                                                      \triangleright Add Product_ID for which the height difference exceeds 10[mm]
563:
                          if \sum_{i=1}^{I} W_i \leq W^{max} \& \sum_{i=1}^{I} H_i \leq H^{max} then S_j = TOP
564:
565:
                               go to 26
566:
567:
                               while W_j + W_{Product\_ID_i} \le W^{max} \& W_j + W_{Product\_ID_i} \le W^{max} do
568:
                                    S_i \cup Product\_ID
569:
```

```
end while
570:
                              S_i = TOP
571:
                              go to 26
572:
                          end if
573:
                      end if
574:
                 end if
575:
              end if
576:
             if fW \in [0.7; 1.0] then
577:
                 S_i \cup Product\_ID
578:
                 if \sum_{i=1}^{I} W_i \leq W^{max} \& \sum_{i=1}^{I} H_i \leq H^{max} then
579:
                      \overrightarrow{\mathbf{if}} \exists_{i,n} : Product\_ID_i, Product\_ID_{i+n} \in z\&Product\_ID_i \sqcup Product\_ID_{i+n} then
580:
                          go to 481
581:
                      else
582:
                         \S_j \leftarrow TOP
583:
                          go to 26
584:
                      end if
585:
                 else
586:
                                                                                                                 \triangleright Add Product_ID to the palette until W^{max} or H^{max} is reached
                      \mathbf{while} \ \ W_j + W_{Product\_ID_i} \leq W^{max} \& W_j + W_{Product\_ID_i} \leq W^{max} \ \ \mathbf{do}
587:
                          S_i \cup Product\_ID_i
588:
                      end while
589:
                      if fw < 0.7 then
590:
                          S_i \leftarrow TOP
591:
592:
                          go to 26
                      end if
593:
                      if fw \in [0.7; 1.0] then
594:
                          if h_{diff} \leq 10 then
595:
                              S_i \leftarrow BASE
596:
597:
                          else
                              S_j \leftarrow TOP
598:
                          end if
599:
                          go to 26
600:
                      end if
601:
                      if fw > 1.0 then
602:
                          while fw > 1.0 do
603:
                              S_j \setminus Product\_ID_i
604:
                          end while
605:
                          if fw < 0.7 then
606:
```

```
S_i \leftarrow TOP
607:
                           end if
608:
                           if fw \in [0.7; 1.0] then
609:
                               S_j \leftarrow BASE
610:
                           end if
611:
                           go to 26
612:
                       end if
613:
                  end if
614:
              end if
615:
616:
              while \sum_{i=1}^{I} W_{i} \leq W^{max} \& \sum_{i=1}^{I} H_{i} \leq H^{max} \& fw \leq 1 do if \exists_{n} Product JD_{n} : H_{n} = max \& \sum_{i=1}^{I} W_{i} + W_{n} \leq W^{max} \& \sum_{i=1}^{I} H_{i} + H_{n} \leq H^{max} \& fw \cap fw_{n} \leq 1 then
617:
618:
                      S_i \sum Product JD_n
619:
                      S_i = TOP
620:
621:
                       go to 26
622:
                  end if
              end while
623:
624:
          end if
          if \exists_{i,...,i+n;n\geq 1} : ||H_i - H_{-i}...n|| \leq 10 then
                                                                                                      > Are there Product_ID items whose height difference does not exceed 10[mm]
625:
              if fw < \overline{0}.7 then
626:
                  if \exists_i : Product\_ID_i \in z then
                                                                                                              > There are items in the order that can be added to the pallet unit load
627:
                       go to 625
628:
629:
                  else
                                                                                            > There are no additional items in the order that can be added to the pallet unit load
                       S_i \cup Product\_ID_{i...n}
                                                                                                                                    ▶ Add those that meet the height difference condition
630:
                      if \sum_{i=1}^{I} W_i \leq W^{max} \| \sum_{i=1}^{I} H_i \leq H^{max} then S_j = TOP
631:
632:
                           go to 26
633:
                       else
634:
                           S_i \setminus Product JD_{i...n}
                                                                                                                          ▶ Remove from the pallet loading unit previously added items
635:
                           if \exists_i : Product\_ID_i \in z then
636:
                               go to ??
637:
                           else
638:
                               go to 26
639:
                           end if
640:
                       end if
641:
                  end if
642:
              end if
643:
```

```
if fw \in [0.7; 1.0] then
644:
                 S_j \cup Product\_ID_{i...n}
645:
                 if \sum_{i=1}^{I} W_i \leq W^{max} \| \sum_{i=1}^{I} H_i \leq H^{max} then if \exists_i : Product\_ID_i \in z then
646:
647:
                          go to 625
648:
                      else
649:
                         S_i = BASE
650:
                         go to 26
651:
                      end if
652:
                 else
653:
                      S_i \setminus Product\_ID_{i...n}
                                                                                                                    ▶ Remove from the pallet loading unit previously added items
654:
                     if \exists_i : Product\_ID_i \in z then
655:
                         go to 625
656:
                      else
657:
                         go to 26
658:
                      end if
659:
                 end if
660:
             end if
661:
             if fw > 1.0 then
662:
                 if \exists_i : Product\_ID_i \in z then
663:
                     go to 625
664:
665:
                     if \sum_{i=1}^{I} W_i > W^{max} then
666:
                         while \sum_{i=1}^{I} W_i > W^{max} do
667:
                             S_i \setminus \overline{Product} ID_i : W_i = max
                                                                      \triangleright Remove the Product_ID of the maximum weight from the pallet unit load until the W^{max} value is
668:
    reached
                         end while
669:
                      end if
670:
                     if \sum_{i=1}^{I} H_i > H^{max} then
671:
                         while \sum_{i=1}^{I} H_i > H^{max} do
672:
                             S_i \setminus \overline{Product} ID_i : H_i = max
                                                                       \triangleright Remove the Product_ID of the maximum height from the pallet unit load until the H^{max} value is
673:
    reached
674:
                         end while
675:
                      end if
                     if fw > 1.0 then
676:
                         while fw > 1.0 do
677:
                              S_i \setminus Product ID_i : fw = max \triangleright Remove the Product ID of the maximum height from the pallet unit load until the fw value of top
678:
```

```
layer is reached
                        end while
679:
                     end if
680:
                    if \forall_{i,j}: Product\_ID_i, Product\_ID_j \in Top_layer\&||H_i - H_j|| \le 10\&fw \in [0.7; 1.0] then
681:
                        S_i = BASE
682:
                        go to 26
683:
                     end if
684:
                    if \forall_{i,j}: Product\_ID_i, Product\_ID_i \in Top_layer\&||H_i - H_i|| > 10\&fw < 0.7 then
685:
                        S_i = TOP
686:
                        go to 26
687:
                     end if
688:
                end if
689:
             end if
690:
         else
691:
             if fw < 0.7 then
692:
                S_i \cup Product\_ID_{i...n}
693:
                if \sum_{i=1}^{I} W_i > W^{max} then
                                                                                              ▷ Check whether the weight of the pallet loading unit has not been exceeded
694:
                    while \sum_{i=1}^{I} W_i > W^{max} do
                                                                     \triangleright Remove those with the lowest weight until the weight of the pallet loading unit W^{max} is reached
695:
                        S_i \setminus Product ID_i : W_i = min
696:
                     end while
697:
                end if
698:
                if \sum_{i=1}^{I} H_i > H^{max} then
                                                                                              ▷ Check whether the weight of the pallet loading unit has not been exceeded
699:
                    while \sum_{i=1}^{I} H_i > H^{max} do
                                                                     \triangleright Remove those with the lowest weight until the weight of the pallet loading unit W^{max} is reached
700:
                        S_i \setminus \overline{Product} ID_i : H_i = min
701:
                     end while
702:
                end if
703:
                S_i = TOP
704:
                go to 26
705:
             end if
706:
             if fw \in [0.7; 1.0] then
707:
                S_i \cup Product\_ID_{i...n}
708:
                if \sum_{i=1}^{I} W_i > W^{max} then
                                                                                              ▷ Check whether the weight of the pallet loading unit has not been exceeded
709:
                     while \sum_{i=1}^{I} W_i > W^{max} do
                                                                     \triangleright Remove those with the lowest weight until the weight of the pallet loading unit H^{max} is reached
710:
                        S_i \setminus \overline{Product} ID_i : W_i = min
711:
                     end while
712:
                end if
713:
                if \sum_{i=1}^{I} H_i > H^{max} then
                                                                                              > Check whether the weight of the pallet loading unit has not been exceeded
714:
```

```
while \sum_{i=1}^{I} H_i > H^{max} do
                                                                   \triangleright Remove those with the lowest weight until the weight of the pallet loading unit H^{max} is reached
715:
                       S_i \setminus Product\_ID_i : H_i = min
716:
                    end while
717:
                end if
718:
                S_i = TOP
719:
                go to 26
720:
            end if
721:
            if fw > 1.0 then
722:
                S_i \cup Product JD_{i...n} : fw_i = max
                                                                            \triangleright Add to the pallet loading unit the Product_ID with the highest degree of layer filling fw_i
723:
                if \sum_{i=1}^{I} W_i > W^{max} then
                                                                                           ▷ Check whether the weight of the pallet loading unit has not been exceeded
724:
                    while \sum_{i=1}^{I} W_i > W^{max} do
                                                                    \triangleright Remove those with the lowest weight until the weight of the pallet loading unit H^{max} is reached
725:
                       S_i \setminus Product\_ID_i : W_i = min
726:
                    end while
727:
                end if
728:
                if \sum_{i=1}^{I} H_i > H^{max} then
                                                                                           ▶ Check whether the weight of the pallet loading unit has not been exceeded
729:
                    while \sum_{i=1}^{I} H_i > H^{max} do
                                                                    \triangleright Remove those with the lowest weight until the weight of the pallet loading unit H^{max} is reached
730:
                       S_i \setminus Product JD_i : H_i = min
731:
                    end while
732:
                end if
733:
            end if
734:
            if fw \in [0.7; 1.0] then
735:
                S_j = BASE
736:
                go to 26
737:
            else
738:
                S_i = TOP
739:
                go to 26
740:
            end if
741:
         end if
742:
         for each Product\_Id_i do
743:
            if CL_i < CL_i then
744:
                go to 282
745:
746:
            else
                go to 431
747:
748:
            end if
         end for each
749:
750: end for each
751: STOP
```