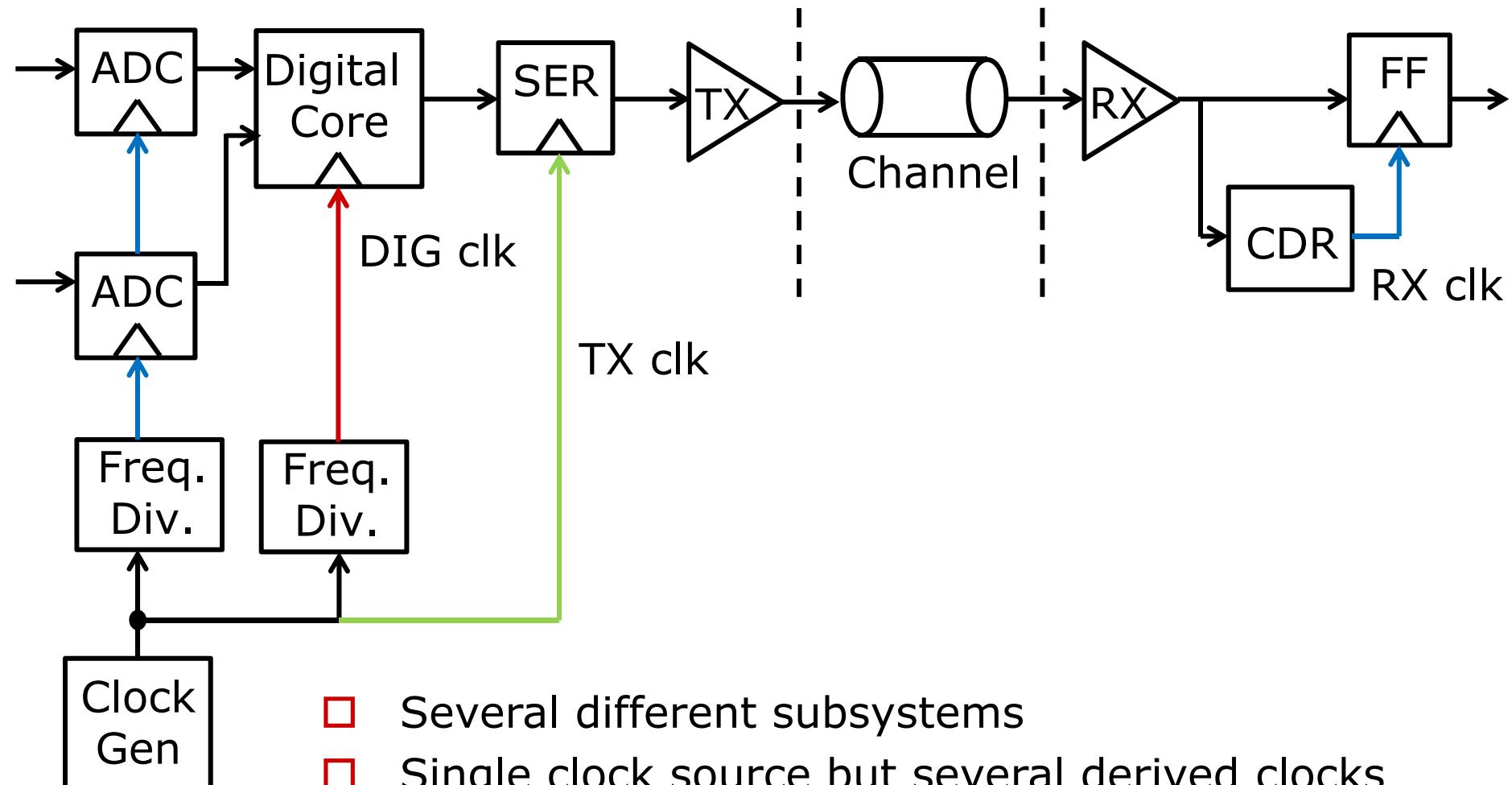

ISSCC 2012 Tutorials

JITTER basic and advanced concepts, statistics and applications

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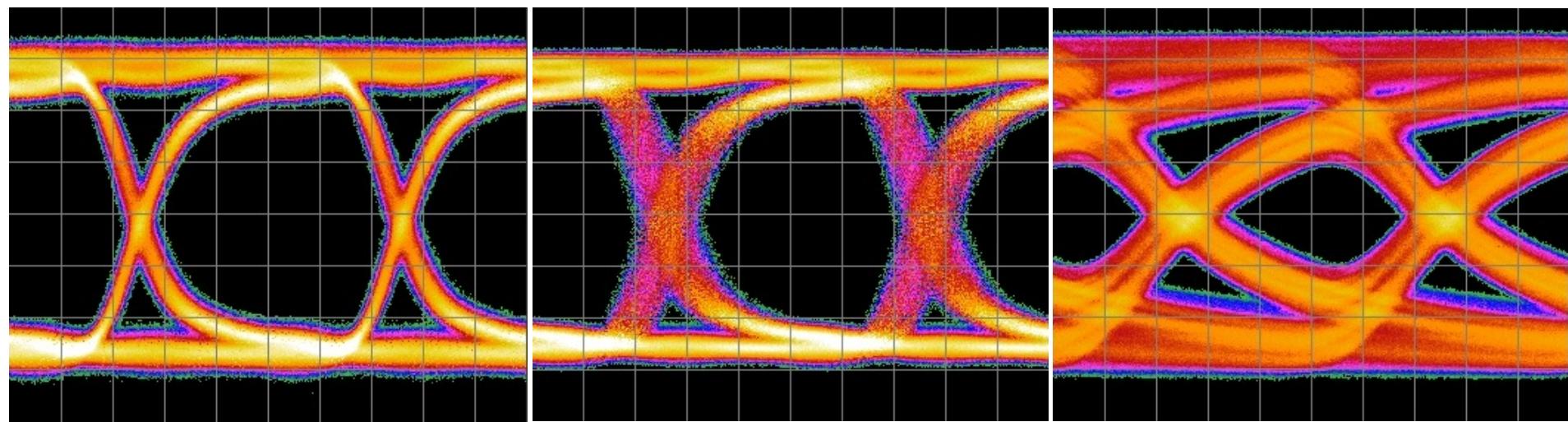
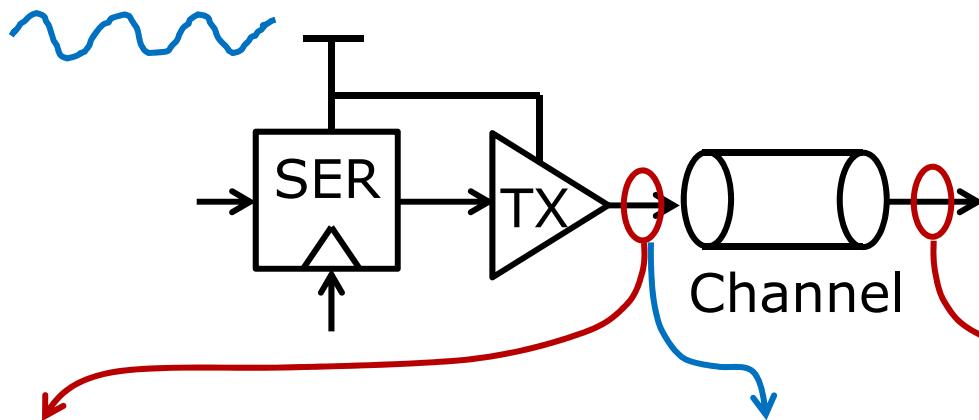
San Francisco, February 19th, 2012

Motivation: a complex system



- ❑ Several different subsystems
- ❑ Single clock source but several derived clocks
- ❑ Each subsystem has own jitter requirements

Motivation: jitter in serial high speed TX

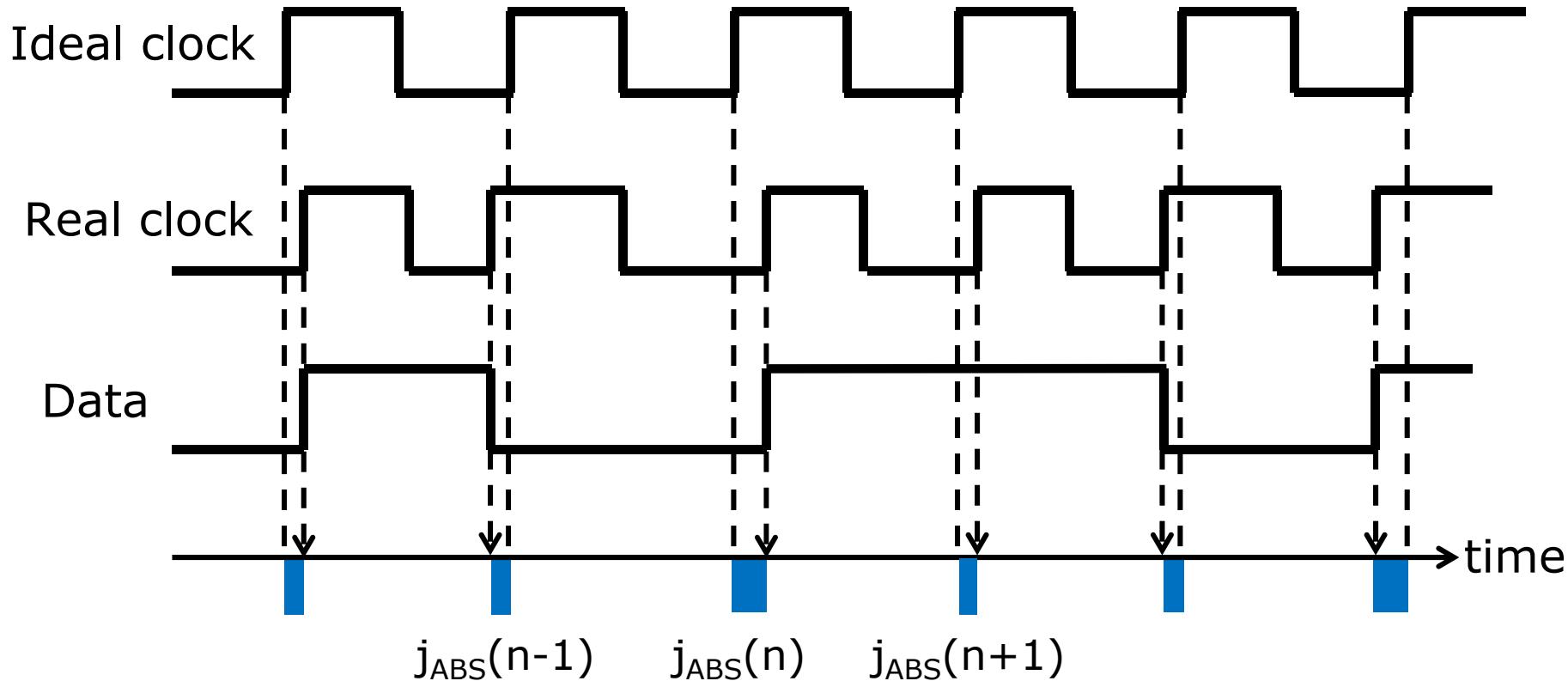


- ☐ Jitter can show different faces. How to define and quantify it?

Overview

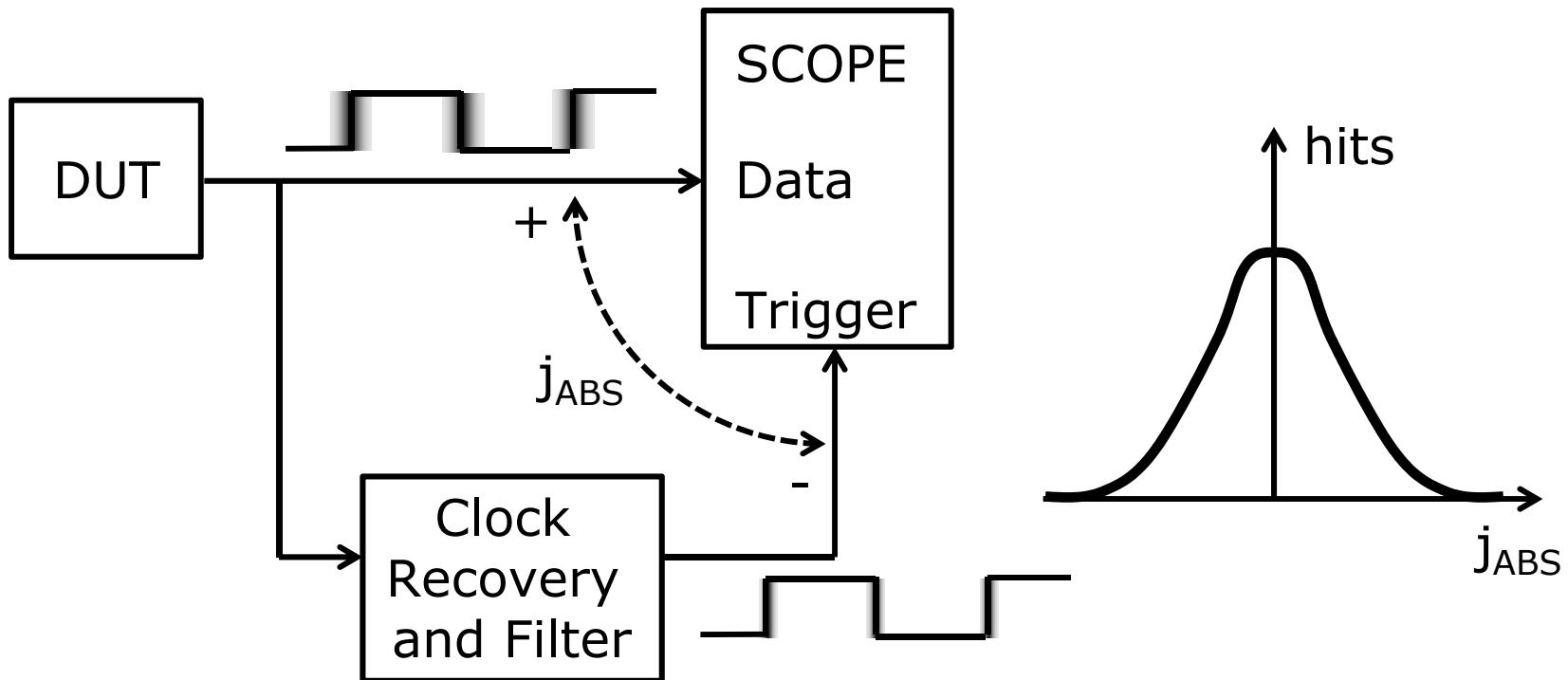
- Definition of absolute jitter
 - Time and frequency domain measurements
 - Phase noise and jitter
 - Jitter in electronics systems and typical applications
 - Self-referenced jitter and additional definitions
 - Jitter statistics for gaussian and non-gaussian distributions
 - Bathtub curves
 - Application to high-speed serial data transmission
 - Jitter and spectral spurious tones
-

Absolute Jitter : definition



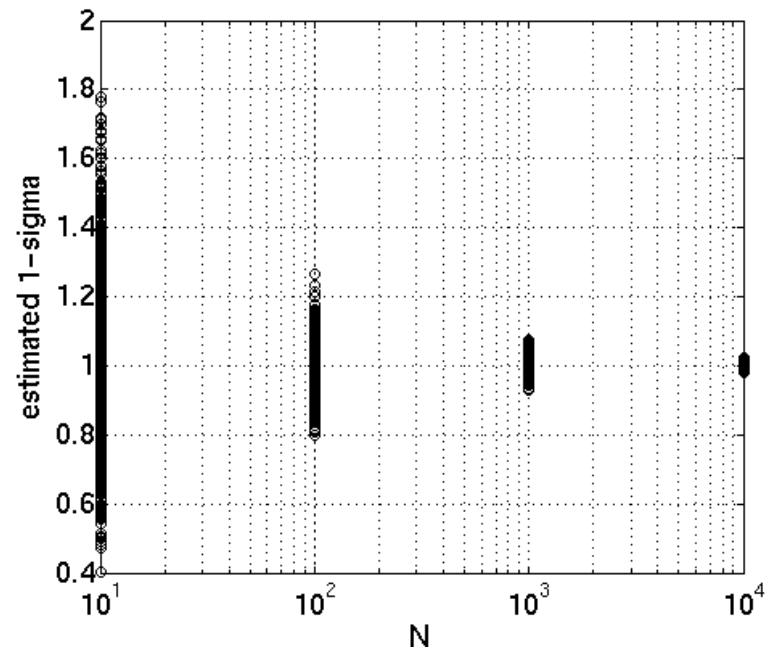
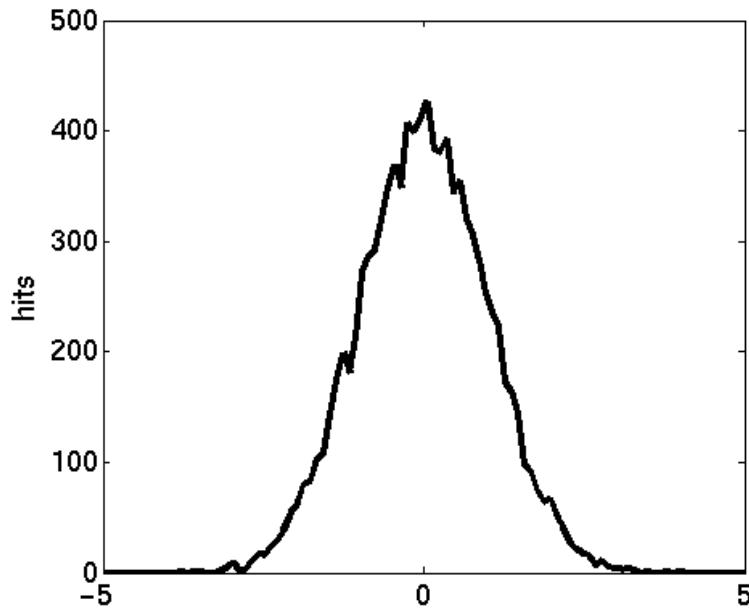
- ☐ **Absolute jitter** := Time difference between real and ideal edges

Absolute Jitter : Time Domain Meas



- ❑ Clock recovery or PLL with clean up function (included in most high-end scopes)
- ❑ Scope measures the time difference from trigger to data
- ❑ Results are typically shown in form of histograms

Estimation of RMS from Histogram (1/3)



- ❑ Estimated 1-sigma $\hat{\sigma}_{ABS} = \sqrt{\frac{1}{N-1} \sum_1^N j_{ABS}^2(i)}$
- ❑ N = number of hits in histogram
- ❑ The larger N , the more accurate the estimation

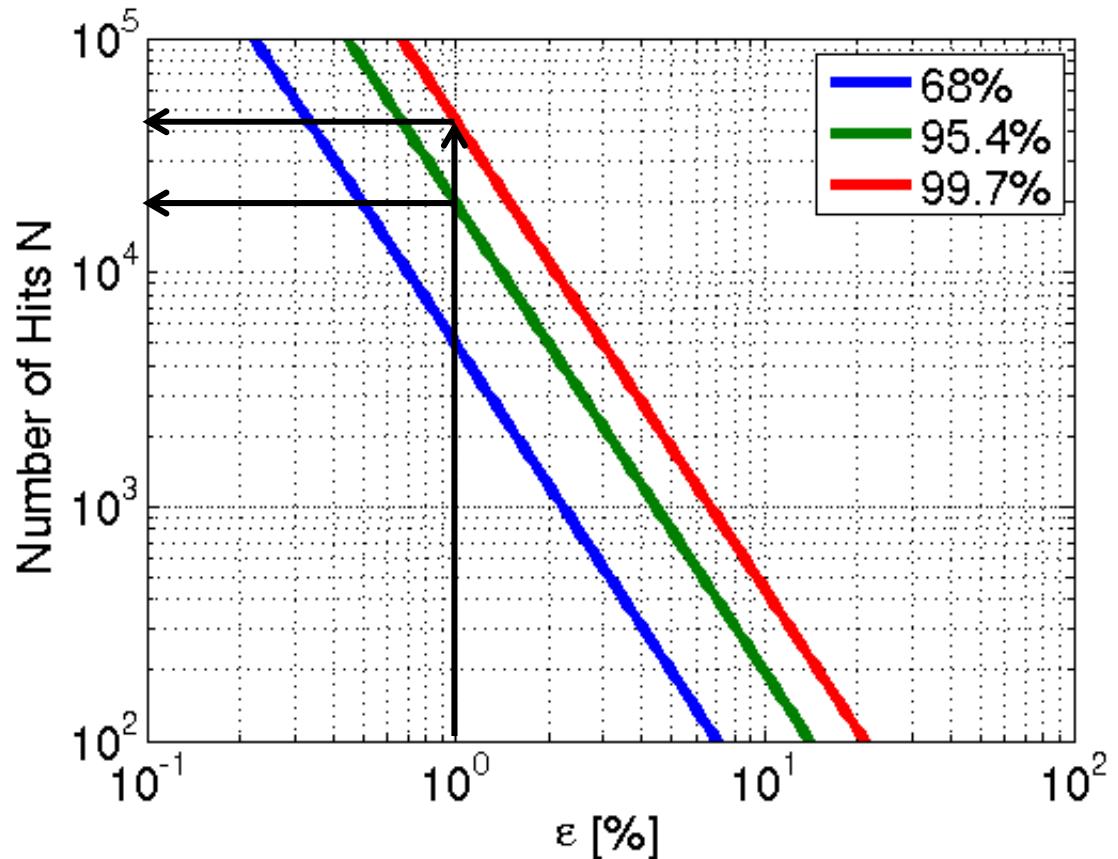
Estimation of RMS from Histogram (2/3)

- A coffee company asks you to estimate the average size of coffee beans of a farm. **You'll have to pay a fine if you are wrong.**
 - Take "N" coffee beans, measure, average = **11mm**
 - You want to reserve a **margin for error** = **+/- 1mm** (this is called **Confidence Interval, CI**)
 - **How sure are you?** You repeat the experiment lots of times (on different beans) and find out that in **90%** of the cases the average is indeed within 11mm +/- 1mm. This "90%" is called **Confidence Level, CL**.
 - With larger N => CI can be tighter or CL improves
-

Estimation of RMS from Histogram (3/3)

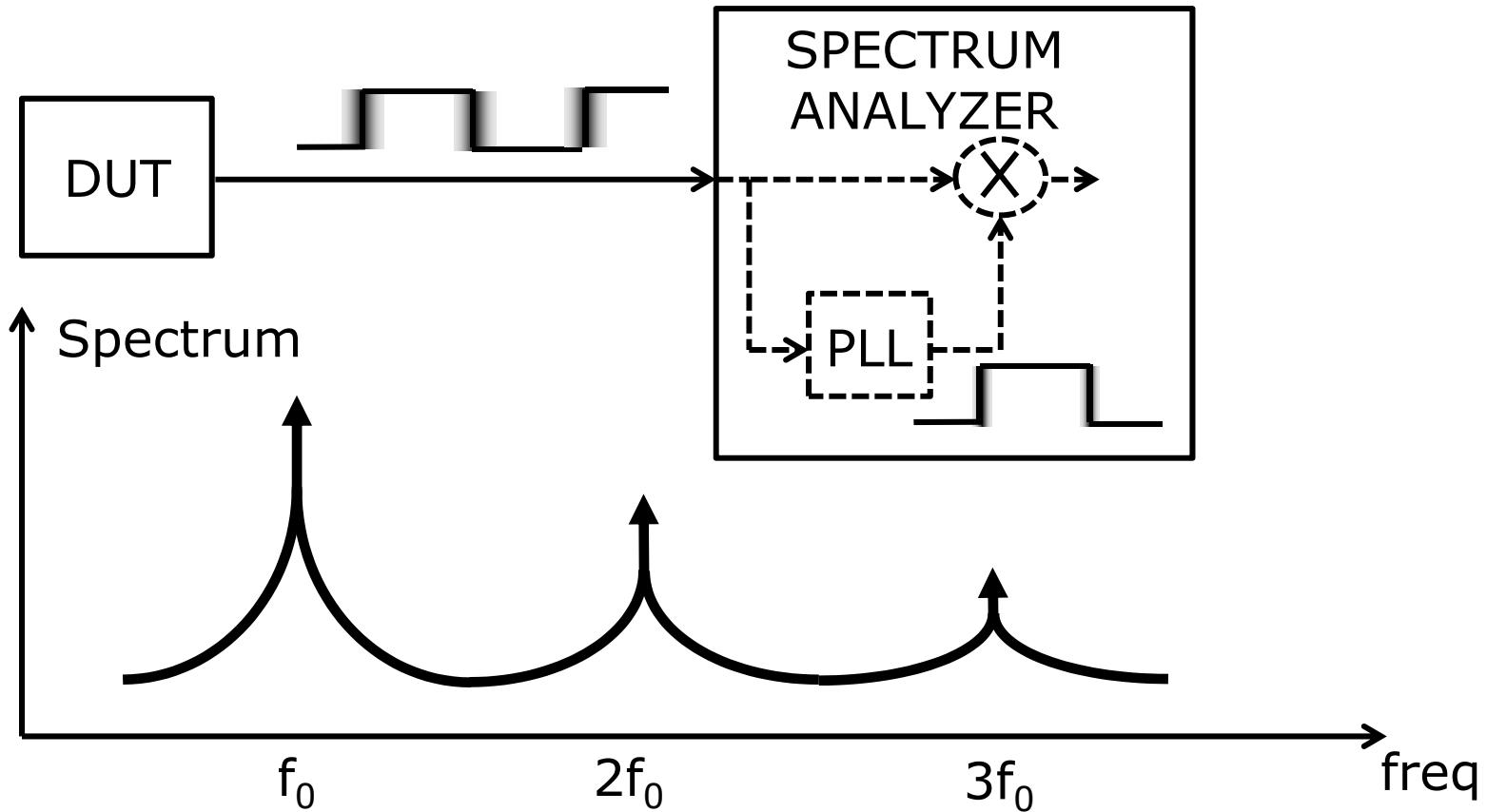
- Goal: Estimate the RMS within an error margin ε (confidence interval) and with a given confidence level
- Question: how large should N be?

$$N \geq \frac{1}{2} \left(\frac{Q}{\varepsilon} \right)^2$$



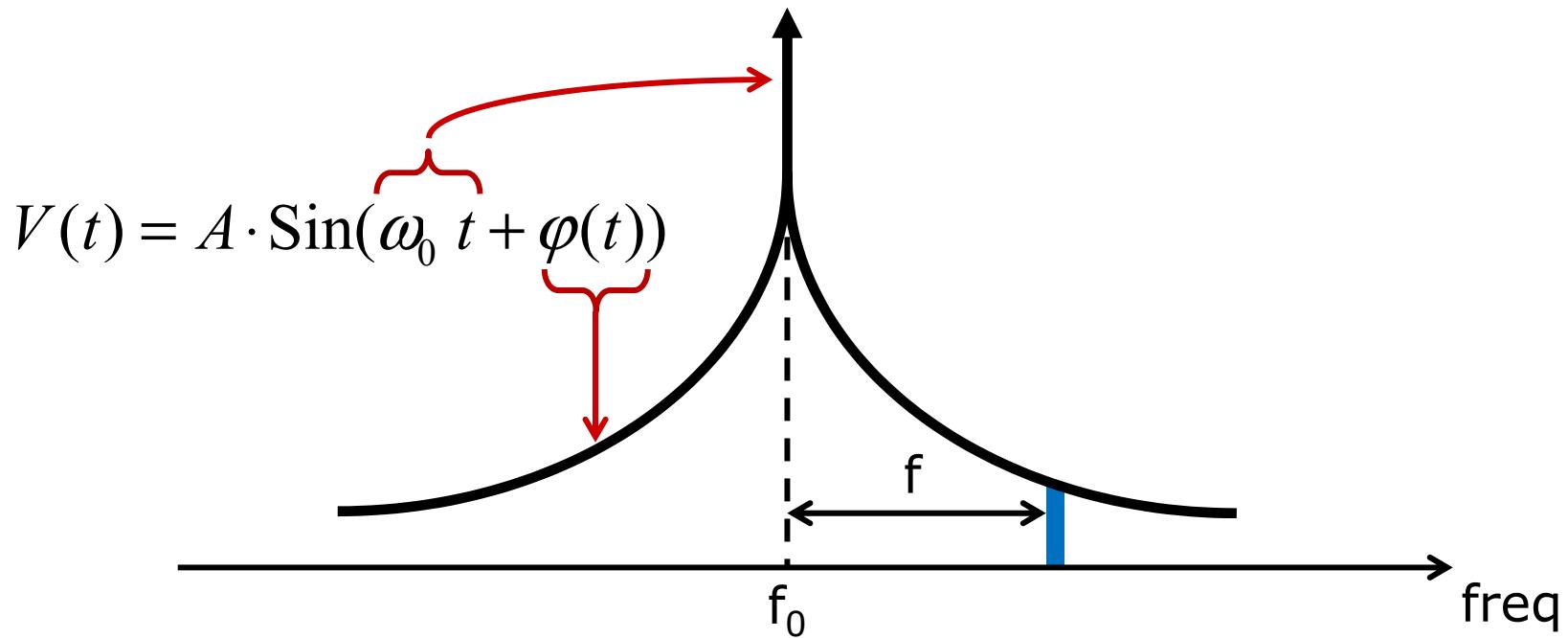
- Confidence Level:
 - 68% ($Q=1$)
 - 95% ($Q=2$)
 - 99.7% ($Q=3$)

Absolute Jitter : Freq Domain Meas



- ❑ Spectrum analyzer locks to ext clock and generates clean one
- ❑ Clean clock is used to mix ext clock and measure its power
- ❑ Result is shown in form of spectrum of voltage signal

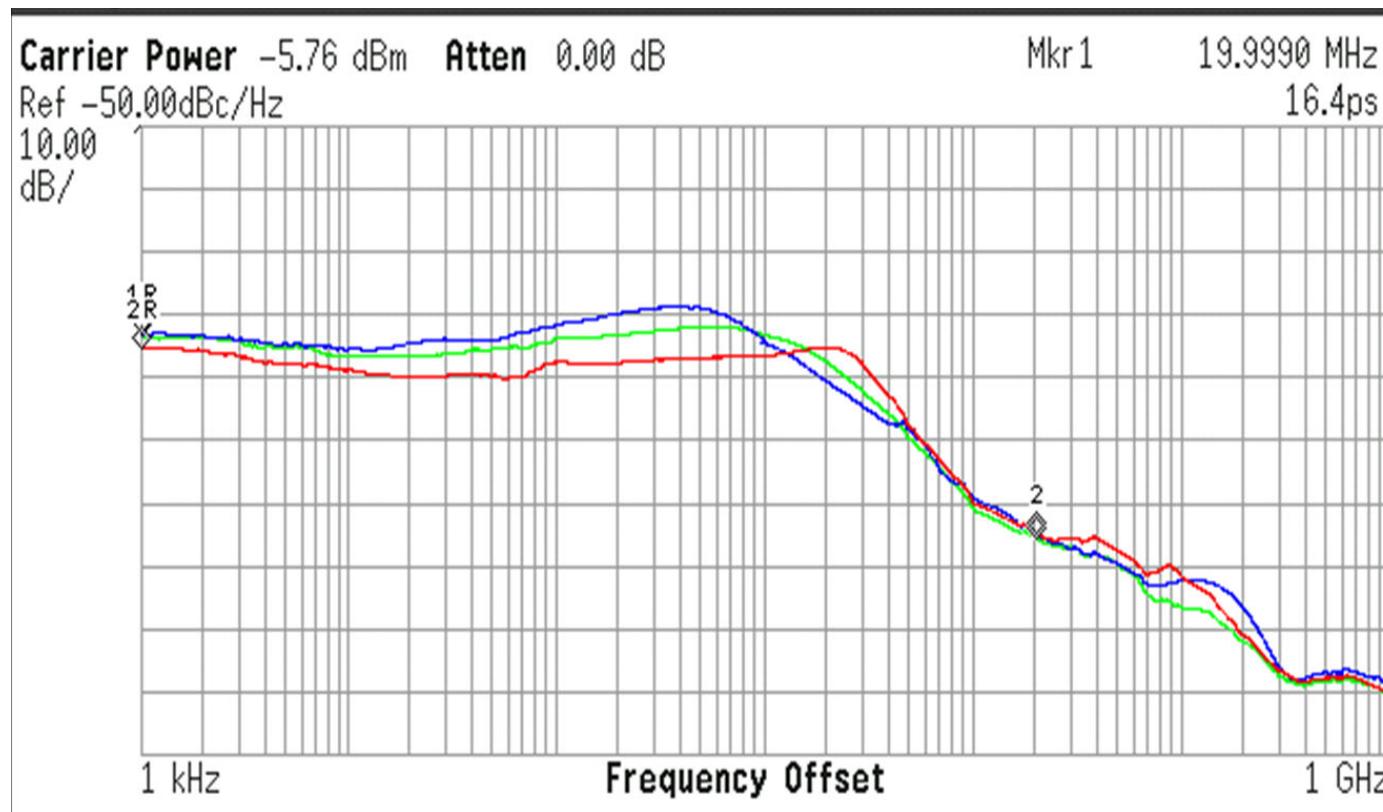
Voltage Spectrum to Phase PSD



$$\frac{\text{Power of in 1 Hz BW @ } f \text{ from Carrier}}{\text{Power of Carrier}} \cong \text{PSD of } \varphi, S_\varphi(f)$$

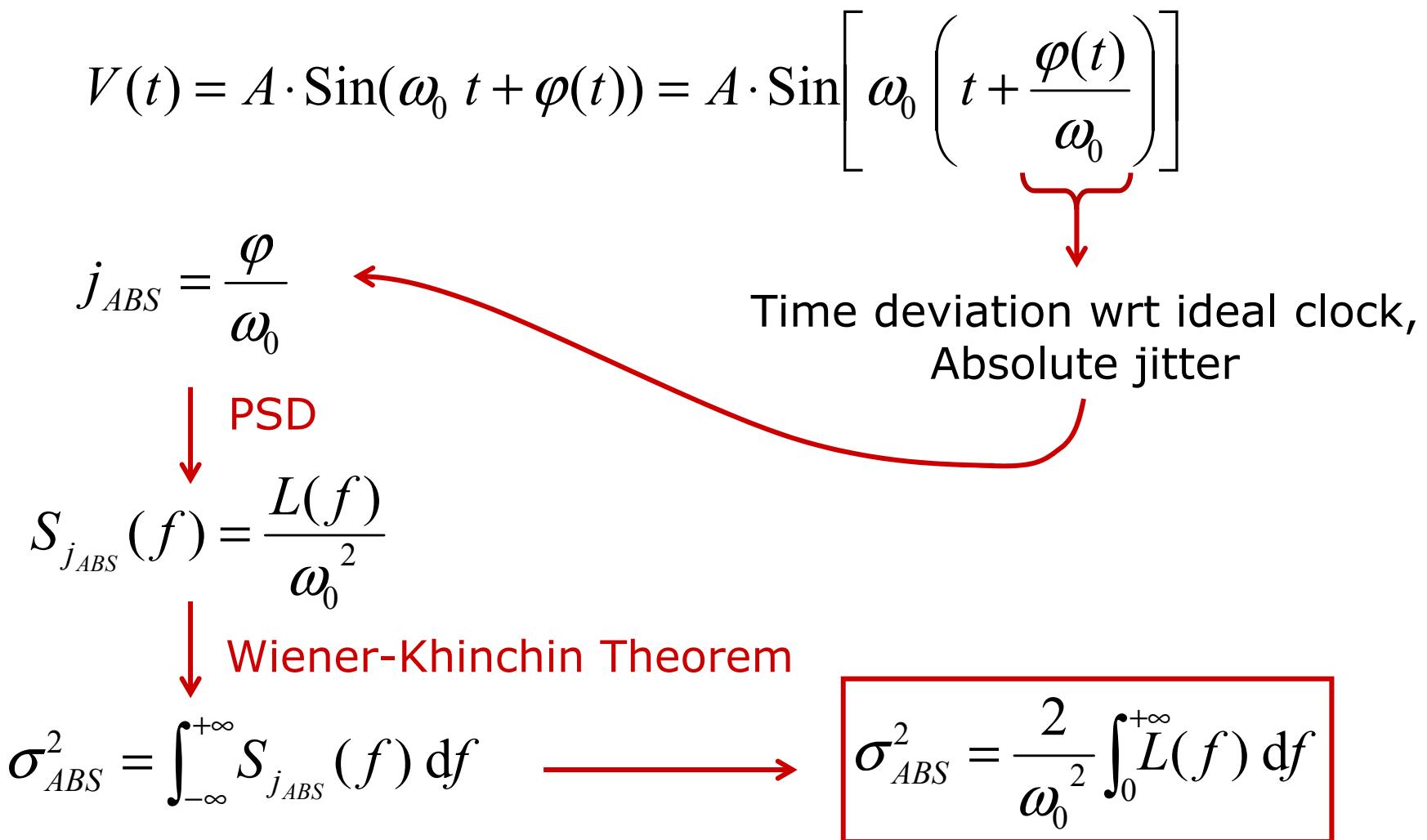
- Assumptions: No AM, Small angle modulation
- PSD is Single Side Band

Phase Noise

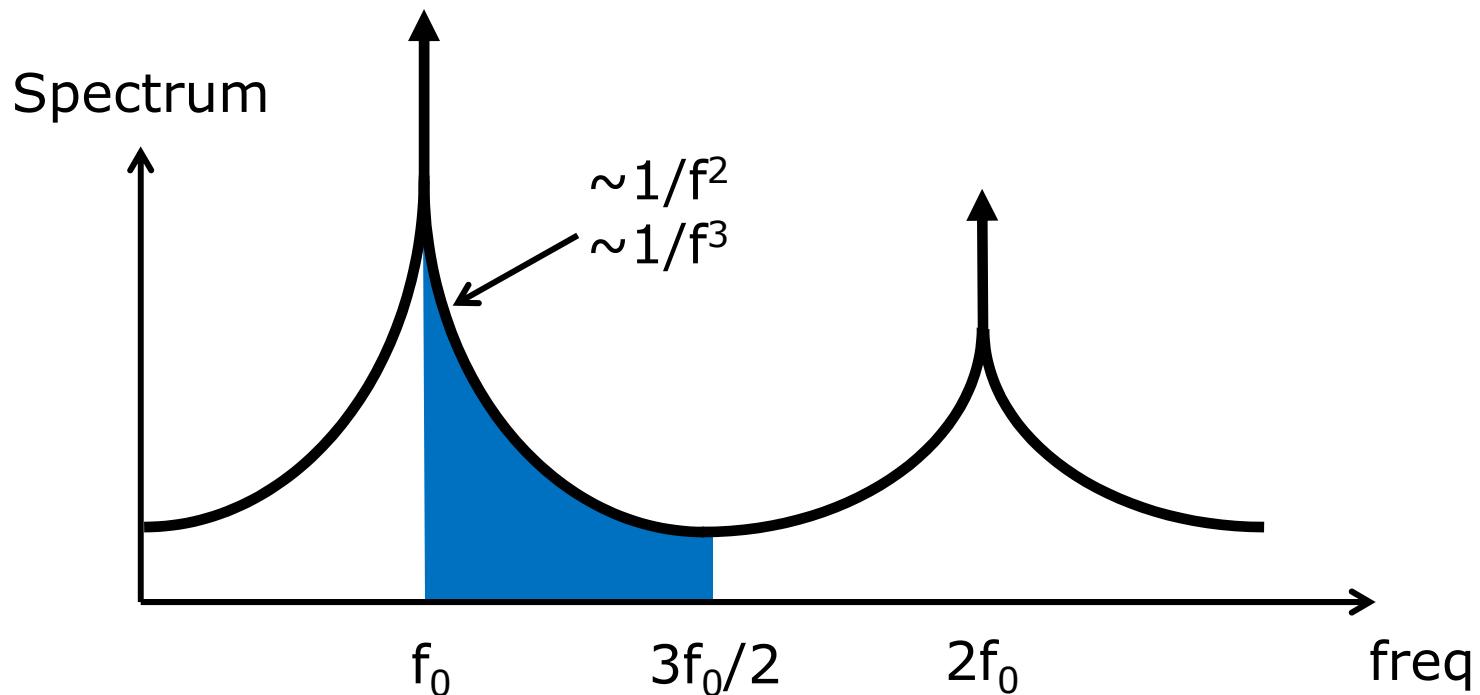


- PSD of φ is called **Phase Noise, $L(f)$**
- Shown in log-log scale vs. frequency from carrier
- Automatically computed by most spectrum analyzers

Phase Noise to Absolute Jitter



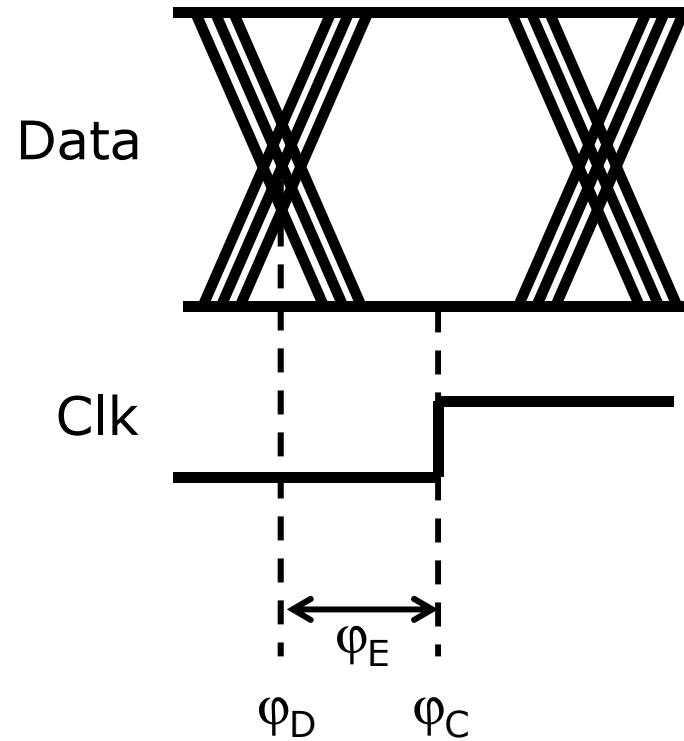
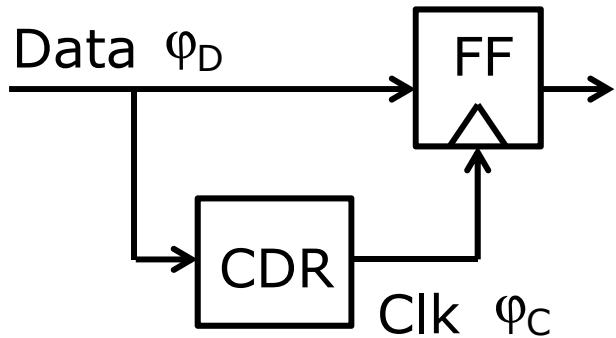
Phase Noise integration limits



$$\sigma_{ABS}^2 = \frac{2}{\omega_0^2} \int_{f_{MIN}}^{f_0/2} L(f) df \quad \sigma_{ABS}^2 = \frac{2}{\omega_0^2} \int_0^{+\infty} L(f) |H_{SYS}(f)|^2 df$$

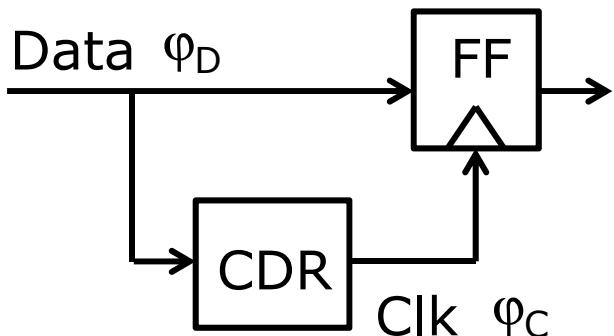
- Hard limits (f_{MIN} to $f_0/2$)
- Jitter transfer function of system under investigation

Jitter filtering in CDR systems (1/3)



- CDR system is sensitive to φ_E
- Low frequency jitter is tracked by CDR, does not hurt the BER
- High frequency jitter is not tracked by CDR, hurts the BER

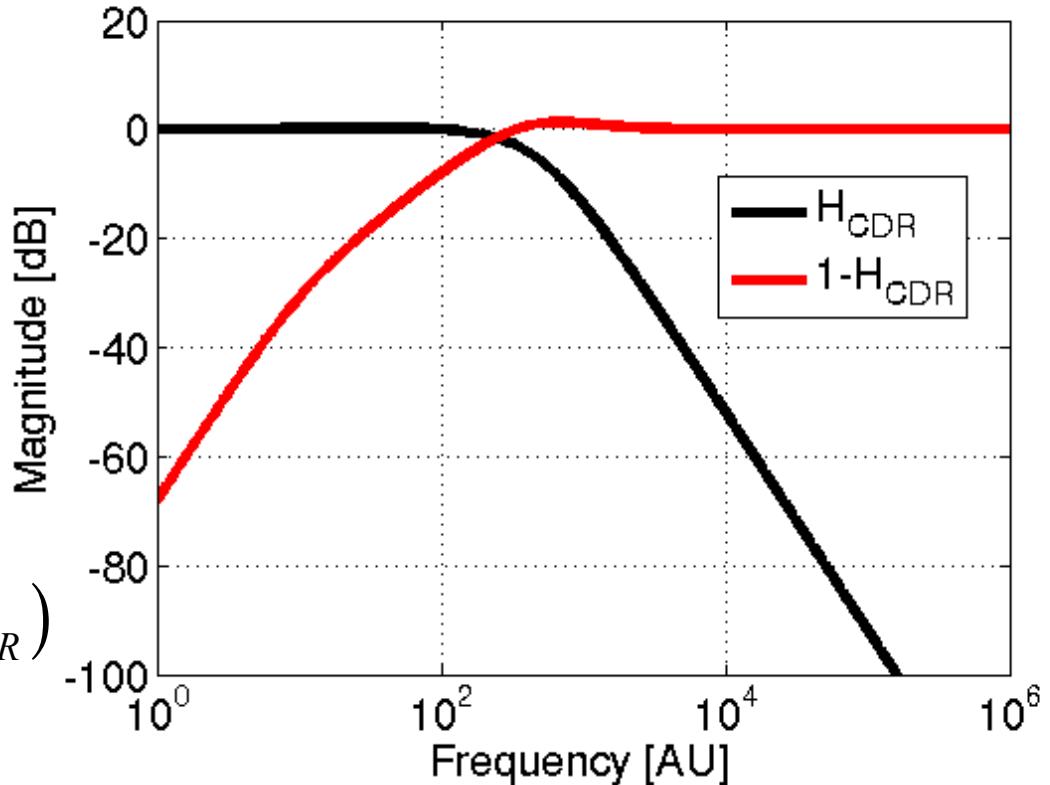
Jitter filtering in CDR systems (2/3)



$$\varphi_C = H_{CDR} \cdot \varphi_D$$

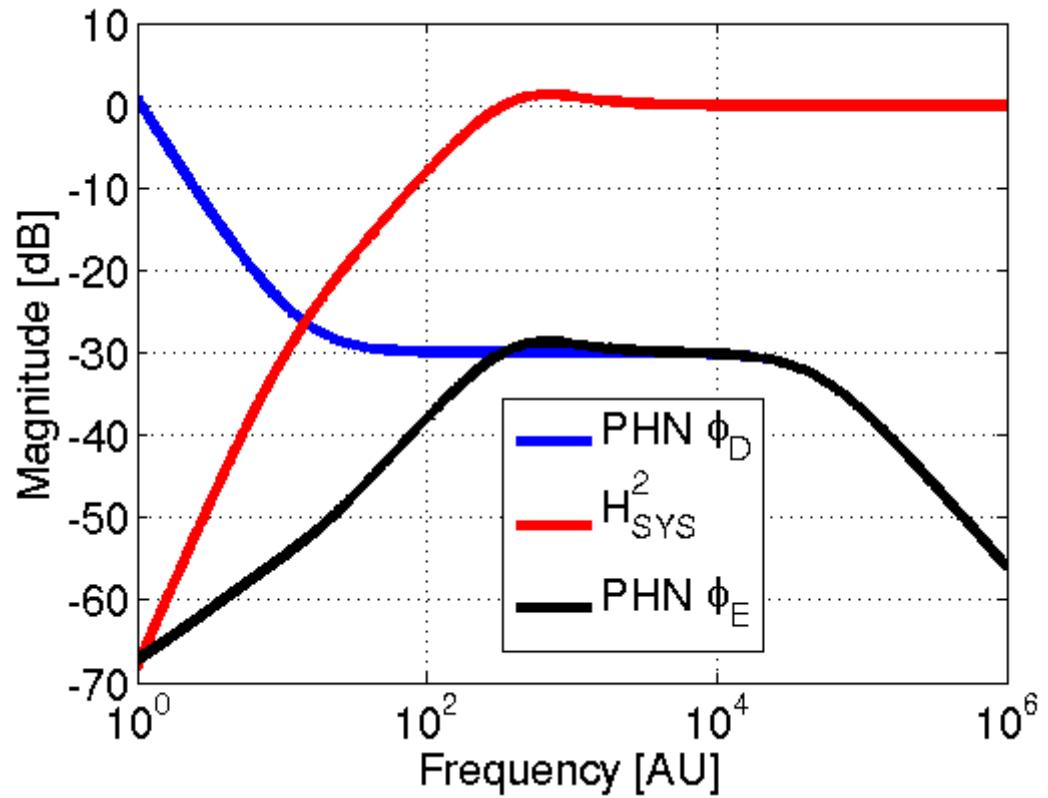
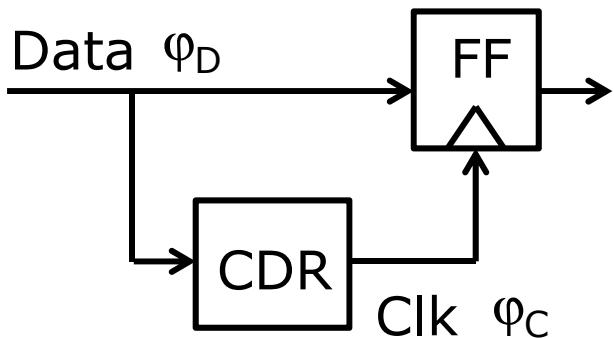
$$\varphi_E = \varphi_D - \varphi_C = \varphi_D (1 - H_{CDR})$$

$$H_{SYS} = 1 - H_{CDR}$$



- Transfer function of CDR is a low-pass
- Transfer function of system (φ_D to φ_E) is a high-pass

Jitter filtering in CDR systems (3/3)



- ❑ Low-frequency jitter is filtered by the H_{sys} before integration
- ❑ Integral from 0 to $f_0/2$ of Phase Noise of φ_E is finite

Summary so far

- Absolute jitter
- Measurement in time domain
- Estimation of 1-sigma value from histogram
- Measurement in frequency domain
- Phase Noise
- Relationship between Phase Noise and Absolute jitter
- Limitation of Phase Noise integration interval

What's next:

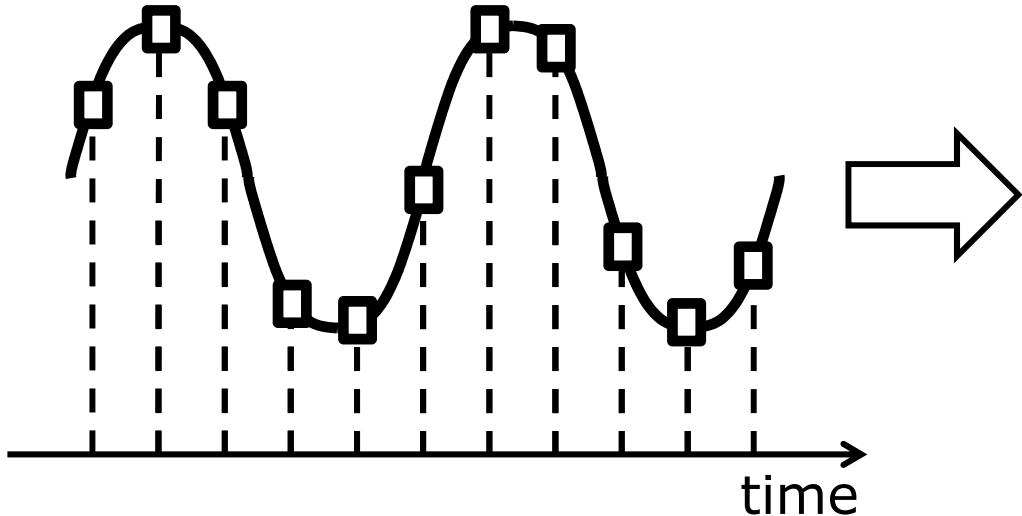
- Analyze typical applications and the type of jitter they are sensitive to
 - New jitter types will be introduced
-

Application Scope of Absolute Jitter

- RX for High Speed interfaces (see example of CDR before)
- Sampling of analog signals (i.e. in ADC)
- Generation of analog signal from digital (i.e. in DACs)
- **NOT** applicable to digital clocking

Sampling of Analog Signals (1/2)

ANALOG DOMAIN



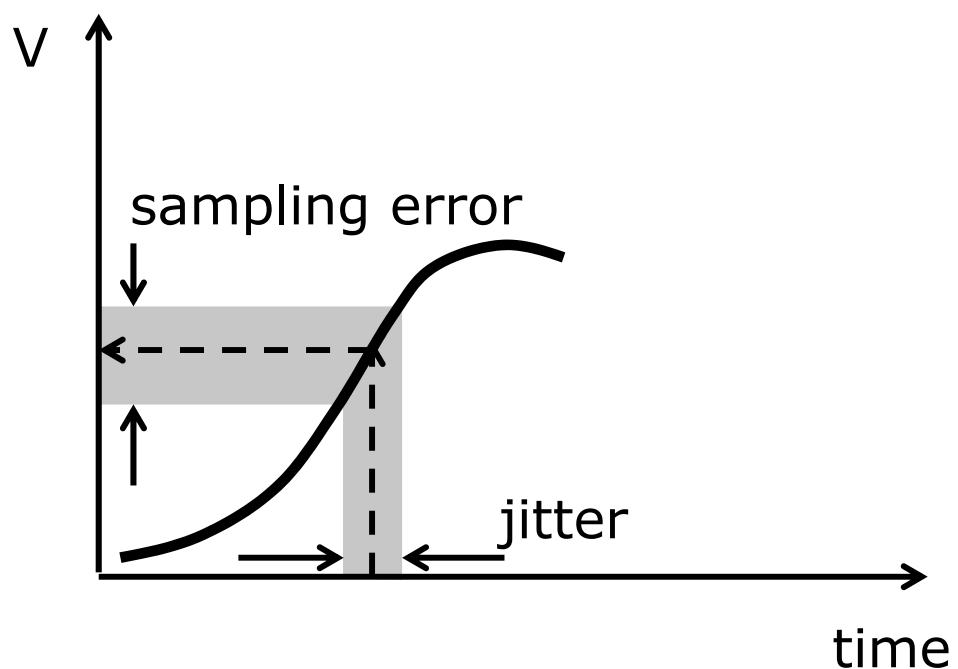
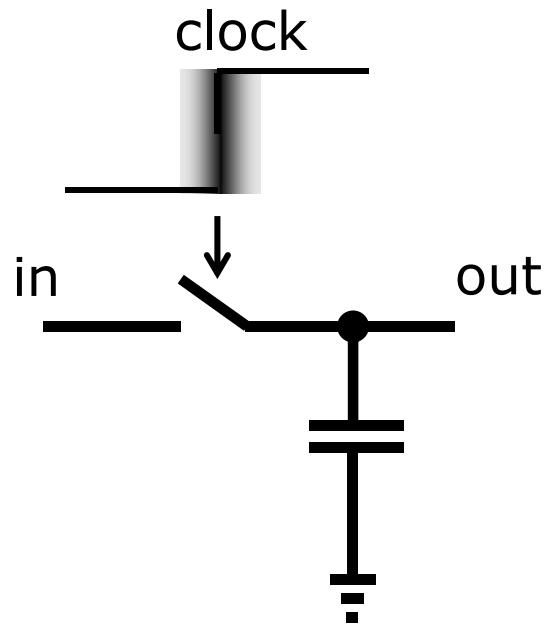
DIGITAL DOMAIN

..., 23, 25, 22, 18, 17, 20, ...

Just a sequence of numbers,
stored in a FIFO

- In the digital domain the time information of the sampling instant is lost
- The implicit assumption is that the samples are taken on the edges of an ideal clock
- What counts is the absolute jitter

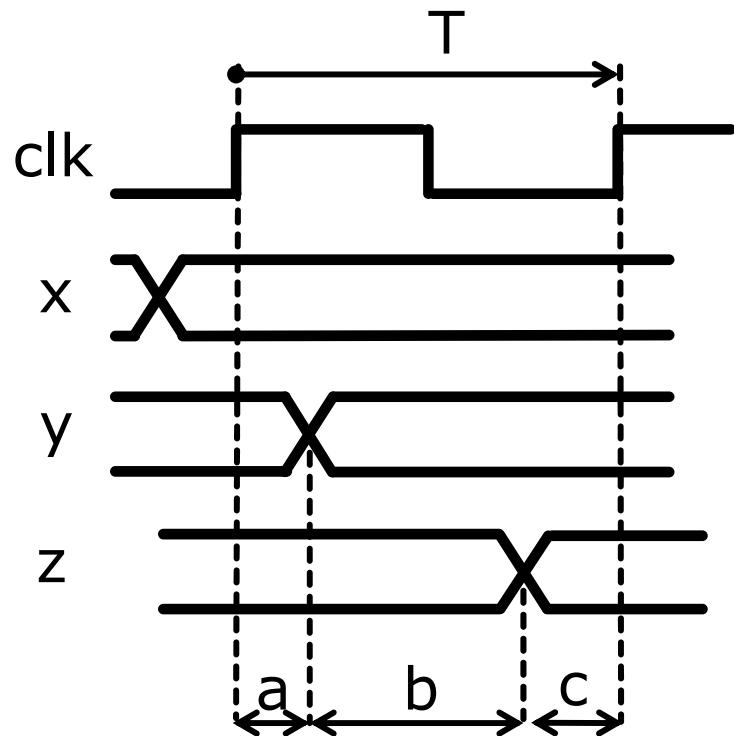
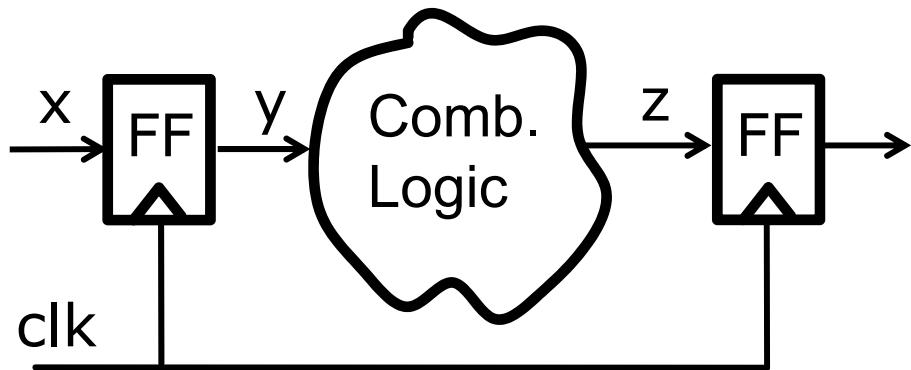
Sampling of Analog Signals (2/2)



- $\text{SNR} = P_{\text{signal}} / P_{\text{error}}$
- $P_{\text{error}} = P_{\text{jitter}} * \langle \text{Slope}^2 \rangle$
- $P_{\text{jitter}} = \sigma_{\text{ABS}}^2$
- $\text{SNR} \sim 1 / \sigma_{\text{ABS}}^2$

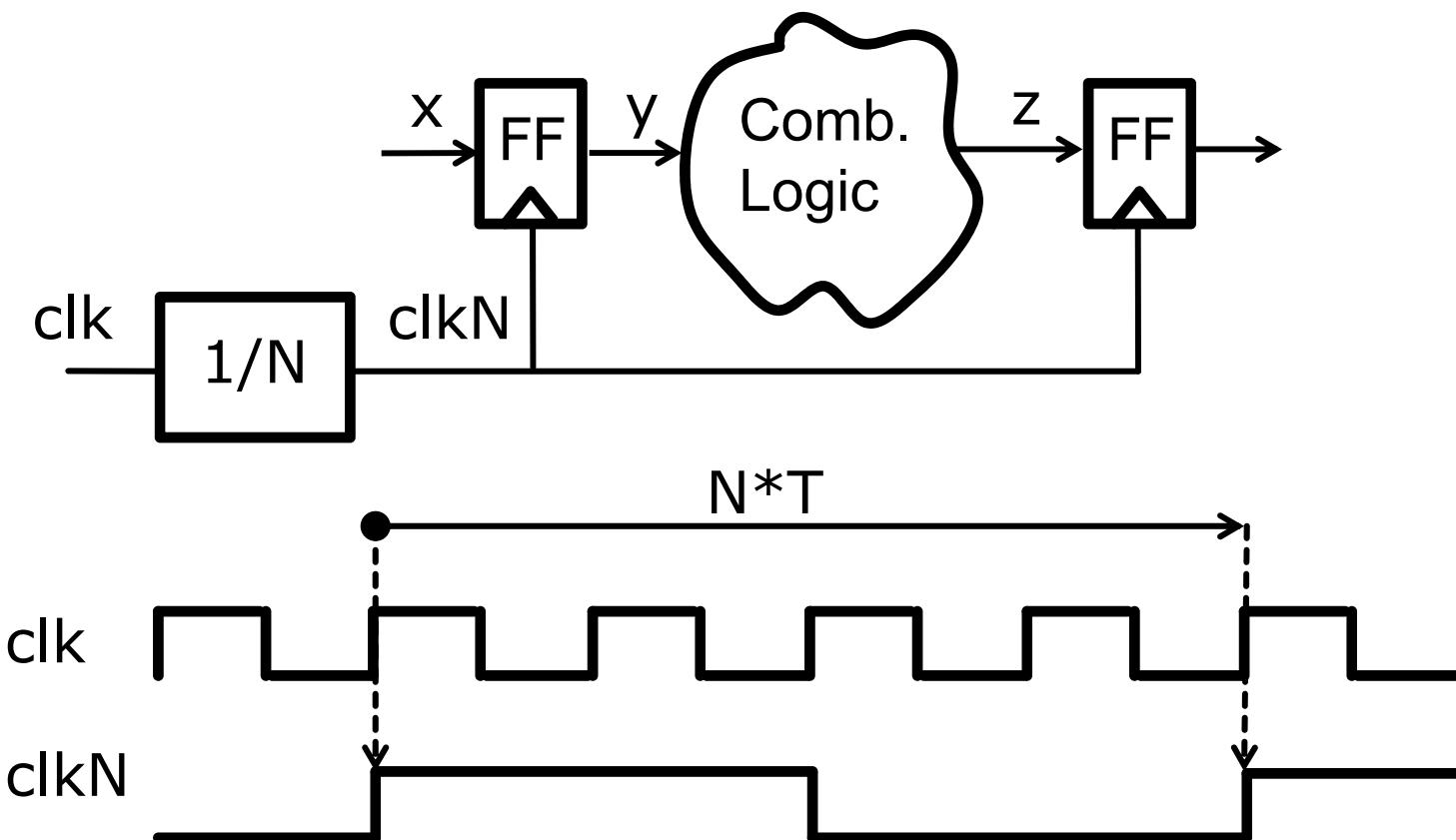
$$SNR = 20 \cdot \log_{10} \left(\frac{1}{2\pi f_{ANA} \sigma_{ABS}} \right) dB$$

Digital Clocking (1/2)



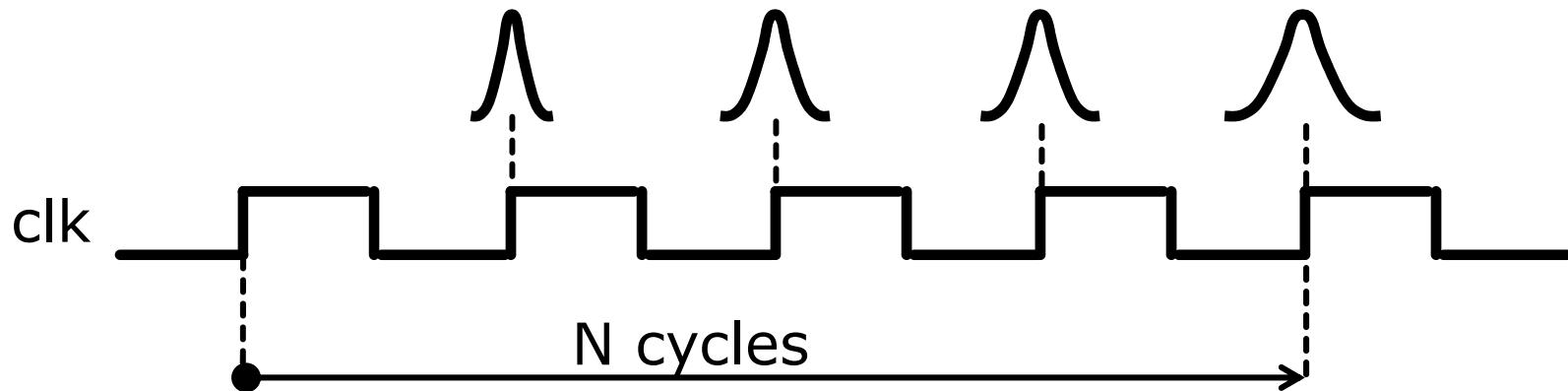
- $a = clk2Q$
- $b = \text{delay of logic}$
- For correct operation: $c > \text{FF setup time}$
- Constraint set on minimum duration of the clock period T (from edge to edge)

Digital Clocking (2/2)



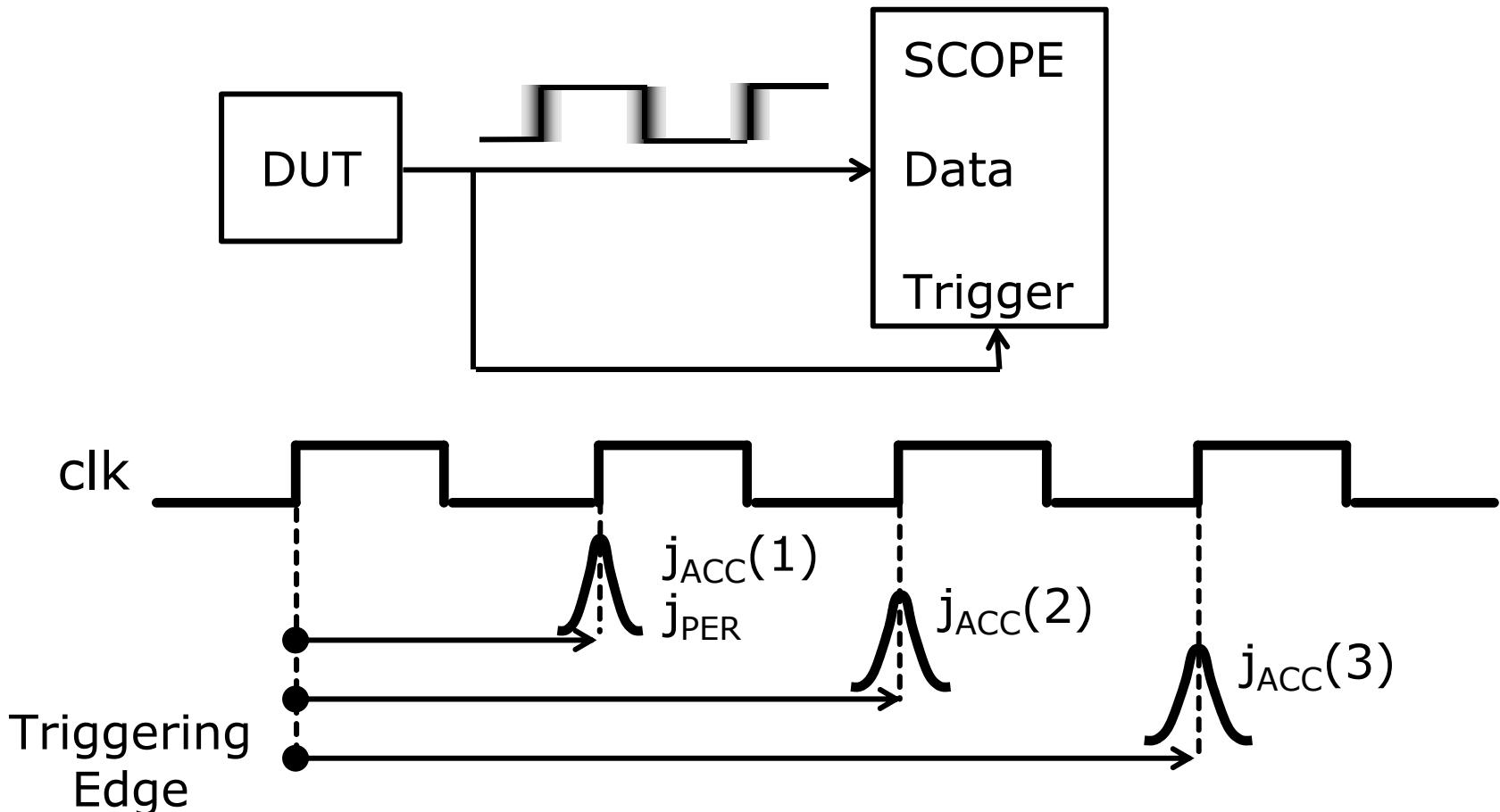
- Constraint set on minimum duration of N clock periods (from edge to the next N th edge)

Accumulated Jitter (j_{Acc})



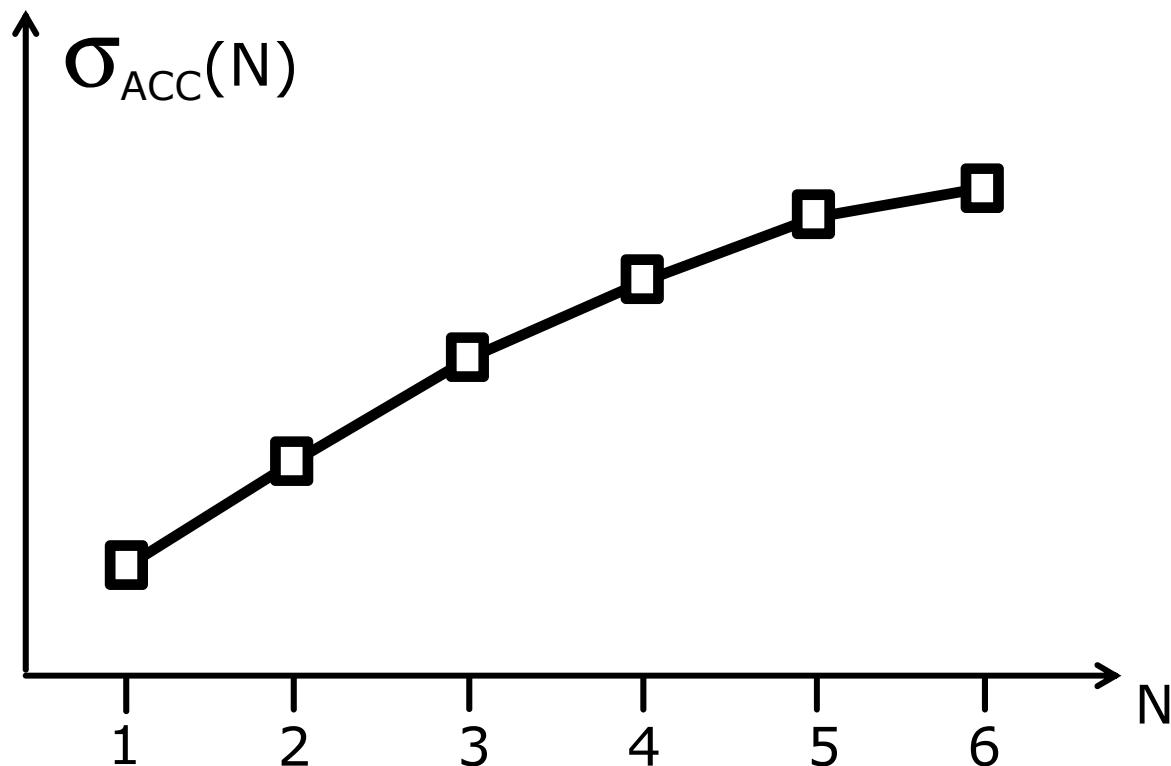
- The jitter of one edge relative to the Nth previous edge is called **Accumulated Jitter on N Cycles, $j_{\text{Acc}}(N)$**
- The Accumulated Jitter on 1 cycle is commonly called **Period Jitter, j_{PER}** (or Edge-to-Edge Jitter)

J_{ACC} : Time Domain Measurement (1/2)



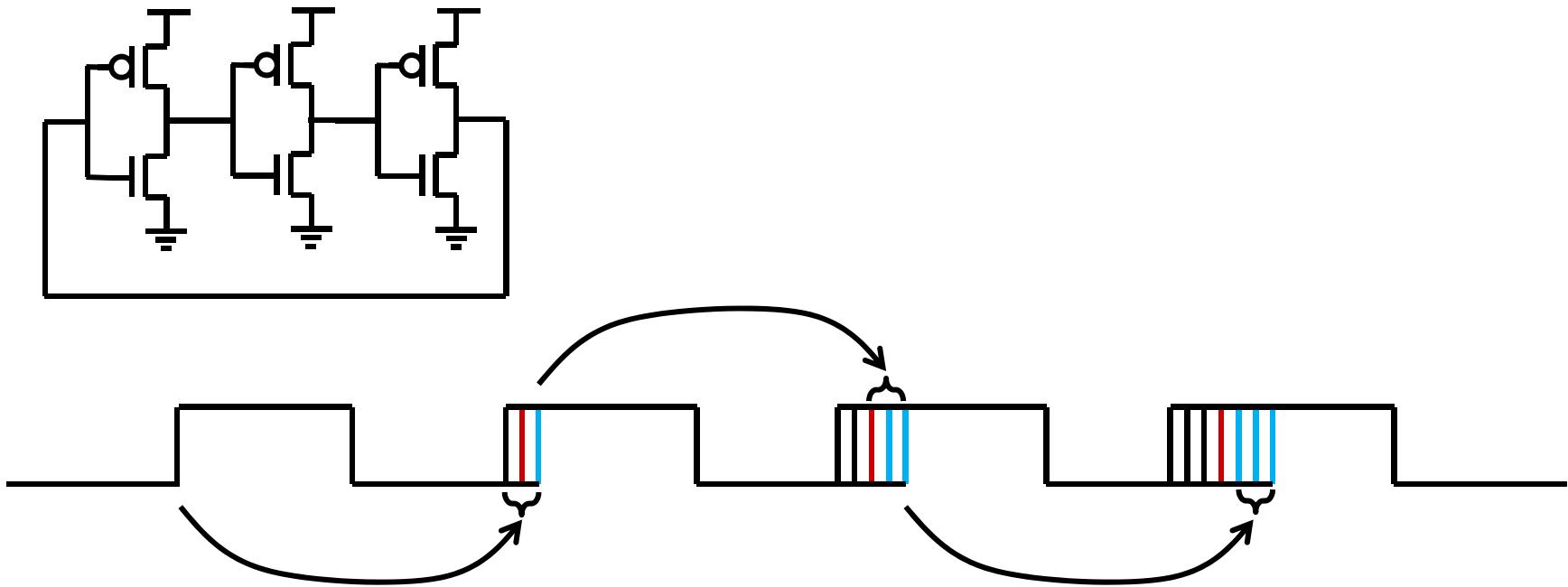
Self-referenced measurement

J_{Acc} : Time Domain Measurement (2/2)



- Function of number of cycles N
- In real physical systems J_{acc} increases for low N

J_{ACC} in Freerunning Oscillators (1/3)



- Jitter on Edge (n) = Jitter on Edge (n-1) + Period Jitter
- Noise in each new cycle is uncorrelated
- Jitter accumulates over cycles
- No mechanism can counteract the accumulation

J_{ACC} in Freerunning Oscillators (2/3)

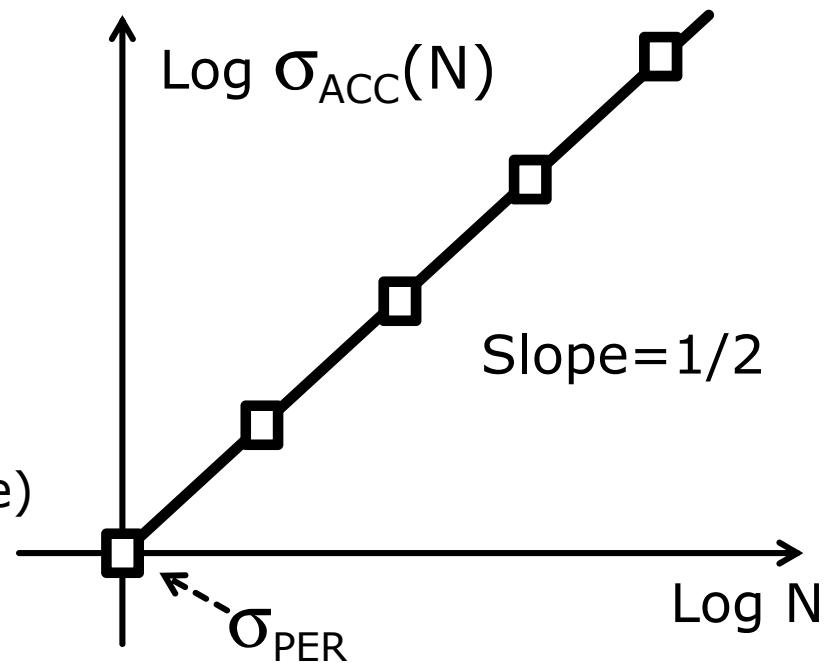
$$j_{ACC}(N) = j_{PER}(1) + j_{PER}(2) + \dots + j_{PER}(N)$$

$$\sigma_{ACC}^2(N) = \sigma_{PER}^2(1) + \sigma_{PER}^2(2) + \dots + \sigma_{PER}^2(N)$$

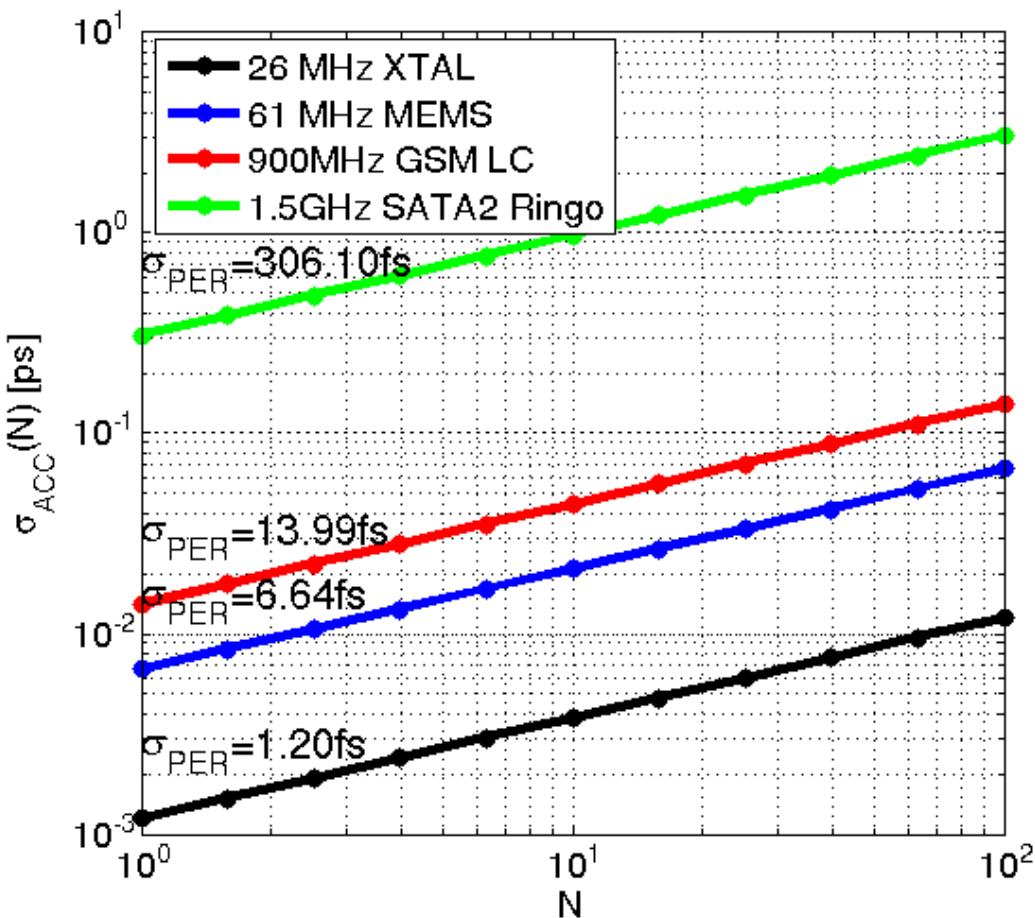
$$\sigma_{ACC}(N) = \sqrt{N} \cdot \sigma_{PER}$$

□ Assumptions

- Jitter in different cycles is uncorrelated (e.g. white noise)
- Jitter is time-independent (stationary random process)

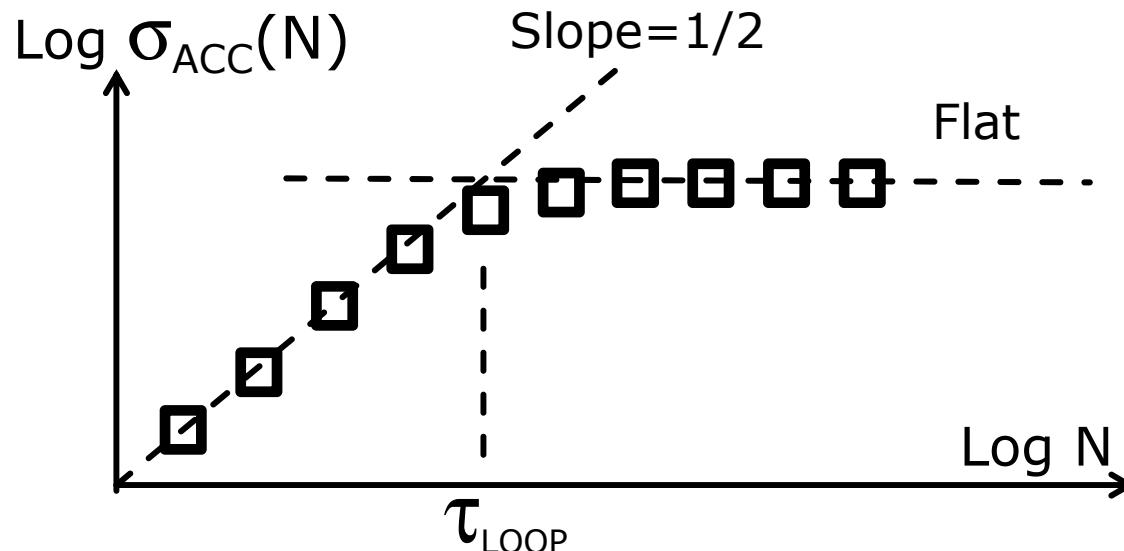
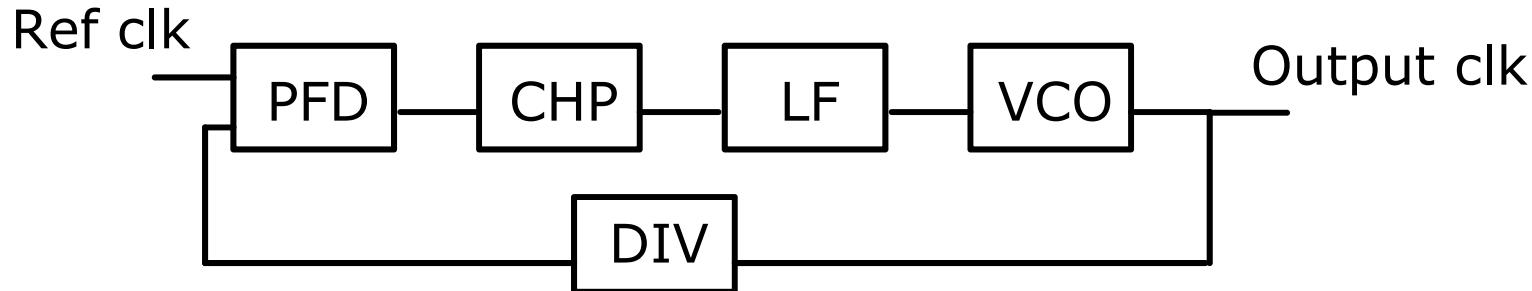


J_{ACC} in Freerunning Oscillators (3/3)



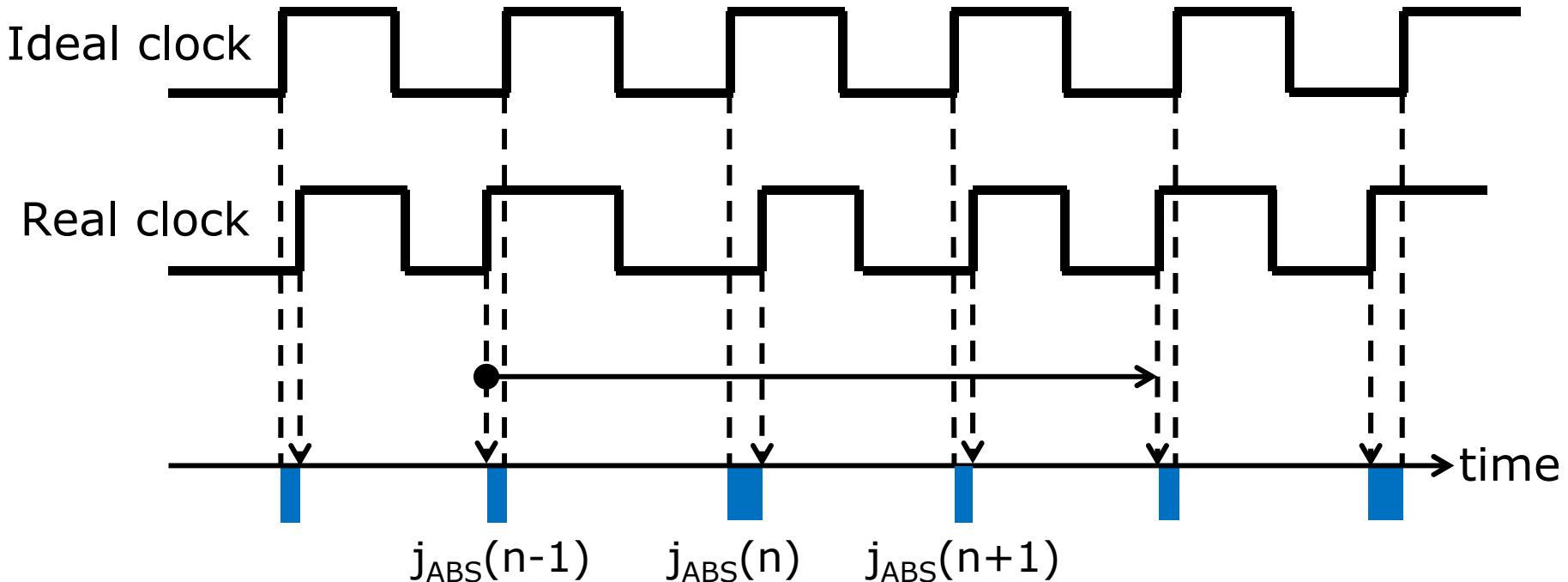
- 1.5G SATA2 RingO (5mA):
 - -115dBc/Hz @ 10e6
- 900MHz GSM LC (15mA):
 - -138dBc/Hz @ 3MHz
- 61MHz MEMS (1mA):
 - -110dBc/Hz @ 1kHz
- 26MHz XTAL (1mA):
 - -136dBc/Hz @ 1kHz
- Slope = $1/2$ for all

J_{ACC} in PLLs



- Comparison with a clean reference limits jitter accumulation

Accumulated vs Absolute Jitter



$$j_{ACC}(N) = j_{ABS}(n+N) - j_{ABS}(n)$$

$$j_{PER} = j_{ABS}(n+1) - j_{ABS}(n)$$

Phase Noise to j_{ACC}

$$j_{ACC}(N) = j_{ABS}(n + N) - j_{ABS}(n) \longrightarrow \boxed{\sigma_{ACC}^2(N \gg 1) = 2 \sigma_{ABS}^2}$$

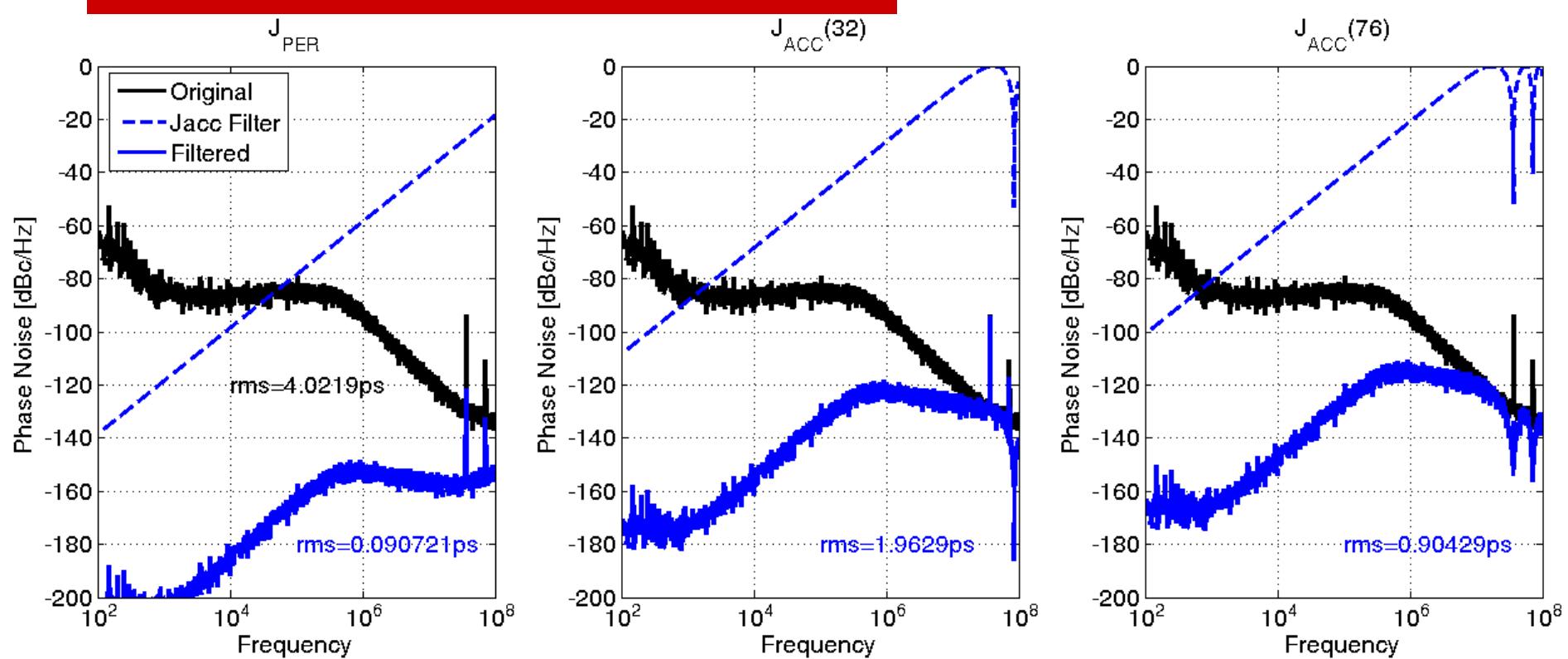
↓ PSD

$$S_{jACC(N)}(f) = \left| 1 - e^{-i2\pi f N / f_0} \right|^2 \cdot S_{jABS}(f) = \frac{4}{\omega_0^2} \sin^2 \left(\frac{\pi f N}{f_0} \right) L(f)$$

↓ Wiener-Khinchin Theorem

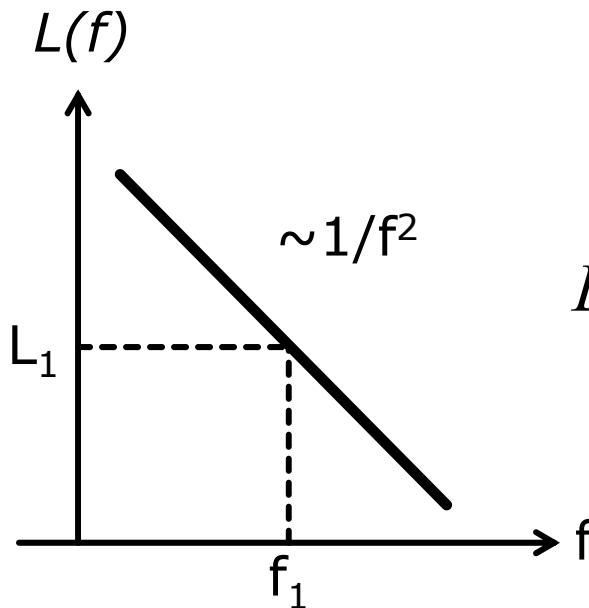
$$\sigma_{ACC(N)}^2 = \frac{8}{\omega_0^2} \int_{f_{MIN}}^{f_0/2} \sin^2 \left(\frac{\pi f N}{f_0} \right) L(f) df$$

Phase Noise to J_{ACC} : Example



- PLL: $F_{\text{REF}}=36\text{MHz}$, $F_{\text{OUT}}=2736\text{MHz}$, DIV=76
- J_{PER} determined by high frequency components
- $J_{\text{ACC}}(N)$ determined by increasingly lower frequency components for increasing N
- $J_{\text{ACC}}(N)$ can mask spurious tones

Phase Noise to J_{ACC} : Freerunning Oscillator



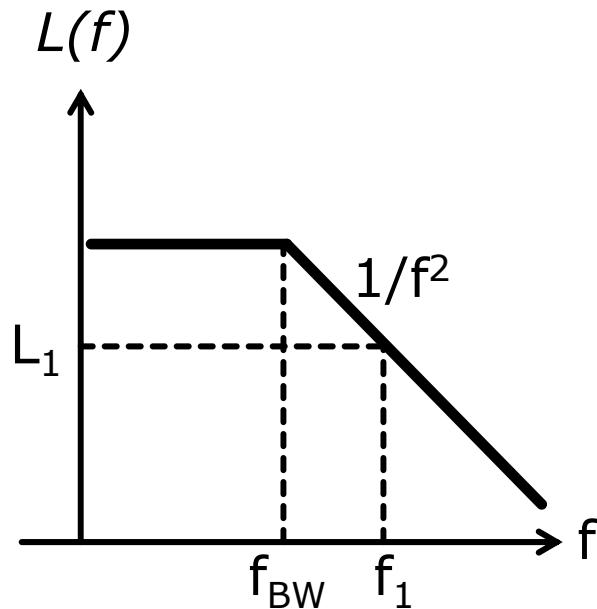
$$L(f) = L_1 \left(\frac{f_1}{f} \right)^2$$

$$\sigma_{ACC(N)}^2 = \frac{L_1 f_1^2}{f_0^3} N$$

$$\boxed{\sigma_{PER} = \sqrt{\frac{L_1 f_1^2}{f_0^3}}}$$

- RMS J_{ACC} increases like \sqrt{N}

Phase Noise to J_{ACC} : PLL



$$L(f) = \frac{L_1 f_1^2}{f_{BW}^2 + f^2}$$

$$\sigma_{ACC(N)}^2 = \frac{L_1 f_1^2}{f_0^3} \frac{f_0}{2\pi f_{BW}} \left(1 - e^{-2\pi f_{BW} N / f_0}\right)$$

Phase Noise to J_{ACC} : PLL

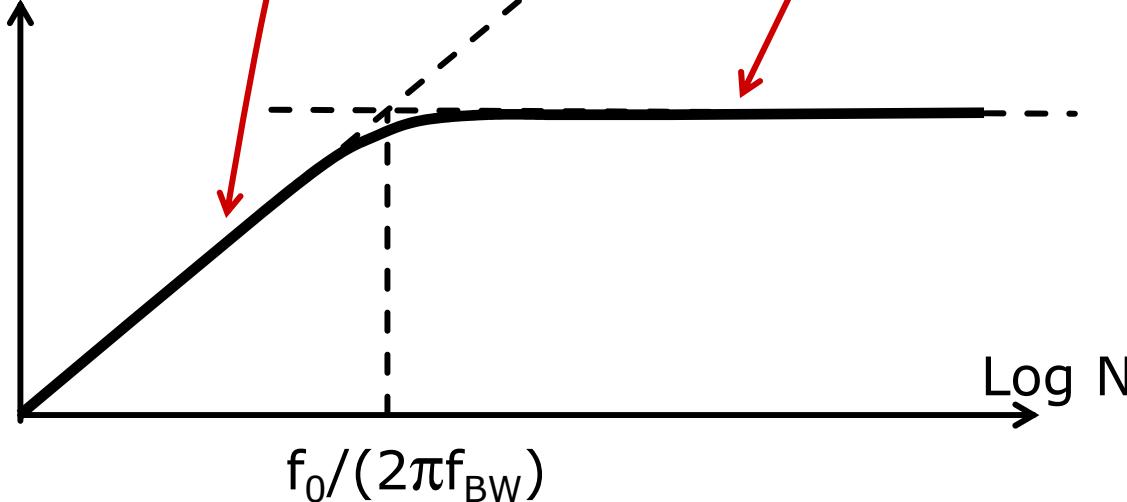
□ For small N:

$$\sigma_{ACC(N)}^2 = \frac{L_1 f_1^2}{f_0^3} N = \sigma_{PER}^2 \cdot N$$

□ For large N:

$$\sigma_{ACC(N)}^2 = \sigma_{PER}^2 \frac{f_0}{2\pi f_{BW}}$$

Log $\sigma_{ACC}(N)$



Summary so far

- Self-Referenced jitter (accumulated, period)
- Application to digital clocking
- Measurement in time domain
- Accumulated jitter for freerunning oscillators and PLLs
- Relation to absolute jitter
- How to compute J_{ACC} from Phase Noise

What's next:

- Analyze the statistical properties of Jitter

Synoptics

Measurement
Procedure

Jitter Type

Data Post
Processing

Time Domain
Ideal Clock

Absolute jitter

Frequency Domain
Ideal Clock

Phase Noise

Time Domain
Self-Referenced

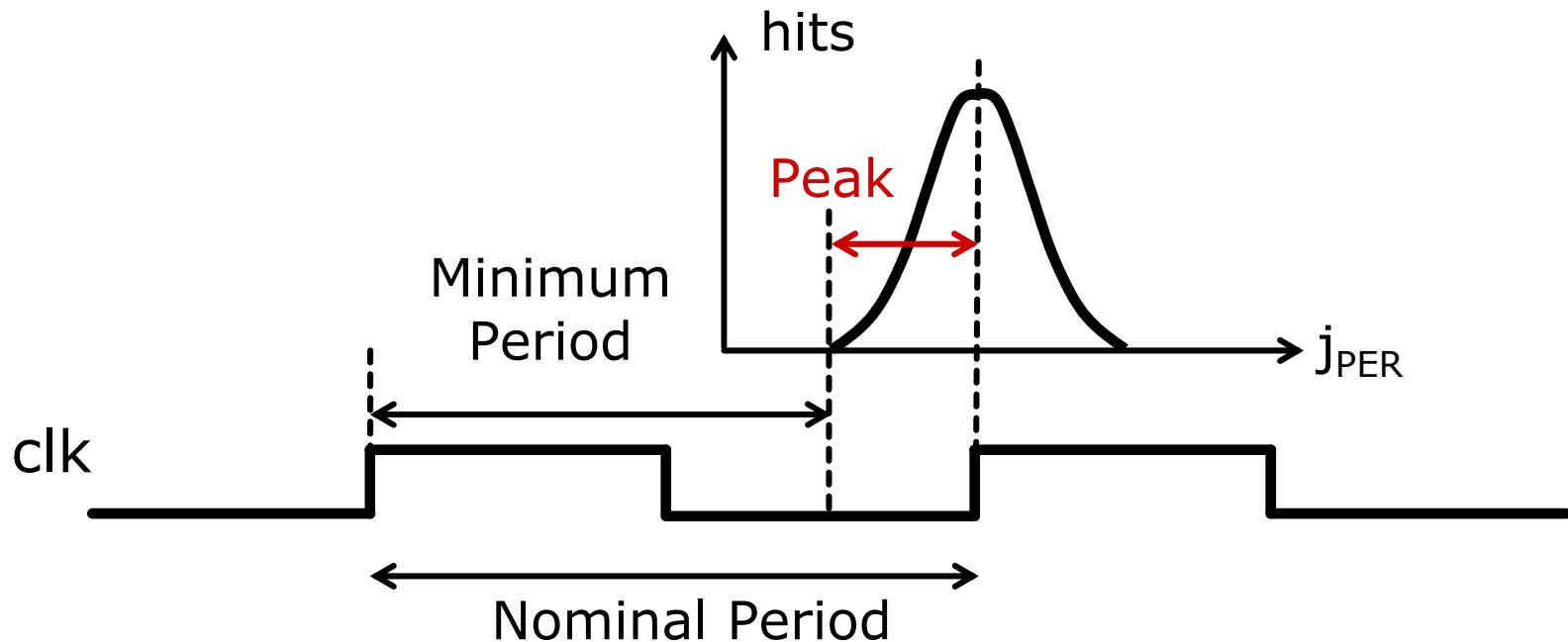
Accumulated Jitter

Period Jitter

RMS

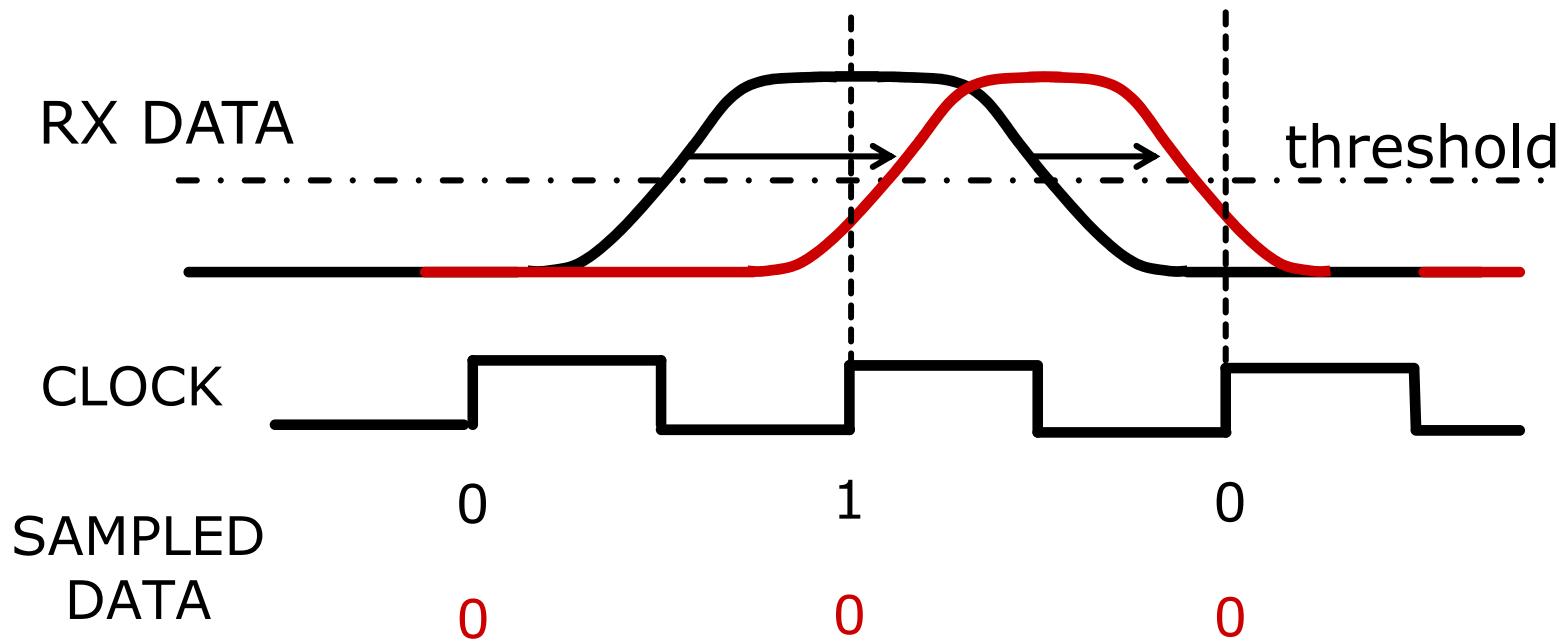
How far can we go with the RMS value?

Digital time constraining



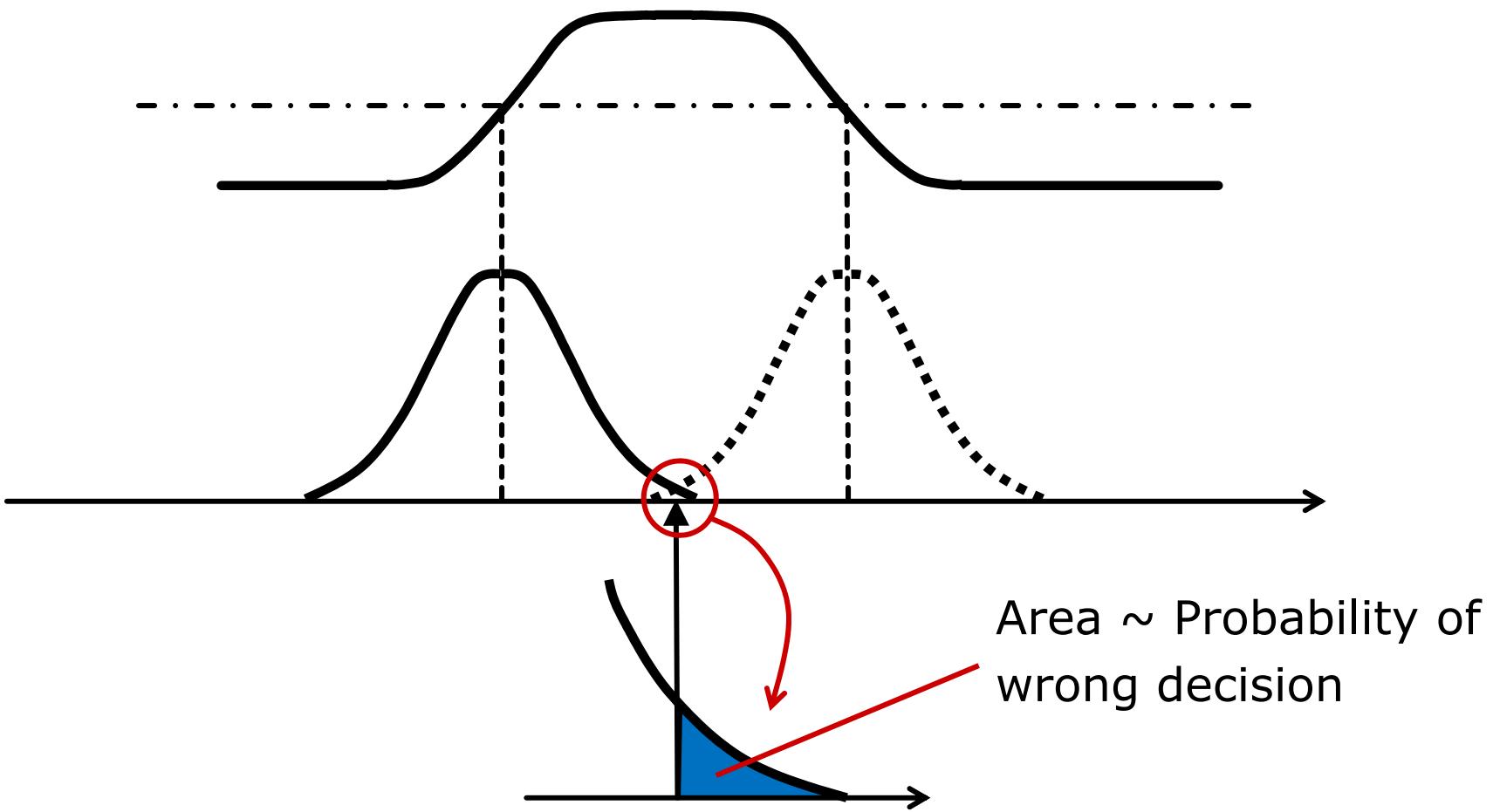
- Digital needs to satisfy setup-time for the digital block
 - Looking for worst case minimum clock period
 - The correct metrics is the peak, not the RMS!
-

High Speed Serial Data Sampling (1/2)



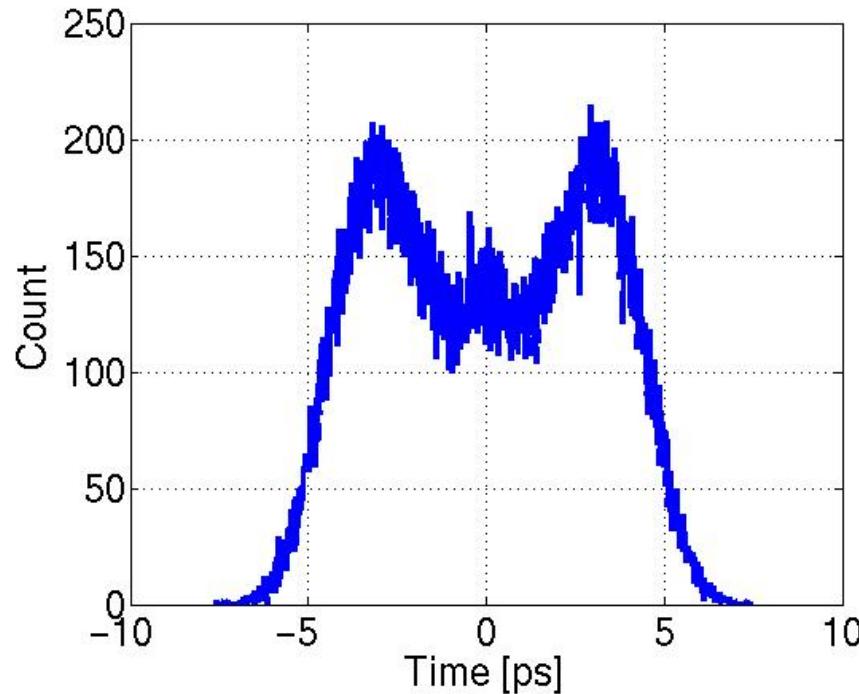
- Standards require Bit Error Rates $\sim 1e-12$
- Jitter on RX data moves data transitions wrt sampling point
- If jitter on data edges is larger than 0.5 UI errors will occur

High Speed Serial Data Sampling (2/2)



- BER determined by tails of the jitter distribution

Jitter Histogram and Distribution

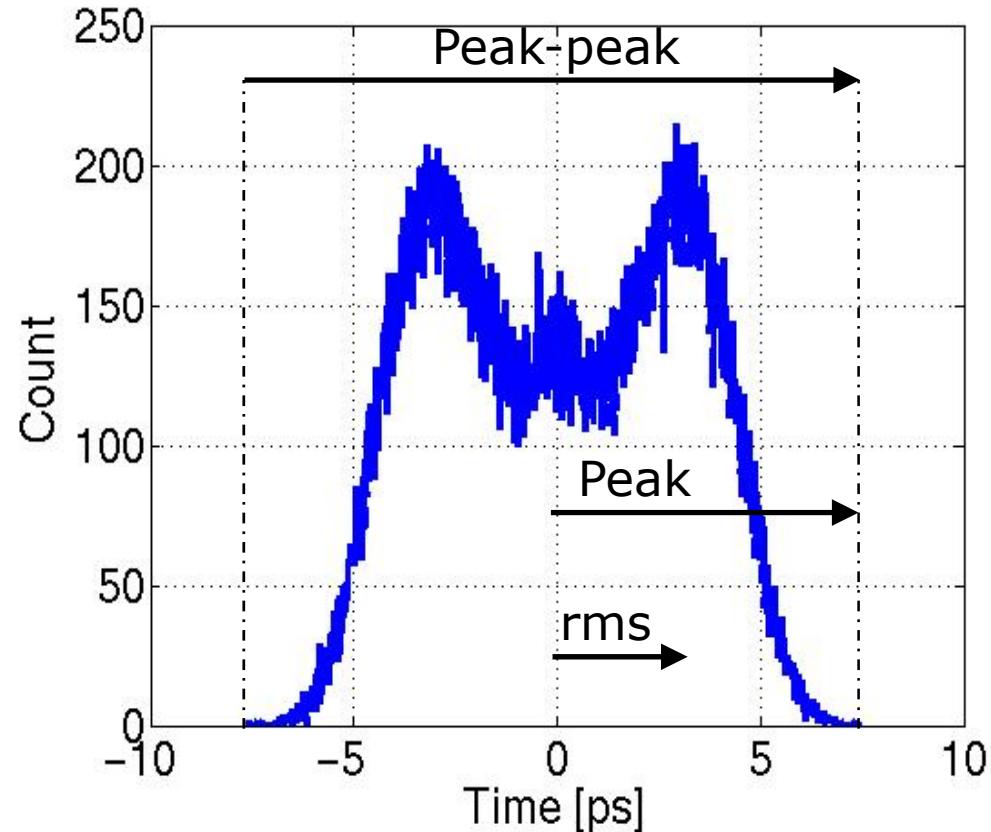


- Histogram is bounded (finite number of hits)
 - Not necessarily gaussian
 - Underlying jitter physical process might be unbounded
-

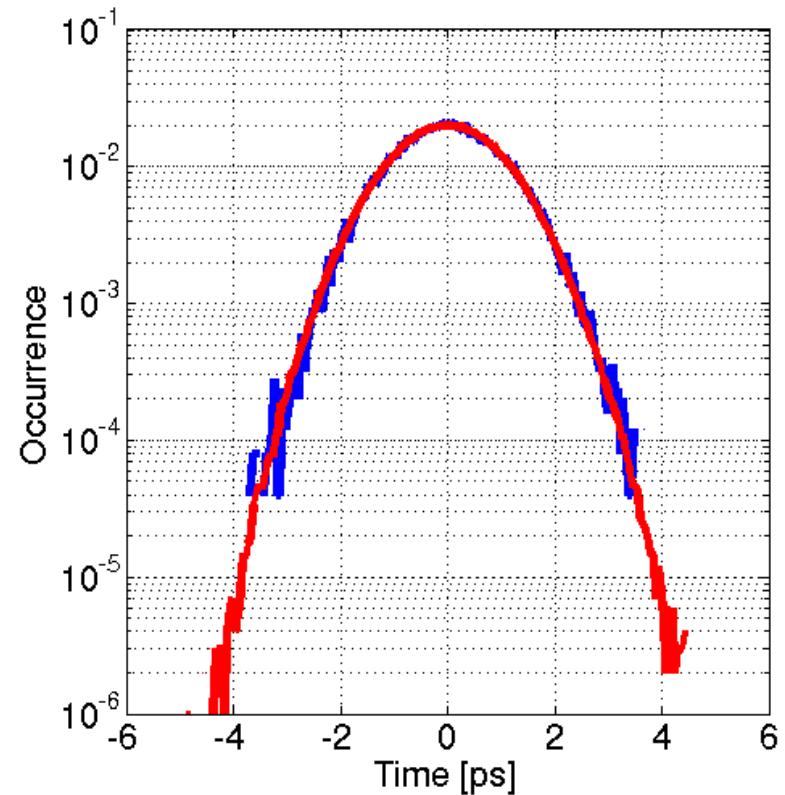
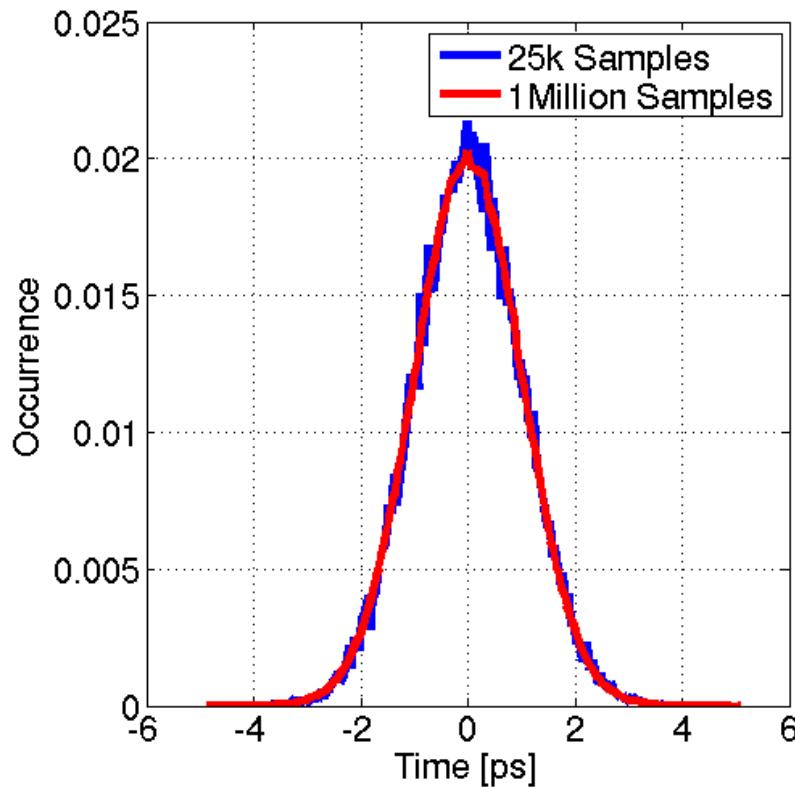
Jitter statistics

- Out of the jitter distribution several different statistical values can be calculated

- Most used
 - rms, 1-sigma
 - peak
 - peak-peak
 - 3-sigma := $3 \times \sigma$



The peak for unbounded jitter (1/4)



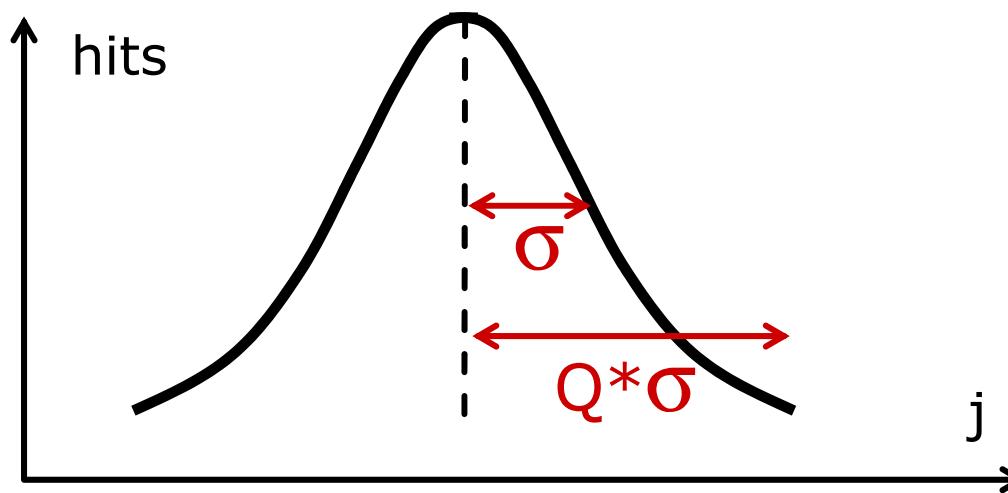
- In real circuits the thermal noise sources are gaussian
- Jitter distributions are therefore unbounded
- The peak-peak in the histogram depends on the number of hits

The peak for unbounded jitter (2/4)

- Calculate the “max-min” from the histogram
 - easy
 - result depends on number of hits
 - not very reliable, not insightful

- Calculate the rms and multiply it by a number Q
 - easy
 - result does not depend on number of hits
 - applicable only to distributions which are close to gaussian

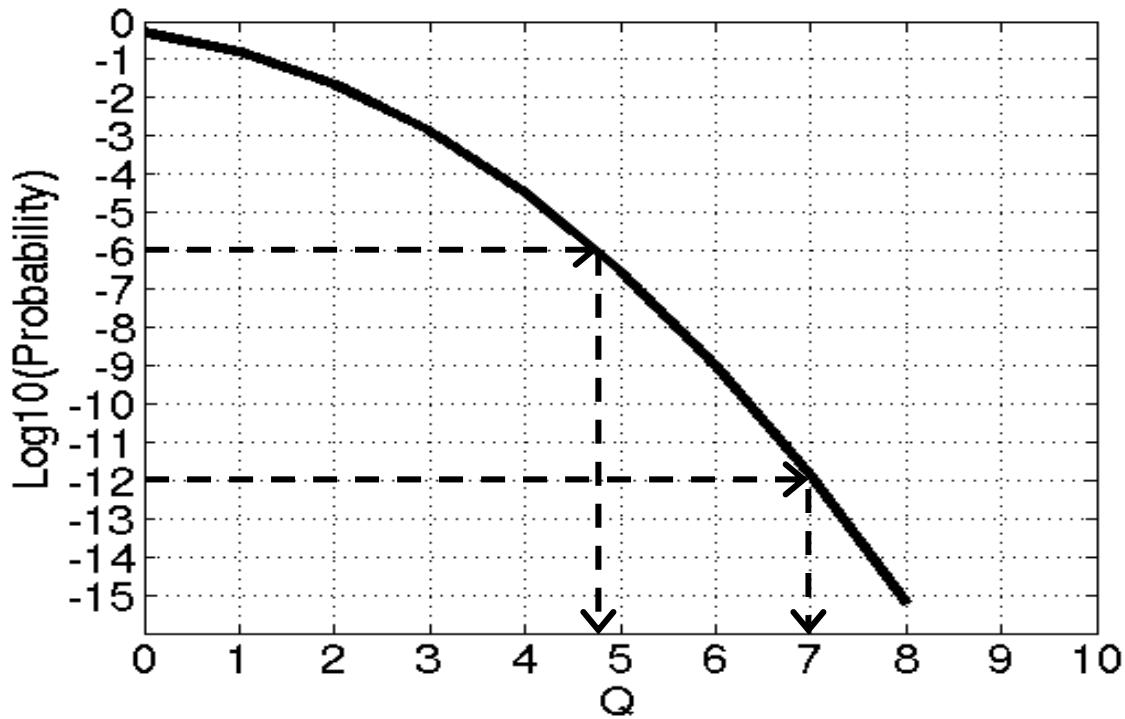
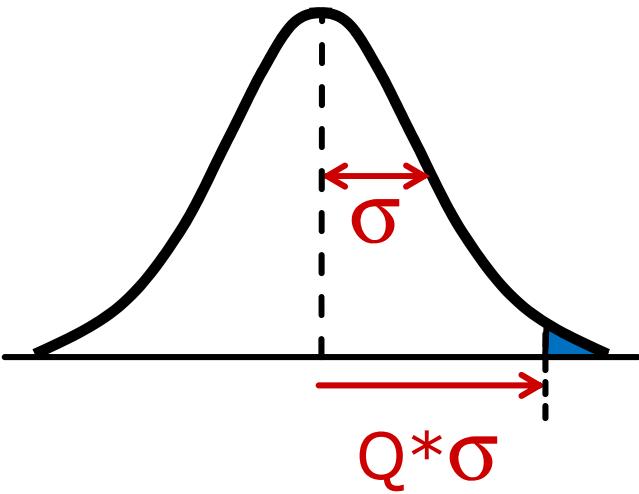
The peak for unbounded jitter (3/4)



$$\text{Peak} := Q^* \sigma, \quad \text{Peak-peak} := 2 * Q^* \sigma$$

- The higher the Q , the lower the probability that a jitter event is beyond the peak or peak-peak (error event)
- Can be applied to any distributions, BUT
- Probability of error easy to know only for gaussian distributions

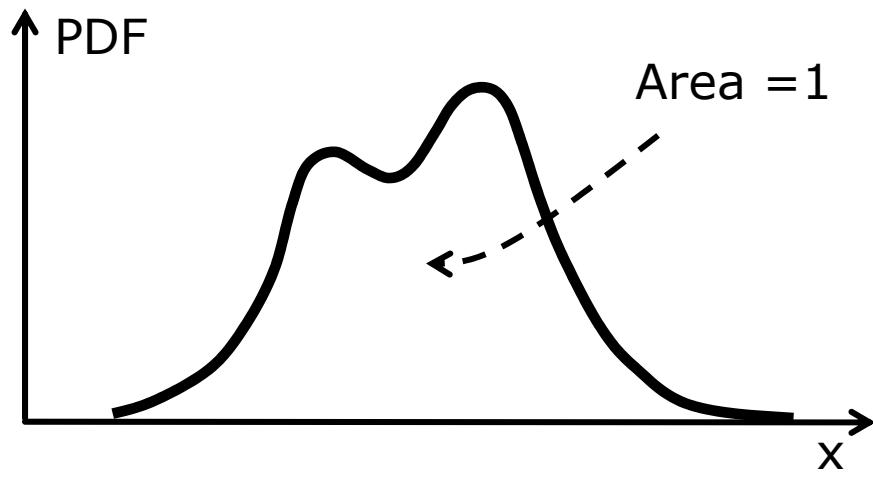
The peak for unbounded jitter (4/4)



- Prob. of jitter event outside of specified peak depends on Q
- For gaussian jitter distributions easy to compute:
 - Prob $< 1e-3 \Rightarrow Q=3.1$
 - Prob $< 1e-6 \Rightarrow Q=4.8$
 - Prob $< 1e-12 \Rightarrow Q=7.0$

$$\int_{Q\sigma}^{+\infty} \frac{1}{\sqrt{2\pi}\sigma} e^{-\frac{x^2}{2\sigma^2}} dx = \frac{1}{2} \operatorname{erfc}\left(\frac{Q}{\sqrt{2}}\right)$$

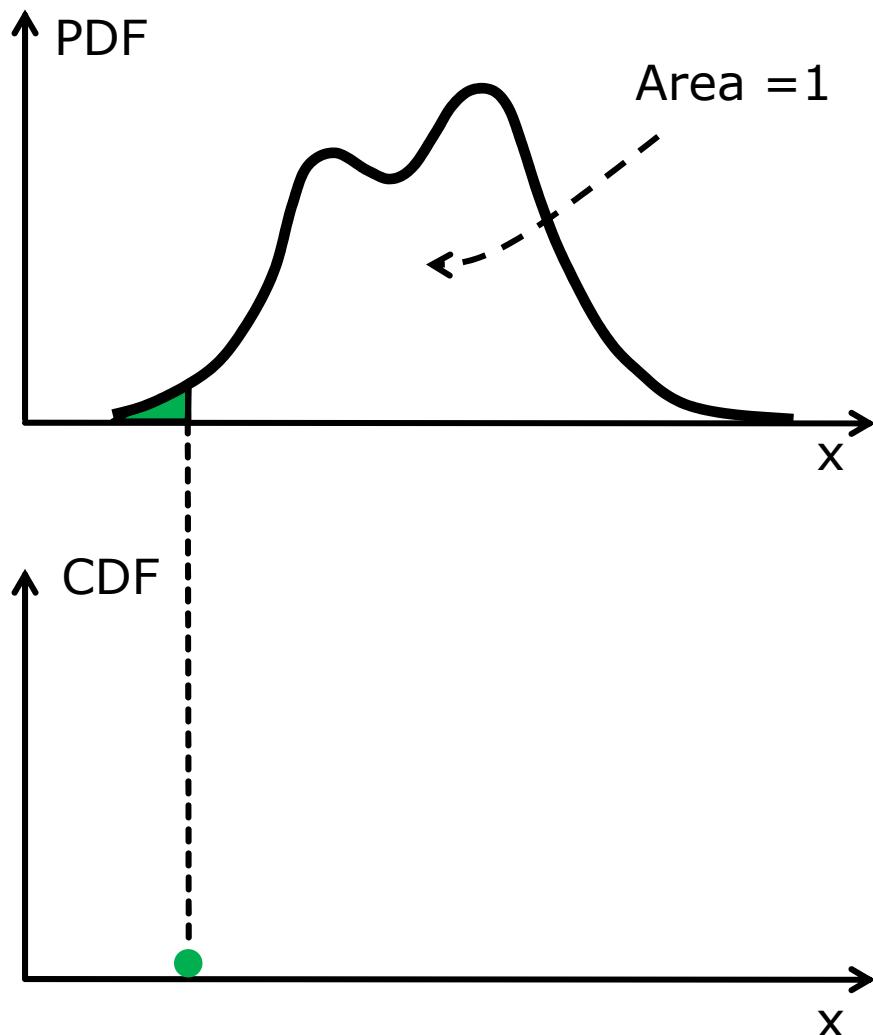
PDF and CDF



- Random Variable "RV"
- Histogram of RV normalized to Area=1 is the **Probability Density Function (PDF)**
- The integral from $-\infty$ to x of the PDF is the **Cumulative Distribution Function (CDF)**
- $\text{CDF}(x) = \text{Prob}[\text{RV} < x]$

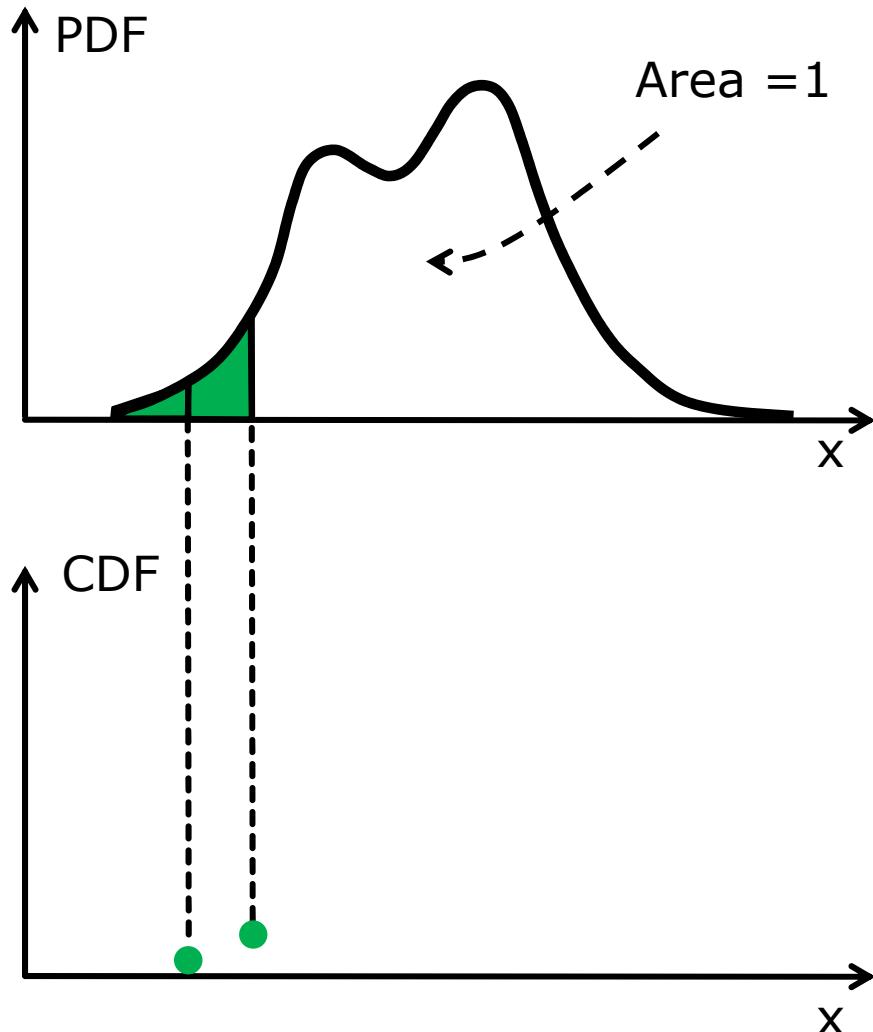


PDF and CDF



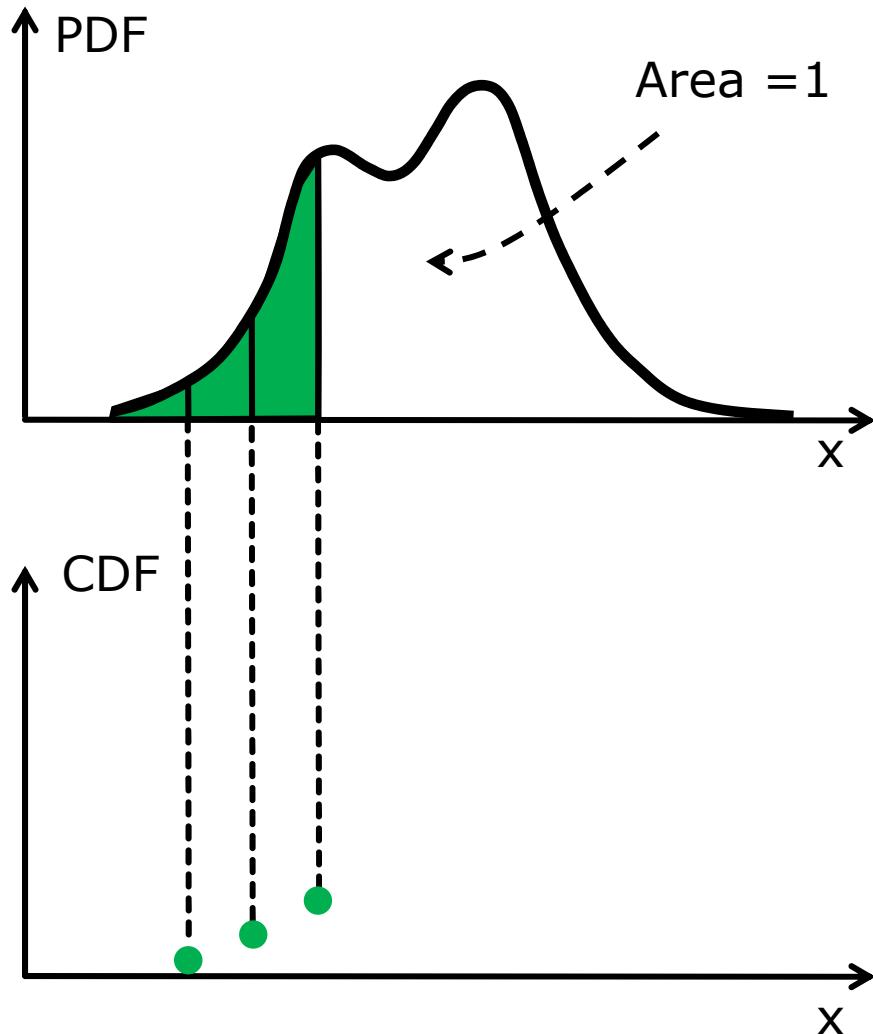
- Random Variable "RV"
- Histogram of RV normalized to Area=1 is the **Probability Density Function (PDF)**
- The integral from $-\infty$ to x of the PDF is the **Cumulative Distribution Function (CDF)**
- $\text{CDF}(x) = \text{Prob}[\text{RV} < x]$

PDF and CDF



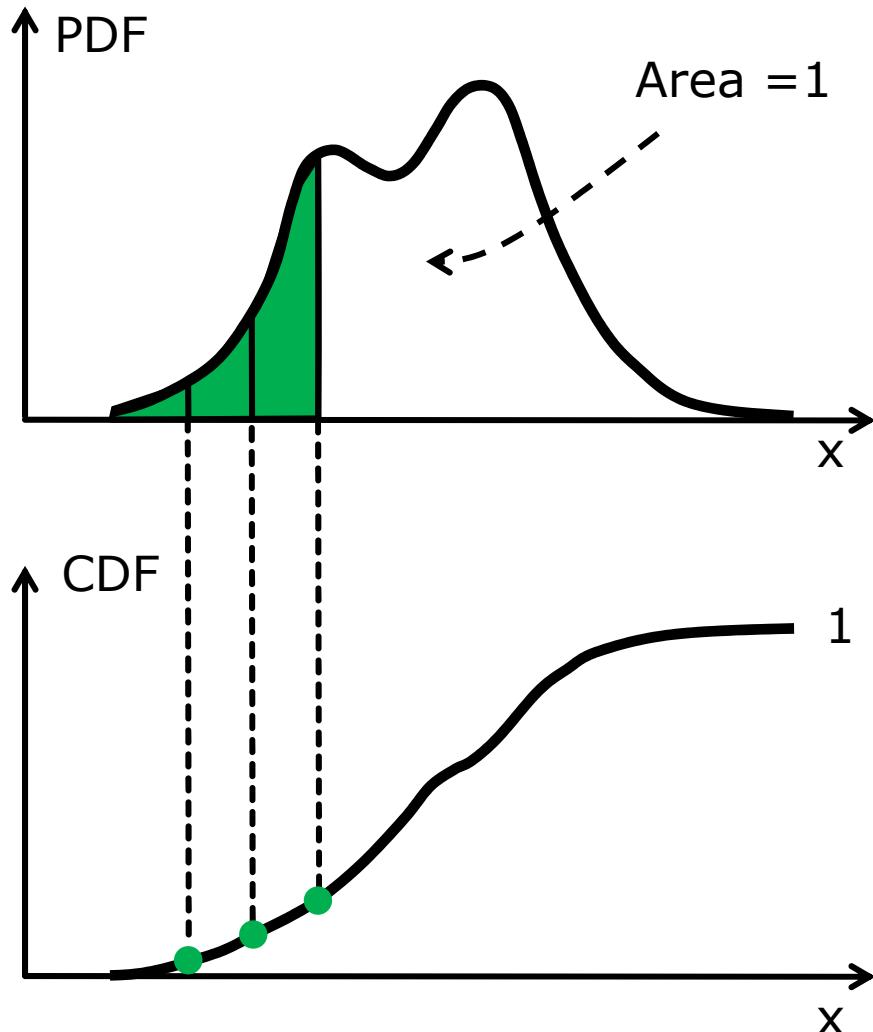
- Random Variable "RV"
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- $\text{CDF}(x) = \text{Prob}[\text{RV} < x]$

PDF and CDF



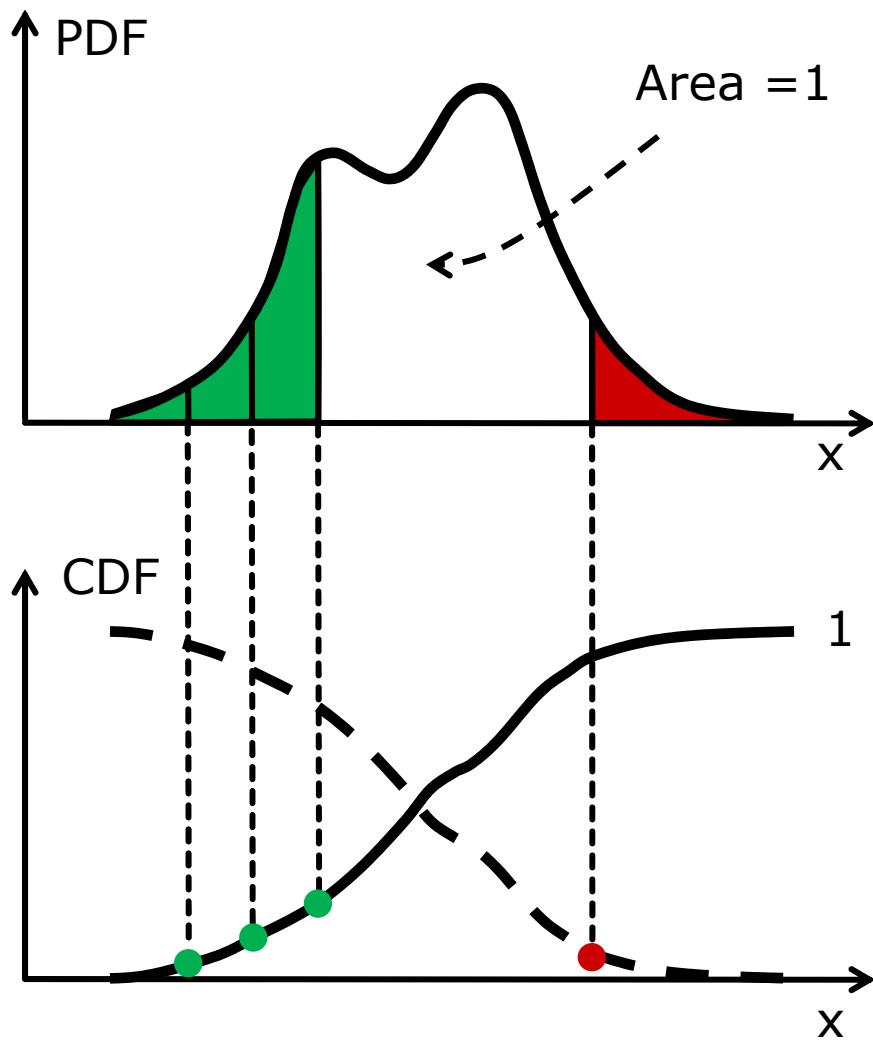
- Random Variable "RV"
- Histogram of RV normalized to Area=1 is the **Probability Density Function (PDF)**
- The integral from $-\infty$ to x of the PDF is the **Cumulative Distribution Function (CDF)**
- $\text{CDF}(x) = \text{Prob}[\text{RV} < x]$

PDF and CDF



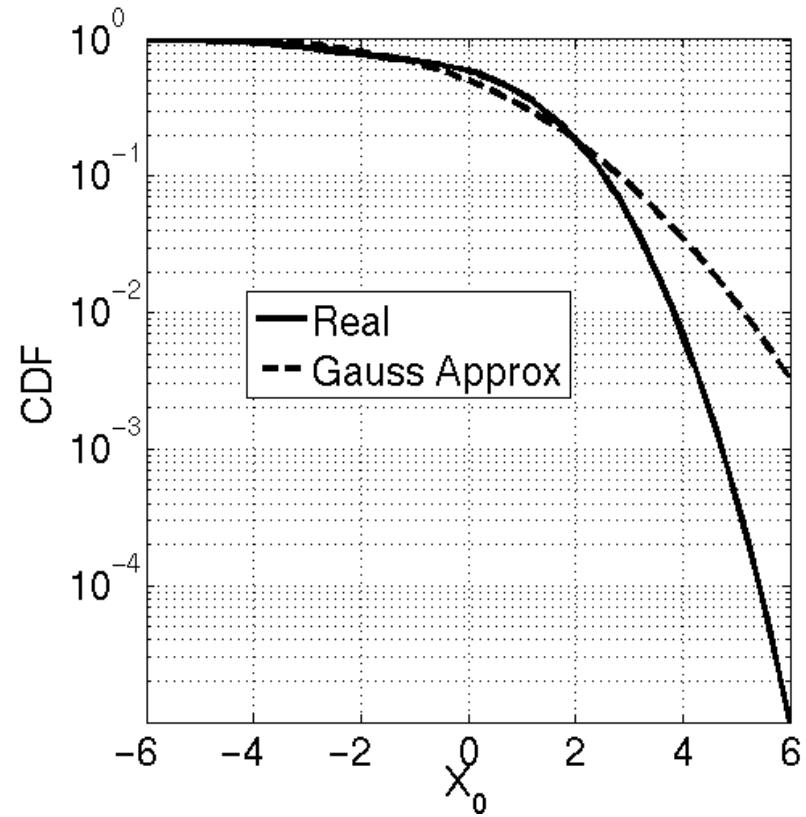
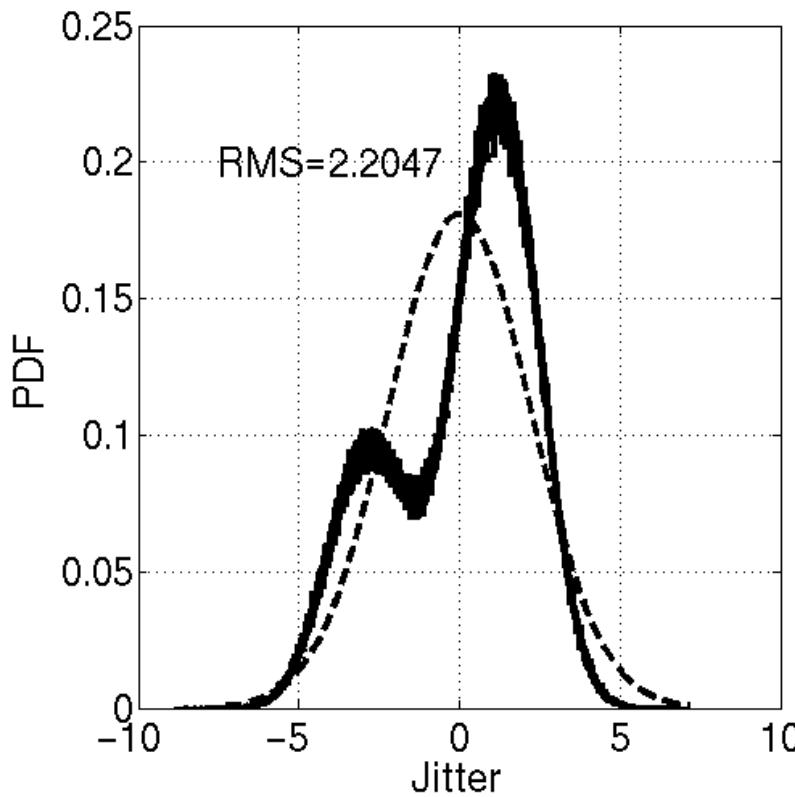
- Random Variable "RV"
- Histogram of RV normalized to Area=1 is the **Probability Density Function (PDF)**
- The integral from $-\infty$ to x of the PDF is the **Cumulative Distribution Function (CDF)**
- $\text{CDF}(x) = \text{Prob}[\text{RV} < x]$

PDF and CDF



- Random Variable "RV"
- Histogram of RV normalized to Area=1 is the **Probability Density Function (PDF)**
- The integral from $-\infty$ to x of the PDF is the **Cumulative Distribution Function (CDF)**
- $\text{CDF}(x) = \text{Prob}[\text{RV} < x]$
- $\text{CDF}'(x) = \text{Prob}[\text{RV} > x]$

What if jitter is not gaussian?



- Q^{*}σ approach for non-gaussian distributions leads to wrong estimation of error probability

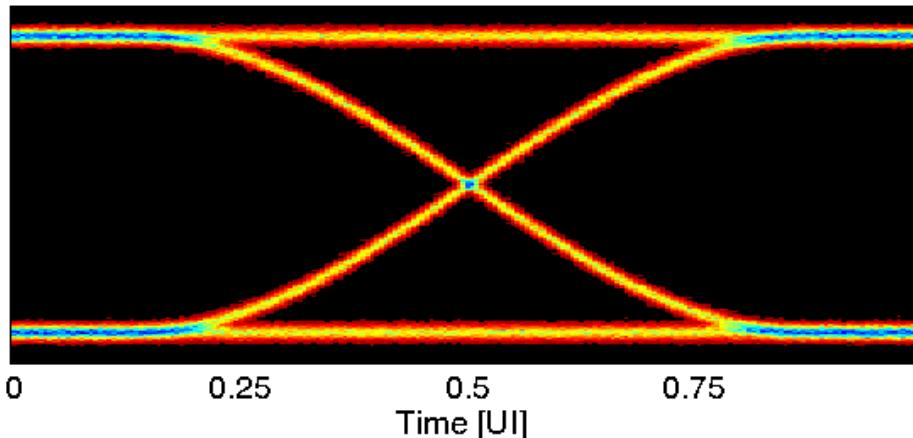
Summary so far

- Lots of important applications are not affected by the RMS value of Jitter
- “Tail” behavior of jitter might be more important
- Statistical properties of gaussian jitter distributions
- Multiplying the rms jitter by factor Q leads to wrong results if jitter is not gaussian

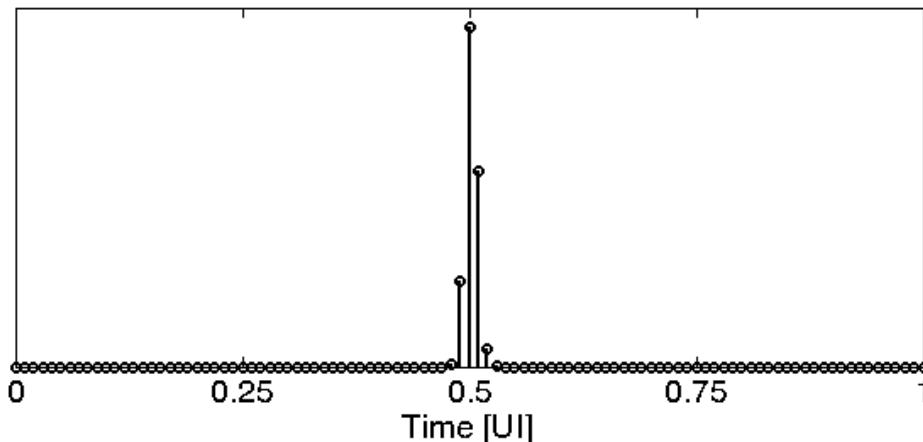
What's next:

- Develop a method to characterize jitter distributions which are not gaussian

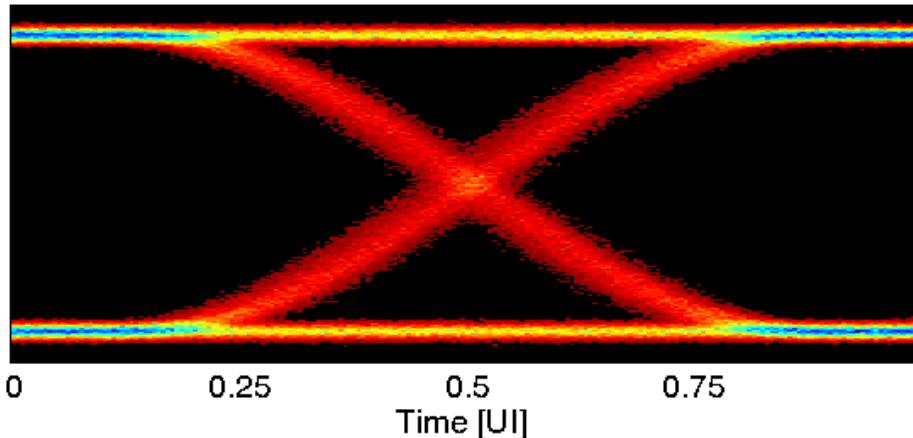
Ideal Eye Diagram



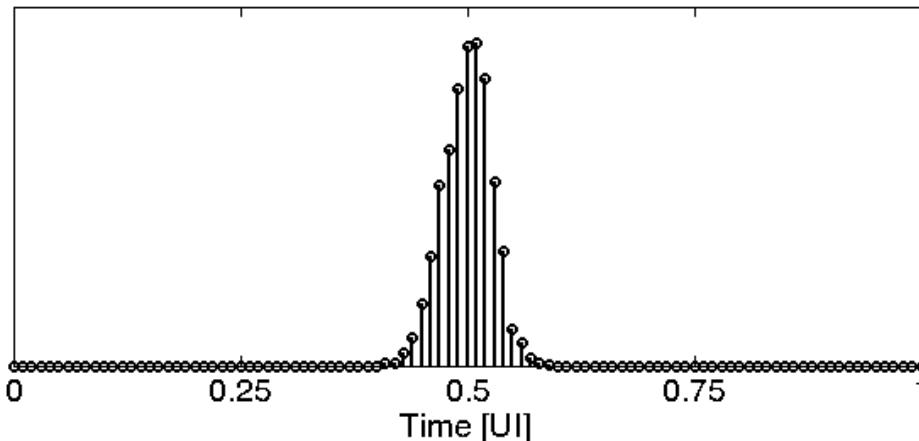
- Sharp Transition
- Histogram shows one peak



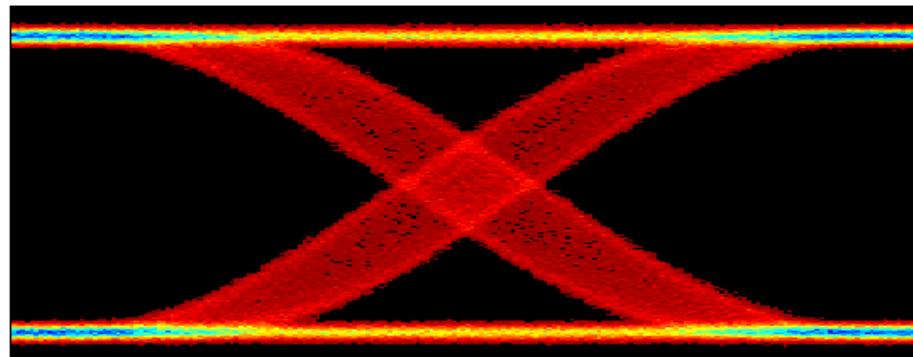
Eye Diagram: Random Jitter (RJ)



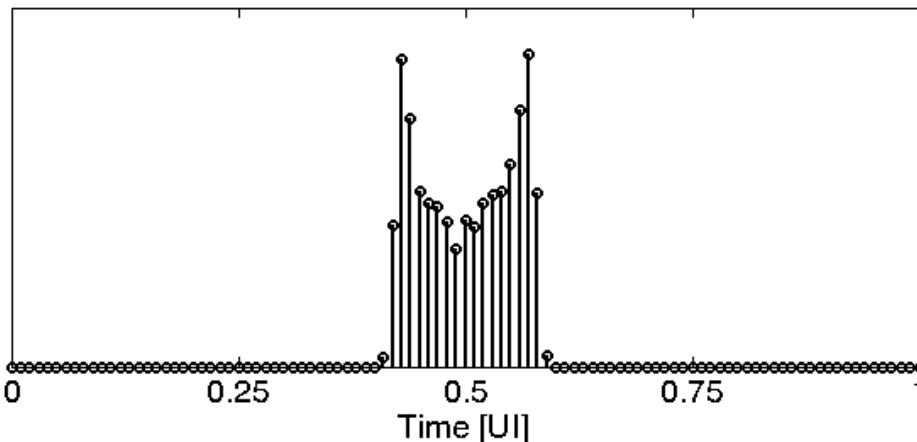
- Transitions are blurred
- Histogram shows “gaussian” distribution
- Due to:
 - Device thermal noise
 - Device flicker noise
 - Composite effect of many uncorrelated noise sources



Eye Diagram: Periodic Jitter (PJ,SJ)



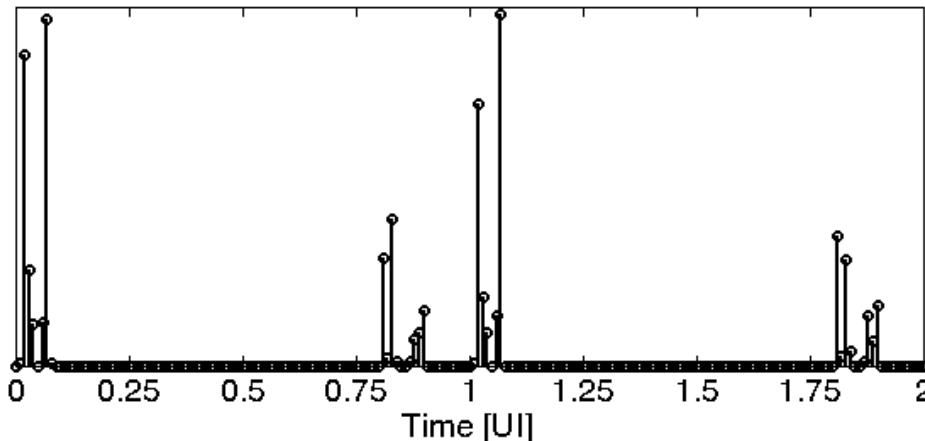
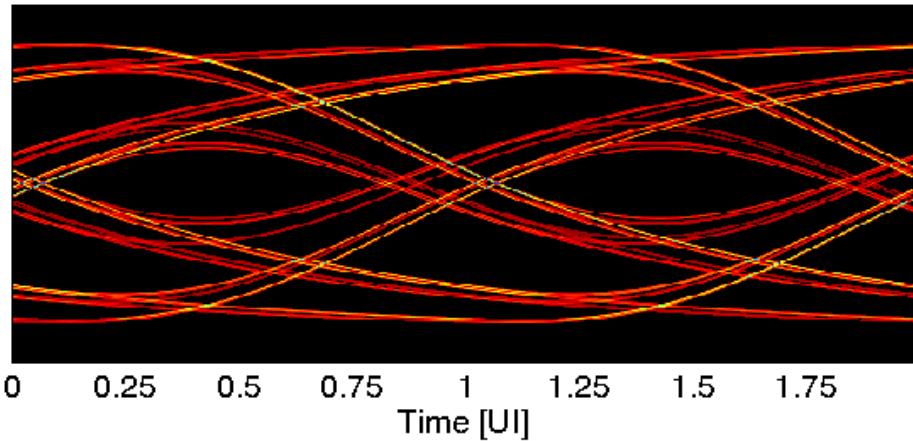
0 0.25 0.5 0.75
Time [UI]



0 0.25 0.5 0.75 1
Time [UI]

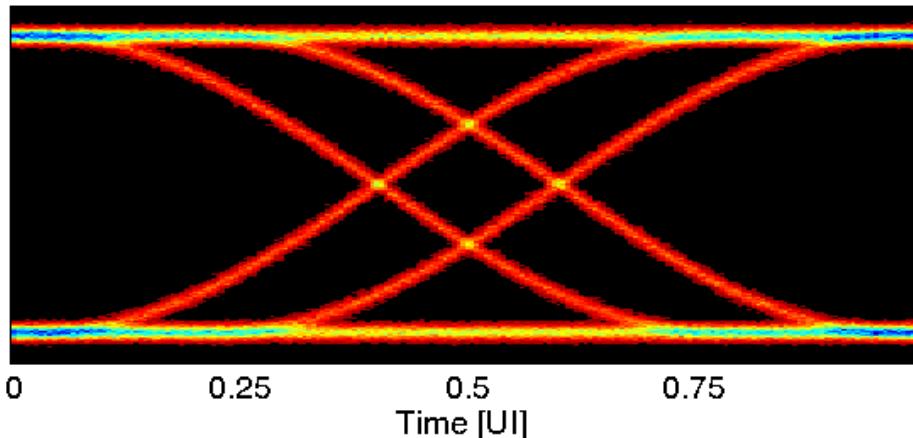
- Transitions are spread
- Histogram shows bounded distribution
- Figure shows example for case of sinusoidal jitter
- Due to:
 - Power supply noise
 - Strong local RF carrier
 - Spurious tones in PLL

Eye Diagram: Data-Dep. Jitter (DDJ, ISI)

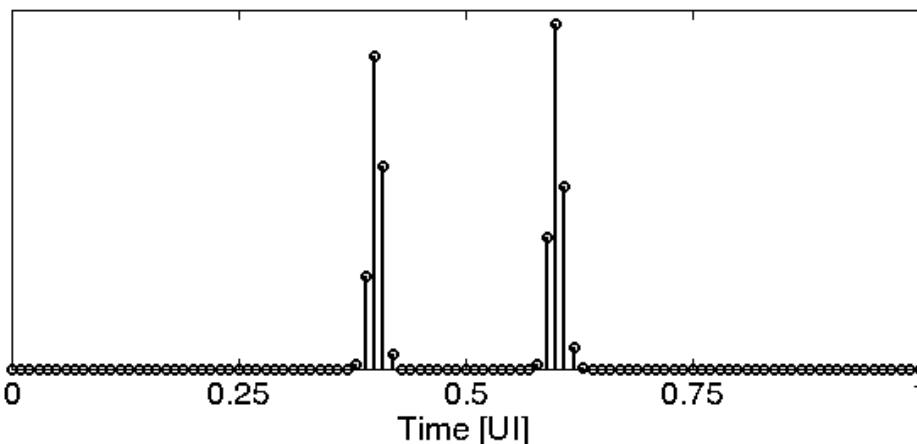


- Transitions are “concentrated” in some “hot Spots”
- Histogram shows discrete peaks
- Due to:
 - Channel or TX bandwidth limitation (waveform does not reach full scale level unless there are several bits in a row with same polarity)

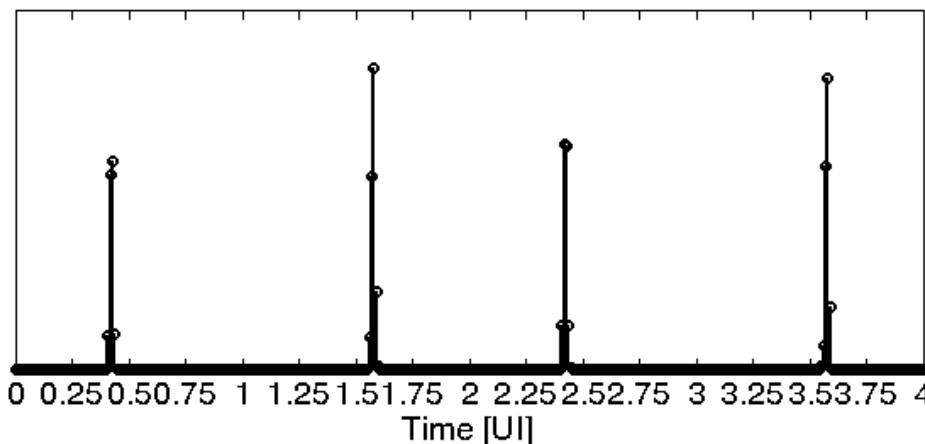
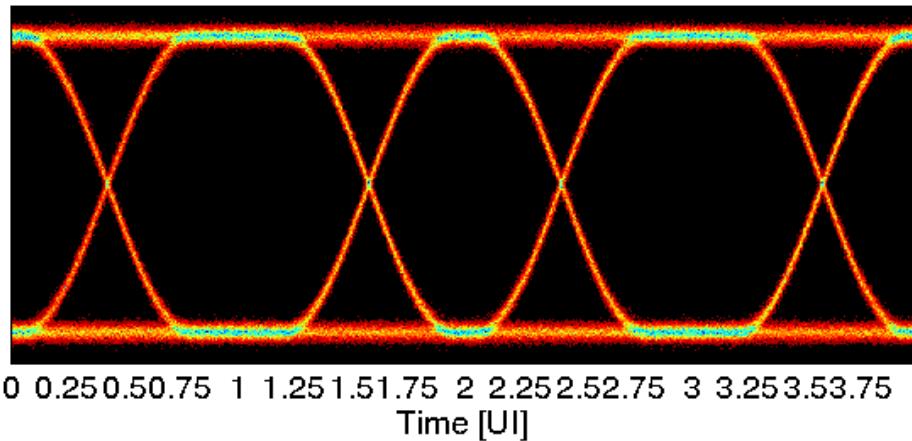
Eye Diagram: Duty Cycle Distortion (DCD)



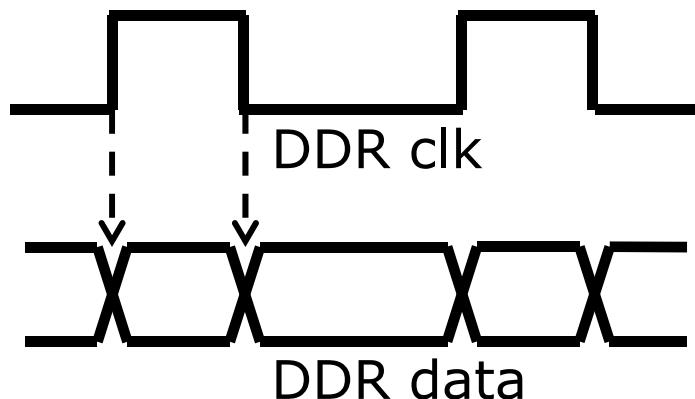
- Transitions are concentrated in two hot spots
- Histogram shows two equally large peaks
- Due to:
 - Duty Cycle Distortion (e.g. in DDR systems)



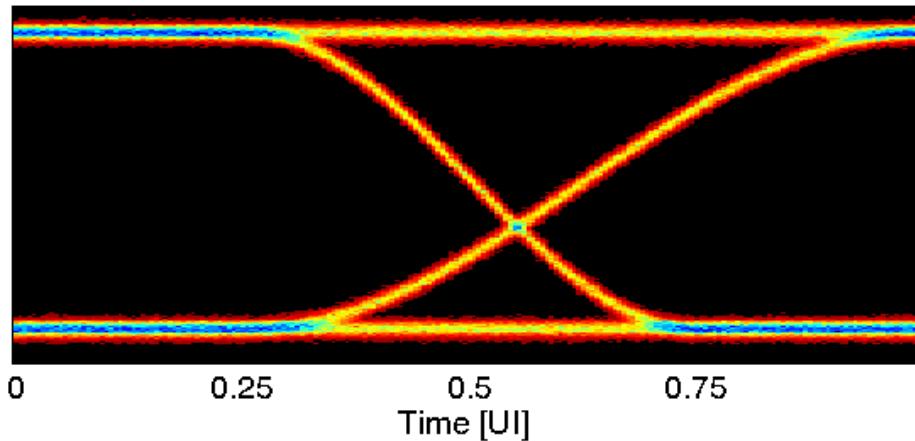
Eye Diagram: Duty Cycle Distortion (DCD)



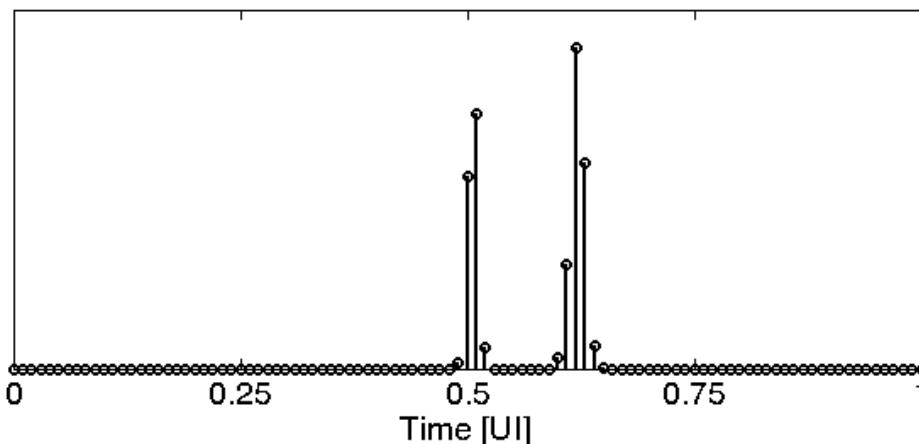
- DCD is evident when the eye is unfolded over more UIs
- Typical in DDR systems



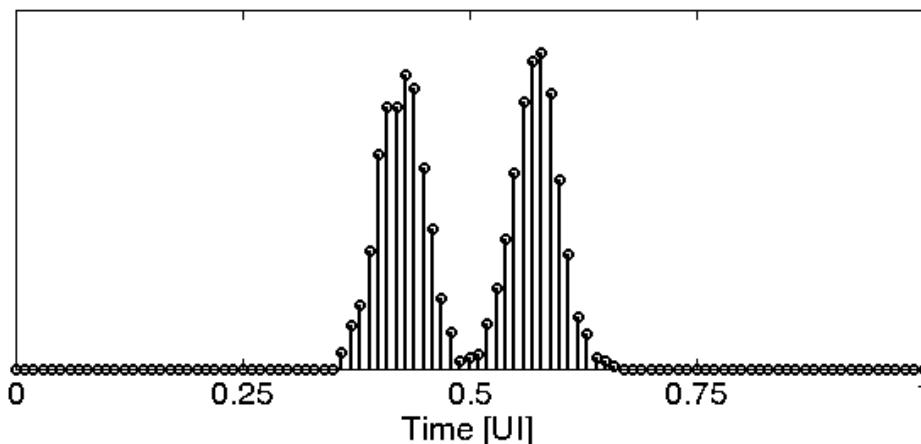
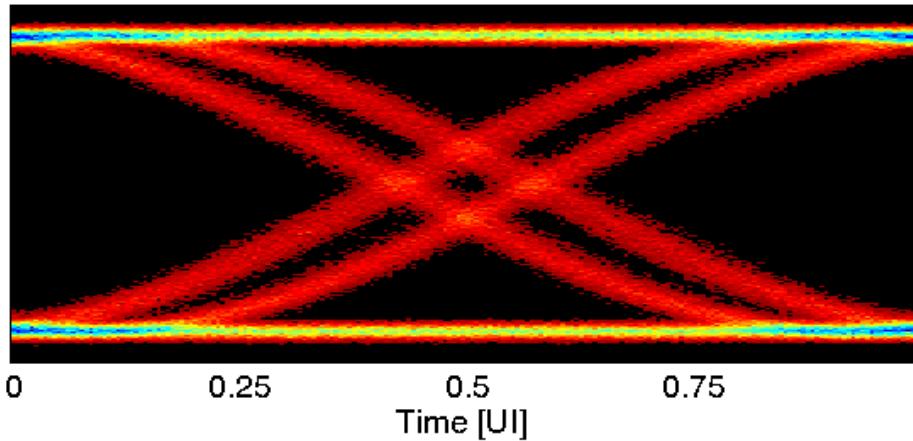
Eye Diagram: Rise/Fall Time Asymm.



- Similar Histogram as for DCD
- Due to:
 - Rise and Fall Time Asymmetry
 - RX threshold not centered

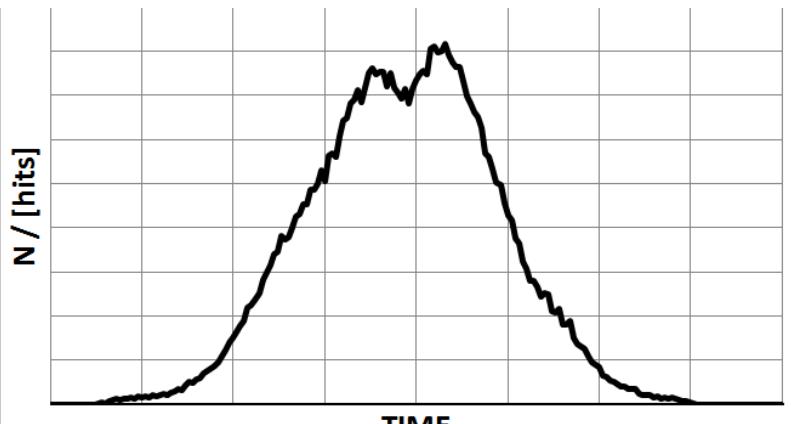
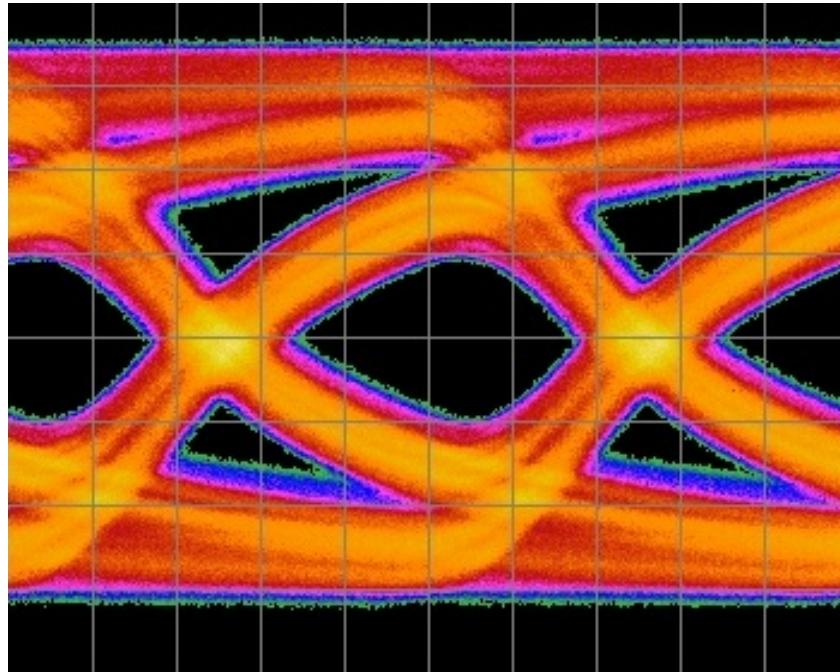


Eye Diagram: Multiple Jitter Sources



- In real systems lots of jitter sources are present at the same time
- In figure: example of DCD + RJ
- **The resulting distribution is the convolution of the single distributions**

Eye Diagram: Multiple Jitter Sources



- Measurement taken after 50 inches of FR4
- Data transitions show deterministic patterns plus blurred behavior
- Histogram shows an unbounded, clearly not gaussian distribution

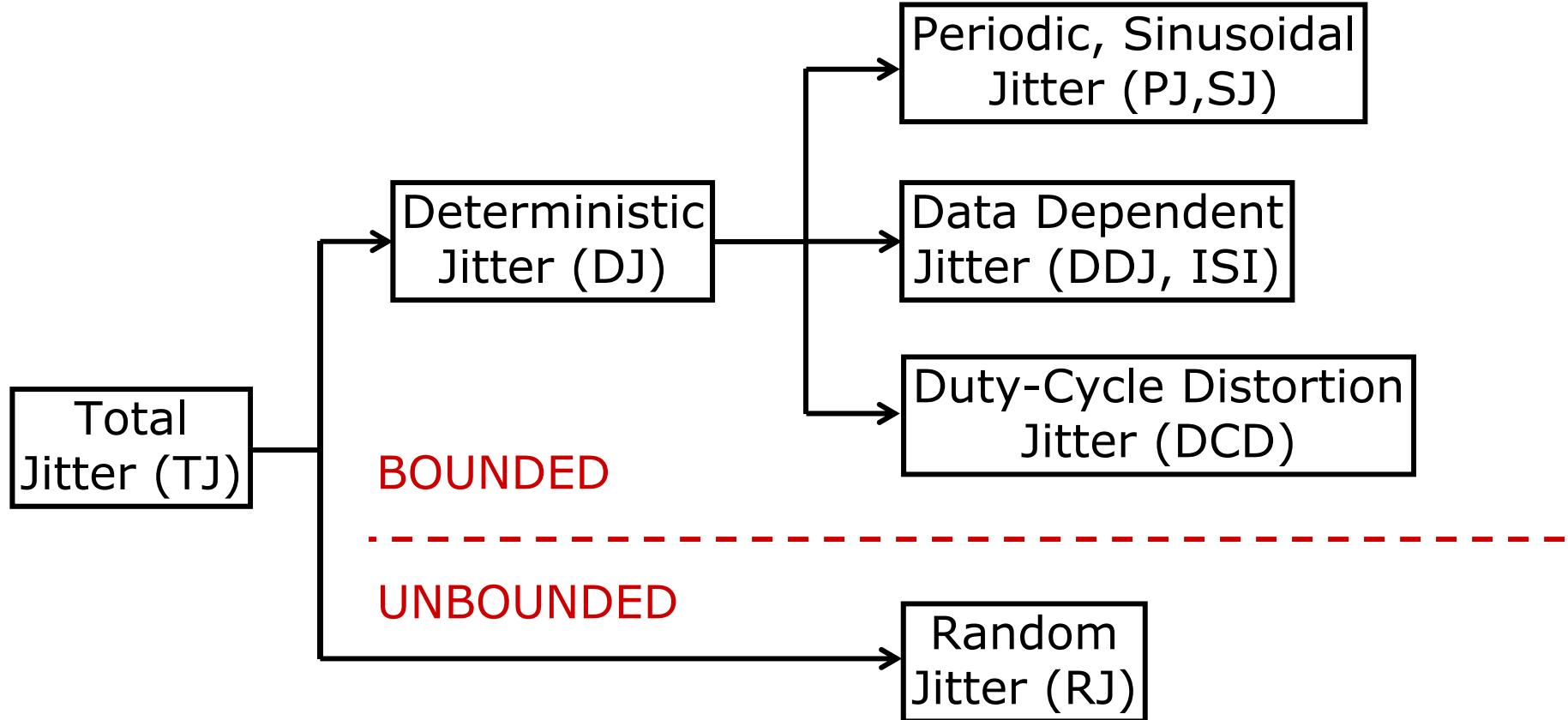
Jitter Decomposition (1/4)

- Jitter is the result of:
 - Device Noise (flicker + thermal)
 - System non-idealities (nonlinearities, limited channel BW, spurious tones in PLL spectrum, duty-cycle, ...)
 - External disturbances (supply noise, switching noise, crosstalk, ...)
- Device noise contributors are gaussian, **unbounded**
- Other contributors generate **bounded** distributions

Jitter Decomposition (2/4)

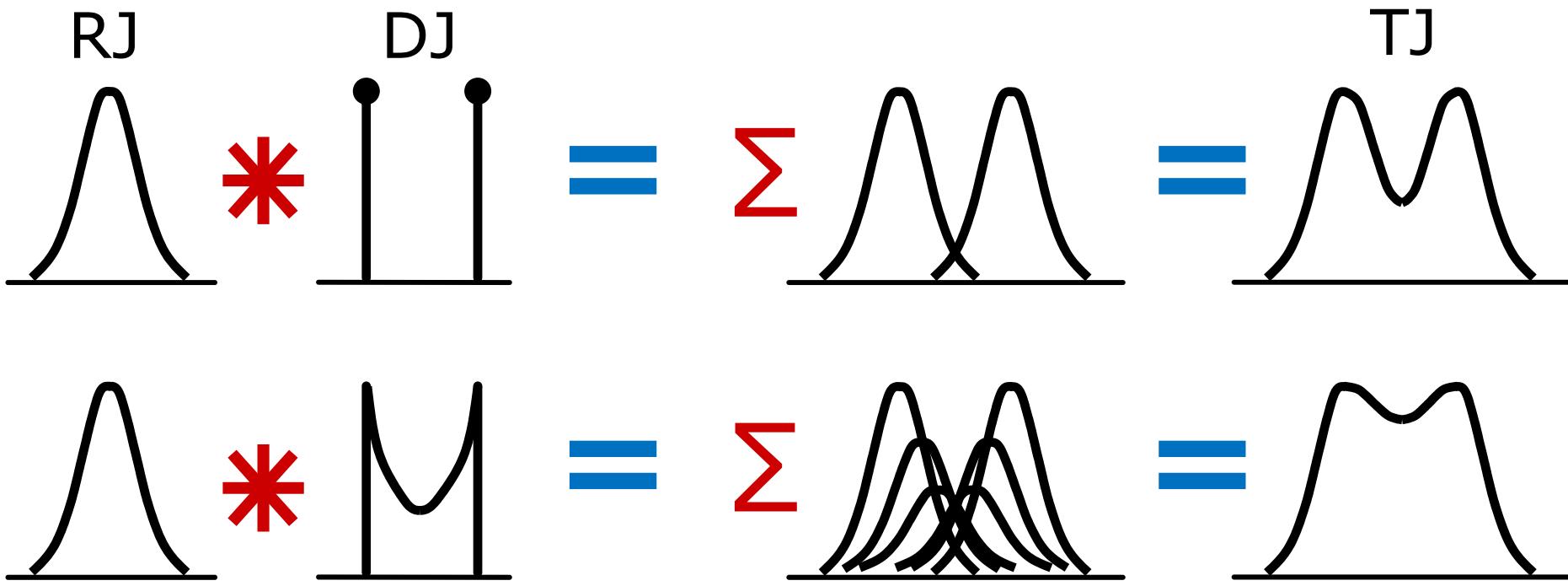
- Idea: consider the total jitter distribution as the combination of:
 - deterministic components
 - random component
- **Deterministic Jitter (DJ)** := any jitter with **bounded** distribution
- **Random Jitter (RJ)** := any jitter with **unbounded** distribution (gaussian)
- The result of DJ and RJ is called **Total Jitter (TJ)**

Jitter Decomposition (3/4)

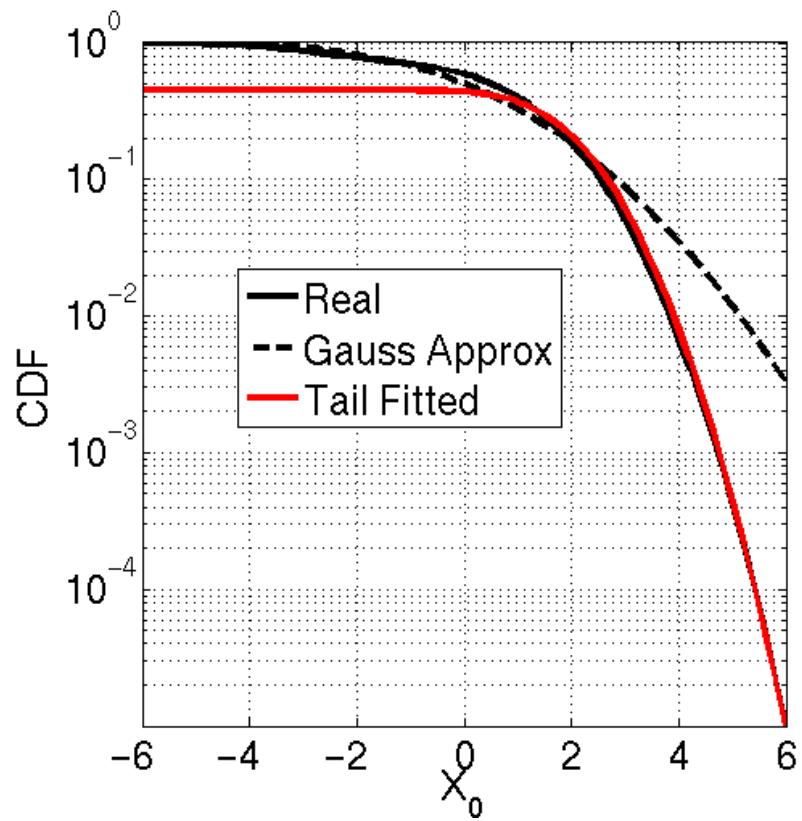
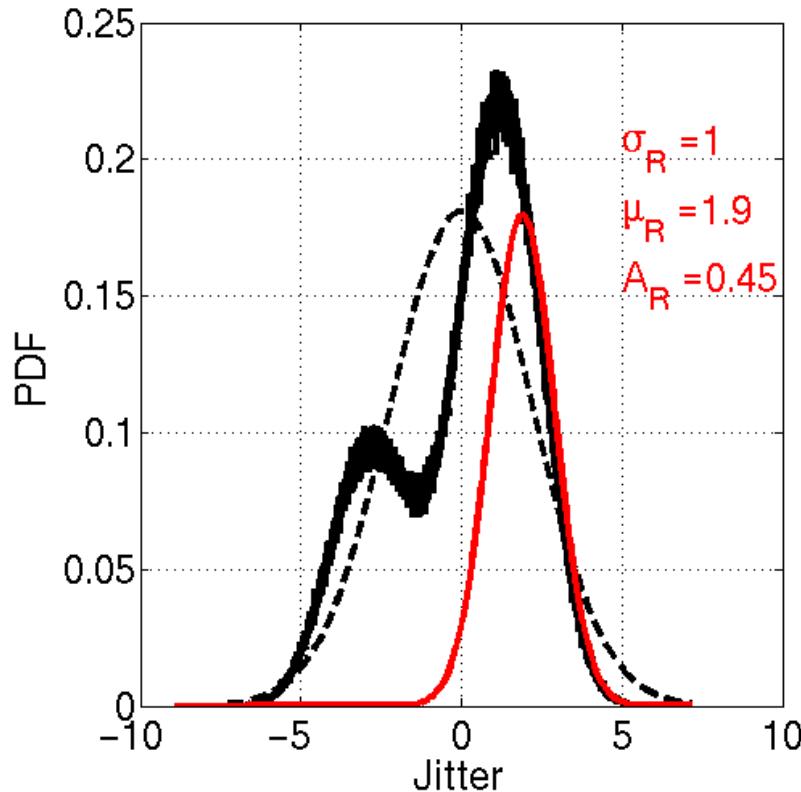


Jitter Decomposition (4/4)

- From Probability Theory: the distribution of the sum of independent random variables is the **convolution** of the single distributions
- Hence: the distribution of TJ is the **convolution** of the distributions of RJ and DJ

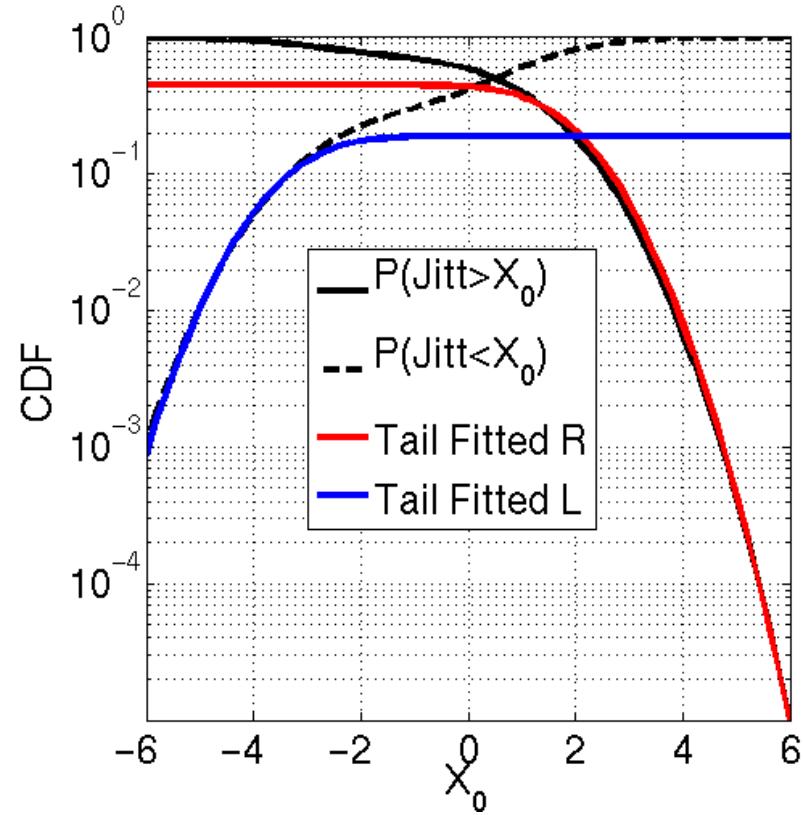
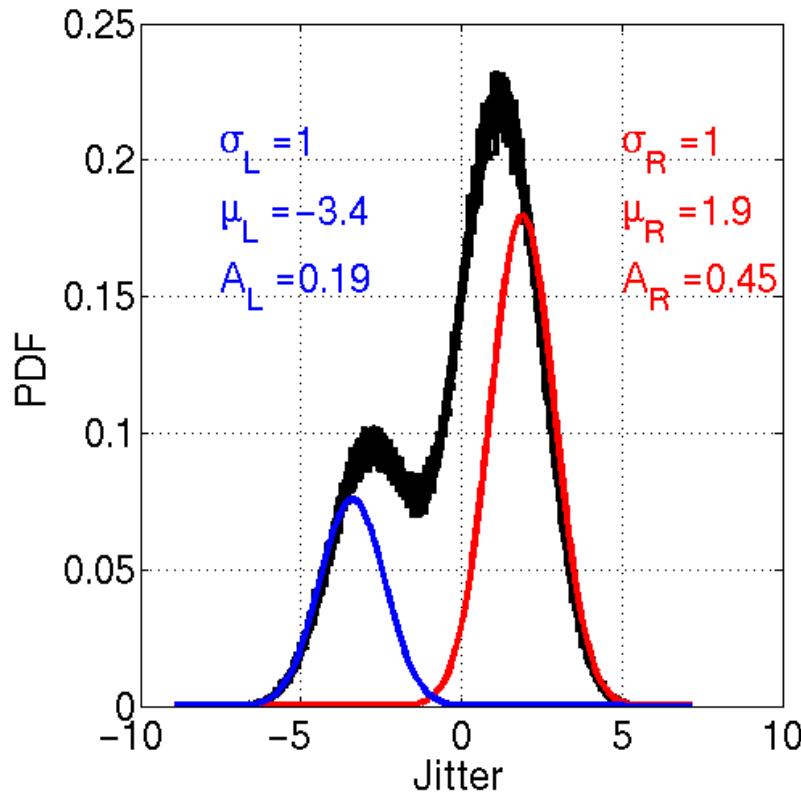


Tail Fitting (1/3)



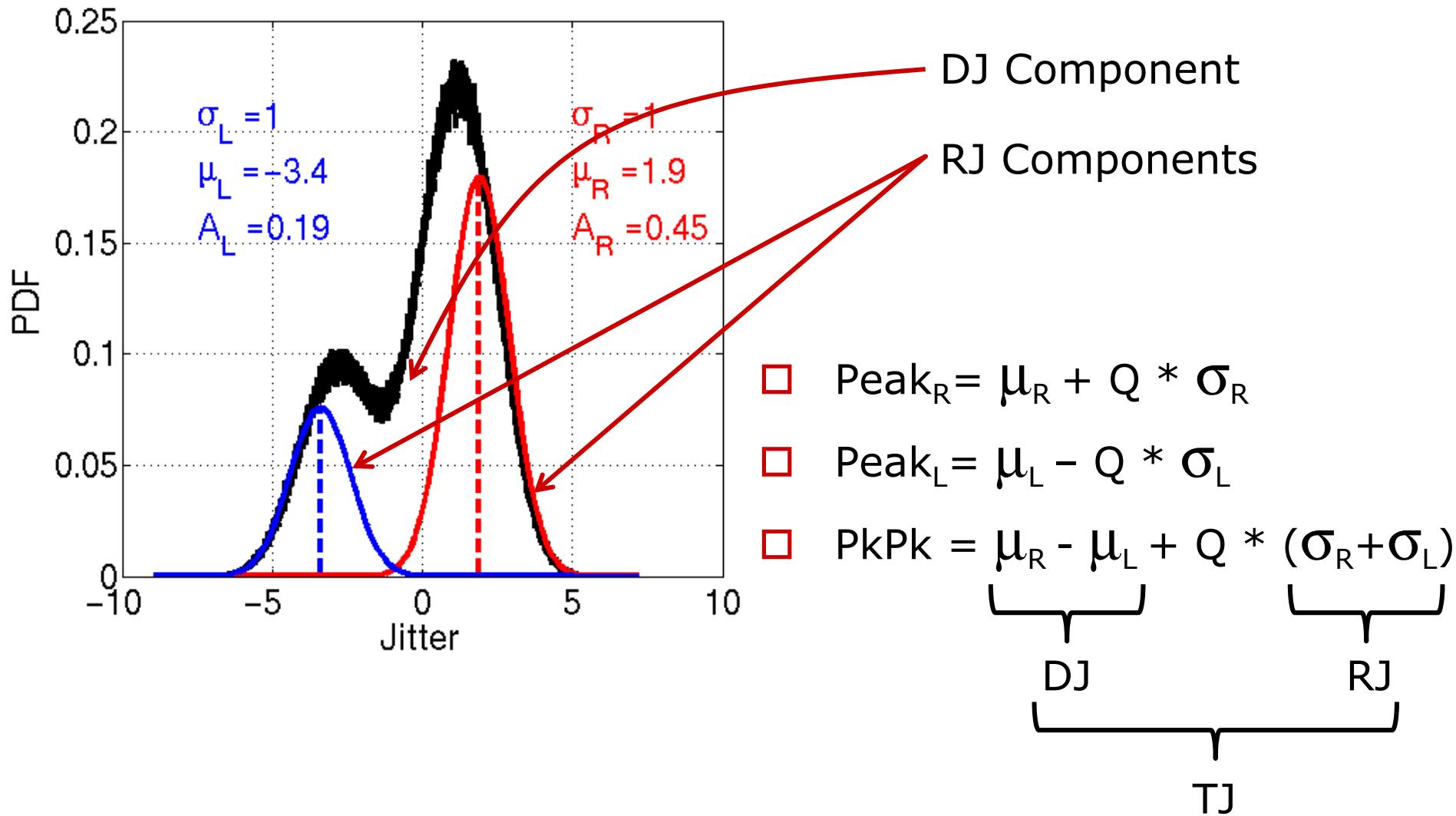
- Idea: fit a gaussian curve to the tail of the distribution
- Probability of error obtained used the fitted curve is matching the real one
- 3 Parameters: σ , μ , A

Tail Fitting (2/3)

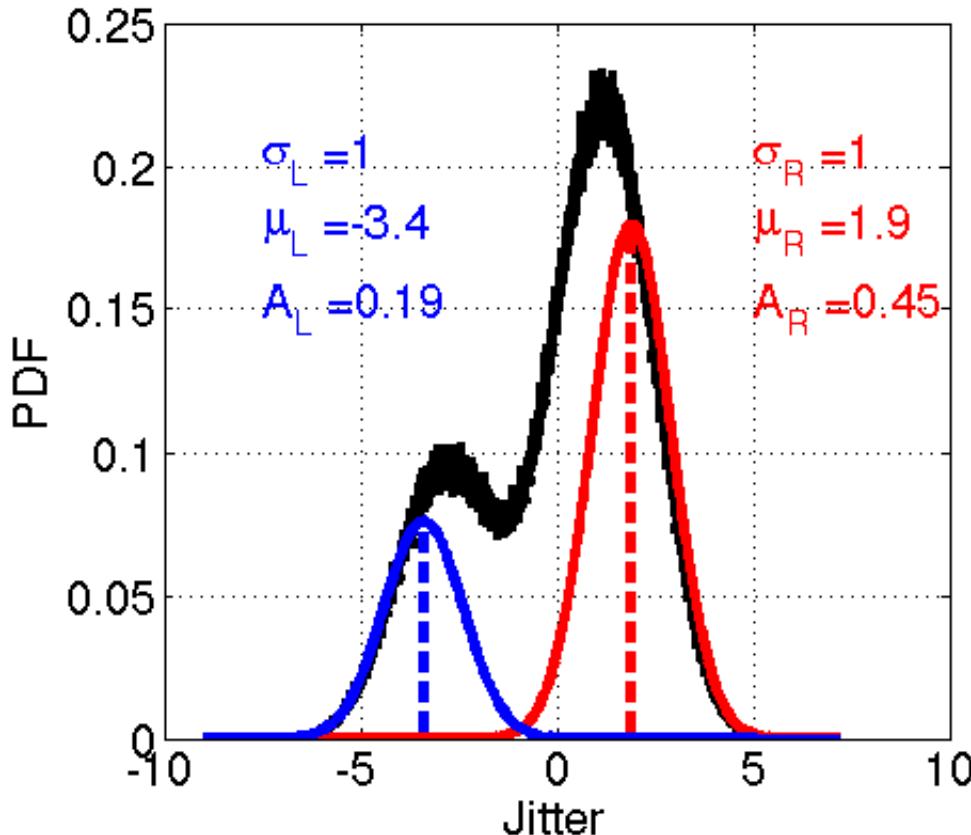


- Do the same for the left tail
- 6 Parameters: σ_R , μ_R , A_R , σ_L , μ_L , A_L
- Probability of error left and right can be accurately described

Tail Fitting (3/3)



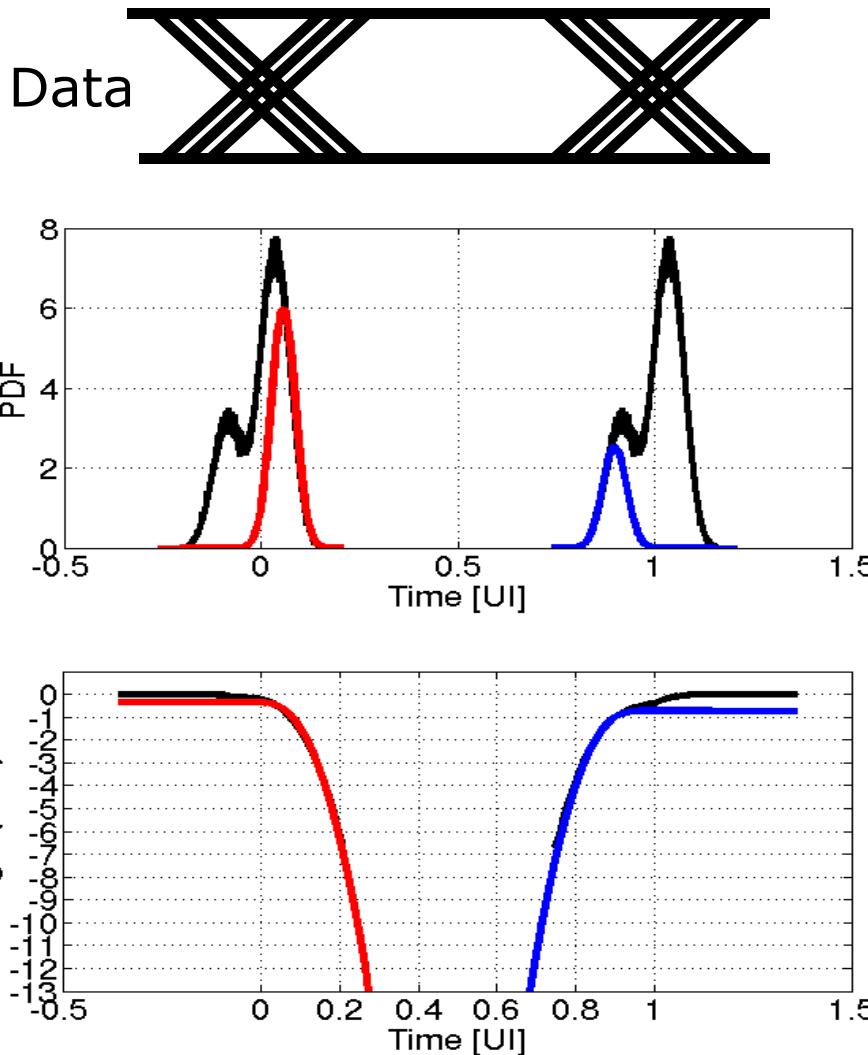
TJ and Probability



- $TJ = \mu_R - \mu_L + Q * (\sigma_R + \sigma_L)$
- Usually $\sigma_R = \sigma_L = \sigma$
- $TJ = DJ + 2 * Q * \sigma$

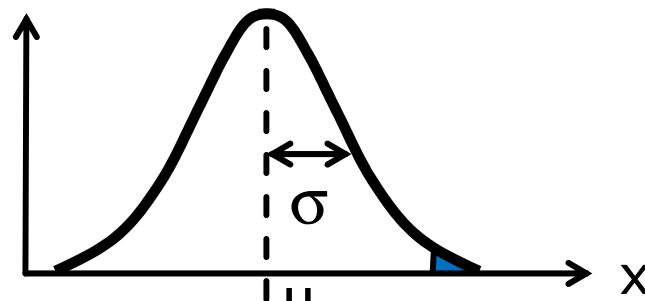
$\text{Prob}(\text{Jitter outside TJ range}) = \frac{A_R + A_L}{2} erfc\left(\frac{Q}{\sqrt{2}}\right) \cong \frac{1}{2} erfc\left(\frac{Q}{\sqrt{2}}\right)$

Bathtub plot (1/3)



- The bathtub plot is obtained by building the CDFs of the jitter on the left and right data edges
- It shows the probability of error versus the sampling point
- Used to estimate the eye opening for very low BER levels

Bathtub plot (2/3): Q-scale

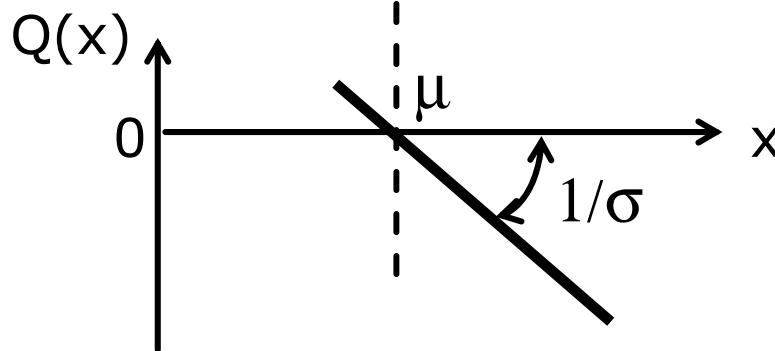


- Q-scale used to linearize the bathtub plot for gaussian distributions

$$P_{err}(x) = \frac{1}{2} \operatorname{erfc}\left(\frac{x - \mu}{\sqrt{2}\sigma}\right)$$

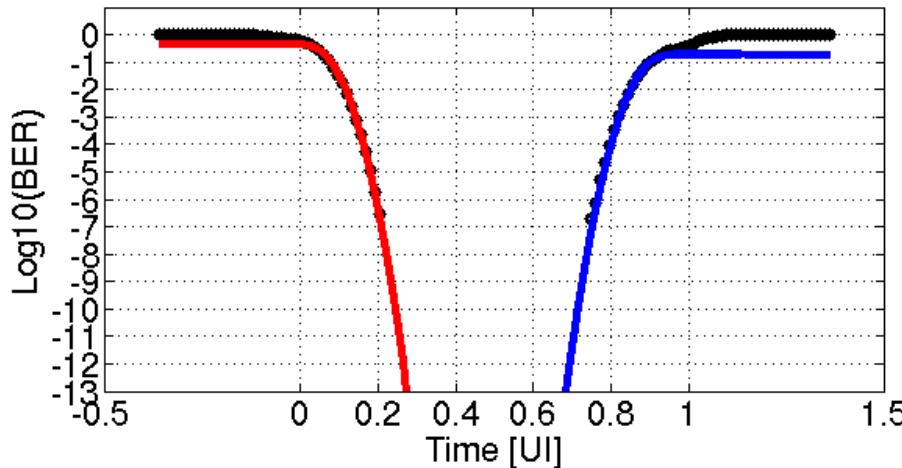
$$Q(x) := -\sqrt{2} \cdot \operatorname{erfc}^{-1}(2 \cdot P_{err}(x))$$

$$Q(x) = \frac{\mu - x}{\sigma}$$

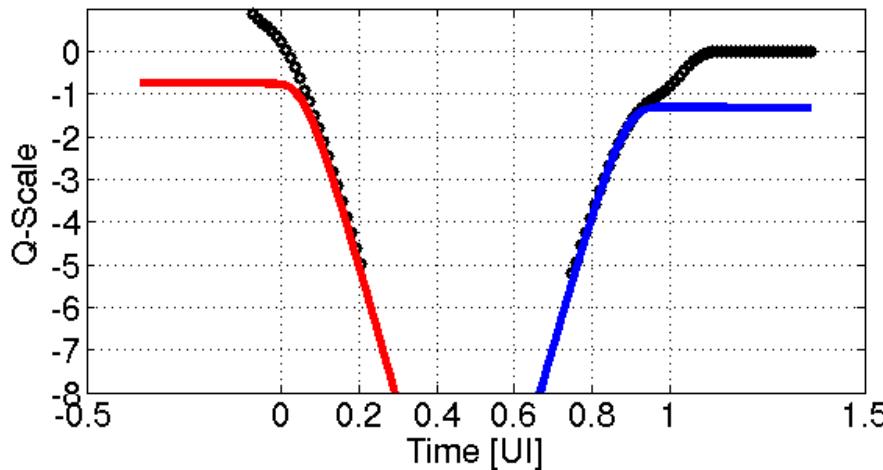


- $P_{err}=10^{-15} \rightarrow Q=-7.95$
- $P_{err}=10^{-12} \rightarrow Q=-7.03$
- $P_{err}=10^{-9} \rightarrow Q=-5.99$
- $P_{err}=10^{-6} \rightarrow Q=-4.75$

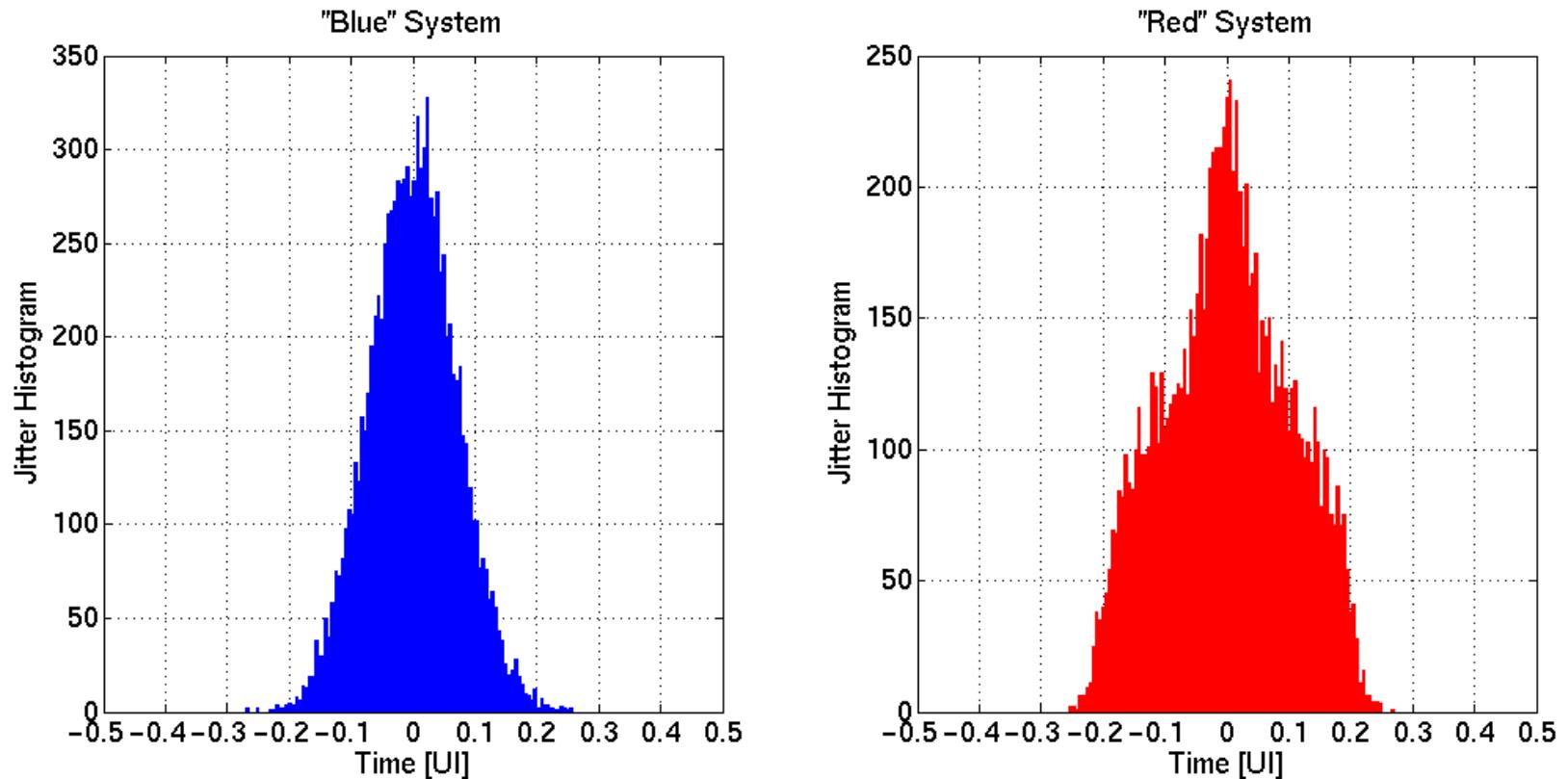
Bathtub plot (3/3)



- Gaussian components in Q-scale are linear
- Linear interpolation to lower Q (BER)
- Used to understand when RJ contribution starts to dominate

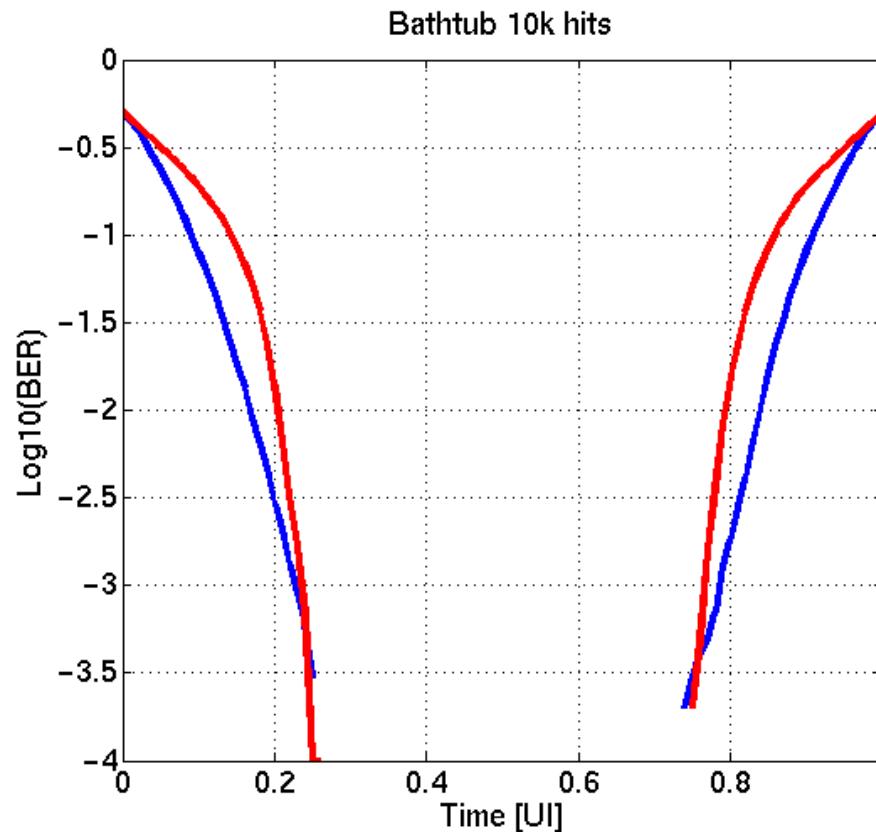


Bathtub Example (1/4)



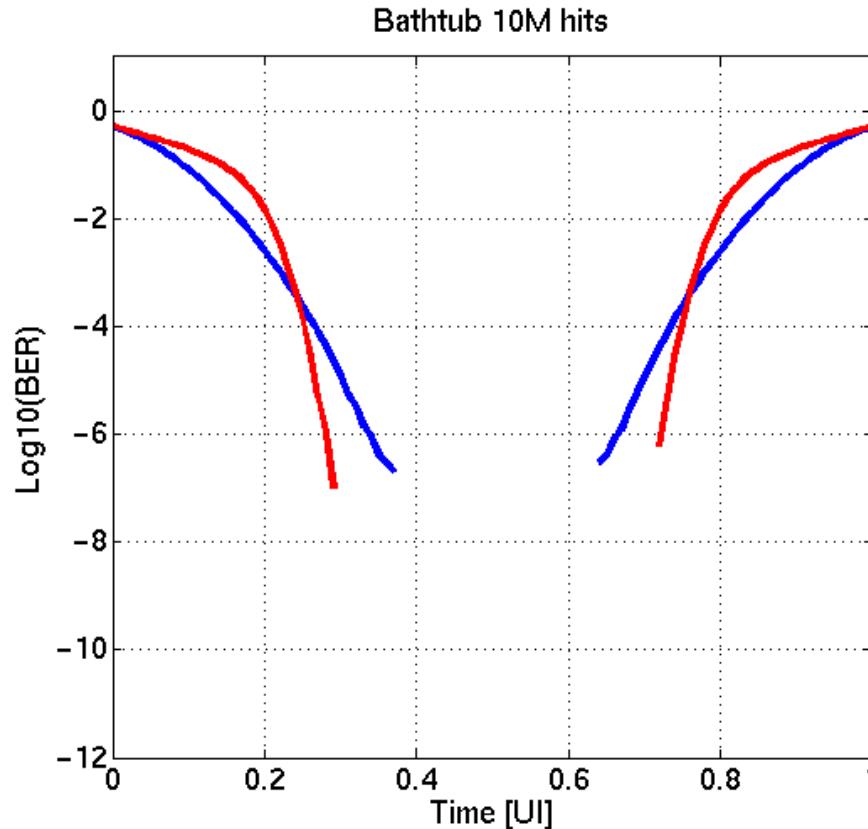
- Two systems with different jitter histograms over 10k hits
- Although the histograms are different the peak to peak jitter seems to be the same

Bathtub Example (2/4)



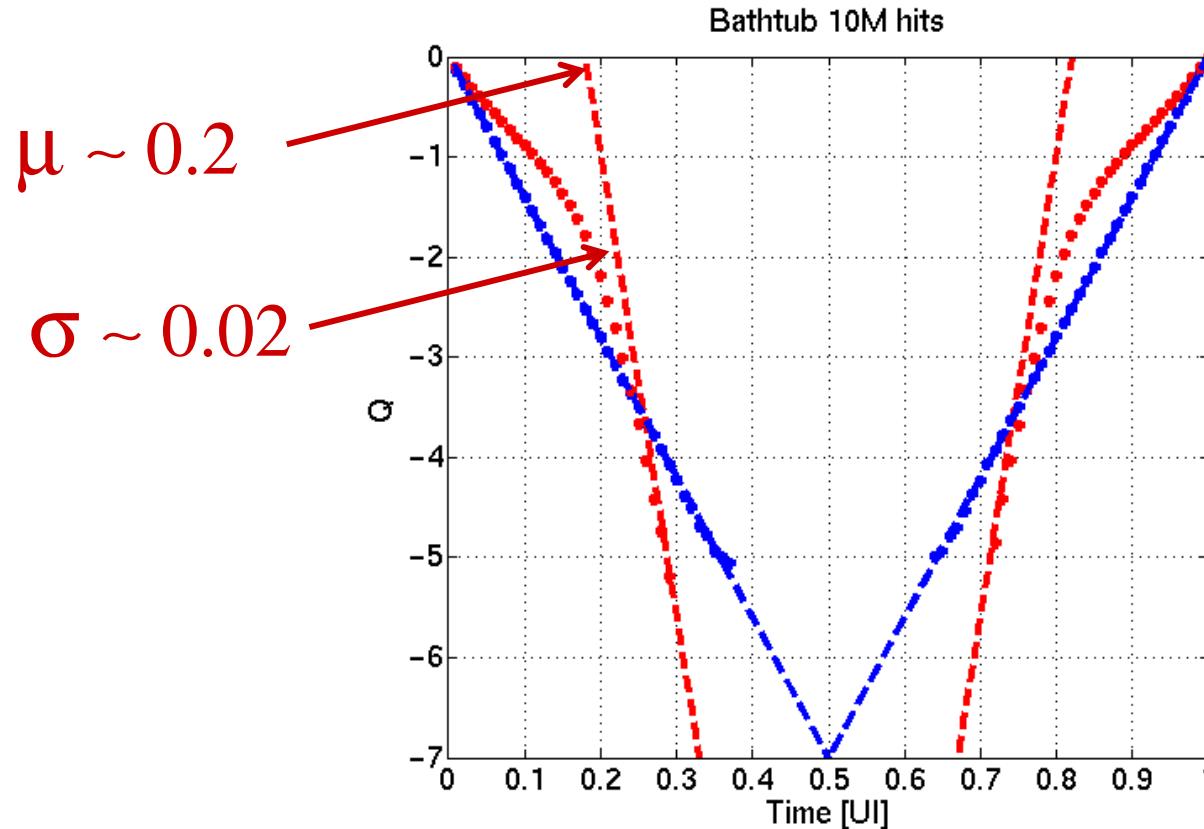
- ❑ Bathtub over 10k hits
- ❑ “Red” system has steeper slopes as “Blue” one
- ❑ For low BER, “Red” system seems to be better

Bathtub Example (3/4)



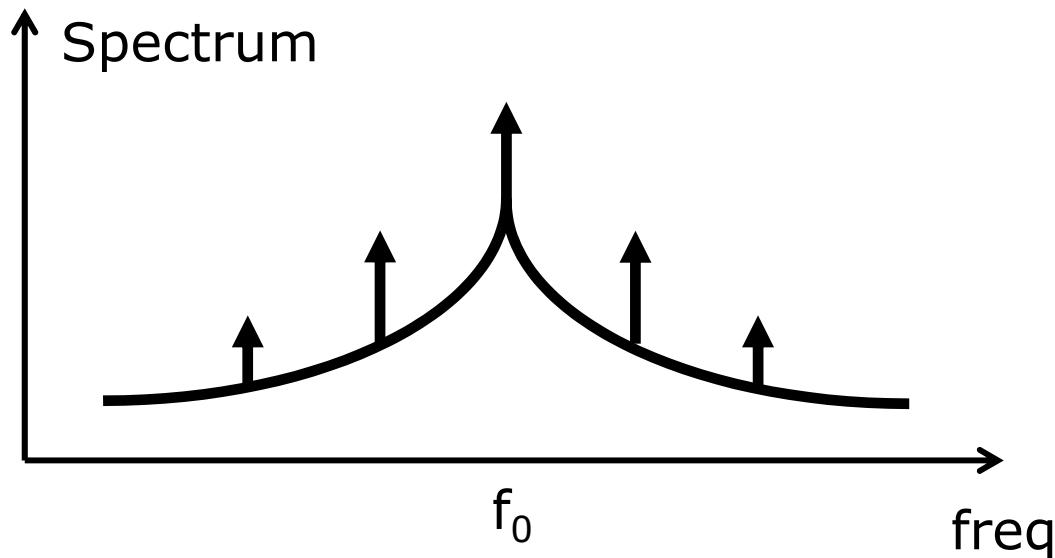
- ❑ Bathtub over 10 Million hits
- ❑ “Red” system definitely has larger eye opening for low BER
- ❑ From this graph Eye Opening @ $1e-12$ not easy to predict

Bathtub Example (4/4)



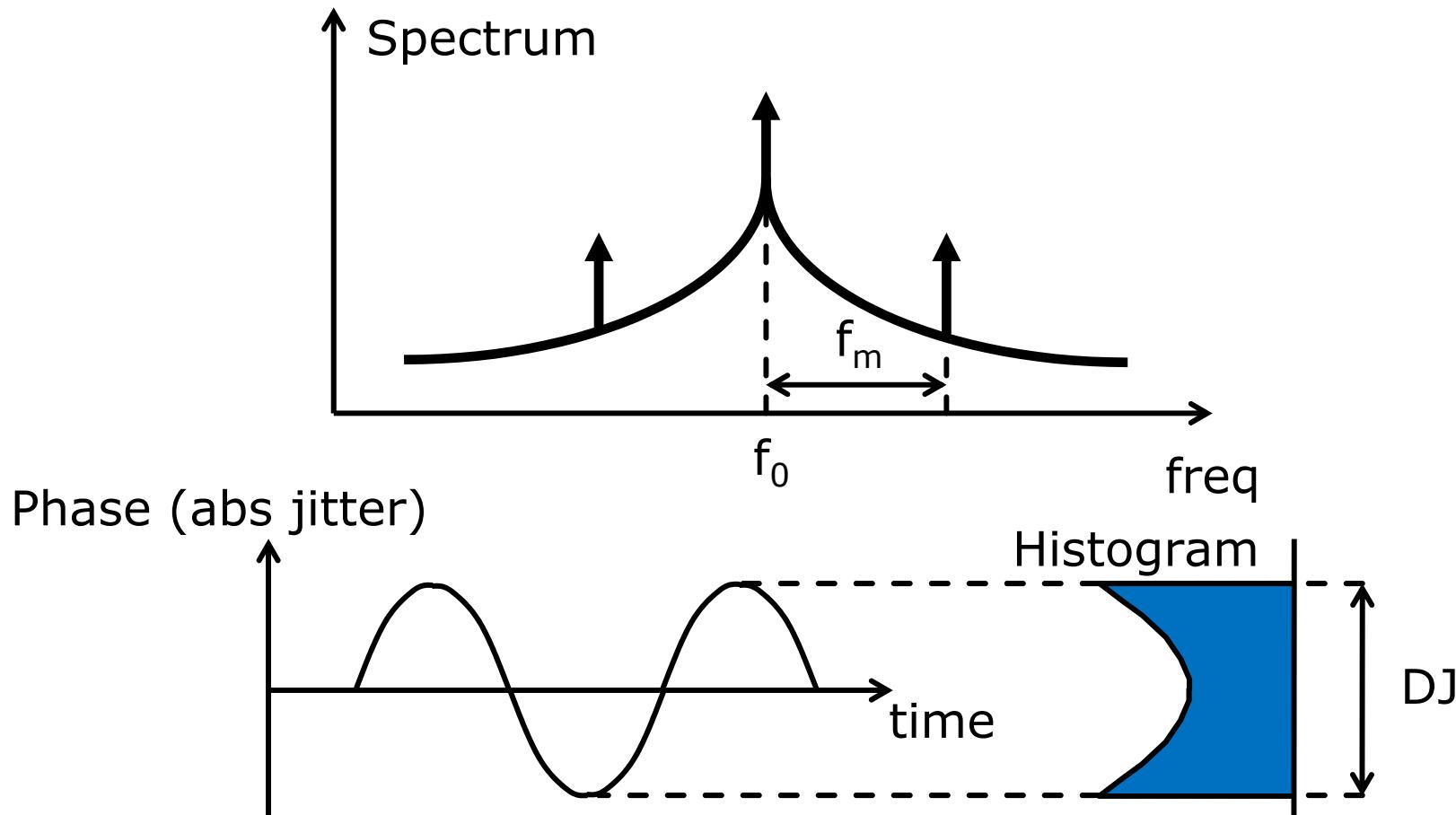
- Bathtub in Q-scale
- “Blue” has closed eye @ $1e-12$ (system not working)
- “Red” system has > 30% eye opening @ $1e-12$

Spurious Tones in Spectrum (1/4)



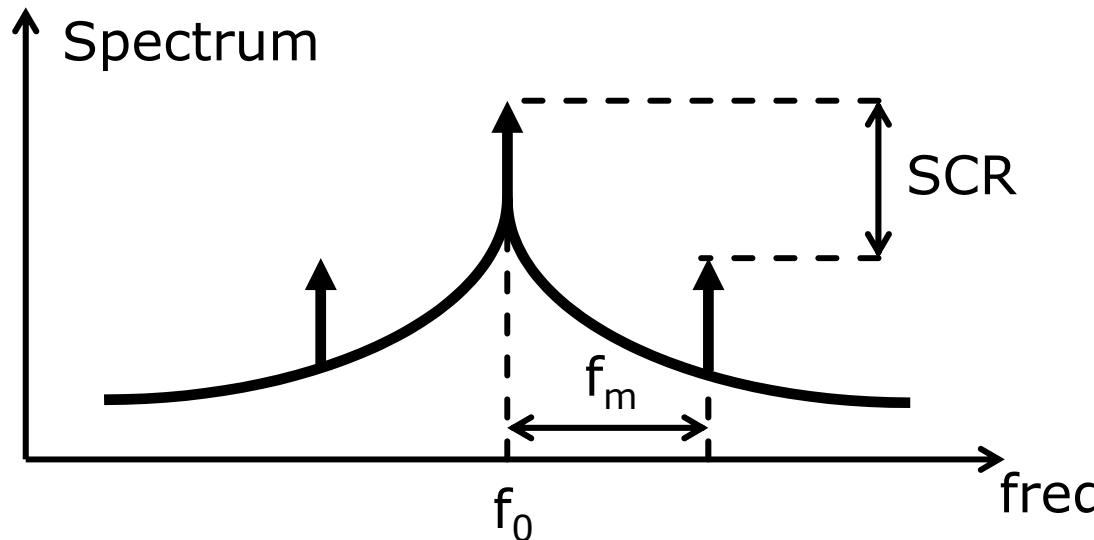
- Spurious tones indicate periodical phase modulation
- Periodic signals can be decomposed in sinusoidal components
- Each sinusoidal component contributes to bounded jitter (DJ)

Spurious Tones in Spectrum (2/4)



- Each sinusoidal component contributes to bounded jitter (DJ)

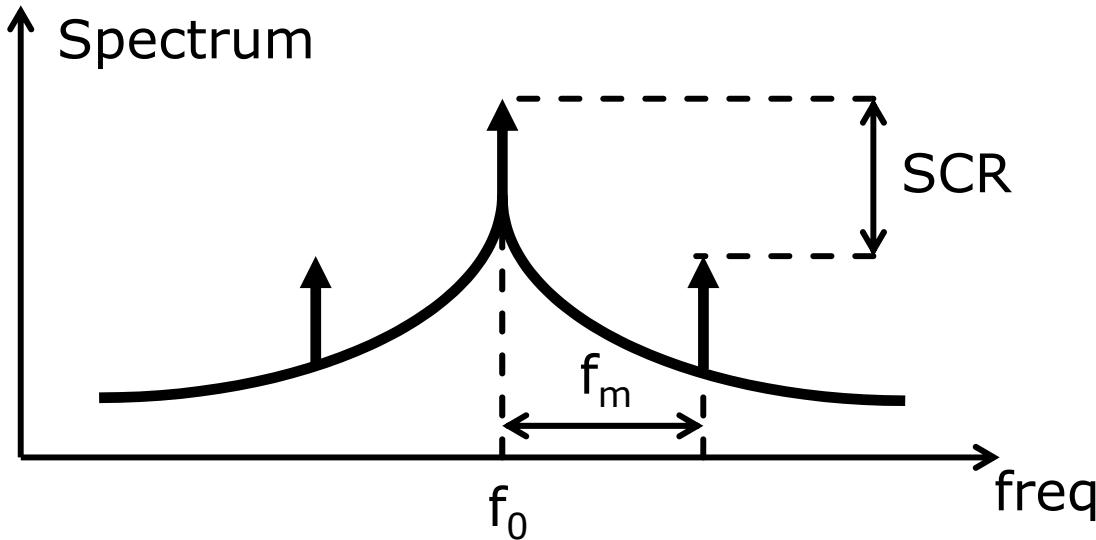
Spurious Tones in Spectrum (3/4)



$$V(t) = V_0 \sin(\omega_0 t + A \cdot \sin(\omega_m t)) = V_0 \cdot \left[J_0(A) \sin(\omega_0 t) - J_1(A) \cos((\omega_0 - \omega_m)t) + \dots + J_1(A) \cos((\omega_0 + \omega_m)t) + \dots \right]$$

$$\text{SCR} = 20 \log_{10} \left(\frac{J_1(A)}{J_0(A)} \right) = 20 \log_{10} \left(\frac{A}{2} \right) \quad \text{for small } A$$

Spurious Tones in Spectrum (4/4)



$$DJ[s] = \frac{2A}{2\pi f_0} = \frac{2}{\pi f_0} 10^{SCR/20}$$

$$DJ[UI] = \frac{2}{\pi} 10^{SCR/20}$$

SCR [dBc]	DJ [UI]
-10	2.0E-01
-15	1.1E-01
-20	6.4E-02
-25	3.6E-02
-30	2.0E-02
-35	1.1E-02
-40	6.4E-03
-45	3.6E-03
-50	2.0E-03
-55	1.1E-03
-60	6.4E-04
-65	3.6E-04
-70	2.0E-04
-75	1.1E-04
-80	6.4E-05

- DJ depends on SCR and f_0 , not on f_m

Summary

- Definition of several Jitter types (Absolute jitter, Period Jitter, Accumulated Jitter)
- Measurement in Time and Frequency Domain
- Phase Noise and relationship to Jitter
- Jitter in typical applications
- Analysis of statistical properties of Jitter for gaussian and non-gaussian distributions
- Jitter decomposition in RJ and DJ
- DJ in High Speed Data Communication (PJ/SJ,DDJ/ISI,DCD,...)
- Tail fitting
- Bathtub plots
- Extrapolation of eye opening @ very low BER

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