

# RSQSim Runs

## Contents

<b>Run 1</b>	<b>1</b>
<b>Run 2</b>	<b>2</b>
<b>Run 3</b>	<b>2</b>
<b>Run 4</b>	<b>2</b>
<b>Run 5</b>	<b>2</b>
<b>Run 6</b>	<b>2</b>
<b>Run 7</b>	<b>3</b>
<b>Run 8</b>	<b>3</b>
<b>Run 100</b>	<b>3</b>
<b>Run 101</b>	<b>3</b>
<b>Run 102</b>	<b>3</b>
<b>Run 103</b>	<b>3</b>
<b>Run 104</b>	<b>3</b>
<b>Results table</b>	<b>4</b>
<b>References</b>	<b>4</b>

NOTE: Results table (at end of document) is latex/pdf specific and does not work in html.

## Run 1

- Main fault
  - 5 km  $\times$  3 km
  - vertical
  - strike-slip
  - 100 m elements
  - top edge at 2 km depth
  - initial normal stress: 100 MPa
  - initial shear stress: 65 MPa
- Random faults
  - n = 2000
  - size: to produce GR between M=0 and M=2

- orientation: parallel to main fault
- position: exponentially distributed distance from random main fault element, random direction
- eliminate those within 10 m of main fault
- initial stresses: same as main fault
- Injection
  - `makeInjectionHistory()`'s default values:
    - \* diffusivity,  $\kappa = 0.008\text{m}^2/\text{s}$
    - \* porosity,  $\phi = 0.05$
    - \* compressibility,  $c = 5 \cdot 10^{-10}\text{Pa}^{-1}$
    - \* injection rate,  $Q = 0.0069\text{m}^3/\text{s}$
  - 500 m from center point of main fault

## Run 2

Same as Run1 except for:

- Random faults
  - orientation: perturbed from that of main fault with a standard deviation of  $10^\circ$  about uniformly distributed random axes

## Run 3

Same as Run 2 except:

- Main fault
  - initial shear stress: 63 MPa
- Random faults
  - initial shear stress:  $63 \pm 1$  MPa (mean  $\pm$  standard deviation)

## Run 4

Same as Run 3 except:

- Main fault
  - initial shear stress: 62 MPa

## Run 5

Same as Run 4 except:

- Main fault
  - initial shear stress: 62.8 MPa

## Run 6

Same as Run 5 except:

- Main fault
  - initial shear stress: 63.2 MPa

## Run 7

Same as Run 6 except:

- Random faults
  - initial shear stress:  $65 \pm 1$  MPa

## Run 8

Same as Run 7 except:

- Random faults
  - initial shear stress:  $66 \pm 1$  MPa

## Run 100

Same as Run 6 except:

- Random faults
  - $n = 5000$

## Run 101

Same as Run 100 except:

- Random faults
  - $n = 10000$

## Run 102

Same as Run 101 except:

- Injection
  - 1500 m from center of fault

## Run 103

Same as Run 102 except:

- Injection
  - 1000 m from center of fault

## Run 104

Same as Run 103 except:

- Main fault
  - initial shear stress: 66.7 MPa

## Results table

	Run	$t_{M \geq 5}$	$N$	$N_b$	$N_a$	$N_{ex}$	$f_{as}$ naive	$f_{as}$ SS-all	(0.16)	$f_{as}$ SS-ex	(0.84)	$f_{as}$ Z-all	$f_{as}$ Z-ex	$f_{as}$ H-all	$f_{as}$ H-ex
1	Run1	6.2	52	20	31	2	0.54	0.93	0.39	0.45	0.57	0.55	0.53	0.96	0.82
2	Run2	6.1	48	20	27	1	0.52	0.92	0.46	0.57	0.83	0.55	0.59	0.96	0.81
3	Run3	38.4	49	19	29	0	0.47	0.62	0.52	0.62	0.89	0.54	0.52	0.81	0.81
4	Run4		22			0	0.00	0.05	0.01	0.04	0.36	0.24	0.24	0.79	0.79
5	Run5	79.2	45	21	23	0	0.49	0.80	0.68	0.80	0.95	0.55	0.55	0.88	0.88
6	Run6	27.8	49	19	29	0	0.57	0.50	0.44	0.50	0.72	0.71	0.71	0.58	0.58
7	Run7	29.9	109	66	42	0	0.36	0.29	0.25	0.29	0.59	0.30	0.29	0.85	0.85
8	Run8	10.5	195	116	78	5	0.37	0.98	0.22	0.25	0.29	0.32	0.33	0.98	0.71
9	Run100	12.6	81	48	32	5	0.35	0.80	0.39	0.52	0.83	0.39	0.40	0.86	0.66
10	Run101	27.8	212	126	85	10	0.35	0.50	0.26	0.30	0.36	0.39	0.42	0.87	0.59
11	Run102		22			0	0.00	0.04	0.01	0.04	0.25	0.33	0.00	0.42	0.42
12	Run103		46			0	0.00	0.09	0.02	0.10	0.43	0.04	0.07	0.51	0.51
13	Run104	18.3	124	34	89	3	0.64	0.95	0.52	0.57	0.65	0.65	0.68	0.96	0.80

Table 1: Summary of run results.  $t_{M \geq 5}$ : time until first  $M \geq 5$  event (yrs).  $N$ : total number of events.  $N_b$ : number of events before first  $M \geq 5$  event.  $N_a$ : number of events after first  $M \geq 5$  event.  $N_{ex}$ : number of very late outlying events.  $f_{as}$ -naive: aftershock fraction taking events within 5 years of  $M \geq 5$  as aftershocks.  $f_{as}$ -SS-all: aftershock fraction from Bayesian fitting of *Saichev and Sornette* [2007] to all events.  $f_{as}$ -SS-ex: as previous but excluding very late events. (0.16) and (0.84): 68% confidence intervals of previous.  $f_{as}$ -Z-all: aftershock fraction ala Zaliapin and Ben-Zion, 2018 using all events.  $f_{as}$ -Z-ex: as previous but excluding very late events.  $f_{as}$ -H-all: aftershock fraction from *Hainzl et al.* [2006]  $f_{as}$ -H-ex: as previous but excluding very late events.

If you take the  $f_{as}$ -naive as being the true answer, and if you count the cases where  $f_{as}$ -naive is 0.00 and the lower end of the 68% CIs for Bayesian fitting of *Saichev and Sornette* [2007] is 0.01 or 0.02 as being close enough, then the true answer falls within the 68% CIs 9 out of 13 times, so 69% of the time (when the late outliers are removed).

The *Hainzl et al.* [2006] method seriously overestimates the aftershock fraction in most cases.

## References

- Hainzl, S., F. Scherbaum, and C. Beauval (2006), Estimating background activity based on interevent-time distribution, *Bulletin of the Seismological Society of America*, 96(1), 313–320.
- Saichev, A., and D. Sornette (2007), Theory of earthquake recurrence times, *Journal of Geophysical Research: Solid Earth*, 112(B4).