

# Algorithms and data structures 5: Matricies-2 (end of lection)

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## When solution exists?: rank

Lets multiply  $m$ -row by  $n$ -column, we get  $M(m, n, R)$  matrix. This is rank 1 matrix.

**Def:** Tensor rank — minimum number of rank 1 matrices to sum.

**Def:** Column/Row rank — number of linear independent columns/rows.

( $v_1, \dots, v_n$  are linear dependent if  $v_1 \in \langle v_2, \dots, v_n \rangle$ )

Both defs are equal in case of  $\mathbb{R}$ ..

- We need  $rkA = n$

# When solution exists?: $\det$

**Def:** Invariant up to primitive operations

**Def:** (Minor definition)

And both defs are equal.

- ▶ We need  $\det A \neq 0$ .

# Strassen matrix multiply

# Summary

- ▶ Different parts of maths operate similar constructions
- ▶ This can be encapsulated in matrix theory
- ▶ We defined several operations on matrices
- ▶ Also we defined one decomposition

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