

Unbounded Arrays

To declare arrays we need to know their size before-hand. Unbounded arrays (**UBA**) overcome this shortcoming of arrays. Internally, in the unbounded array struct we use an array `data` which can store at most `limit` many items. The number of items in the array `data` is stored in the variable `size`. The main idea is that when `size==limit`, we have the `data` array filled to capacity. At this point we can not add any more new items without increasing the size of the array `data`, so we create a new array with size equal to `2*limit` and copy all the items in it.

Struct

```
1 | typedef struct uba_header uba;
2 | struct uba_header {
3 |     int size;           // 0 <= size && size < limit
4 |     int limit;          // 0 < limit
5 |     string[] data;      // \length(data) == limit
6 | };
```

Interface (Client Side View)

A client can use the following functions of the library.

```

1  /***** Interface *****/
2
3  // typedef _____* uba_t;
4
5  //returns the number of strings stored in the uba
6  int uba_len(uba_t A)
7  /*@requires A != NULL;   @*/
8  /*@ensures \result >= 0; @*/ ;
9
10 //creates and returns a new uba, with given size.
11 uba_t uba_new(int size)
12 /*@requires 0 <= size;   @*/
13 /*@ensures \result != NULL; @*/
14 /*@ensures uba_len(\result) == size; @*/ ;
15
16 //returns item stored at index i
17 string uba_get(uba_t A, int i)
18 /*@requires A != NULL;   @*/
19 /*@requires 0 <= i && i < uba_len(A); @*/ ;
20
21 //stores x at the ith index in A
22 void uba_set(uba_t A, int i, string x)
23 /*@requires A != NULL;   @*/
24 /*@requires 0 <= i && i < uba_len(A); @*/ ;
25
26 //adds a new element at the end in A
27 void uba_add(uba_t A, string x)
28 /*@requires A != NULL; @*/ ;
29
30 //removes the last element from A
31 string uba_rem(uba_t A)
32 /*@requires A != NULL;   @*/
33 /*@requires 0 < uba_len(A); @*/ ;
34
35 // bonus function
36 void uba_print(uba_t A)
37 /*@requires A != NULL;   @*/ ;

```

The functions `uba_add` and `uba_rem` are new as compared to the interface of a self-sorting array (**SSA**). One major difference in the function `uba_set` is that we no longer keep the array sorted.

Implementation (Library Side View)

The following functions are library only functions which help in checking the UBA invariants.

Exercise: Go through the functions and write the invariants as mathematical statements.

```

1 | bool is_array_expected_length(string[] A, int length) {
2 |     //@assert \length(A) == length;
3 |     return true;
4 | }
5 |
6 | bool is_uba(uba* A) {
7 |     return A != NULL
8 |         && 0 <= A->size && A->size < A->limit
9 |         && is_array_expected_length(A->data, A->limit);
10 | }

```

The following functions are similar to SSA.

```

1 | int uba_len(uba* A)
2 |     //@requires is_uba(A);
3 |     //@ensures 0 <= \result && \result < \length(A->data);
4 | {
5 |     return A->size;
6 | }
7 |
8 | string uba_get(uba* A, int i)
9 |     //@requires is_uba(A);
10 |    //@requires 0 <= i && i < uba_len(A);
11 | {
12 |     return A->data[i];
13 | }
14 |
15 | void uba_set(uba* A, int i, string x)
16 |     //@requires is_uba(A);
17 |     //@requires 0 <= i && i < uba_len(A);
18 |     //@ensures is_uba(A);
19 | {
20 |     A->data[i] = x;
21 | }

```

Creating a new UBA

The following function creates a UBA with given initial size. An explanation about line 7 follows after the code.

```

1 | uba* uba_new(int size)
2 | //@requires 0 <= size;
3 | //@ensures is_uba(\result);
4 | //@ensures uba_len(\result) == size;
5 | {
6 |     uba* A = alloc(uba);
7 |     int limit = size == 0 ? 1 : size*2;
8 |     A->data = alloc_array(string, limit);
9 |     A->size = size;
10 |    A->limit = limit;
11 |
12 |    return A;
13 | }

```

Ternary Conditional Operator

It uses the ternary conditional operator `?:` on line 7. The conditional operator is of the form

```

1 | variable = Expression1 ? Expression2 : Expression3

```

It can be visualized as an if-else statement as follows:

```

1 | if(Expression1)
2 | {
3 |     variable = Expression2;
4 | }
5 | else
6 | {
7 |     variable = Expression3;
8 | }

```

Since the operator `?:` takes three operands to work, it is called as a ternary operator.

Exercise: Write Line 7 in function `uba_new` as an if-else statement.

Adding New Elements at the end of UBA

For the `uba_add` function we need a library side helper function `uba_resize` which resizes the `data` array if array capacity is reached.

```

1 void uba_resize(uba* A, int new_limit)
2 /* A may not be a valid array since A->size == A->limit is possible! */
3 //@requires A != NULL;
4 //@requires 0 <= A->size && A->size < new_limit;
5 //@requires \length(A->data) == A->limit;
6 //@ensures is_uba(A);
7 {
8     string[] B = alloc_array(string, new_limit);
9
10    //copy elements of A->data into B.
11    for (int i = 0; i < A->size; i++)
12        //@loop_invariant 0 <= i;
13        {
14            B[i] = A->data[i];
15        }
16
17    //update limit
18    A->limit = new_limit;
19
20    //set data to be the new larger array B.
21    A->data = B;
22 }
23
24 void uba_add(uba* A, string x)
25 //@requires is_uba(A);
26 //@ensures is_uba(A);
27 {
28     //put x at the last location.
29     A->data[A->size] = x;
30     (A->size)++; //one item more in A
31
32     //is the array full?
33     if (A->size < A->limit) return;
34
35     //if the array requires too much memory, then halt the program.
36     //the following non-contract function is also present in C.
37     assert(A->limit <= int_max() / 2); // Fail if array would get too big
38
39     //assertion above holds, therefore safe to create a bigger array.
40     uba_resize(A, A->limit * 2);
41 }

```

Rest of the functions

```
1 string uba_rem(uba* A)
2 //@requires is_uba(A);
3 //@requires 0 < uba_len(A);
4 //@ensures is_uba(A);
5 {
6     (A->size)--;
7     string x = A->data[A->size];
8
9     if (A->limit >= 4 && A->size <= A->limit / 4)
10         uba_resize(A, A->limit / 2);
11
12     return x;
13 }
14
15 void uba_print(uba* A)
16 //@requires is_uba(A);
17 {
18     print("[");
19     for (int i = 0; i < A->size; i++)
20     {
21         print(A->data[i]);
22         if (i+1 != A->size) print(", ");
23     }
24     print("]");
25 }
26
27 // Client type
28 typedef uba* uba_t;
```