Topics in Algebra (Sample Quiz)

Date: May 1, 2019. Name:

Let N = 11. The genus of $X_1(N)$ is one.

- 1. List representatives for the orbits of $\Gamma_1(N)$ acting on $\mathbb{P}^1(\mathbb{Q})$.
- 2. Among the representatives listed above, determine which one is equivalent to $\frac{8}{9}$.
- 3. Compute the dimensions of $H^1_{\text{cusp}}(\Gamma_1(N), L_{k-2}(\mathbb{Q}))$ for k = 2, 4.

| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
|----|---|---|---|---|---|---|---|---|---|---|----|
| 0 | | | | | | | | | | | |
| 1 | | | | | | | | | | | |
| 2 | | | | | | | | | | | |
| 3 | | | | | | | | | | | |
| 4 | | | | | | | | | | | |
| 5 | | | | | | | | | | | |
| 6 | | | | | | | | | | | |
| 7 | | | | | | | | | | | |
| 8 | | | | | | | | | | | |
| 9 | | | | | | | | | | | |
| 10 | | | | | | | | | | | |

You may use http://cmfs.lmfdb.xyz to check your answer. Note that they display dimensions over \mathbb{C} .