

# Review

**Problem 1:** Input a 3x4 matrix of your choice, display it in nice matrix form, then RREF it and display the reduced form nicely. See Mathematica Homework 2 for help.

**Problem 2:** Using your 3x4 matrix from above, pick off the 1st column, the 2nd row, and the 3-4 entry. Again, see Mathematica Homework 2 for help.

```
In[ ]:= A={{1,8,9,2},{5,3,8,7},{3,6,1,4}}  
MatrixForm[A]  
MatrixForm[RowReduce[A]]
```

```
Out[ ]= { {1, 8, 9, 2}, {5, 3, 8, 7}, {3, 6, 1, 4} }
```

```
Out[ ]//MatrixForm=  

$$\begin{pmatrix} 1 & 8 & 9 & 2 \\ 5 & 3 & 8 & 7 \\ 3 & 6 & 1 & 4 \end{pmatrix}$$

```

```
Out[ ]//MatrixForm=  

$$\begin{pmatrix} 1 & 0 & 0 & \frac{95}{74} \\ 0 & 1 & 0 & \frac{1}{74} \\ 0 & 0 & 1 & \frac{5}{74} \end{pmatrix}$$

```

```
In[ ]:= A[[All,1]]  
A[[2,All]]  
A[[3,4]]
```

```
Out[ ]= {1, 5, 3}
```

```
Out[ ]= {5, 3, 8, 7}
```

```
Out[ ]= 4
```

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⋮ Thread: Objects of unequal length in {1, 2, 3} + {7, 8} cannot be combined. ⓘ

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... Solve: Equations may not give solutions for all "solve" variables. [i](#)

## Exercises

1. Do Problems 1-2 above.

2. Let A be the matrix:  $\{\{0,0,2,2,4\},\{0,1,2,4,8\},\{1,2,1,2,1\},\{1,2,4,5,7\}\}$

```
In[ ]:= A={ {0,0,2,2,4}, {0,1,2,4,8}, {1,2,1,2,1}, {1,2,4,5,7} }
        u={0,0,0,0}
        v={1,1,1,1}
```

```
Out[ ]:= { {0, 0, 2, 2, 4}, {0, 1, 2, 4, 8}, {1, 2, 1, 2, 1}, {1, 2, 4, 5, 7} }
```

```
Out[ ]:= {0, 0, 0, 0}
```

```
Out[ ]:= {1, 1, 1, 1}
```

2.1. Input the matrix and name it A.

2.2. Input the vectors  $u=[0,0,0,0]$  and  $v=[1,1,1,1]$ .

2.3. Append vector u to A as a column vector and call the new matrix Au. Do the same for v, calling the appended matrix Av.

```
In[ ]:= Au = Transpose[Append[Transpose[A], u]]
Av = Transpose[Append[Transpose[A], v]]
MatrixForm[RowReduce[Au]]
MatrixForm[RowReduce[Av]]
```

```
Out[ ]= {{0, 0, 2, 2, 4, 0}, {0, 1, 2, 4, 8, 0}, {1, 2, 1, 2, 1, 0}, {1, 2, 4, 5, 7, 0}}
```

```
Out[ ]= {{0, 0, 2, 2, 4, 1}, {0, 1, 2, 4, 8, 1}, {1, 2, 1, 2, 1, 1}, {1, 2, 4, 5, 7, 1}}
```

```
Out[ ]//MatrixForm=
```

$$\begin{pmatrix} 1 & 0 & 0 & -3 & -9 & 0 \\ 0 & 1 & 0 & 2 & 4 & 0 \\ 0 & 0 & 1 & 1 & 2 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

```
Out[ ]//MatrixForm=
```

$$\begin{pmatrix} 1 & 0 & 0 & -3 & -9 & 0 \\ 0 & 1 & 0 & 2 & 4 & 0 \\ 0 & 0 & 1 & 1 & 2 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}$$

**2.4.** Use RowReduce to RREF the matrices Au and Av.

**2.5.** Describe the solution sets to the augmented systems  $[A|u]$  and  $[A|v]$  algebraically.

The augmented system  $[A|u]$  has two free variables,  $x_4$  and  $x_5$ . The only solution is the trivial solution, meaning that this system is linearly independent.

The augmented system  $[A|v]$  also has  $x_4$  and  $x_5$  as free variables. Because the bottom row shows  $0=1$ , the system is inconsistent and cannot be solved.

**3.** Use File-Save As... to save your file as a **pdf**, then upload just the solutions to the exercises above to Moodle.