Optimization for Fully Connected Networks

In this notebook, we will implement different optimization rules for gradient descent. We have provided starter code; however, you will need to copy and paste your code from your implementation of the modular fully connected nets in HW #3 to build upon this.

CS231n has built a solid API for building these modular frameworks and training them, and we will use their very well implemented framework as opposed to "reinventing the wheel." This includes using their Solver, various utility functions, and their layer structure. This also includes nndl.fc_net, nndl.layers, and nndl.layer_utils. As in prior assignments, we thank Serena Yeung & Justin Johnson for permission to use code written for the CS 231n class (cs231n.stanford.edu).

```
## Import and setups
import time
import numpy as np
import matplotlib.pyplot as plt
from nndl.fc net import *
from utils.data utils import get CIFAR10 data
from utils.gradient_check import eval_numerical_gradient,
eval numerical gradient array
from utils.solver import Solver
%matplotlib inline
plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of
plt.rcParams['image.interpolation'] = 'nearest'
plt.rcParams['image.cmap'] = 'gray'
# for auto-reloading external modules
# see http://stackoverflow.com/questions/1907993/autoreload-of-
modules-in-ipython
%load ext autoreload
%autoreload 2
def rel error(x, y):
  """ returns relative error """
  return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) +
np.abs(y)))
# Load the (preprocessed) CIFAR10 data.
data = get CIFAR10 data()
for k in data.keys():
  print('{}: {} '.format(k, data[k].shape))
X train: (49000, 3, 32, 32)
y train: (49000,)
X val: (1000, 3, 32, 32)
```

```
y_val: (1000,)
X_test: (1000, 3, 32, 32)
y_test: (1000,)
```

Building upon your HW #3 implementation

Copy and paste the following functions from your HW #3 implementation of a modular FC net:

- affine_forward in nndl/layers.py
- affine_backward in nndl/layers.py
- relu_forward in nndl/layers.py
- relu_backward in nndl/layers.py
- affine relu forward in nndl/layer utils.py
- affine relu backwardin nndl/layer utils.py
- The FullyConnectedNet class in nndl/fc net.py

Test all functions you copy and pasted

```
from nndl.layer tests import *
affine forward test(); print('\n')
affine backward_test(); print('\n')
relu forward test(); print('\n')
relu backward test(); print('\n')
affine relu test(); print('\n')
fc net test()
If affine_forward function is working, difference should be less than
difference: 9.769849468192957e-10
If affine backward is working, error should be less than 1e-9::
dx error: 6.501491362954244e-10
dw error: 4.064162742661063e-11
db error: 7.414168664595107e-12
If relu forward function is working, difference should be around 1e-8:
difference: 4.999999798022158e-08
If relu_forward function is working, error should be less than 1e-9:
dx error: 3.275618457618382e-12
If affine relu forward and affine relu backward are working, error
should be less than 1e-9::
dx error: 1.105662793138624e-10
```

```
dw error: 7.3374048856773584e-09
db error: 4.1311479701329975e-10
Running check with reg = 0
Initial loss: 2.305869793849734
W1 relative error: 3.0804139558156004e-08
W2 relative error: 2.3778256029777398e-07
W3 relative error: 3.932763146842659e-08
bl relative error: 5.829911539522352e-09
b2 relative error: 1.8234759836310827e-09
b3 relative error: 9.364774879700393e-11
Running check with reg = 3.14
Initial loss: 6.9548560863228746
W1 relative error: 1.5041175033511533e-08
W2 relative error: 1.8533372309838707e-07
W3 relative error: 3.341534664182953e-08
b1 relative error: 2.98185923243827e-08
b2 relative error: 9.287729904632382e-09
b3 relative error: 2.092220967523909e-10
```

Training a larger model

In general, proceeding with vanilla stochastic gradient descent to optimize models may be fraught with problems and limitations, as discussed in class. Thus, we implement optimizers that improve on SGD.

SGD + momentum

In the following section, implement SGD with momentum. Read the nndl/optim.py API, which is provided by CS231n, and be sure you understand it. After, implement sgd_momentum in nndl/optim.py. Test your implementation of sgd_momentum by running the cell below.

```
11)
  [ 1.14244211,
                1.20923158, 1.27602105,
                                         1.34281053,
                                                       1.4096
expected velocity = np.asarray([
  [0.5406,
                0.55475789, 0.56891579, 0.58307368,
                                                      0.59723158],
  [ 0.61138947,
               0.62554737, 0.63970526, 0.65386316,
                                                       0.66802105],
  [ 0.68217895, 0.69633684, 0.71049474,
                                          0.72465263,
                                                       0.73881053],
  [ 0.75296842, 0.76712632, 0.78128421,
                                          0.79544211,
                                                       0.8096
                                                                 ]])
print('next w error: {}'.format(rel error(next w, expected next w)))
print('velocity error: {}'.format(rel_error(expected_velocity,
config['velocity'])))
next w error: 8.882347033505819e-09
velocity error: 4.269287743278663e-09
```

SGD + Nesterov momentum

Implement sgd_nesterov_momentum in ndl/optim.py.

```
from nndl.optim import sqd nesterov momentum
N, D = 4, 5
w = np.linspace(-0.4, 0.6, num=N*D).reshape(N, D)
dw = np.linspace(-0.6, 0.4, num=N*D).reshape(N, D)
v = np.linspace(0.6, 0.9, num=N*D).reshape(N, D)
config = {'learning_rate': 1e-3, 'velocity': v}
next_w, _ = sgd_nesterov_momentum(w, dw, config=config)
expected next w = np.asarray([
  [0.08714,
                 0.15246105,
                              0.21778211,
                                           0.28310316,
                                                        0.34842421],
                              0.54438737,
  [0.41374526,
                 0.47906632,
                                           0.60970842,
                                                        0.67502947],
  [0.74035053,
                 0.80567158,
                              0.87099263,
                                           0.93631368.
                                                        1.00163474],
  [1.06695579,
                 1.13227684,
                                                        1.32824
                                                                  ]])
                              1.19759789,
                                           1.26291895,
expected velocity = np.asarray([
  [0.5406,
                0.55475789, 0.56891579,
                                           0.58307368,
                                                        0.59723158],
  [ 0.61138947, 0.62554737, 0.63970526,
                                           0.65386316,
                                                        0.66802105],
  [ 0.68217895, 0.69633684, 0.71049474,
                                           0.72465263,
                                                        0.738810531.
  [ 0.75296842, 0.76712632, 0.78128421,
                                           0.79544211,
                                                        0.8096
                                                                  11)
print('next w error: {}'.format(rel error(next w, expected next w)))
print('velocity error: {}'.format(rel_error(expected_velocity,
config['velocity'])))
next w error: 1.0875187099974104e-08
velocity error: 4.269287743278663e-09
```

Evaluating SGD, SGD+Momentum, and SGD+NesterovMomentum

Run the following cell to train a 6 layer FC net with SGD, SGD+momentum, and SGD+Nesterov momentum. You should see that SGD+momentum achieves a better loss than SGD, and that SGD+Nesterov momentum achieves a slightly better loss (and training accuracy) than SGD+momentum.

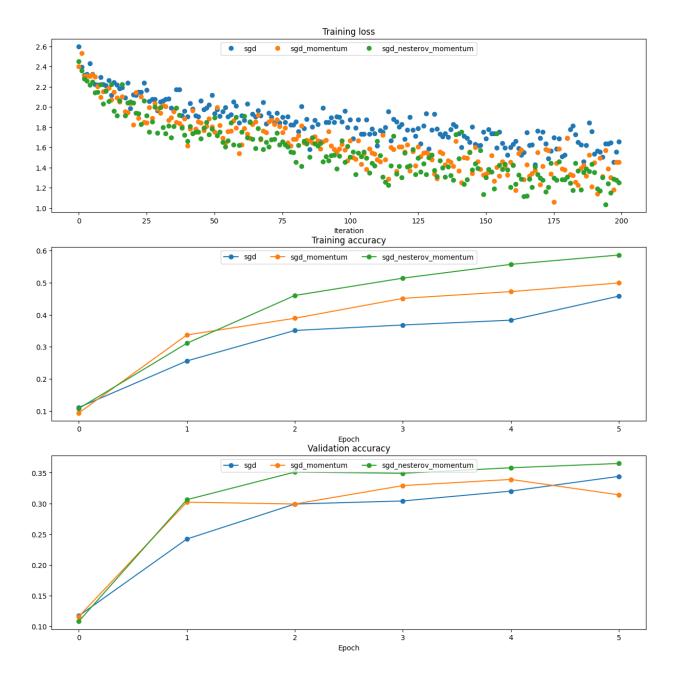
```
num train = 4000
small data = {
  'X train': data['X train'][:num train],
  'y_train': data['y_train'][:num_train],
  'X val': data['X val'],
  'y_val': data['y_val'],
solvers = {}
for update rule in ['sqd', 'sqd momentum', 'sqd nesterov momentum']:
  print('Optimizing with {}'.format(update rule))
  model = FullyConnectedNet([100, 100, 100, 100, 100],
weight scale=5e-2)
  solver = Solver(model, small data,
                  num epochs=5, batch size=100,
                  update rule=update rule,
                  optim config={
                    'learning rate': 1e-2,
                  },
                  verbose=False)
  solvers[update rule] = solver
  solver.train()
  print
plt.subplot(3, 1, 1)
plt.title('Training loss')
plt.xlabel('Iteration')
plt.subplot(3, 1, 2)
plt.title('Training accuracy')
plt.xlabel('Epoch')
plt.subplot(3, 1, 3)
plt.title('Validation accuracy')
plt.xlabel('Epoch')
for update_rule, solver in solvers.items():
  plt.subplot(3, 1, 1)
  plt.plot(solver.loss history, 'o', label=update rule)
```

```
plt.subplot(3, 1, 2)
plt.plot(solver.train_acc_history, '-o', label=update_rule)

plt.subplot(3, 1, 3)
plt.plot(solver.val_acc_history, '-o', label=update_rule)

for i in [1, 2, 3]:
   plt.subplot(3, 1, i)
   plt.legend(loc='upper center', ncol=4)
plt.gcf().set_size_inches(15, 15)
plt.show()

Optimizing with sgd
Optimizing with sgd_momentum
Optimizing with sgd_nesterov_momentum
```



RMSProp

Now we go to techniques that adapt the gradient. Implement rmsprop in nndl/optim.py. Test your implementation by running the cell below.

```
from nndl.optim import rmsprop

N, D = 4, 5
w = np.linspace(-0.4, 0.6, num=N*D).reshape(N, D)
dw = np.linspace(-0.6, 0.4, num=N*D).reshape(N, D)
a = np.linspace(0.6, 0.9, num=N*D).reshape(N, D)
```

```
config = {'learning rate': le-2, 'a': a}
next_w, _ = rmsprop(w, dw, config=config)
expected next w = np.asarray([
  [-0.39223849, -0.34037513, -0.28849239, -0.23659121, -0.18467247],
  [-0.132737,
                -0.08078555, -0.02881884,
                                           0.02316247,
                                                        0.07515774],
  [ 0.12716641, 0.17918792, 0.23122175,
                                           0.28326742,
                                                        0.33532447],
  [ 0.38739248, 0.43947102,
                              0.49155973,
                                           0.54365823,
                                                       0.59576619]])
expected cache = np.asarray([
  [ 0.5976,
                0.6126277,
                             0.6277108,
                                           0.64284931,
                                                        0.65804321],
  [ 0.67329252,
               0.68859723, 0.70395734,
                                                        0.73484377],
                                           0.71937285,
  [ 0.75037008, 0.7659518,
                                           0.79728144,
                             0.78158892,
                                                        0.81302936],
                            0.86060554,
                                                                  11)
  [ 0.82883269, 0.84469141,
                                           0.87657507, 0.8926
print('next w error: {}'.format(rel error(expected next w, next w)))
print('cache error: {}'.format(rel_error(expected_cache,
config['a'])))
next w error: 9.524687511038133e-08
cache error: 2.6477955807156126e-09
```

Adaptive moments

Now, implement adam in nndl/optim.py. Test your implementation by running the cell below.

```
# Test Adam implementation; you should see errors around 1e-7 or less
from nndl.optim import adam
N, D = 4, 5
w = np.linspace(-0.4, 0.6, num=N*D).reshape(N, D)
dw = np.linspace(-0.6, 0.4, num=N*D).reshape(N, D)
v = np.linspace(0.6, 0.9, num=N*D).reshape(N, D)
a = np.linspace(0.7, 0.5, num=N*D).reshape(N, D)
config = {'learning rate': 1e-2, 'v': v, 'a': a, 't': 5}
next_w, _ = adam(w, dw, config=config)
expected next w = np.asarray([
  [-0.40094747, -0.34836187, -0.29577703, -0.24319299, -0.19060977],
                                           0.01971428,
  [-0.1380274, -0.08544591, -0.03286534,
                                                        0.07229291,
  [ 0.1248705,
               0.17744702, 0.23002243,
                                           0.28259667,
                                                        0.33516969],
  [ 0.38774145,
               0.44031188.
                             0.49288093,
                                           0.54544852,
                                                       0.59801459]])
expected a = np.asarray([
  [0.69966,
                 0.68908382, 0.67851319,
                                           0.66794809,
                                                        0.65738853,],
                                           0.61520571,
  [ 0.64683452, 0.63628604, 0.6257431,
                                                        0.60467385,],
  [ 0.59414753, 0.58362676, 0.57311152,
                                           0.56260183,
                                                        0.55209767,],
  [ 0.54159906, 0.53110598,
                             0.52061845,
                                           0.51013645,
                                                        0.49966,
                                                                   ]])
```

```
expected v = np.asarray([
             0.49947368, 0.51894737,
  0.48,
                                          0.53842105, 0.55789474],
  [ 0.57736842, 0.59684211,
                             0.61631579,
                                          0.63578947, 0.65526316],
  [ 0.67473684, 0.69421053, 0.71368421,
                                          0.73315789.
                                                       0.752631581.
  [ 0.77210526, 0.79157895,
                             0.81105263,
                                          0.83052632, 0.85
                                                                 11)
print('next_w error: {}'.format(rel_error(expected_next_w, next_w)))
print('a error: {}'.format(rel error(expected a, config['a'])))
print('v error: {}'.format(rel_error(expected_v, config['v'])))
next w error: 1.1395691798535431e-07
a error: 4.208314038113071e-09
v error: 4.214963193114416e-09
```

Comparing SGD, SGD+NesterovMomentum, RMSProp, and Adam

The following code will compare optimization with SGD, Momentum, Nesterov Momentum, RMSProp and Adam. In our code, we find that RMSProp, Adam, and SGD + Nesterov Momentum achieve approximately the same training error after a few training epochs.

```
learning rates = {'rmsprop': 2e-4, 'adam': 1e-3}
for update rule in ['adam', 'rmsprop']:
  print('Optimizing with {}'.format(update rule))
  model = FullyConnectedNet([100, 100, 100, 100, 100],
weight scale=5e-2)
  solver = Solver(model, small data,
                  num epochs=5, batch size=100,
                  update rule=update rule,
                  optim config={
                    'learning rate': learning rates[update rule]
                  verbose=False)
  solvers[update rule] = solver
  solver.train()
  print
plt.subplot(3, 1, 1)
plt.title('Training loss')
plt.xlabel('Iteration')
plt.subplot(3, 1, 2)
plt.title('Training accuracy')
plt.xlabel('Epoch')
plt.subplot(3, 1, 3)
plt.title('Validation accuracy')
```

```
plt.xlabel('Epoch')

for update_rule, solver in solvers.items():
    plt.subplot(3, 1, 1)
    plt.plot(solver.loss_history, 'o', label=update_rule)

plt.subplot(3, 1, 2)
    plt.plot(solver.train_acc_history, '-o', label=update_rule)

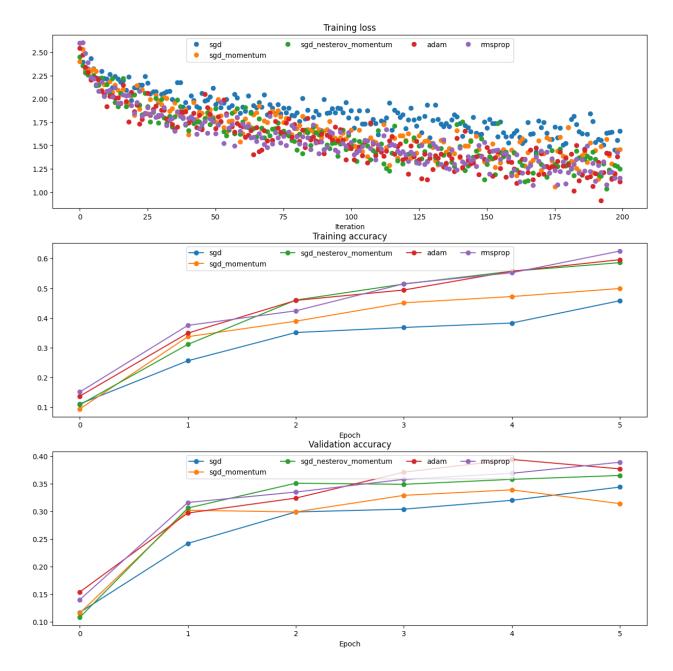
plt.subplot(3, 1, 3)
    plt.plot(solver.val_acc_history, '-o', label=update_rule)

for i in [1, 2, 3]:
    plt.subplot(3, 1, i)
    plt.legend(loc='upper center', ncol=4)

plt.gcf().set_size_inches(15, 15)

plt.show()

Optimizing with adam
Optimizing with rmsprop
```



Easier optimization

In the following cell, we'll train a 4 layer neural network having 500 units in each hidden layer with the different optimizers, and find that it is far easier to get up to 50+% performance on CIFAR-10. After we implement batchnorm and dropout, we'll ask you to get 55+% on CIFAR-10.

```
optimizer = 'adam'
best_model = None

layer_dims = [500, 500, 500]
weight_scale = 0.01
```

```
learning rate = 1e-3
lr decay = 0.9
model = FullyConnectedNet(layer dims, weight scale=weight scale,
                          use batchnorm=True)
solver = Solver(model, data,
                num epochs=10, batch size=100,
                update rule=optimizer,
                optim config={
                  'learning rate': learning rate,
                lr decay=lr decay,
                verbose=True, print every=50)
solver.train()
(Iteration 1 / 4900) loss: 2.320216
(Epoch 0 / 10) train acc: 0.201000; val acc: 0.215000
(Iteration 51 / 4900) loss: 1.802697
(Iteration 101 / 4900) loss: 1.839267
(Iteration 151 / 4900) loss: 1.642738
(Iteration 201 / 4900) loss: 1.675290
(Iteration 251 / 4900) loss: 1.674492
(Iteration 301 / 4900) loss: 1.422024
(Iteration 351 / 4900) loss: 1.485432
(Iteration 401 / 4900) loss: 1.482620
(Iteration 451 / 4900) loss: 1.431989
(Epoch 1 / 10) train acc: 0.482000; val acc: 0.478000
(Iteration 501 / 4900) loss: 1.520223
(Iteration 551 / 4900) loss: 1.412681
(Iteration 601 / 4900) loss: 1.211547
(Iteration 651 / 4900) loss: 1.431844
(Iteration 701 / 4900) loss: 1.455634
(Iteration 751 / 4900) loss: 1.300787
(Iteration 801 / 4900) loss: 1.336608
(Iteration 851 / 4900) loss: 1.292135
(Iteration 901 / 4900) loss: 1.313295
(Iteration 951 / 4900) loss: 1.579138
(Epoch 2 / 10) train acc: 0.580000; val_acc: 0.515000
(Iteration 1001 / 4900) loss: 1.260819
(Iteration 1051 / 4900) loss: 1.107324
(Iteration 1101 / 4900) loss: 0.995973
(Iteration 1151 / 4900) loss: 1.258211
(Iteration 1201 / 4900) loss: 1.495768
(Iteration 1251 / 4900) loss: 1.232023
(Iteration 1301 / 4900) loss: 1.316851
(Iteration 1351 / 4900) loss: 1.124855
(Iteration 1401 / 4900) loss: 1.227120
(Iteration 1451 / 4900) loss: 1.224893
(Epoch 3 / 10) train acc: 0.625000; val acc: 0.547000
```

```
(Iteration 1501 / 4900) loss: 1.331305
(Iteration 1551 / 4900) loss: 1.248914
(Iteration 1601 / 4900) loss: 1.115145
(Iteration 1651 / 4900) loss: 1.183321
(Iteration 1701 / 4900) loss: 1.126724
(Iteration 1751 / 4900) loss: 1.120186
(Iteration 1801 / 4900) loss: 1.080077
(Iteration 1851 / 4900) loss: 0.958713
(Iteration 1901 / 4900) loss: 1.149974
(Iteration 1951 / 4900) loss: 1.206972
(Epoch 4 / 10) train acc: 0.646000; val acc: 0.540000
(Iteration 2001 / 4900) loss: 0.950351
(Iteration 2051 / 4900) loss: 0.785877
(Iteration 2101 / 4900) loss: 0.930028
(Iteration 2151 / 4900) loss: 1.078887
(Iteration 2201 / 4900) loss: 0.922855
(Iteration 2251 / 4900) loss: 1.203087
(Iteration 2301 / 4900) loss: 1.115383
(Iteration 2351 / 4900) loss: 1.043127
(Iteration 2401 / 4900) loss: 1.017699
(Epoch 5 / 10) train acc: 0.666000; val acc: 0.564000
(Iteration 2451 / 4900) loss: 1.208598
(Iteration 2501 / 4900) loss: 0.836278
(Iteration 2551 / 4900) loss: 0.963328
(Iteration 2601 / 4900) loss: 0.937147
(Iteration 2651 / 4900) loss: 0.813613
(Iteration 2701 / 4900) loss: 0.865801
(Iteration 2751 / 4900) loss: 1.139042
(Iteration 2801 / 4900) loss: 0.806744
(Iteration 2851 / 4900) loss: 0.726715
(Iteration 2901 / 4900) loss: 0.810212
(Epoch 6 / 10) train acc: 0.701000; val acc: 0.561000
(Iteration 2951 / 4900) loss: 0.848263
(Iteration 3001 / 4900) loss: 0.917435
(Iteration 3051 / 4900) loss: 0.701462
(Iteration 3101 / 4900) loss: 0.700631
(Iteration 3151 / 4900) loss: 0.718690
(Iteration 3201 / 4900) loss: 0.787667
(Iteration 3251 / 4900) loss: 0.761422
(Iteration 3301 / 4900) loss: 0.931597
(Iteration 3351 / 4900) loss: 0.949510
(Iteration 3401 / 4900) loss: 0.740956
(Epoch 7 / 10) train acc: 0.710000; val acc: 0.566000
(Iteration 3451 / 4900) loss: 0.817906
(Iteration 3501 / 4900) loss: 0.721976
(Iteration 3551 / 4900) loss: 0.736508
(Iteration 3601 / 4900) loss: 0.807700
(Iteration 3651 / 4900) loss: 0.784453
(Iteration 3701 / 4900) loss: 0.837618
```

```
(Iteration 3751 / 4900) loss: 0.610160
(Iteration 3801 / 4900) loss: 0.734950
(Iteration 3851 / 4900) loss: 0.926549
(Iteration 3901 / 4900) loss: 0.755103
(Epoch 8 / 10) train acc: 0.765000; val acc: 0.555000
(Iteration 3951 / 4900) loss: 0.592995
(Iteration 4001 / 4900) loss: 0.686560
(Iteration 4051 / 4900) loss: 0.656597
(Iteration 4101 / 4900) loss: 0.545963
(Iteration 4151 / 4900) loss: 0.672857
(Iteration 4201 / 4900) loss: 0.576171
(Iteration 4251 / 4900) loss: 0.433184
(Iteration 4301 / 4900) loss: 0.544410
(Iteration 4351 / 4900) loss: 0.595788
(Iteration 4401 / 4900) loss: 0.534230
(Epoch 9 / 10) train acc: 0.784000; val acc: 0.550000
(Iteration 4451 / 4900) loss: 0.659326
(Iteration 4501 / 4900) loss: 0.381986
(Iteration 4551 / 4900) loss: 0.709688
(Iteration 4601 / 4900) loss: 0.592681
(Iteration 4651 / 4900) loss: 0.470972
(Iteration 4701 / 4900) loss: 0.468080
(Iteration 4751 / 4900) loss: 0.854547
(Iteration 4801 / 4900) loss: 0.510759
(Iteration 4851 / 4900) loss: 0.718478
(Epoch 10 / 10) train acc: 0.783000; val acc: 0.563000
y test pred = np.argmax(model.loss(data['X test']), axis=1)
y val pred = np.argmax(model.loss(data['X val']), axis=1)
print('Validation set accuracy: {}'.format(np.mean(y val pred ==
data['y val'])))
print('Test set accuracy: {}'.format(np.mean(y test pred ==
data['y test'])))
Validation set accuracy: 0.575
Test set accuracy: 0.598
```

Batch Normalization

In this notebook, you will implement the batch normalization layers of a neural network to increase its performance. Please review the details of batch normalization from the lecture notes.

CS231n has built a solid API for building these modular frameworks and training them, and we will use their very well implemented framework as opposed to "reinventing the wheel." This includes using their Solver, various utility functions, and their layer structure. This also includes nndl.fc_net, nndl.layers, and nndl.layer_utils. As in prior assignments, we thank Serena Yeung & Justin Johnson for permission to use code written for the CS 231n class (cs231n.stanford.edu).

```
## Import and setups
import time
import numpy as np
import matplotlib.pyplot as plt
from nndl.fc net import *
from nndl.layers import *
from utils.data utils import get CIFAR10 data
from utils.gradient check import eval numerical gradient,
eval numerical gradient array
from utils.solver import Solver
%matplotlib inline
plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of
plots
plt.rcParams['image.interpolation'] = 'nearest'
plt.rcParams['image.cmap'] = 'gray'
# for auto-reloading external modules
# see http://stackoverflow.com/questions/1907993/autoreload-of-
modules-in-ipython
%load ext autoreload
%autoreload 2
def rel error(x, y):
  """ returns relative error """
  return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) +
np.abs(y)))
# Load the (preprocessed) CIFAR10 data.
data = get CIFAR10 data()
for k in data.keys():
  print('{}: {} '.format(k, data[k].shape))
```

```
X_train: (49000, 3, 32, 32)
y_train: (49000,)
X_val: (1000, 3, 32, 32)
y_val: (1000,)
X_test: (1000, 3, 32, 32)
y_test: (1000,)
```

Batchnorm forward pass

Implement the training time batchnorm forward pass, batchnorm_forward, in nndl/layers.py. After that, test your implementation by running the following cell.

```
# Check the training-time forward pass by checking means and variances
# of features both before and after batch normalization
# Simulate the forward pass for a two-layer network
N, D1, D2, D3 = 200, 50, 60, 3
X = np.random.randn(N, D1)
W1 = np.random.randn(D1, D2)
W2 = np.random.randn(D2, D3)
a = np.maximum(0, X.dot(W1)).dot(W2)
print('Before batch normalization:')
print(' means: ', a.mean(axis=0))
print(' stds: ', a.std(axis=0))
# Means should be close to zero and stds close to one
print('After batch normalization (gamma=1, beta=0)')
a_norm, _ = batchnorm_forward(a, np.ones(D3), np.zeros(D3), {'mode':
'train'})
print(' mean: ', a_norm.mean(axis=0))
print(' std: ', a norm.std(axis=0))
# Now means should be close to beta and stds close to gamma
gamma = np.asarray([1.0, 2.0, 3.0])
beta = np.asarray([11.0, 12.0, 13.0])
a norm, = batchnorm forward(a, gamma, beta, {'mode': 'train'})
print('After batch normalization (nontrivial gamma, beta)')
print(' means: ', a_norm.mean(axis=0))
print(' stds: ', a_norm.std(axis=0))
Before batch normalization:
  means: [ -4.51045011 -25.23872982 -15.39102202]
  stds: [37.43318233 29.59913505 34.08348347]
After batch normalization (gamma=1, beta=0)
  mean: [ 3.60822483e-18 2.16493490e-17 -1.07136522e-16]
  std:
        [1.
                    0.99999999 1.
After batch normalization (nontrivial gamma, beta)
```

```
means: [11. 12. 13.]
stds: [1. 1.99999999 2.99999999]
```

Implement the testing time batchnorm forward pass, batchnorm_forward, in nndl/layers.py. After that, test your implementation by running the following cell.

```
# Check the test-time forward pass by running the training-time
# forward pass many times to warm up the running averages, and then
# checking the means and variances of activations after a test-time
# forward pass.
N, D1, D2, D3 = 200, 50, 60, 3
W1 = np.random.randn(D1, D2)
W2 = np.random.randn(D2, D3)
bn param = {'mode': 'train'}
gamma = np.ones(D3)
beta = np.zeros(D3)
for t in np.arange(50):
 X = np.random.randn(N, D1)
  a = np.maximum(0, X.dot(W1)).dot(W2)
  batchnorm forward(a, gamma, beta, bn param)
bn param['mode'] = 'test'
X = np.random.randn(N, D1)
a = np.maximum(0, X.dot(W1)).dot(W2)
a norm, = batchnorm forward(a, gamma, beta, bn param)
# Means should be close to zero and stds close to one, but will be
# noisier than training-time forward passes.
print('After batch normalization (test-time):')
print(' means: ', a_norm.mean(axis=0))
print(' stds: ', a_norm.std(axis=0))
After batch normalization (test-time):
  means: [ 0.13365287 -0.05110971  0.0227401 ]
         [0.9829348 0.96158819 1.07653778]
```

Batchnorm backward pass

Implement the backward pass for the batchnorm layer, batchnorm_backward in nndl/layers.py. Check your implementation by running the following cell.

```
# Gradient check batchnorm backward pass
N, D = 4, 5
x = 5 * np.random.randn(N, D) + 12
gamma = np.random.randn(D)
beta = np.random.randn(D)
dout = np.random.randn(N, D)
```

```
bn_param = {'mode': 'train'}
fx = lambda x: batchnorm_forward(x, gamma, beta, bn_param)[0]
fg = lambda a: batchnorm_forward(x, gamma, beta, bn_param)[0]
fb = lambda b: batchnorm_forward(x, gamma, beta, bn_param)[0]

dx_num = eval_numerical_gradient_array(fx, x, dout)
da_num = eval_numerical_gradient_array(fg, gamma, dout)
db_num = eval_numerical_gradient_array(fb, beta, dout)

_, cache = batchnorm_forward(x, gamma, beta, bn_param)
dx, dgamma, dbeta = batchnorm_backward(dout, cache)
print('dx error: ', rel_error(dx_num, dx))
print('dgamma error: ', rel_error(da_num, dgamma))
print('dbeta error: ', rel_error(db_num, dbeta))

dx error: 7.398552612290057e-09
dgamma error: 3.7353060584699584e-11
dbeta error: 2.0034911289409793e-11
```

Implement a fully connected neural network with batchnorm layers

Modify the FullyConnectedNet() class in nndl/fc_net.py to incorporate batchnorm layers. You will need to modify the class in the following areas:

- (1) The gammas and betas need to be initialized to 1's and 0's respectively in __init__.
- (2) The batchnorm_forward layer needs to be inserted between each affine and relu layer (except in the output layer) in a forward pass computation in loss. You may find it helpful to write an affine_batchnorm_relu() layer in nndl/layer_utils.py although this is not necessary.
- (3) The batchnorm_backward layer has to be appropriately inserted when calculating gradients.

After you have done the appropriate modifications, check your implementation by running the following cell.

Note, while the relative error for W3 should be small, as we backprop gradients more, you may find the relative error increases. Our relative error for W1 is on the order of 1e-4.

```
N, D, H1, H2, C = 2, 15, 20, 30, 10
X = np.random.randn(N, D)
y = np.random.randint(C, size=(N,))

for reg in [0, 3.14]:
    print('Running check with reg = ', reg)
    model = FullyConnectedNet([H1, H2], input_dim=D, num_classes=C,
```

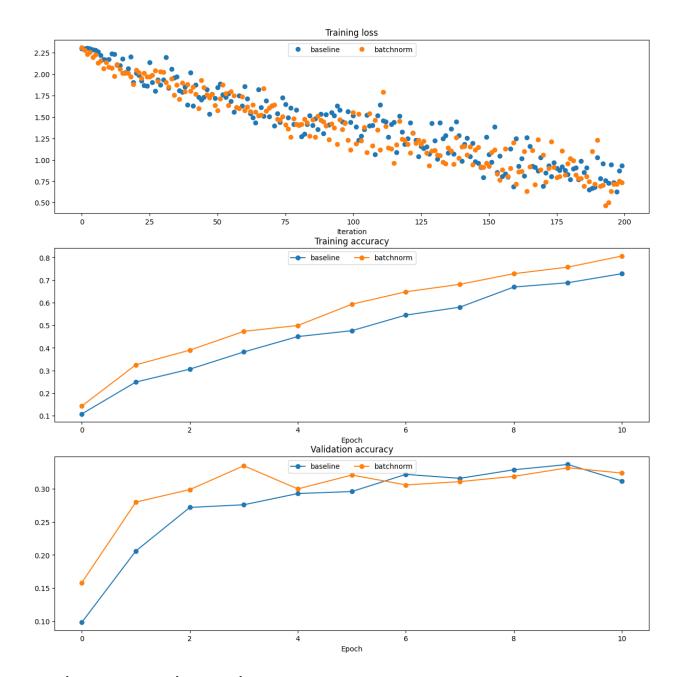
```
reg=reg, weight scale=5e-2,
dtype=np.float64,
                            use batchnorm=True)
  loss, grads = model.loss(X, y)
  print('Initial loss: ', loss)
  for name in sorted(grads):
    f = lambda : model.loss(X, y)[0]
    grad num = eval numerical gradient(f, model.params[name],
verbose=False, h=1e-5)
    print('{} relative error: {}'.format(name, rel error(grad num,
grads[name])))
  if reg == 0: print('\n')
Running check with reg = 0
Initial loss: 2.3404982120116467
W1 relative error: 2.5130849524940887e-05
W2 relative error: 1.6345099705830662e-05
W3 relative error: 4.375564261986615e-09
bl relative error: 4.440892098500626e-08
b2 relative error: 1.1102230246251565e-08
b3 relative error: 1.6613648691674668e-10
betal relative error: 7.0391977817731525e-09
beta2 relative error: 7.876860071650845e-09
gammal relative error: 7.017721124482609e-09
gamma2 relative error: 1.848686419088185e-08
Running check with reg = 3.14
Initial loss: 6.495633072163115
W1 relative error: 8.842970999879126e-07
W2 relative error: 4.140098393385853e-06
W3 relative error: 6.849233261288271e-08
b1 relative error: 4.440892098500626e-08
b2 relative error: 2.220446049250313e-08
b3 relative error: 1.5080365895775672e-10
betal relative error: 1.2132329874790447e-07
beta2 relative error: 5.149465424540515e-09
gammal relative error: 4.097745877207364e-08
gamma2 relative error: 9.13428947347349e-09
```

Training a deep fully connected network with batch normalization.

To see if batchnorm helps, let's train a deep neural network with and without batch normalization.

```
# Try training a very deep net with batchnorm
hidden dims = [100, 100, 100, 100, 100]
num train = 1000
small data = {
  'X_train': data['X_train'][:num_train],
  'y_train': data['y_train'][:num_train],
  'X val': data['X val'],
  'y_val': data['y_val'],
}
weight scale = 2e-2
bn model = FullyConnectedNet(hidden dims, weight scale=weight scale,
use batchnorm=True)
model = FullyConnectedNet(hidden dims, weight scale=weight scale,
use batchnorm=False)
bn solver = Solver(bn model, small data,
                num epochs=10, batch size=50,
                update rule='adam',
                optim config={
                  'learning rate': 1e-3,
                },
                verbose=True, print_every=200)
bn solver.train()
solver = Solver(model, small_data,
                num epochs=10, batch size=50,
                update rule='adam',
                optim config={
                  'learning rate': 1e-3,
                verbose=True, print every=200)
solver.train()
(Iteration 1 / 200) loss: 2.310554
(Epoch 0 / 10) train acc: 0.143000; val acc: 0.158000
(Epoch 1 / 10) train acc: 0.325000; val acc: 0.280000
(Epoch 2 / 10) train acc: 0.390000; val acc: 0.299000
(Epoch 3 / 10) train acc: 0.473000; val_acc: 0.335000
(Epoch 4 / 10) train acc: 0.499000; val acc: 0.300000
(Epoch 5 / 10) train acc: 0.593000; val_acc: 0.321000
(Epoch 6 / 10) train acc: 0.648000; val acc: 0.306000
(Epoch 7 / 10) train acc: 0.681000; val_acc: 0.311000
(Epoch 8 / 10) train acc: 0.728000; val acc: 0.319000
(Epoch 9 / 10) train acc: 0.757000; val acc: 0.332000
(Epoch 10 / 10) train acc: 0.806000; val_acc: 0.324000
(Iteration 1 / 200) loss: 2.302546
(Epoch 0 / 10) train acc: 0.108000; val acc: 0.098000
(Epoch 1 / 10) train acc: 0.249000; val acc: 0.206000
```

```
(Epoch 2 / 10) train acc: 0.306000; val acc: 0.272000
(Epoch 3 / 10) train acc: 0.382000; val acc: 0.276000
(Epoch 4 / 10) train acc: 0.450000; val acc: 0.293000
(Epoch 5 / 10) train acc: 0.476000; val acc: 0.296000
(Epoch 6 / 10) train acc: 0.545000; val acc: 0.322000
(Epoch 7 / 10) train acc: 0.580000; val_acc: 0.316000
(Epoch 8 / 10) train acc: 0.669000; val acc: 0.329000
(Epoch 9 / 10) train acc: 0.688000; val acc: 0.337000
(Epoch 10 / 10) train acc: 0.728000; val acc: 0.312000
plt.subplot(3, 1, 1)
plt.title('Training loss')
plt.xlabel('Iteration')
plt.subplot(3, 1, 2)
plt.title('Training accuracy')
plt.xlabel('Epoch')
plt.subplot(3, 1, 3)
plt.title('Validation accuracy')
plt.xlabel('Epoch')
plt.subplot(3, 1, 1)
plt.plot(solver.loss_history, 'o', label='baseline')
plt.plot(bn_solver.loss_history, 'o', label='batchnorm')
plt.subplot(3, 1, 2)
plt.plot(solver.train_acc_history, '-o', label='baseline')
plt.plot(bn solver.train acc history, '-o', label='batchnorm')
plt.subplot(3, 1, 3)
plt.plot(solver.val_acc_history, '-o', label='baseline')
plt.plot(bn_solver.val_acc_history, '-o', label='batchnorm')
for i in [1, 2, 3]:
  plt.subplot(3, 1, i)
  plt.legend(loc='upper center', ncol=4)
plt.gcf().set size inches(15, 15)
plt.show()
```



Batchnorm and initialization

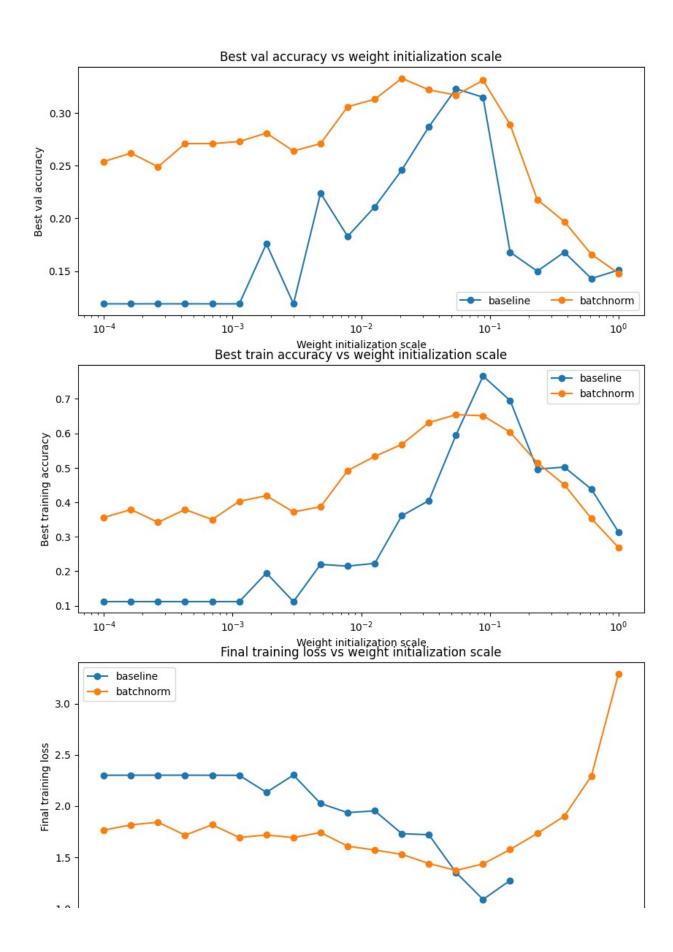
The following cells run an experiment where for a deep network, the initialization is varied. We do training for when batchnorm layers are and are not included.

```
# Try training a very deep net with batchnorm
hidden_dims = [50, 50, 50, 50, 50, 50]

num_train = 1000
small_data = {
  'X_train': data['X_train'][:num_train],
```

```
'y_train': data['y_train'][:num_train],
  'X val': data['X val'],
  'y_val': data['y val'],
bn solvers = \{\}
solvers = {}
weight scales = np.logspace(-4, 0, num=20)
for i, weight scale in enumerate(weight scales):
  print('Running weight scale {} / {}'.format(i + 1,
len(weight scales)))
  bn model = FullyConnectedNet(hidden dims, weight scale=weight scale,
use batchnorm=True)
  model = FullyConnectedNet(hidden dims, weight scale=weight scale,
use batchnorm=False)
  bn solver = Solver(bn model, small data,
                  num epochs=10, batch size=50,
                  update rule='adam',
                  optim config={
                    'learning rate': 1e-3,
                  verbose=False, print every=200)
  bn solver.train()
  bn solvers[weight scale] = bn solver
  solver = Solver(model, small data,
                  num epochs=10, batch size=50,
                  update rule='adam',
                  optim config={
                    'learning rate': 1e-3,
                  verbose=False, print every=200)
  solver.train()
  solvers[weight scale] = solver
Running weight scale 1 / 20
Running weight scale 2 / 20
# Plot results of weight scale experiment
best train accs, bn best train accs = [], []
best val accs, bn best val accs = [], []
final train loss, bn_final_train_loss = [], []
for ws in weight scales:
  best train accs.append(max(solvers[ws].train_acc_history))
  bn best train accs.append(max(bn solvers[ws].train acc history))
  best val accs.append(max(solvers[ws].val acc history))
  bn best val accs.append(max(bn solvers[ws].val acc history))
```

```
final train loss.append(np.mean(solvers[ws].loss history[-100:]))
  bn final train loss.append(np.mean(bn solvers[ws].loss history[-
100:\bar{1}))
plt.subplot(3, 1, 1)
plt.title('Best val accuracy vs weight initialization scale')
plt.xlabel('Weight initialization scale')
plt.ylabel('Best val accuracy')
plt.semilogx(weight scales, best val accs, '-o', label='baseline')
plt.semilogx(weight_scales, bn_best_val_accs, '-o', label='batchnorm')
plt.legend(ncol=2, loc='lower right')
plt.subplot(3, 1, 2)
plt.title('Best train accuracy vs weight initialization scale')
plt.xlabel('Weight initialization scale')
plt.ylabel('Best training accuracy')
plt.semilogx(weight scales, best train accs, '-o', label='baseline')
plt.semilogx(weight scales, bn best train accs, '-o',
label='batchnorm')
plt.legend()
plt.subplot(3, 1, 3)
plt.title('Final training loss vs weight initialization scale')
plt.xlabel('Weight initialization scale')
plt.ylabel('Final training loss')
plt.semilogx(weight scales, final train loss, '-o', label='baseline')
plt.semilogx(weight scales, bn final train loss, '-o',
label='batchnorm')
plt.legend()
plt.gcf().set size inches(10, 15)
plt.show()
```



Question:

In the cell below, summarize the findings of this experiment, and WHY these results make sense.

Answer:

Batch normalization helps make training neural networks easier and more reliable. One big advantage is that it makes the model less picky about how the starting weights are set. When you look at pictures of models with and without batch normalization, you can see that the ones with it look smoother and steadier. For example, in one case, the final training loss of a model with batch normalization stays pretty much the same, no matter how the weights are set at the beginning. But without batch normalization, the loss can jump around a lot, especially when the weights start around 0.095. Batch normalization keeps the training process more consistent, making it easier for the model to learn well no matter how it starts. So, it's a helpful tool for making neural networks more reliable and easier to work with.

Dropout

In this notebook, you will implement dropout. Then we will ask you to train a network with batchnorm and dropout, and acheive over 55% accuracy on CIFAR-10.

CS231n has built a solid API for building these modular frameworks and training them, and we will use their very well implemented framework as opposed to "reinventing the wheel." This includes using their Solver, various utility functions, and their layer structure. This also includes nndl.fc_net, nndl.layers, and nndl.layer_utils. As in prior assignments, we thank Serena Yeung & Justin Johnson for permission to use code written for the CS 231n class (cs231n.stanford.edu).

```
## Import and setups
import time
import numpy as np
import matplotlib.pyplot as plt
from nndl.fc net import *
from nndl.layers import *
from utils.data utils import get CIFAR10 data
from utils.gradient check import eval numerical gradient,
eval numerical gradient array
from utils.solver import Solver
%matplotlib inline
plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of
plots
plt.rcParams['image.interpolation'] = 'nearest'
plt.rcParams['image.cmap'] = 'gray'
# for auto-reloading external modules
# see http://stackoverflow.com/questions/1907993/autoreload-of-
modules-in-ipython
%load ext autoreload
%autoreload 2
def rel error(x, y):
  """ returns relative error """
  return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) +
np.abs(y)))
# Load the (preprocessed) CIFAR10 data.
data = get CIFAR10 data()
for k in data.keys():
  print('{}: {} '.format(k, data[k].shape))
X train: (49000, 3, 32, 32)
y train: (49000,)
```

```
X_val: (1000, 3, 32, 32)
y_val: (1000,)
X_test: (1000, 3, 32, 32)
y_test: (1000,)
```

Dropout forward pass

Implement the training and test time dropout forward pass, dropout_forward, in nndl/layers.py. After that, test your implementation by running the following cell.

```
x = np.random.randn(500, 500) + 10
for p in [0.3, 0.6, 0.75]:
  out, = dropout forward(x, {'mode': 'train', 'p': p})
  out_test, _ = dropout_forward(x, {'mode': 'test', 'p': p})
  print('Running tests with p = ', p)
  print('Mean of input: ', x.mean())
  print('Mean of train-time output: ', out.mean())
  print('Mean of test-time output: ', out_test.mean())
  print('Fraction of train-time output set to zero: ', (out ==
0).mean())
  print('Fraction of test-time output set to zero: ', (out test ==
0).mean())
Running tests with p = 0.3
Mean of input: 10.000972387639752
Mean of train-time output: 10.001491307235057
Mean of test-time output: 10.000972387639752
Fraction of train-time output set to zero: 0.70006
Fraction of test-time output set to zero: 0.0
Running tests with p = 0.6
Mean of input:
               10.000972387639752
Mean of train-time output: 9.989596249687274
Mean of test-time output: 10.000972387639752
Fraction of train-time output set to zero: 0.400688
Fraction of test-time output set to zero: 0.0
Running tests with p = 0.75
Mean of input: 10.000972387639752
Mean of train-time output: 9.992740797967008
Mean of test-time output: 10.000972387639752
Fraction of train-time output set to zero: 0.25056
Fraction of test-time output set to zero: 0.0
```

Dropout backward pass

Implement the backward pass, dropout_backward, in nndl/layers.py. After that, test your gradients by running the following cell:

```
x = np.random.randn(10, 10) + 10
dout = np.random.randn(*x.shape)

dropout_param = {'mode': 'train', 'p': 0.8, 'seed': 123}
out, cache = dropout_forward(x, dropout_param)
dx = dropout_backward(dout, cache)
dx_num = eval_numerical_gradient_array(lambda xx: dropout_forward(xx, dropout_param)[0], x, dout)

print('dx relative error: ', rel_error(dx, dx_num))
dx relative error: 5.445610966555297e-11
```

Implement a fully connected neural network with dropout layers

Modify the FullyConnectedNet() class in nndl/fc_net.py to incorporate dropout. A dropout layer should be incorporated after every ReLU layer. Concretely, there shouldn't be a dropout at the output layer since there is no ReLU at the output layer. You will need to modify the class in the following areas:

- (1) In the forward pass, you will need to incorporate a dropout layer after every relu layer.
- (2) In the backward pass, you will need to incorporate a dropout backward pass layer.

Check your implementation by running the following code. Our W1 gradient relative error is on the order of 1e-6 (the largest of all the relative errors).

```
N, D, H1, H2, C = 2, 15, 20, 30, 10
X = np.random.randn(N, D)
y = np.random.randint(C, size=(N,))
for dropout in [0, 0.25, 0.5]:
  print('Running check with dropout = ', dropout)
  model = FullyConnectedNet([H1, H2], input dim=D, num classes=C,
                            weight scale=5e-2, dtype=np.float64,
                            dropout=dropout, seed=123)
  loss, grads = model.loss(X, y)
  print('Initial loss: ', loss)
  for name in sorted(grads):
    f = lambda : model.loss(X, y)[0]
    grad num = eval numerical gradient(f, model.params[name],
verbose=False, h=1e-5)
    print('{} relative error: {}'.format(name, rel error(grad num,
grads[name])))
  print('\n')
```

```
Running check with dropout = 0
Initial loss: 2.3051948273987857
W1 relative error: 2.5272575344376073e-07
W2 relative error: 1.5034484929313676e-05
W3 relative error: 2.753446833630168e-07
b1 relative error: 2.936957476400148e-06
b2 relative error: 5.051339805546953e-08
b3 relative error: 1.1740467838205477e-10
Running check with dropout = 0.25
Initial loss: 2.3126468345657742
W1 relative error: 1.483854795975875e-08
W2 relative error: 2.3427832149940254e-10
W3 relative error: 3.564454999162522e-08
b1 relative error: 1.5292167232408546e-09
b2 relative error: 1.842268868410678e-10
b3 relative error: 8.701800136729388e-11
Running check with dropout = 0.5
Initial loss: 2.302437587710995
W1 relative error: 4.553387957138422e-08
W2 relative error: 2.974218050584597e-08
W3 relative error: 4.3413247403122424e-07
b1 relative error: 1.872462967441693e-08
b2 relative error: 5.045591219274328e-09
b3 relative error: 8.009887154529434e-11
```

Dropout as a regularizer

In class, we claimed that dropout acts as a regularizer by effectively bagging. To check this, we will train two small networks, one with dropout and one without dropout.

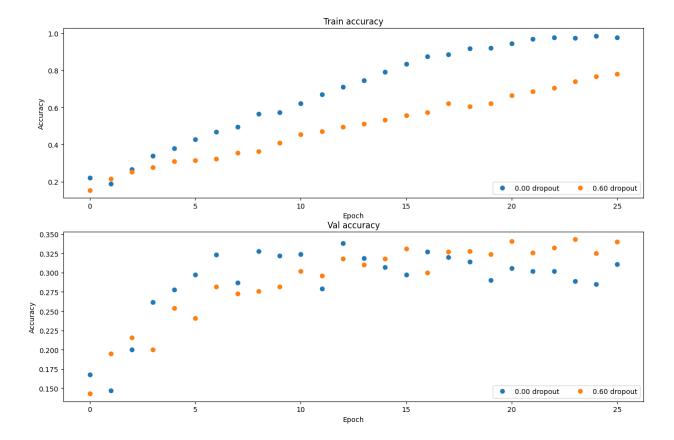
```
# Train two identical nets, one with dropout and one without

num_train = 500
small_data = {
    'X_train': data['X_train'][:num_train],
    'y_train': data['y_train'][:num_train],
    'X_val': data['X_val'],
    'y_val': data['y_val'],
}

solvers = {}
dropout_choices = [0, 0.6]
```

```
for dropout in dropout choices:
 model = FullyConnectedNet([100, 100, 100], dropout=dropout)
  solver = Solver(model, small data,
                  num epochs=25, batch size=100,
                  update rule='adam',
                  optim config={
                    'learning rate': 5e-4,
                  verbose=True, print every=100)
 solver.train()
 solvers[dropout] = solver
(Iteration 1 / 125) loss: 2.300804
(Epoch 0 / 25) train acc: 0.220000; val acc: 0.168000
(Epoch 1 / 25) train acc: 0.188000; val acc: 0.147000
(Epoch 2 / 25) train acc: 0.266000; val acc: 0.200000
(Epoch 3 / 25) train acc: 0.338000; val acc: 0.262000
(Epoch 4 / 25) train acc: 0.378000; val acc: 0.278000
(Epoch 5 / 25) train acc: 0.428000; val acc: 0.297000
(Epoch 6 / 25) train acc: 0.468000; val acc: 0.323000
(Epoch 7 / 25) train acc: 0.494000; val acc: 0.287000
(Epoch 8 / 25) train acc: 0.566000; val acc: 0.328000
(Epoch 9 / 25) train acc: 0.572000; val acc: 0.322000
(Epoch 10 / 25) train acc: 0.622000; val acc: 0.324000
(Epoch 11 / 25) train acc: 0.670000; val acc: 0.279000
(Epoch 12 / 25) train acc: 0.710000; val acc: 0.338000
(Epoch 13 / 25) train acc: 0.746000; val acc: 0.319000
(Epoch 14 / 25) train acc: 0.792000; val acc: 0.307000
(Epoch 15 / 25) train acc: 0.834000; val acc: 0.297000
(Epoch 16 / 25) train acc: 0.876000; val acc: 0.327000
(Epoch 17 / 25) train acc: 0.886000; val acc: 0.320000
(Epoch 18 / 25) train acc: 0.918000; val_acc: 0.314000
(Epoch 19 / 25) train acc: 0.922000; val acc: 0.290000
(Epoch 20 / 25) train acc: 0.944000; val acc: 0.306000
(Iteration 101 / 125) loss: 0.156105
(Epoch 21 / 25) train acc: 0.968000; val acc: 0.302000
(Epoch 22 / 25) train acc: 0.978000; val acc: 0.302000
(Epoch 23 / 25) train acc: 0.976000; val acc: 0.289000
(Epoch 24 / 25) train acc: 0.986000; val acc: 0.285000
(Epoch 25 / 25) train acc: 0.978000; val acc: 0.311000
(Iteration 1 / 125) loss: 2.301328
(Epoch 0 / 25) train acc: 0.154000; val acc: 0.143000
(Epoch 1 / 25) train acc: 0.214000; val acc: 0.195000
(Epoch 2 / 25) train acc: 0.252000; val acc: 0.216000
(Epoch 3 / 25) train acc: 0.276000; val acc: 0.200000
(Epoch 4 / 25) train acc: 0.308000; val acc: 0.254000
(Epoch 5 / 25) train acc: 0.316000; val acc: 0.241000
(Epoch 6 / 25) train acc: 0.322000; val acc: 0.282000
(Epoch 7 / 25) train acc: 0.354000; val acc: 0.273000
```

```
(Epoch 8 / 25) train acc: 0.364000; val acc: 0.276000
(Epoch 9 / 25) train acc: 0.408000; val acc: 0.282000
(Epoch 10 / 25) train acc: 0.454000; val acc: 0.302000
(Epoch 11 / 25) train acc: 0.472000; val acc: 0.296000
(Epoch 12 / 25) train acc: 0.496000; val acc: 0.318000
(Epoch 13 / 25) train acc: 0.512000; val_acc: 0.310000
(Epoch 14 / 25) train acc: 0.532000; val acc: 0.318000
(Epoch 15 / 25) train acc: 0.558000; val acc: 0.331000
(Epoch 16 / 25) train acc: 0.574000; val acc: 0.300000
(Epoch 17 / 25) train acc: 0.622000; val acc: 0.327000
(Epoch 18 / 25) train acc: 0.606000; val acc: 0.328000
(Epoch 19 / 25) train acc: 0.622000; val acc: 0.324000
(Epoch 20 / 25) train acc: 0.666000; val_acc: 0.341000
(Iteration 101 / 125) loss: 1.296328
(Epoch 21 / 25) train acc: 0.686000; val acc: 0.326000
(Epoch 22 / 25) train acc: 0.706000; val acc: 0.332000
(Epoch 23 / 25) train acc: 0.740000; val acc: 0.343000
(Epoch 24 / 25) train acc: 0.766000; val acc: 0.325000
(Epoch 25 / 25) train acc: 0.782000; val acc: 0.340000
# Plot train and validation accuracies of the two models
train accs = []
val accs = []
for dropout in dropout choices:
  solver = solvers[dropout]
  train accs.append(solver.train acc history[-1])
  val accs.append(solver.val acc history[-1])
plt.subplot(3, 1, 1)
for dropout in dropout choices:
  plt.plot(solvers[dropout].train acc history, 'o', label='%.2f
dropout' % dropout)
plt.title('Train accuracy')
plt.xlabel('Epoch')
plt.ylabel('Accuracy')
plt.legend(ncol=2, loc='lower right')
plt.subplot(3, 1, 2)
for dropout in dropout choices:
  plt.plot(solvers[dropout].val acc history, 'o', label='%.2f dropout'
% dropout)
plt.title('Val accuracy')
plt.xlabel('Epoch')
plt.ylabel('Accuracy')
plt.legend(ncol=2, loc='lower right')
plt.gcf().set size inches(15, 15)
plt.show()
```



Question

Based off the results of this experiment, is dropout performing regularization? Explain your answer.

Answer:

Yes, in this casem dropout is performing regularization. As seen in the graph above, the 0.60 dropout has a lower train accuracy than the 0.0 dropout, which would be expected for a regularized model. However on the validation set, it can be observed that the accuracy is quite similar for both 0.0 and 0.6 dropouts, and as more interations are done, the regulairzer with 0.6 dropoutimproved in validation accuracy while the 0.0 regularized model decreases in accuracy(suggesting that it is being overfit). Thus, according to the graphs above, dropout is performing regularization

Final part of the assignment

Get over 55% validation accuracy on CIFAR-10 by using the layers you have implemented. You will be graded according to the following equation:

min(floor((X - 32%)) / 23%, 1) where if you get 55% or higher validation accuracy, you get full points.

```
# YOUR CODE HERE:
   Implement a FC-net that achieves at least 55% validation accuracy
   on CIFAR-10.
# =========== #
model = FullyConnectedNet([600, 400, 200, 50], dropout=0.75,
weight scale=4e-2, use batchnorm=True)
solver = Solver(model, data,
               num epochs=20, batch size=500,
               update rule='adam',
               optim_config={'learning_rate': 3e-3,},
               lr decay=0.95,
               verbose=True, print every=100)
solver.train()
# ============= #
# END YOUR CODE HERE
(Iteration 1 / 1960) loss: 2.337023
(Epoch 0 / 20) train acc: 0.161000; val acc: 0.212000
(Epoch 1 / 20) train acc: 0.432000; val acc: 0.453000
(Iteration 101 / 1960) loss: 1.622446
(Epoch 2 / 20) train acc: 0.523000; val acc: 0.485000
(Iteration 201 / 1960) loss: 1.475042
(Epoch 3 / 20) train acc: 0.494000; val acc: 0.512000
(Iteration 301 / 1960) loss: 1.512597
(Epoch 4 / 20) train acc: 0.526000; val acc: 0.542000
(Iteration 401 / 1960) loss: 1.488515
(Epoch 5 / 20) train acc: 0.556000; val acc: 0.536000
(Iteration 501 / 1960) loss: 1.361152
(Epoch 6 / 20) train acc: 0.579000; val acc: 0.560000
(Iteration 601 / 1960) loss: 1.350820
(Epoch 7 / 20) train acc: 0.602000; val_acc: 0.557000
(Iteration 701 / 1960) loss: 1.357386
KeyboardInterrupt
                                        Traceback (most recent call
last)
Cell In[10], line 17
     7 model = FullyConnectedNet([600, 400, 200, 50], dropout=0.7,
weight scale=4e-2, use batchnorm=True)
     9 solver = Solver(model, data,
                       num_epochs=20, batch size=500,
    10
    11
                       update rule='adam',
   (\ldots)
    15
                       lr decay=0.95,
                       verbose=True, print every=100)
    16
---> 17 solver.train()
    19 #
```

```
20 # END YOUR CODE HERE
    21 #
______#
File ~/Desktop/HW4 code/utils/solver.py:264, in Solver.train(self)
   261 num_iterations = self.num_epochs * iterations_per_epoch
   263 for t in range(num iterations):
         self._step()
--> 264
         # Maybe print training loss
   266
   if self.verbose and t % self.print_every == 0:
File ~/Desktop/HW4 code/utils/solver.py:180, in Solver. step(self)
   177 y_batch = self.y_train[batch_mask]
   179 # Compute loss and gradient
--> 180 loss, grads = self.model.loss(X batch, y batch)
   181 self.loss history.append(loss)
   183 # Perform a parameter update
File ~/Desktop/HW4 code/nndl/fc net.py:283, in
FullyConnectedNet.loss(self, X, y)
   281 for i in range(self.num layers):
   282
         if i == 0:
--> 283
            a, cache = affine forward(X, self.params['W1'],
self.params['b1'])
   284
            caches.append(cache)
   285
            if self.use batchnorm:
File ~/Desktop/HW4 code/nndl/layers.py:33, in affine forward(x, w, b)
    26 #
         27 # YOUR CODE HERE:
    28 #
        Calculate the output of the forward pass. Notice the
dimensions
    29 # of w are D \times M, which is the transpose of what we did in
earlier
    30 # assignments.
    31 #
______#
    32 X = x.reshape((x.shape[0],-1))
---> 33 out = np.dot(X,w)+b
    35 #
36 # END YOUR CODE HERE
    37 #
39 cache = (x, w, b)
KeyboardInterrupt:
```

```
import numpy as np
import pdb
from .layers import *
from .layer utils import *
This code was originally written for CS 231n at Stanford University
(cs231n.stanford.edu). It has been modified in various areas for use in the
ECE 239AS class at UCLA. This includes the descriptions of what code to
implement as well as some slight potential changes in variable names to be
consistent with class nomenclature. We thank Justin Johnson & Serena Yeung for
permission to use this code. To see the original version, please visit
cs231n.stanford.edu.
class TwoLayerNet (object):
 A two-layer fully-connected neural network with ReLU nonlinearity and
 softmax loss that uses a modular layer design. We assume an input dimension
 of D, a hidden dimension of H, and perform classification over C classes.
 The architecure should be affine - relu - affine - softmax.
 Note that this class does not implement gradient descent; instead, it
 will interact with a separate Solver object that is responsible for running
 optimization.
 The learnable parameters of the model are stored in the dictionary
 self.params that maps parameter names to numpy arrays.
 def init (self, input dim=3*32*32, hidden dims=100, num classes=10,
             dropout=0, weight scale=1e-3, reg=0.0):
   Initialize a new network.
   Inputs:
   - input dim: An integer giving the size of the input
   - hidden dims: An integer giving the size of the hidden layer
   - num classes: An integer giving the number of classes to classify
   - dropout: Scalar between 0 and 1 giving dropout strength.
   - weight scale: Scalar giving the standard deviation for random
     initialization of the weights.
   - reg: Scalar giving L2 regularization strength.
   self.params = {}
   self.reg = reg
   # YOUR CODE HERE:
      Initialize W1, W2, b1, and b2. Store these as self.params['W1'],
      self.params['W2'], self.params['b1'] and self.params['b2']. The
     biases are initialized to zero and the weights are initialized
     so that each parameter has mean 0 and standard deviation weight scale.
     The dimensions of W1 should be (input dim, hidden_dim) and the
     dimensions of W2 should be (hidden dims, num classes)
   # ------ #
   self.params['W1'] = weight scale * np.random.randn(input dim, hidden dims)
   self.params['W2'] = weight scale * np.random.randn(hidden dims, num classes)
   self.params['b1'] = np.zeros(hidden dims)
   self.params['b2'] = np.zeros(num classes)
   # END YOUR CODE HERE
   # ----- #
```

```
def loss(self, X, y=None):
 Compute loss and gradient for a minibatch of data.
 Inputs:
 - X: Array of input data of shape (N, d 1, ..., d k)
 - y: Array of labels, of shape (N,). y[i] gives the label for X[i].
 Returns:
 If y is None, then run a test-time forward pass of the model and return:
 - scores: Array of shape (N, C) giving classification scores, where
  scores[i, c] is the classification score for X[i] and class c.
 If y is not None, then run a training-time forward and backward pass and
 return a tuple of:
 - loss: Scalar value giving the loss
 - grads: Dictionary with the same keys as self.params, mapping parameter
  names to gradients of the loss with respect to those parameters.
 scores = None
 # YOUR CODE HERE:
   Implement the forward pass of the two-layer neural network. Store
   the class scores as the variable 'scores'. Be sure to use the layers
   you prior implemented.
 # ------ #
 W1 = self.params['W1']
 W2 = self.params['W2']
 b1 = self.params['b1']
 b2 = self.params['b2']
 a, fc cache = affine forward(X, W1, b1)
 h, relu cache = relu forward(a)
 scores, fc cache2 = affine forward(h, W2, b2)
 # ----- #
 # END YOUR CODE HERE
 # ----- #
 # If y is None then we are in test mode so just return scores
 if y is None:
   return scores
 loss, grads = 0, {}
 # ============== #
 # YOUR CODE HERE:
   Implement the backward pass of the two-layer neural net. Store
   the loss as the variable 'loss' and store the gradients in the
    'grads' dictionary. For the grads dictionary, grads['W1'] holds
 #
   the gradient for W1, grads['b1'] holds the gradient for b1, etc.
    i.e., grads[k] holds the gradient for self.params[k].
    Add L2 regularization, where there is an added cost 0.5*self.reg*W^2
 # for each W. Be sure to include the 0.5 multiplying factor to
 #
   match our implementation.
    And be sure to use the layers you prior implemented.
 W1, W2 = self.params['W1'], self.params['W2']
 loss, dscores = softmax loss(scores, y)
 loss += 0.5 * self.reg * (np.sum(W1 * W1) + np.sum(W2 * W2))
 dh, dW2, db2 = affine backward(dscores, fc cache2)
 da = relu backward(dh, relu cache)
 dx, dW1, db1 = affine backward(da, fc cache)
 grads['W1'] = dW1 + self.reg * W1
```

```
grads['W2'] = dW2 + self.reg * W2
   # END YOUR CODE HERE
   # ------ #
   return loss, grads
class FullyConnectedNet(object):
 A fully-connected neural network with an arbitrary number of hidden layers,
 ReLU nonlinearities, and a softmax loss function. This will also implement
 dropout and batch normalization as options. For a network with L layers,
 the architecture will be
 \{affine - [batch norm] - relu - [dropout]\} \times (L - 1) - affine - softmax
 where batch normalization and dropout are optional, and the {...} block is
 repeated L - 1 times.
 Similar to the TwoLayerNet above, learnable parameters are stored in the
 self.params dictionary and will be learned using the Solver class.
 def init (self, hidden dims, input dim=3*32*32, num classes=10,
             dropout=0, use_batchnorm=False, reg=0.0,
             weight scale=1e-2, dtype=np.float32, seed=None):
   11 11 11
   Initialize a new FullyConnectedNet.
   Inputs:
   - hidden dims: A list of integers giving the size of each hidden layer.
   - input dim: An integer giving the size of the input.
   - num classes: An integer giving the number of classes to classify.
   - dropout: Scalar between 0 and 1 giving dropout strength. If dropout=0 then
     the network should not use dropout at all.
   - use batchnorm: Whether or not the network should use batch normalization.
   - reg: Scalar giving L2 regularization strength.
   - weight scale: Scalar giving the standard deviation for random
     initialization of the weights.
   - dtype: A numpy datatype object; all computations will be performed using
     this datatype. float32 is faster but less accurate, so you should use
     float64 for numeric gradient checking.
   - seed: If not None, then pass this random seed to the dropout layers. This
     will make the dropout layers deteriminstic so we can gradient check the
     model.
   self.use_batchnorm = use_batchnorm
   self.use dropout = dropout > 0
   self.reg = reg
   self.num_layers = 1 + len(hidden_dims)
   self.dtype = dtype
   self.params = {}
   # YOUR CODE HERE:
      Initialize all parameters of the network in the self.params dictionary.
       The weights and biases of layer 1 are W1 and b1; and in general the
      weights and biases of layer i are Wi and bi. The
      biases are initialized to zero and the weights are initialized
      so that each parameter has mean 0 and standard deviation weight scale.
      BATCHNORM: Initialize the gammas of each layer to 1 and the beta
      parameters to zero. The gamma and beta parameters for layer 1 should
     be self.params['gamma1'] and self.params['beta1']. For layer 2, they
     should be gamma2 and beta2, etc. Only use batchnorm if self.use batchnorm
      is true and DO NOT do batch normalize the output scores.
```

```
for i in range(self.num layers):
       if i == 0:
           self.params['W1'] = weight scale * np.random.randn(input dim, hidden dims[i])
           self.params['b1'] = np.zeros(hidden dims[i])
           if self.use batchnorm:
               self.params['gamma1'] = np.ones(hidden dims[i])
               self.params['beta1'] = np.zeros(hidden dims[i])
       elif i == self.num_layers - 1:
           self.params['W' + str(i + 1)] = weight_scale * np.random.randn(hidden_dims[i - 1],
num classes)
           self.params['b' + str(i + 1)] = np.zeros(num classes)
           self.params['W' + str(i + 1)] = weight scale * np.random.randn(hidden dims[i - 1],
hidden dims[i])
           self.params['b' + str(i + 1)] = np.zeros(hidden dims[i])
           if self.use batchnorm:
               self.params['gamma' + str(i + 1)] = np.ones(hidden dims[i])
               self.params['beta' + str(i + 1)] = np.zeros(hidden dims[i])
   # ------ #
    # END YOUR CODE HERE
    # When using dropout we need to pass a dropout param dictionary to each
   # dropout layer so that the layer knows the dropout probability and the mode
   # (train / test). You can pass the same dropout param to each dropout layer.
   self.dropout param = {}
   if self.use dropout:
     self.dropout param = {'mode': 'train', 'p': dropout}
     if seed is not None:
       self.dropout param['seed'] = seed
   # With batch normalization we need to keep track of running means and
   # variances, so we need to pass a special bn param object to each batch
   # normalization layer. You should pass self.bn params[0] to the forward pass
   # of the first batch normalization layer, self.bn params[1] to the forward
   # pass of the second batch normalization layer, etc.
   self.bn params = []
   if self.use batchnorm:
     self.bn params = [{'mode': 'train'} for i in np.arange(self.num layers - 1)]
   # Cast all parameters to the correct datatype
   for k, v in self.params.items():
     self.params[k] = v.astype(dtype)
 def loss(self, X, y=None):
   Compute loss and gradient for the fully-connected net.
   Input / output: Same as TwoLayerNet above.
   X = X.astype(self.dtype)
   mode = 'test' if y is None else 'train'
   # Set train/test mode for batchnorm params and dropout param since they
   # behave differently during training and testing.
   if self.dropout param is not None:
     self.dropout param['mode'] = mode
   if self.use batchnorm:
     for bn param in self.bn params:
       bn param[mode] = mode
   scores = None
```

```
# YOUR CODE HERE:
      Implement the forward pass of the FC net and store the output
     scores as the variable "scores".
      BATCHNORM: If self.use batchnorm is true, insert a bathnorm layer
   #
     between the affine forward and relu forward layers. You may
      also write an affine batchnorm relu() function in layer utils.py.
      DROPOUT: If dropout is non-zero, insert a dropout layer after
      every ReLU layer.
   # ============== #
   caches = []
   for i in range(self.num layers):
       if i == 0:
          a, cache = affine forward(X, self.params['W1'], self.params['b1'])
          caches.append(cache)
          if self.use batchnorm:
              a, cache = batchnorm forward(a, self.params['gamma1'], self.params['beta1'],
self.bn params[0])
             caches.append(cache)
          h, cache = relu forward(a)
          caches.append(cache)
          if self.use dropout:
              h, cache = dropout forward(h, self.dropout param)
              caches.append(cache)
       elif i == self.num layers - 1:
          scores, cache = affine forward(h, self.params['W' + str(i + 1)], self.params['b' +
str(i + 1))
          caches.append(cache)
          a, cache = affine forward(h, self.params['W' + str(i + 1)], self.params['b' +
str(i + 1)])
          caches.append(cache)
          if self.use batchnorm:
             a, cache = batchnorm forward(a, self.params['gamma' + str(i + 1)],
self.params['beta' + str(i + 1)], self.bn params[i])
             caches.append(cache)
          h, cache = relu forward(a)
          caches.append(cache)
          if self.use dropout:
             h, cache = dropout_forward(h, self.dropout_param)
              caches.append(cache)
   # ------ #
   # END YOUR CODE HERE
   # If test mode return early
   if mode == 'test':
     return scores
   loss, grads = 0.0, {}
   # YOUR CODE HERE:
     Implement the backwards pass of the FC net and store the gradients
      in the grads dict, so that grads[k] is the gradient of self.params[k]
      Be sure your L2 regularization includes a 0.5 factor.
      BATCHNORM: Incorporate the backward pass of the batchnorm.
      DROPOUT: Incorporate the backward pass of dropout.
   loss, dscores = softmax loss(scores, y)
   for i in range(self.num layers):
```

```
loss += 0.5 * self.reg * np.sum(self.params['W' + str(i + 1)] ** 2)
   dh, grads['W' + str(self.num_layers)], grads['b' + str(self.num_layers)] =
affine backward(dscores, caches.pop())
   grads['W' + str(self.num_layers)] += self.reg * self.params['W' + str(self.num_layers)]
   for i in range(self.num layers - 1, 0, -1):
      if self.use dropout:
          dh = dropout backward(dh, caches.pop())
      da = relu backward(dh, caches.pop())
      if self.use_batchnorm:
          da, dgamma, dbeta = batchnorm backward(da, caches.pop())
          grads['gamma' + str(i)] = dgamma
          grads['beta' + str(i)] = dbeta
      dh, grads['W' + str(i)], grads['b' + str(i)] = affine backward(da, caches.pop())
      grads['W' + str(i)] += self.reg * self.params['W' + str(i)]
   # ----- #
   # END YOUR CODE HERE
   # ------ #
   return loss, grads
```

```
This code was originally written for CS 231n at Stanford University
(cs231n.stanford.edu). It has been modified in various areas for use in the
ECE 239AS class at UCLA. This includes the descriptions of what code to
implement as well as some slight potential changes in variable names to be
consistent with class nomenclature. We thank Justin Johnson & Serena Yeung for
permission to use this code. To see the original version, please visit
cs231n.stanford.edu.
from nndl.layers import *
from utils.gradient_check import eval_numerical_gradient, eval_numerical_gradient_array
from nndl.layer utils import affine relu forward, affine relu backward
from nndl.fc net import FullyConnectedNet
def rel error(x, y):
  """ returns relative error """
  return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y))))
def affine forward test():
    # Test the affine forward function
    num inputs = 2
    input shape = (4, 5, 6)
    output dim = 3
    input_size = num_inputs * np.prod(input_shape)
   weight size = output dim * np.prod(input shape)
   x = np.linspace(-0.1, 0.5, num=input size).reshape(num inputs, *input shape)
    w = np.linspace(-0.2, 0.3, num=weight size).reshape(np.prod(input shape), output dim)
   b = np.linspace(-0.3, 0.1, num=output dim)
    out, = affine forward(x, w, b)
    correct out = np.array([[1.49834967, 1.70660132, 1.91485297],
                            [ 3.25553199, 3.5141327, 3.77273342]])
    # Compare your output with ours. The error should be around 1e-9.
   print('If affine forward function is working, difference should be less than 1e-9:')
   print('difference: {}'.format(rel error(out, correct out)))
def affine backward test():
    # Test the affine_backward function
   x = np.random.randn(10, 2, 3)
    w = np.random.randn(6, 5)
   b = np.random.randn(5)
    dout = np.random.randn(10, 5)
   dx num = eval numerical gradient array(lambda x: affine forward(x, w, b)[0], x, dout)
    dw_num = eval_numerical_gradient_array(lambda w: affine_forward(x, w, b)[0], w, dout)
    db num = eval numerical gradient array(lambda b: affine forward(x, w, b)[0], b, dout)
    , cache = affine forward(x, w, b)
   dx, dw, db = affine backward(dout, cache)
    # The error should be around 1e-10
    print('If affine backward is working, error should be less than 1e-9::')
   print('dx error: {}'.format(rel error(dx num, dx)))
   print('dw error: {}'.format(rel error(dw num, dw)))
   print('db error: {}'.format(rel error(db num, db)))
def relu forward test():
    # Test the relu forward function
   x = np.linspace(-0.5, 0.5, num=12).reshape(3, 4)
```

```
out, _ = relu_forward(x)
                                           0.,
                                                                     0.,
    correct_out = np.array([[ 0.,
                                                        0.,
                                                                     0.13636364,],
                            [ 0.,
                                         0.,
                                                        0.04545455,
                            [ 0.22727273, 0.31818182, 0.40909091,
                                                                     0.5,
                                                                                ]])
    # Compare your output with ours. The error should be around 1e-8
    print('If relu forward function is working, difference should be around 1e-8:')
    print('difference: {}'.format(rel error(out, correct out)))
def relu backward test():
    x = np.random.randn(10, 10)
    dout = np.random.randn(*x.shape)
    dx num = eval numerical gradient array(lambda x: relu forward(x)[0], x, dout)
    _, cache = relu forward(x)
    dx = relu backward(dout, cache)
    # The error should be around 1e-12
   print('If relu forward function is working, error should be less than 1e-9:')
    print('dx error: {}'.format(rel error(dx num, dx)))
def affine relu test():
    x = np.random.randn(2, 3, 4)
    w = np.random.randn(12, 10)
    b = np.random.randn(10)
    dout = np.random.randn(2, 10)
    out, cache = affine relu forward(x, w, b)
    dx, dw, db = affine relu backward(dout, cache)
    dx num = eval numerical gradient array(lambda x: affine relu forward(x, w, b)[0], x, dout)
    dw num = eval numerical gradient array(lambda w: affine relu forward(x, w, b)[0], w, dout)
    db num = eval numerical gradient array(lambda b: affine relu forward(x, w, b)[0], b, dout)
   print('If affine relu forward and affine relu backward are working, error should be less
than 1e-9::')
   print('dx error: {}'.format(rel error(dx num, dx)))
   print('dw error: {}'.format(rel error(dw num, dw)))
   print('db error: {}'.format(rel_error(db_num, db)))
def fc_net_test():
   N, D, H1, H2, C = 2, 15, 20, 30, 10
    X = np.random.randn(N, D)
    y = np.random.randint(C, size=(N,))
    for reg in [0, 3.14]:
      print('Running check with reg = {}'.format(reg))
      model = FullyConnectedNet([H1, H2], input dim=D, num classes=C,
                                reg=reg, weight_scale=5e-2, dtype=np.float64)
      loss, grads = model.loss(X, y)
      print('Initial loss: {}'.format(loss))
      for name in sorted(grads):
        f = lambda : model.loss(X, y)[0]
        grad_num = eval_numerical_gradient(f, model.params[name], verbose=False, h=1e-5)
       print('{} relative error: {}'.format(name, rel_error(grad num, grads[name])))
```

```
def affine relu forward(x, w, b):
    Convenience layer that performs an affine transform followed by a ReLU
    Inputs:
    - x: Input to the affine layer
    - w, b: Weights for the affine layer
   Returns a tuple of:
    - out: Output from the ReLU
    - cache: Object to give to the backward pass
    a, fc cache = affine forward(x, w, b)
    out, relu_cache = relu forward(a)
    cache = (fc_cache, relu_cache)
    return out, cache
def affine relu backward(dout, cache):
    Backward pass for the affine-relu convenience layer
    fc cache, relu cache = cache
    da = relu backward(dout, relu_cache)
    dx, dw, db = affine backward(da, fc cache)
    return dx, dw, db
def affine batchnorm relu forward(x, w, b, gamma, beta, bn param):
    Convenience layer that performs an affine transform followed by a batchnorm and ReLU
    Inputs:
    - x: Input to the affine layer
    - w, b: Weights for the affine layer
    - gamma: Scale parameter of shape (D,)
    - beta: Shift paremeter of shape (D,)
    - bn param: Dictionary with the following keys:
      - mode: 'train' or 'test'; required
      - eps: Constant for numeric stability
      - momentum: Constant for running mean / variance.
      - running_mean: Array of shape (D,) giving running mean of features
      - running_var Array of shape (D,) giving running variance of features
    Returns a tuple of:
    - out: Output from the ReLU
    - cache: Object to give to the backward pass
    a, fc cache = affine forward(x, w, b)
    a_norm, bn_cache = batchnorm_forward(a, gamma, beta, bn_param)
    out, relu cache = relu forward(a norm)
    cache = (fc cache, bn cache, relu cache)
   return out, cache
def affine_batchnorm_relu_backward(dout, cache):
    Backward pass for the affine-batchnorm-relu convenience layer
    fc cache, bn cache, relu cache = cache
    da norm = relu backward(dout, relu cache)
    da, dgamma, dbeta = batchnorm backward(da norm, bn cache)
    dx, dw, db = affine backward(da, fc cache)
    return dx, dw, db, dgamma, dbeta
```

from .layers import *

```
import pdb
def affine forward(x, w, b):
 Computes the forward pass for an affine (fully-connected) layer.
 The input x has shape (N, d_1, ..., d_k) and contains a minibatch of N
 examples, where each example x[i] has shape (d_1, \ldots, d_k). We will
 reshape each input into a vector of dimension D = d \ 1 \ * \ldots \ * \ d \ k, and
 then transform it to an output vector of dimension M.
 Inputs:
 - x: A numpy array containing input data, of shape (N, d 1, ..., d k)
 - w: A numpy array of weights, of shape (D, M)
 - b: A numpy array of biases, of shape (M,)
 Returns a tuple of:
 - out: output, of shape (N, M)
 - cache: (x, w, b)
 # YOUR CODE HERE:
   Calculate the output of the forward pass. Notice the dimensions
   of w are D x M, which is the transpose of what we did in earlier
   assignments.
 X = x.reshape((x.shape[0], -1))
 out = np.dot(X, w) + b
 # ------ #
 # END YOUR CODE HERE
 # ------ #
 cache = (x, w, b)
 return out, cache
def affine backward(dout, cache):
 Computes the backward pass for an affine layer.
 Inputs:
 - dout: Upstream derivative, of shape (N, M)
 - cache: Tuple of:
   - x: Input data, of shape (N, d 1, ... d k)
   - w: Weights, of shape (D, M)
 Returns a tuple of:
 - dx: Gradient with respect to x, of shape (N, d1, ..., d k)
 - dw: Gradient with respect to w, of shape (D, M)
 - db: Gradient with respect to b, of shape (M,)
 11 11 11
 x, w, b = cache
 dx, dw, db = None, None, None
 # ------ #
 # YOUR CODE HERE:
   Calculate the gradients for the backward pass.
 # ----- #
 X = x.reshape((x.shape[0], -1))
 db = np.sum(dout,axis=0)
 dw = np.dot(X.T,dout)
```

import numpy as np

```
dx = np.dot(dout, w.T).reshape(x.shape)
 # dout is N x M
 # dx should be N x d1 x ... x dk; it relates to dout through multiplication with w, which is
 \# dw should be D x M; it relates to dout through multiplication with x, which is N x D after
reshaping
 # db should be M; it is just the sum over dout examples
 # ----- #
 # END YOUR CODE HERE
 # ============== #
 return dx, dw, db
def relu forward(x):
 Computes the forward pass for a layer of rectified linear units (ReLUs).
 Input:
 - x: Inputs, of any shape
 Returns a tuple of:
 - out: Output, of the same shape as x
 - cache: x
 # ============== #
 # YOUR CODE HERE:
   Implement the ReLU forward pass.
 # ----- #
 out = np.maximum(0,x)
 # END YOUR CODE HERE
 # ------ #
 cache = x
 return out, cache
def relu backward(dout, cache):
 Computes the backward pass for a layer of rectified linear units (ReLUs).
 - dout: Upstream derivatives, of any shape
 - cache: Input x, of same shape as dout
 Returns:
 - dx: Gradient with respect to x
 x = cache
 # ------ #
 # YOUR CODE HERE:
   Implement the ReLU backward pass
 # ReLU directs linearly to those > 0
 dx = dout*(x>0)
 # ============== #
 # END YOUR CODE HERE
```

return dx

```
def batchnorm_forward(x, gamma, beta, bn_param):
  Forward pass for batch normalization.
 During training the sample mean and (uncorrected) sample variance are
 computed from minibatch statistics and used to normalize the incoming data.
 During training we also keep an exponentially decaying running mean of the mean
 and variance of each feature, and these averages are used to normalize data
 at test-time.
 At each timestep we update the running averages for mean and variance using
 an exponential decay based on the momentum parameter:
 running mean = momentum * running mean + (1 - momentum) * sample mean
  running var = momentum * running var + (1 - momentum) * sample var
 Note that the batch normalization paper suggests a different test-time
 behavior: they compute sample mean and variance for each feature using a
  large number of training images rather than using a running average. For
  this implementation we have chosen to use running averages instead since
  they do not require an additional estimation step; the torch7 implementation
  of batch normalization also uses running averages.
 Input:
  - x: Data of shape (N, D)
  - gamma: Scale parameter of shape (D,)
  - beta: Shift paremeter of shape (D,)
  - bn param: Dictionary with the following keys:
   - mode: 'train' or 'test'; required
   - eps: Constant for numeric stability
   - momentum: Constant for running mean / variance.
   - running mean: Array of shape (D,) giving running mean of features
   - running var Array of shape (D,) giving running variance of features
  Returns a tuple of:
  - out: of shape (N, D)
  - cache: A tuple of values needed in the backward pass
 mode = bn param['mode']
  eps = bn param.get('eps', 1e-5)
  momentum = bn_param.get('momentum', 0.9)
 N, D = x.shape
  running_mean = bn_param.get('running_mean', np.zeros(D, dtype=x.dtype))
  running var = bn param.get('running var', np.zeros(D, dtype=x.dtype))
  out, cache = None, None
  if mode == 'train':
   # ----- #
   # YOUR CODE HERE:
      A few steps here:
         (1) Calculate the running mean and variance of the minibatch.
        (2) Normalize the activations with the sample mean and variance.
        (3) Scale and shift the normalized activations. Store this
            as the variable 'out'
         (4) Store any variables you may need for the backward pass in
         the 'cache' variable.
   # ----- #
   sample mean = np.mean(x, axis=0)
   sample var = np.var(x, axis=0)
   x hat = (x - sample mean) / np.sqrt(sample var + eps)
   out = gamma * x_hat + beta
   cache = (x, x hat, sample mean, sample var, gamma, beta, eps)
   running mean = momentum * running mean + (1 - momentum) * sample mean
   running_var = momentum * running_var + (1 - momentum) * sample_var
```

```
# END YOUR CODE HERE
      elif mode == 'test':
      # ------ #
      # YOUR CODE HERE:
          Calculate the testing time normalized activation. Normalize using
          the running mean and variance, and then scale and shift appropriately.
          Store the output as 'out'.
      # ----- #
      x hat = (x - running mean) / np.sqrt(running var + eps)
      out = gamma * x hat + beta
      # ----- #
      # END YOUR CODE HERE
      # ----- #
   else:
     raise ValueError ('Invalid forward batchnorm mode "%s"' % mode)
   # Store the updated running means back into bn param
   bn param['running mean'] = running mean
   bn param['running var'] = running var
   return out, cache
def batchnorm backward(dout, cache):
   Backward pass for batch normalization.
  For this implementation, you should write out a computation graph for
  batch normalization on paper and propagate gradients backward through
  intermediate nodes.
   Inputs:
   - dout: Upstream derivatives, of shape (N, D)
   - cache: Variable of intermediates from batchnorm forward.
  Returns a tuple of:
   - dx: Gradient with respect to inputs x, of shape (N, D)
   - dgamma: Gradient with respect to scale parameter gamma, of shape (D,)
   - dbeta: Gradient with respect to shift parameter beta, of shape (D,)
   11 11 11
   dx, dgamma, dbeta = None, None, None
   # YOUR CODE HERE:
      Implement the batchnorm backward pass, calculating dx, dgamma, and dbeta.
   # ----- #
   x, x_hat, sample_mean, sample_var, gamma, beta, eps = cache
   N, D = x.shape
   dbeta = np.sum(dout, axis=0)
   dgamma = np.sum(dout * x hat, axis=0)
   dx hat = dout * gamma
   dsample\_var = np.sum(dx\_hat * (x-sample\_mean) * (-0.5) * (sample\_var + eps) ** (-1.5), axis=0)
   dsample\_mean = np.sum(dx\_hat * (-1)/np.sqrt(sample\_var + eps), axis=0) + dsample\_var + eps), axis=0) + dsample\_var + eps), axis=0 +
np.mean(-2 * (x - sample mean), axis=0)
   dx = dx_hat / np.sqrt(sample_var + eps) + dsample_var * 2 * (x - sample_mean) / N +
dsample mean / N
   # END YOUR CODE HERE
   # ------ #
```

```
return dx, dgamma, dbeta
def dropout forward(x, dropout param):
 Performs the forward pass for (inverted) dropout.
 Inputs:
 - x: Input data, of any shape
 - dropout param: A dictionary with the following keys:
   - p: Dropout parameter. We keep each neuron output with probability p.
   - mode: 'test' or 'train'. If the mode is train, then perform dropout;
    if the mode is test, then just return the input.
   - seed: Seed for the random number generator. Passing seed makes this
    function deterministic, which is needed for gradient checking but not in
    real networks.
 Outputs:
 - out: Array of the same shape as x.
 - cache: A tuple (dropout param, mask). In training mode, mask is the dropout
  mask that was used to multiply the input; in test mode, mask is None.
 p, mode = dropout_param['p'], dropout param['mode']
 if 'seed' in dropout param:
   np.random.seed(dropout param['seed'])
 mask = None
 out = None
 if mode == 'train':
   # ----- #
   # YOUR CODE HERE:
     Implement the inverted dropout forward pass during training time.
     Store the masked and scaled activations in out, and store the
    dropout mask as the variable mask.
   # ------ #
   mask = (np.random.rand(*x.shape) < p) / p</pre>
   out = x*mask
   # END YOUR CODE HERE
   elif mode == 'test':
   # ----- #
   # YOUR CODE HERE:
     Implement the inverted dropout forward pass during test time.
   # ----- #
   out = x
   # ------ #
   # END YOUR CODE HERE
   # ----- #
 cache = (dropout param, mask)
 out = out.astype(x.dtype, copy=False)
 return out, cache
def dropout backward(dout, cache):
 Perform the backward pass for (inverted) dropout.
 Inputs:
 - dout: Upstream derivatives, of any shape
 - cache: (dropout param, mask) from dropout forward.
 dropout param, mask = cache
```

```
mode = dropout param['mode']
 dx = None
 if mode == 'train':
                     ______ #
   # YOUR CODE HERE:
    Implement the inverted dropout backward pass during training time.
   dx = dout*mask
   # ----- #
   # END YOUR CODE HERE
   # ----- #
 elif mode == 'test':
   # YOUR CODE HERE:
   # Implement the inverted dropout backward pass during test time.
   # ------ #
  dx = dout
   # END YOUR CODE HERE
   # ----- #
 return dx
def svm loss(x, y):
 Computes the loss and gradient using for multiclass SVM classification.
 - x: Input data, of shape (N, C) where x[i, j] is the score for the jth class
  for the ith input.
 - y: Vector of labels, of shape (N,) where y[i] is the label for x[i] and
  0 <= y[i] < C
 Returns a tuple of:
 - loss: Scalar giving the loss
 - dx: Gradient of the loss with respect to x
 N = x.shape[0]
 correct class scores = x[np.arange(N), y]
 margins = np.maximum(0, x - correct_class_scores[:, np.newaxis] + 1.0)
 margins[np.arange(N), y] = 0
 loss = np.sum(margins) / N
 num_pos = np.sum(margins > 0, axis=1)
 dx = np.zeros like(x)
 dx[margins > 0] = 1
 dx[np.arange(N), y] -= num pos
 dx /= N
 return loss, dx
def softmax loss(x, y):
 Computes the loss and gradient for softmax classification.
 Inputs:
 - x: Input data, of shape (N, C) where x[i, j] is the score for the jth class
   for the ith input.
 - y: Vector of labels, of shape (N,) where y[i] is the label for x[i] and
  0 <= y[i] < C
 Returns a tuple of:
 - loss: Scalar giving the loss
 - dx: Gradient of the loss with respect to x
 probs = np.exp(x - np.max(x, axis=1, keepdims=True))
```

```
probs /= np.sum(probs, axis=1, keepdims=True)
N = x.shape[0]
loss = -np.sum(np.log(probs[np.arange(N), y])) / N
dx = probs.copy()
dx[np.arange(N), y] -= 1
dx /= N
return loss, dx
```

```
import numpy as np
```

11 11 1

This code was originally written for CS 231n at Stanford University (cs231n.stanford.edu). It has been modified in various areas for use in the ECE 239AS class at UCLA. This includes the descriptions of what code to implement as well as some slight potential changes in variable names to be consistent with class nomenclature. We thank Justin Johnson & Serena Yeung for permission to use this code. To see the original version, please visit cs231n.stanford.edu.

11 11 11

.....

This file implements various first-order update rules that are commonly used for training neural networks. Each update rule accepts current weights and the gradient of the loss with respect to those weights and produces the next set of weights. Each update rule has the same interface:

def update(w, dw, config=None):

Inputs:

- w: A numpy array giving the current weights.
- dw: A numpy array of the same shape as w giving the gradient of the loss with respect to w.
- config: A dictionary containing hyperparameter values such as learning rate, momentum, etc. If the update rule requires caching values over many iterations, then config will also hold these cached values.

Returns

- next w: The next point after the update.
- config: The config dictionary to be passed to the next iteration of the update rule.

NOTE: For most update rules, the default learning rate will probably not perform well; however the default values of the other hyperparameters should work well for a variety of different problems.

For efficiency, update rules may perform in-place updates, mutating w and setting next_w equal to w.

```
def sgd(w, dw, config=None):
```

Performs vanilla stochastic gradient descent.

```
config format:
    - learning_rate: Scalar learning rate.
"""
if config is None: config = {}
config.setdefault('learning_rate', 1e-2)
w -= config['learning_rate'] * dw
return w, config
```

def sgd_momentum(w, dw, config=None):

Performs stochastic gradient descent with momentum.

config format:

- learning_rate: Scalar learning rate.
- momentum: Scalar between 0 and 1 giving the momentum value. Setting momentum = 0 reduces to sgd.
- velocity: A numpy array of the same shape as w and dw used to store a moving average of the gradients.

" " "

```
if config is None: config = {}
 config.setdefault('learning rate', 1e-2)
 config.setdefault('momentum', 0.9) # set momentum to 0.9 if it wasn't there
 v = config.get('velocity', np.zeros_like(w)) # gets velocity, else sets it to zero.
 # ============== #
 # YOUR CODE HERE:
 # Implement the momentum update formula. Return the updated weights
   as next w, and the updated velocity as v.
 # ----- #
 momentum_update = config['momentum'] * v - config['learning_rate'] * dw
 next_w = w + momentum_update
 v = momentum update
 # ------ #
 # END YOUR CODE HERE
 config['velocity'] = v
 return next w, config
def sgd nesterov momentum(w, dw, config=None):
 Performs stochastic gradient descent with Nesterov momentum.
 config format:
 - learning rate: Scalar learning rate.
 - momentum: Scalar between 0 and 1 giving the momentum value.
  Setting momentum = 0 reduces to sgd.
 - velocity: A numpy array of the same shape as w and dw used to store a moving
   average of the gradients.
 if config is None: config = {}
 config.setdefault('learning rate', 1e-2)
 config.setdefault('momentum', 0.9) # set momentum to 0.9 if it wasn't there
 v = config.get('velocity', np.zeros_like(w)) # gets velocity, else sets it to zero.
 # ------ #
 # YOUR CODE HERE:
   Implement the momentum update formula. Return the updated weights
   as next w, and the updated velocity as v.
 # ------ #
 v prev = v
 v = config['momentum']*v - config['learning rate'] * dw
 next_w = w - config['momentum'] * v_prev + (1 + config['momentum']) * v
 # ------ #
 # END YOUR CODE HERE
 config['velocity'] = v
 return next w, config
def rmsprop(w, dw, config=None):
 Uses the RMSProp update rule, which uses a moving average of squared gradient
 values to set adaptive per-parameter learning rates.
 config format:
 - learning rate: Scalar learning rate.
 - decay rate: Scalar between 0 and 1 giving the decay rate for the squared
  gradient cache.
 - epsilon: Small scalar used for smoothing to avoid dividing by zero.
 - beta: Moving average of second moments of gradients.
```

```
if config is None: config = {}
 config.setdefault('learning rate', 1e-2)
 config.setdefault('decay rate', 0.99)
 config.setdefault('epsilon', 1e-8)
 config.setdefault('a', np.zeros like(w))
 next w = None
 # ------ #
 # YOUR CODE HERE:
    Implement RMSProp. Store the next value of w as next_w. You need
   to also store in config['a'] the moving average of the second
 # moment gradients, so they can be used for future gradients. Concretely,
 # config['a'] corresponds to "a" in the lecture notes.
 # ----- #
 config['a'] = config['decay rate'] * config['a'] + (1 - config['decay rate'])*dw**2
 next w = w - config['learning rate'] * dw / (np.sqrt(config['a']) + config['epsilon'])
 # END YOUR CODE HERE
 # ----- #
 return next w, config
def adam(w, dw, config=None):
 Uses the Adam update rule, which incorporates moving averages of both the
 gradient and its square and a bias correction term.
 config format:
 - learning rate: Scalar learning rate.
 - betal: Decay rate for moving average of first moment of gradient.
 - beta2: Decay rate for moving average of second moment of gradient.
 - epsilon: Small scalar used for smoothing to avoid dividing by zero.
 - m: Moving average of gradient.
 - v: Moving average of squared gradient.
 - t: Iteration number.
 if config is None: config = {}
 config.setdefault('learning rate', 1e-3)
 config.setdefault('beta1', 0.9)
 config.setdefault('beta2', 0.999)
 config.setdefault('epsilon', 1e-8)
 config.setdefault('v', np.zeros_like(w))
 config.setdefault('a', np.zeros like(w))
 config.setdefault('t', 0)
 next w = None
 # ------ #
 # YOUR CODE HERE:
   Implement Adam. Store the next value of w as next w. You need
 # to also store in config['a'] the moving average of the second
 # moment gradients, and in config['v'] the moving average of the
 # first moments. Finally, store in config['t'] the increasing time.
 # ----- #
 config['t'] += 1
 config['v'] = config['beta1'] * config['v'] + (1 - config['beta1']) * dw
 config['a'] = config['beta2'] * config['a'] + (1 - config['beta2']) * dw**2
 v corrected = config['v'] / (1 - config['betal']**config['t'])
 a corrected = config['a'] / (1 - config['beta2']**config['t'])
 next_w = w - config['learning_rate'] * v_corrected / (np.sqrt(a_corrected) +
config['epsilon'])
```

```
# ----- #
# END YOUR CODE HERE
# ----- #
```

return next_w, config