Numbers in C

Balance Sheet ... so far

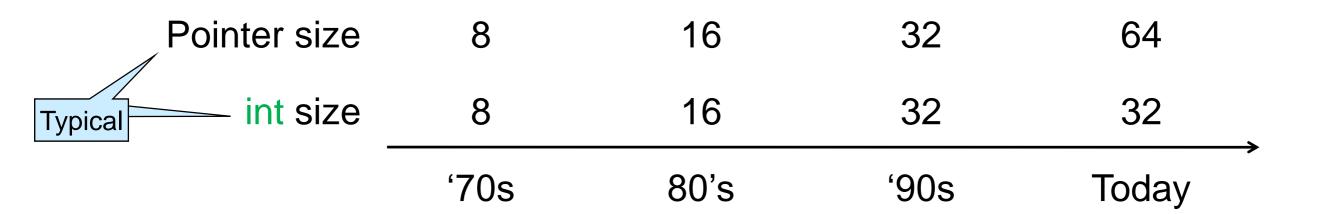
Lost	Gained
Contracts	Preprocessor
 Safety 	 Undefined behavior
 Garbage collection 	 Explicit memory management
 Memory initialization 	 Separate compilation
 Well-behaved arrays 	 Pointer arithmetic
 Fully-defined language 	 Stack-allocated arrays and structs
• Strings	Generalized address-of

Undefined Behavior

Reading/writing to non-allocated memory Reading uninitialized memory Memory · even if correctly allocated Use after free • Double free Freeing memory not returned by malloc/calloc Writing to read-only memory Numbers **Today**

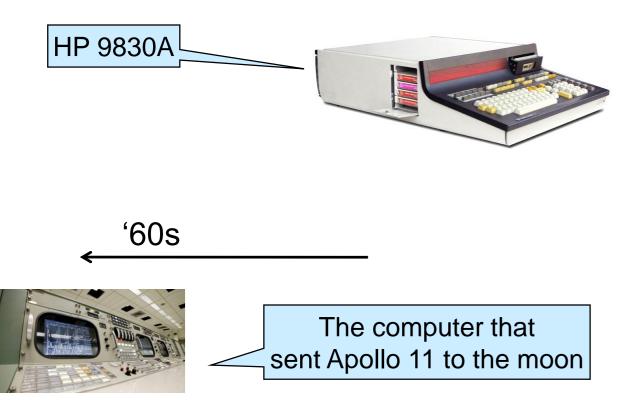
The type int

- In C0/C1, the size of values of type int is 32 bits
 and pointers are 64 bits
- In C, the size of an int has evolved over time
 and pointers too



In C, the size of an int has evolved over time
 and pointers too

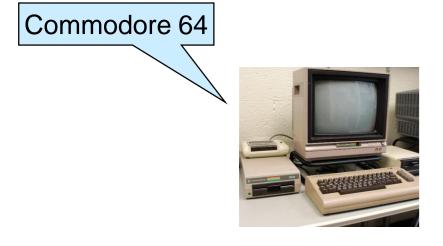
	'70s	80's	'90s	Today	
int size	8	16	32	32	→
Pointer size	8	16	32	64	



- Early computers had 8-bit addresses
 - 256 *bytes* of memory
 - > RAM was very expensive
 - o ints ranged from -128 to 127

In C, the size of an int has evolved over timeand pointers too

	'70s	80's	'90s	Today
int size	8	16	32	32
Pointer size	8	16	32	64

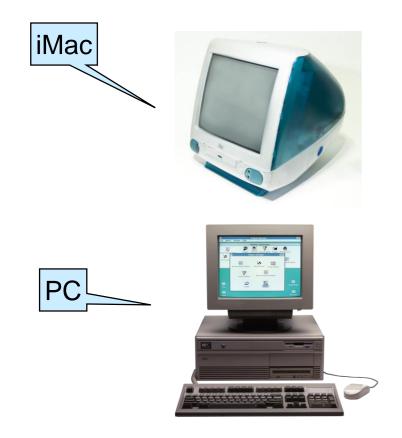




- 16-bit addresses
 - (up to) 64 kilobytes of memory
 - > the Commodore 64
 - o ints ranged from -32768 to 32767

In C, the size of an int has evolved over time
 and pointers too

	'70s	80's	'90s	Todav	
int size	8	16	32	32	→
Pointer size	8	16	32	64	



- 32-bit addresses
 - (up to) 4 gigabytes of memory
 - o ints ranged in the billions

In C, the size of an int has evolved over time
 and pointers too

	'70s	80's	'90s	Today
int size	8	16	32	32
Pointer size	8	16	32	64





- 64-bit addresses
 - o nobody has 2⁶⁴ bytes memory
 - billions are still Ok for ints

Implementation-defined Behavior

- The C standard says that it is for the compiler to define the size of an int
 - > with some constraints
- It is implementation-defined
 - The compiler decides, but
 - o it remains fixed
 - o the programmer can find out how big an int is
 - > the file < limits.h > defines the values of INT_MIN and INT_MAX
 - and therefore the size of an int

Undefined behavior ≠ implementation-defined behavior

- undefined behavior does not have to be consistent
- the programmer has no way to find out from inside the program

Implementation-defined Behavior

- Most programmers don't need to know how big an int is
 - just write code normally, possibly using INT_MIN and INT_MAX
 - the compiler will use whatever internal size it has chosen

This is not true of code that uses the bits of an int to encode data: bit patterns (e.g., pixels)

- Same thing for pointers
- Code written in the 1970s still works on today's computers
 - o as long as the code doesn't depend on the size of an int
 - o and the programmer used sizeof inside malloc

int's Undefined Behaviors

Safety violations in C0 are undefined behavior in C

- division/modulus by 0, or INT_MIN divided/mod'ed by -1
- shifting by more than the size of an int

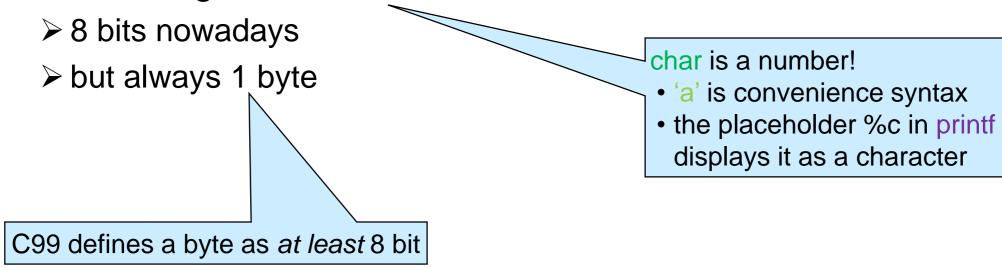
Overflow!

- C programs do not necessarily use two's complement
 - > this makes it essentially impossible to reason about ints in a C program
 - \triangleright an optimizing compiler cannot simplify n + n n to n
- gcc provides the flag -fwrapv to force the use of two's complement for ints

Other Integer Types

Signed Integer Types

- C0 has a single type of integers: int
- C has many more
 - long: integers that are larger than int
 - ➤ 64 bits nowadays
 - short: integers that are smaller than int
 - ➤ 16 bits nowadays
 - char: integers that are smaller than short



o ... and there are more

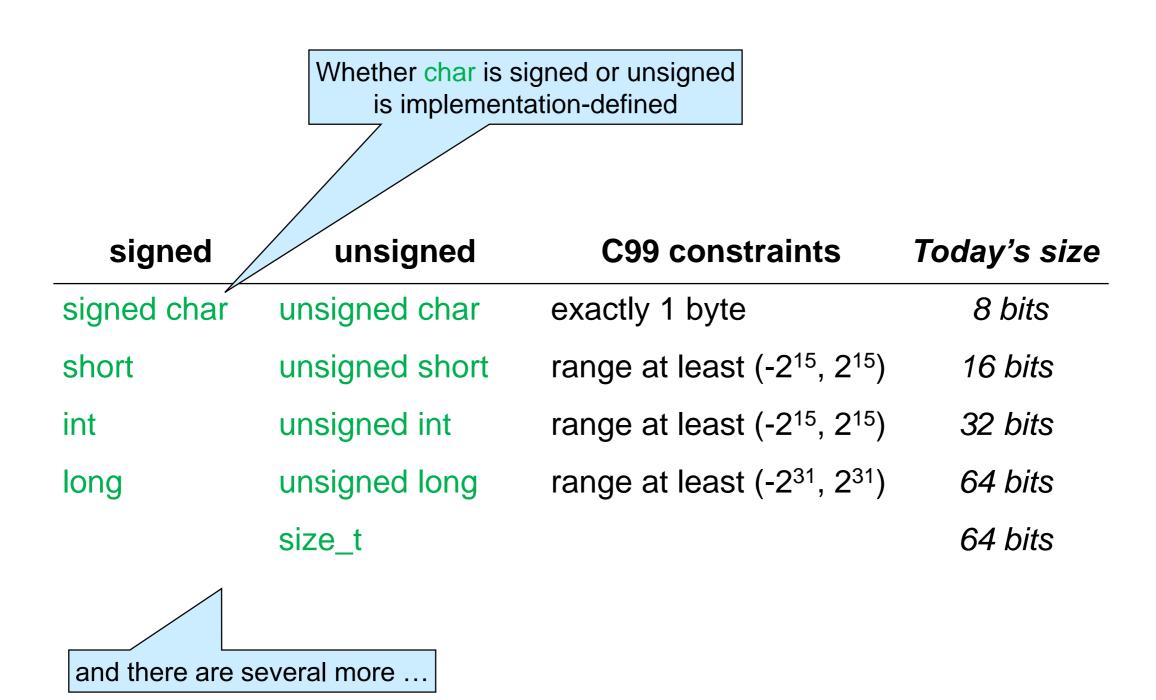
Unsigned Integer Types

- Lots of code doesn't use negative numbers
- C provides unsigned variants of each integer type
 - same number of bits but sign bit can be used to represent more numbers
 twice as many numbers
 - o unsigned long
 - o unsigned int ______ or just unsigned
 - o unsigned short
 - o unsigned char
- Overflow on unsigned numbers is defined to wrap around
 - unsigned numbers do follow the laws of modular arithmetic

Unsigned Integer Types

- size_t is the size of a pointer
 - o the argument of malloc and calloc
 - array indices
 - return type of sizeof
 - O ...

Implementation-defined Integers



Casting Integers

Integer Casts

 We go back and forth between different number types with casts

int
$$x = 3$$
; $x = 3$; $y = (long)x$;

Literal numbers have always type int

The compiler introduces implicit casts as needed

long
$$x = 3$$
;

> is implicitly turned into

$$long x = (long)3;$$

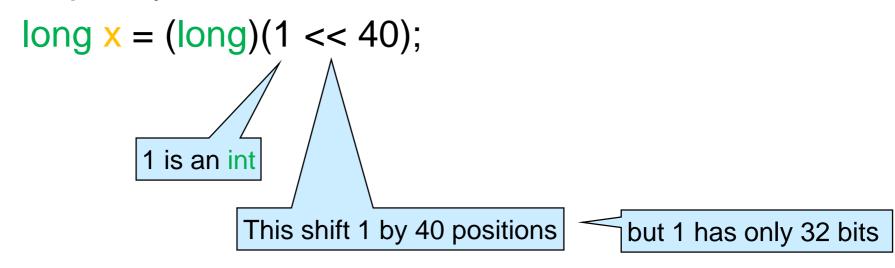
Integer Casts

- Literal numbers have always type int
- The compiler introduces implicit casts as needed
- This can lead to unexpected outcome

$$long x = 1 << 40;$$

is undefined behavior

This is implicitly turned into



> Fix: long x = ((long)1) << 40;

Casting Rules

 When casting between signed and unsigned integers of the same size, the bit pattern is preserved

> This is actually implementation-defined (but commonplace)

Example 1

```
signed char x = 3; // x is 3 (\neq 0 unsigned char y = (unsigned char)x; // y is 3 (\neq 0
```

Example 2

```
signed char x = -3; // x is -3 (\neq unsigned char y = (unsigned char)x; // y is 253 (\neq
```

Casting Rules

 When casting small to big integers of the same signedness, the value is preserved

Casting Rules

- When casting big to small integers of the same signedness, the value is preserved if it fits
 - o the behavior is undefined otherwise

```
Example 1
    int x = 3;
                                     // x is 3 (= 0x00000003)
    signed char y = (signed char)x; // y is 3 (= 0x03)
Example 2
    int x = -3;
                                    // x is -3 (= 0xFFFFFFD)
    signed char y = (signed char)x; // y is -3 (= 0xFD)
Example 3
    int x = INT_MAX;
                                     // x is -3 (= 0x7FFFFFFF)
    signed char y = (signed char)x; // y is ??
```

Casting across Signedness and Size

The compiler may apply the rules in either order

```
unsigned char x = 0xFD;
                                           // x is 253
    int y = (int)x;
                                           // y is ...
                                 0xFD
      cast to unsigned int
                                              cast to signed char
         preserves value
                                              preserves bit pattern
    253
            0x000000FD
                                                   0xFD
cast to (signed) int
                                                       cast to (signed) int
preserves bit pattern
                                                         preserves value
            0x000000FD
```

• is y 253 or -3?

Casting across Signedness and Size

The compiler may apply the rules in either order

```
unsigned char x = 0xFD; // x is 253
int y = (int)x; // y is ...
```

- Is y -3 or 253?
 - > the order of casts is actually defined
 - but who remembers it?



- Solution: be explicit
 - Write either

```
int y = (int)(unsigned int)x; // y is 253
```

to change first the size and then the signedness

o or

int
$$y = (int)(signed char)x;$$
 // y is -3

to change first the signedness and then the size

Fixed-size Numbers

Fixed-size Integers

- For bit patterns, the program needs the number of bits to remain the same as C evolves
- Header file <stdint.h> provides fixed-size integer types
 in signed and unsigned variants

Fixed-size signed	Today's signed equivalent	Today's unsigned equivalent	Fixed-size unsigned
int8_t	signed char	unsigned char	uint8_t
int16_t	short	unsigned short	uint16_t
int32_t	int	unsigned int	uint32_t
int64_t	long	unsigned long	uint64_t

That's the number of bits

Floating Point Numbers

The type float represents floating point numbers

```
> nowadays 32 bits float x = 0.1; Numbers with a decimal point float y = 2.0235E-27; That's 2.0235 * 10^{-27}
```

- float and int use the same number of bits, but float has a much larger range
 - o some numbers with a decimal point are not representable
 - the larger range comes at the cost of precision
 - > operations on floats may cause rounding errors



Operations on floats may cause rounding errors

```
O Example 1

#include <math.h>

#define PI 3.14159265

float x = \sin(PI);

In math, \sin(\pi) is 0 but \sin(PI) is not 0.0

O Example 2

float y = (10E20 / 10E10) * 10E10;

That's (10^{20}/10^{10}) * 10^{10}

Positive sin, cos, log, ...

Any more decimals would be ignored

That's (10^{20}/10^{10}) * 10^{10}

That's (10^{20}/10^{10}) * 10^{10}

Positive sin, cos, log, ...

Any more decimals would be ignored
```

- ➤ but it isn't always
 - ☐ it depends on the compiler



- Operations on floats may cause rounding errors
 - Example 3

```
for (float res = 0.0; res != 5.0; res += 0.1)
printf("res = %f\n", res);
```

- > we expect the loop to terminate after 50 iterations
- > instead it runs for ever
- > That's because 0.1 decimal is a **periodic** number in binary: 0.00011

```
This is how we convert 0.1 to binary

0.1 * 2 = 0.2

0.2 * 2 = 0.4

0.4 * 2 = 0.8

0.8 * 2 = 1.6

0.6 * 2 = 1.2

0.2

At this point, it repeats
```

- Operations on floats may cause rounding errors
- This makes it impossible to reason about programs
 - This is why there are no floats in C0

- Adding more bits does not solve the problem
 - The type double of double-precision floating point numbers has typically 64 bits nowadays
 - > similar issues

Union and Enum Types

Sample Problem

- Print a message based on the season
- How to encode seasons?
 - use strings ...
 - > testing which season we are in is costly
 - use integers
- Drawbacks
 - The encoding is not mnemonic
 - > we will make mistakes
 - A whole int for 4 values seems wasteful

```
// 0 = Winter
// 1 = Spring
// 2 = Summer
// 3 = Fall

int today = 3;
if (today == 0)
  printf("snow!\n");
else if (today == 3)
  printf("leaves!\n");
else
  printf("sun!\n");
```

Enum Types

- The encoding is not mnemonic
- A whole int for 4 values seems wasteful

An enum type lets

- the programmer choose mnemonic values
 - □ no need to remember the encoding just use the names
- the compiler decide how to implement them
 - > what actual type to map them to
 - > what values to use

The compiler maps enum names to some numerical values

the compiler optimizes space usage

```
enum season { WINTER, SPRING, SUMMER, FALL }:

enum season today = FALL:

if (today == WINTER)

printf("snow!\n");

else if (today == FALL)

printf("leaves!\n");

else

printf("sun!\n");
```

By convention, enum

values are written in

all caps

Switch Statements

A switch statement is an alternative to cascaded if-elses

for numerical values

- > including union types
- They make the code more readable
- Each value considered is handled by a case
 - The execution of a case continues till the next break or the end of the switch statement
 - > it exits the switch statement
 - The default case handles any remaining value

```
enum season { WINTER, SPRING, SUMMER, FALL };
enum season today = FALL;
switch (today) {
 case WINTER:
                                a case
  printf("snow!\n");
  break;
 case FALL:
                                another case
  printf("leaves!\n");
  break;
 default:
                                the default case
  printf("sun!\n");
```

Switch Statements



 If a break is missing, the execution continues with the next case

```
This the source of many bugs!
```

```
enum season { WINTER, SPRING, SUMMER, FALL };
enum season today = FALL;
switch (today) {
 case WINTER:
                                a case
  printf("snow!\n");
  break;
 case FALL:
                                another case
  printf("leaves!\n");
  break;
 default:
                                the default case
  printf("sun!\n");
```

Recent versions of gcc issue a warning when this happens

Another Sample Problem

- Define a type for binary trees with int data only in their leaves
 - > and where the empty tree is **not** represented as NULL
 - A leafy tree could be
 ➤ an inner node with pointers to two children
 ➤ a leaf with int data
 ➤ an empty tree

 The empty tree
 A leaf

O Then:

```
enum nodekind = { INNER, LEAF, EMPTY };

struct Itree {
    enum nodekind kind;
    int data;
    leafytree *left;
    leafytree *right;
    };
    typedef struct Itree leafytree;
```

Sample Problem

This representation wastes memory

- the compiler will pick a small numerical type for kind
 - ➤ probably a char

```
enum nodekind = { INNER, LEAF, EMPTY };

struct ltree {
   enum nodekind kind;
   int data;
   leafytree *left;
   leafytree *right;
   };

typedef struct ltree leafytree;
```

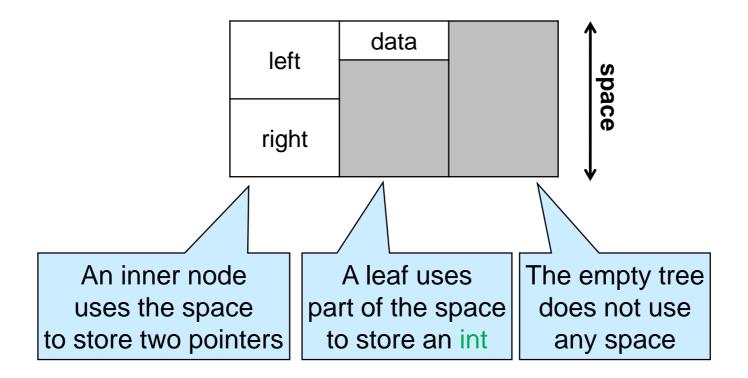
but

- o the remaining 3 fields are never fully utilized for any node type
 - > inner nodes do not make use of the data field
 - ➤ leaves do not use left and right
 - > the empty tree does not need any



Union Types

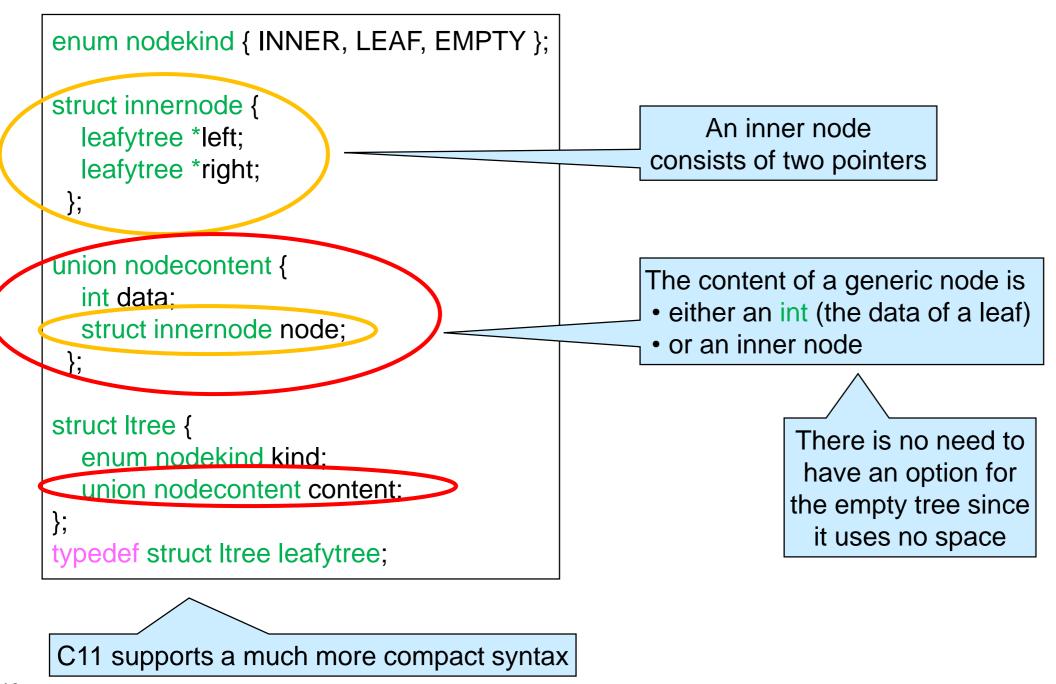
- A union type allows using the same space in different ways
- Consider the space needed for a node, aside from its type



left data space

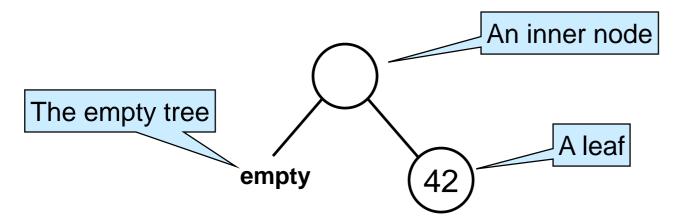
Union Types

A union type allows using the same space in different ways



Building a Tree

Let's write code that create this tree



```
enum nodekind { INNER, LEAF, EMPTY };

struct innernode {
    leafytree *left;
    leafytree *right;
    };

union nodecontent {
    int data;
    struct innernode node;
    };

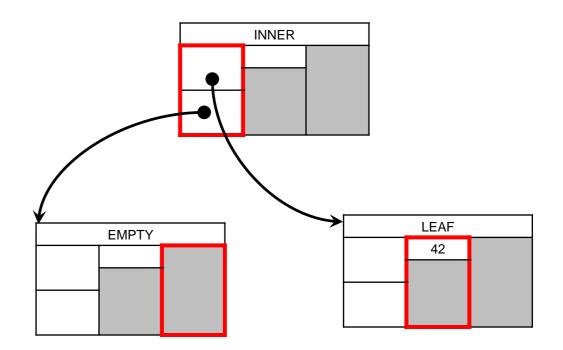
struct Itree {
    enum nodekind kind;
    union nodecontent content;
};

typedef struct Itree leafytree;
```

```
leafytree *T = malloc(sizeof(leafytree));
T->kind = INNER;
T->content.node.left = malloc(sizeof(leafytree));
T->content.node.left->kind = EMPTY;
T->content.node.right = malloc(sizeof(leafytree));
T->content.node.right->kind = LEAF;
T->content.node.right->content.data = 42;

Whenever not following a pointer,
```

we must use the dot notation



Adding up a Leafy Tree

- We use a switch statement to write clear code
 - we discriminate on T->kind
 - it has three possible values
 - ➤ INNER, LEAF and EMPTY

```
int add_tree(leafytree *T) {
 int n = 0;
 switch (T->kind) {
  case INNER:
    n += add_tree(T->content.node.left);
    n += add_tree(T->content.node.right);
    break;
  case LEAF:
    n = T->content.data;
    break;
  default:
    n = 0:
 return n;
```

Summary

Undefined Behavior

Reading/writing to non-allocated memory Reading uninitialized memory Memory even if correctly allocated Use after free Double free Freeing memory not returned by malloc/calloc Writing to read-only memory Division/mod by zero Numbers INT_MIN divided/mod'ed by -1 Shift by more than the number of bits Signed overflow