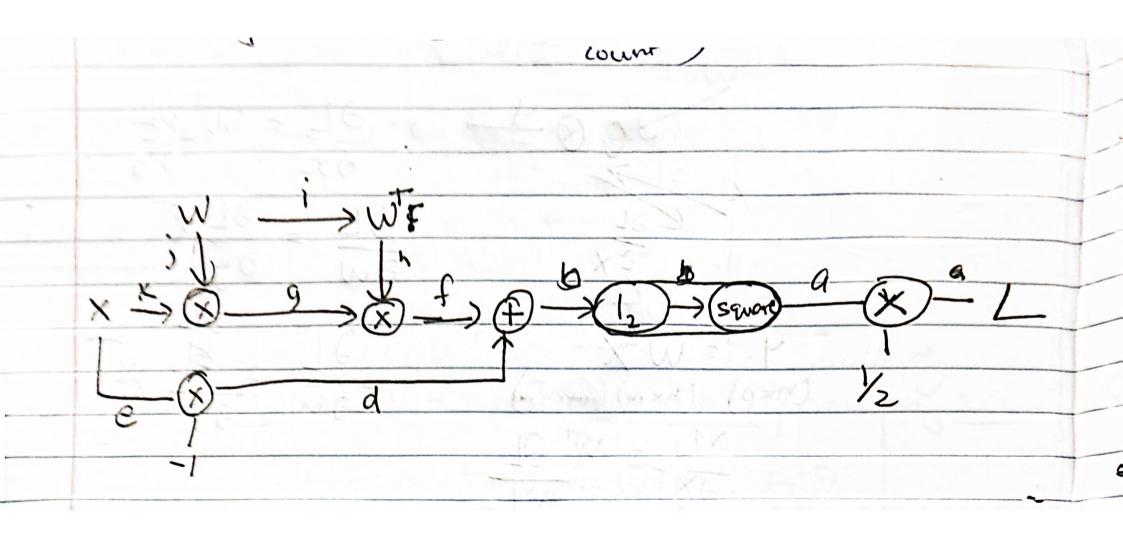
60s 796227 E(E 147 KRISH PATEL Homeworls 3 W E RMYN a) When wis a square motion, (assumption) WIW would minimize the value of + the ranchormation (If we is 6 14hogonal, WW would be equal to I, thus minimizing WTWX -X). Now, moving to this example, is used for the dimensionality of x, with 15 used for the reconstruction (similar to PCA). By this By minimizing the difference of The x' (reduced x dimensionity, which is the reconstruted to is original dimención) and X, we are prinimizing information 1055. Encoder Square

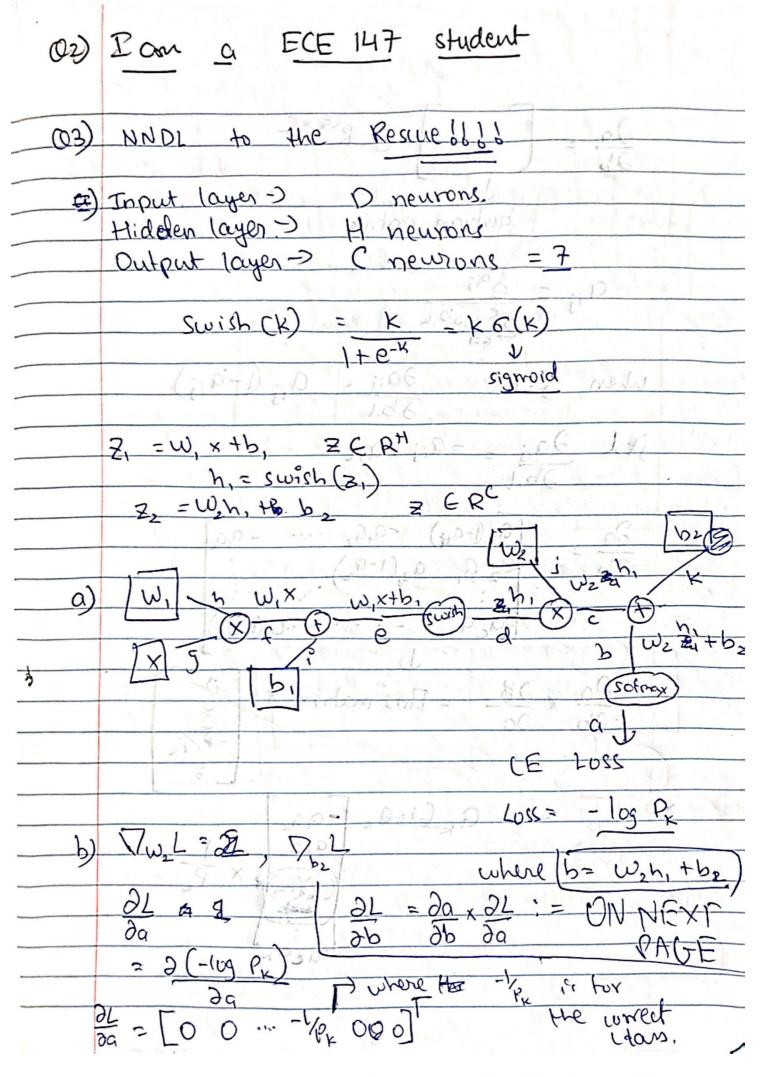


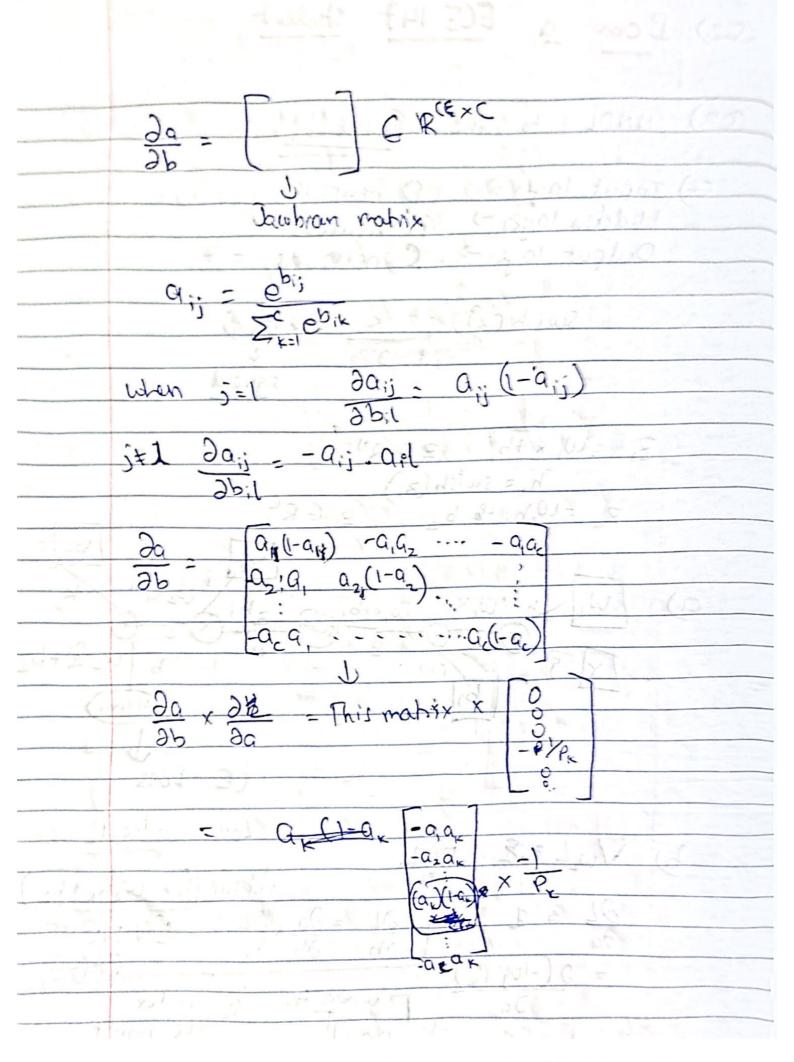
Whos 2 paths, one through Wx and one through W -> 0 -> WT -> W!Wx.

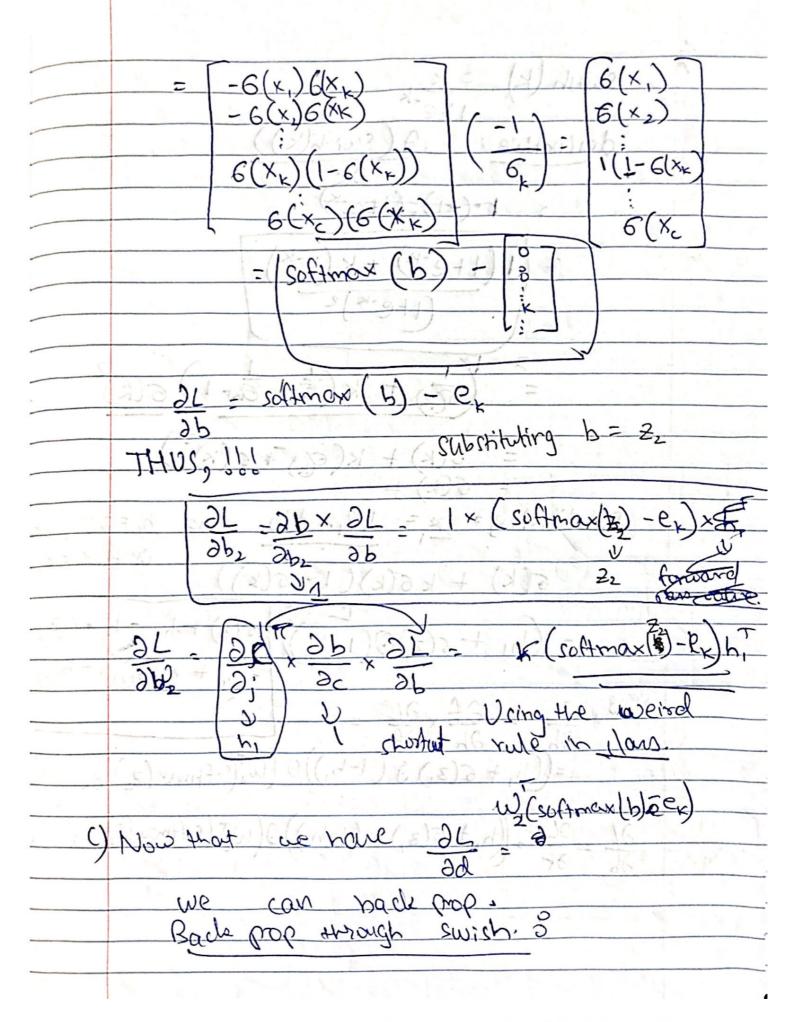
These converge at WTWX

Thus, we can just add they to $\frac{\partial L}{\partial W} = \frac{\partial g}{\partial W} = \frac{\partial L}{\partial W} + \frac{\partial g}{\partial W} = \frac{\partial L}{\partial W} =$ = 2 f , 2L = Usigg the Mickin class, Tours

= b x (Wx) T = bx TWT $\frac{\partial L}{\partial g} = \frac{\partial f}{\partial g} \times \frac{\partial L}{\partial g} = \frac{\partial f}{\partial g} \times \frac{\partial f}{\partial g} = \frac{\partial W}{\partial W} \times \frac{\partial W}{\partial \frac{\partial W}{\partial w} \times$ $\frac{\partial L}{\partial i} = \left(\frac{\partial L}{\partial k}\right)^{T} = \left(\frac{\partial$







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swish (K)
derlustive: (shains) 1 (1+6-K) + K (B-K) w (6K) + K(84 G) 6(K) = 6(K) + K(QK) + 6(K) Substituting = ze = W, x +6 and h, = swith(wx+1) 6(k) + k6(k)(1-6(k) h, + 6(z,)0(1-h,) 6(z)+h, -h, × 6(z,) =(h, + 6(z,)(1-h,) =((h, + 6(z,) 0 (1-h,)) 0 (W_2 (soffmax(z) -ex)) x DL DL = ((h, + 6(z,) 0 (1-h,)) 0 (W, (softmax(z))-ek))

Fully connected networks

In the previous notebook, you implemented a simple two-layer neural network class. However, this class is not modular. If you wanted to change the number of layers, you would need to write a new loss and gradient function. If you wanted to optimize the network with different optimizers, you'd need to write new training functions. If you wanted to incorporate regularizations, you'd have to modify the loss and gradient function.

Instead of having to modify functions each time, for the rest of the class, we'll work in a more modular framework where we define forward and backward layers that calculate losses and gradients respectively. Since the forward and backward layers share intermediate values that are useful for calculating both the loss and the gradient, we'll also have these function return "caches" which store useful intermediate values.

The goal is that through this modular design, we can build different sized neural networks for various applications.

In this HW #3, we'll define the basic architecture, and in HW #4, we'll build on this framework to implement different optimizers and regularizations (like BatchNorm and Dropout).

Modular layers

This notebook will build modular layers in the following manner. First, there will be a forward pass for a given layer with inputs (x) and return the output of that layer (out) as well as cached variables (cache) that will be used to calculate the gradient in the backward pass.

```
def layer_forward(x, w):
    """ Receive inputs x and weights w """
    # Do some computations ...
    z = # ... some intermediate value
    # Do some more computations ...
    out = # the output

cache = (x, w, z, out) # Values we need to compute gradients
    return out, cache
```

The backward pass will receive upstream derivatives and the cache object, and will return gradients with respect to the inputs and weights, like this:

```
def layer_backward(dout, cache):
    Receive derivative of loss with respect to outputs and cache,
    and compute derivative with respect to inputs.
    # Unpack cache values
    x, w, z, out = cache
```

```
# Use values in cache to compute derivatives
 dx = \# Derivative of loss with respect to x
 dw = # Derivative of loss with respect to w
  return dx, dw
## Import and setups
import time
import numpy as np
import matplotlib.pyplot as plt
from nndl.fc net import *
from utils.data utils import get CIFAR10 data
from utils.gradient check import eval numerical gradient,
eval numerical gradient array
from utils.solver import Solver
%matplotlib inline
plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of
plt.rcParams['image.interpolation'] = 'nearest'
plt.rcParams['image.cmap'] = 'gray'
# for auto-reloading external modules
# see http://stackoverflow.com/questions/1907993/autoreload-of-
modules-in-ipython
%load ext autoreload
%autoreload 2
from utils.data utils import load CIFAR10
def rel error(x, y):
  """ returns relative error """
  return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) +
np.abs(y)))
The autoreload extension is already loaded. To reload it, use:
 %reload ext autoreload
# Load the (preprocessed) CIFAR10 data.
# you may find an error here, this is may be because you forgot to use
correct path in get CIFAR10 data()
data = get CIFAR10 data()
for k in data.keys():
  print('{}: {} '.format(k, data[k].shape))
X train: (49000, 3, 32, 32)
y train: (49000,)
X val: (1000, 3, 32, 32)
y_val: (1000,)
```

```
X_test: (1000, 3, 32, 32)
y_test: (1000,)
```

Linear layers

In this section, we'll implement the forward and backward pass for the linear layers.

The linear layer forward pass is the function affine_forward in nndl/layers.py and the backward pass is affine_backward.

After you have implemented these, test your implementation by running the cell below.

Affine layer forward pass

Implement affine forward and then test your code by running the following cell.

```
# Test the affine forward function
num inputs = 2
input\_shape = (4, 5, 6)
output dim = 3
input size = num inputs * np.prod(input shape)
weight_size = output_dim * np.prod(input_shape)
x = np.linspace(-0.1, 0.5, num=input size).reshape(num inputs,
*input shape)
w = np.linspace(-0.2, 0.3,
num=weight size).reshape(np.prod(input shape), output dim)
b = np.linspace(-0.3, 0.1, num=output dim)
out, _ = affine_forward(x, w, b)
correct out = np.array([[1.49834967, 1.70660132, 1.91485297],
                        [ 3.25553199, 3.5141327, 3.77273342]])
# Compare your output with ours. The error should be around 1e-9.
print('Testing affine forward function:')
print('difference: {}'.format(rel error(out, correct out)))
Testing affine forward function:
difference: 9.769849468192957e-10
```

Affine layer backward pass

Implement affine backward and then test your code by running the following cell.

```
# Test the affine_backward function
x = np.random.randn(10, 2, 3)
```

```
w = np.random.randn(6, 5)
b = np.random.randn(5)
dout = np.random.randn(10, 5)
dx num = eval numerical gradient array(lambda x: affine forward(x, w,
b)[0], x, dout)
dw_num = eval_numerical_gradient_array(lambda w: affine_forward(x, w,
b)[0], w, dout)
db num = eval numerical gradient array(lambda b: affine forward(x, w,
b)[0], b, dout)
, cache = affine forward(x, w, b)
dx, dw, db = affine backward(dout, cache)
# The error should be around 1e-10
print('Testing affine backward function:')
print('dx error: {}'.format(rel_error(dx_num, dx)))
print('dw error: {}'.format(rel error(dw num, dw)))
print('db error: {}'.format(rel error(db num, db)))
Testing affine backward function:
dx error: 5.991058029944563e-11
dw error: 1.8299032572524863e-10
db error: 1.2667152476749587e-11
```

Activation layers

In this section you'll implement the ReLU activation.

ReLU forward pass

Implement the relu_forward function in nndl/layers.py and then test your code by running the following cell.

```
Testing relu_forward function: difference: 4.999999798022158e-08
```

ReLU backward pass

Implement the relu_backward function in nndl/layers.py and then test your code by running the following cell.

```
x = np.random.randn(10, 10)
dout = np.random.randn(*x.shape)

dx_num = eval_numerical_gradient_array(lambda x: relu_forward(x)[0],
x, dout)

_, cache = relu_forward(x)
dx = relu_backward(dout, cache)

# The error should be around 1e-12
print('Testing relu_backward function:')
print('dx error: {}'.format(rel_error(dx_num, dx)))

Testing relu_backward function:
dx error: 3.2756301865463762e-12
```

Combining the affine and ReLU layers

Often times, an affine layer will be followed by a ReLU layer. So let's make one that puts them together. Layers that are combined are stored in nndl/layer utils.py.

Affine-ReLU layers

We've implemented affine_relu_forward() and affine_relu_backward in nndl/layer_utils.py. Take a look at them to make sure you understand what's going on. Then run the following cell to ensure its implemented correctly.

```
from nndl.layer_utils import affine_relu_forward, affine_relu_backward

x = np.random.randn(2, 3, 4)
w = np.random.randn(12, 10)
b = np.random.randn(10)
dout = np.random.randn(2, 10)

out, cache = affine_relu_forward(x, w, b)
dx, dw, db = affine_relu_backward(dout, cache)

dx_num = eval_numerical_gradient_array(lambda x:
affine_relu_forward(x, w, b)[0], x, dout)
dw_num = eval_numerical_gradient_array(lambda w:
affine_relu_forward(x, w, b)[0], w, dout)
```

```
db_num = eval_numerical_gradient_array(lambda b:
affine_relu_forward(x, w, b)[0], b, dout)

print('Testing affine_relu_forward and affine_relu_backward:')
print('dx error: {}'.format(rel_error(dx_num, dx)))
print('dw error: {}'.format(rel_error(dw_num, dw)))
print('db error: {}'.format(rel_error(db_num, db)))

Testing affine_relu_forward and affine_relu_backward:
dx error: 4.513409204256411e-11
dw error: 2.2558493655605755e-10
db error: 8.307388460239596e-12
```

Softmax loss

You've already implemented it, so we have written it in layers.py. The following code will ensure they are working correctly.

```
num_classes, num_inputs = 10, 50
x = 0.001 * np.random.randn(num_inputs, num_classes)
y = np.random.randint(num_classes, size=num_inputs)

dx_num = eval_numerical_gradient(lambda x: softmax_loss(x, y)[0], x, verbose=False)
loss, dx = softmax_loss(x, y)

# Test softmax_loss function. Loss should be 2.3 and dx error should be 1e-8
print('\nTesting softmax_loss:')
print('loss: {}'.format(loss))
print('dx error: {}'.format(rel_error(dx_num, dx)))
Testing softmax_loss:
loss: 2.302868247381982
dx error: 1.0033469892341686e-08
```

Implementation of a two-layer NN

In nndl/fc_net.py, implement the class TwoLayerNet which uses the layers you made here. When you have finished, the following cell will test your implementation.

```
N, D, H, C = 3, 5, 50, 7
X = np.random.randn(N, D)
y = np.random.randint(C, size=N)
std = le-2
```

```
model = TwoLayerNet(input dim=D, hidden dims=H, num classes=C,
weight scale=std)
print('Testing initialization ... ')
W1 std = abs(model.params['W1'].std() - std)
b1 = model.params['b1']
W2 std = abs(model.params['W2'].std() - std)
b2 = model.params['b2']
assert W1_std < std / 10, 'First layer weights do not seem right'
assert np.all(b1 == 0), 'First layer biases do not seem right'
assert W2_std < std / 10, 'Second layer weights do not seem right'
assert np.all(b2 == 0), 'Second layer biases do not seem right'
print('Testing test-time forward pass ... ')
model.params['W1'] = np.linspace(-0.7, 0.3, num=D*H).reshape(D, H)
model.params['b1'] = np.linspace(-0.1, 0.9, num=H)
model.params['W2'] = np.linspace(-0.3, 0.4, num=H*C).reshape(H, C)
model.params['b2'] = np.linspace(-0.9, 0.1, num=C)
X = np.linspace(-5.5, 4.5, num=N*D).reshape(D, N).T
scores = model.loss(X)
correct scores = np.asarray(
  [[11.53165108, 12.2917344,
                                                13.81190102,
                                 13.05181771,
14.57198434, 15.33206765, 16.09215096],
   [12.05769098, 12.74614105, 13.43459113,
                                                14.1230412.
14.81149128, 15.49994135, 16.18839143],
   [12.58373087, 13.20054771, 13.81736455, 14.43418138,
15.05099822, 15.66781506, 16.2846319 11)
scores diff = np.abs(scores - correct scores).sum()
assert scores diff < 1e-6, 'Problem with test-time forward pass'
print('Testing training loss (no regularization)')
y = np.asarray([0, 5, 1])
loss, grads = model.loss(X, y)
correct loss = 3.4702243556
assert abs(loss - correct_loss) < 1e-10, 'Problem with training-time
loss'
model.reg = 1.0
loss, grads = model.loss(X, y)
correct loss = 26.5948426952
assert <a href="mailto:abs">assert <a href="mailto:abs">abs</a>(loss - correct_loss) < <a href="mailto:1e-10">1e-10</a>, 'Problem with regularization
loss'
for reg in [0.0, 0.7]:
  print('Running numeric gradient check with reg = {}'.format(reg))
  model.reg = reg
  loss, grads = model.loss(X, y)
  for name in sorted(grads):
    f = lambda _: model.loss(X, y)[0]
```

```
grad num = eval numerical gradient(f, model.params[name],
verbose=False)
    print('{} relative error: {}'.format(name, rel error(grad num,
grads[name])))
Testing initialization ...
Testing test-time forward pass ...
Testing training loss (no regularization)
Running numeric gradient check with reg = 0.0
W1 relative error: 1.5215703686475096e-08
W2 relative error: 3.2068321167375225e-10
b1 relative error: 8.368195737354163e-09
b2 relative error: 4.3291360264321544e-10
Running numeric gradient check with reg = 0.7
W1 relative error: 2.527915175868136e-07
W2 relative error: 2.8508510893102143e-08
b1 relative error: 1.5646801536371197e-08
b2 relative error: 7.759095355706557e-10
```

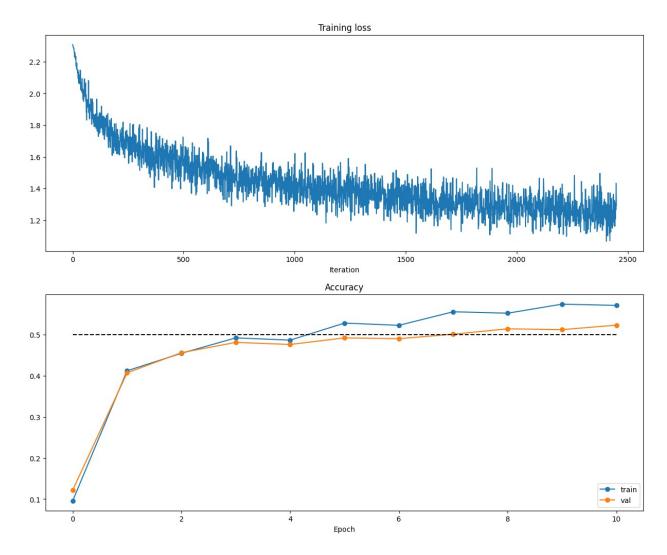
Solver

We will now use the utils Solver class to train these networks. Familiarize yourself with the API in utils/solver.py. After you have done so, declare an instance of a TwoLayerNet with 200 units and then train it with the Solver. Choose parameters so that your validation accuracy is at least 50%.

```
model = TwoLayerNet()
solver = None
# ================= #
# YOUR CODE HERE:
 Declare an instance of a TwoLayerNet and then train
   it with the Solver. Choose hyperparameters so that your validation
   accuracy is at least 50%. We won't have you optimize this further
   since you did it in the previous notebook.
#
model = TwoLayerNet(hidden dims=200)
solver = Solver(model=model, data=data, optim config={'learning rate':
0.0006}, lr decay=0.9, num train samples=2000, num epochs=10,
batch size=200, print every=50)
solver.train()
# END YOUR CODE HERE
# =========================== #
```

```
(Iteration 1 / 2450) loss: 2.307713
(Epoch 0 / 10) train acc: 0.096000; val acc: 0.122000
(Iteration 51 / 2450) loss: 1.966872
(Iteration 101 / 2450) loss: 1.864860
(Iteration 151 / 2450) loss: 1.808187
(Iteration 201 / 2450) loss: 1.705319
(Epoch 1 / 10) train acc: 0.412000; val acc: 0.407000
(Iteration 251 / 2450) loss: 1.726427
(Iteration 301 / 2450) loss: 1.585869
(Iteration 351 / 2450) loss: 1.648523
(Iteration 401 / 2450) loss: 1.542064
(Iteration 451 / 2450) loss: 1.547593
(Epoch 2 / 10) train acc: 0.454500; val acc: 0.456000
(Iteration 501 / 2450) loss: 1.572598
(Iteration 551 / 2450) loss: 1.569514
(Iteration 601 / 2450) loss: 1.493878
(Iteration 651 / 2450) loss: 1.500578
(Iteration 701 / 2450) loss: 1.556493
(Epoch 3 / 10) train acc: 0.492000; val acc: 0.481000
(Iteration 751 / 2450) loss: 1.384368
(Iteration 801 / 2450) loss: 1.415504
(Iteration 851 / 2450) loss: 1.627007
(Iteration 901 / 2450) loss: 1.555354
(Iteration 951 / 2450) loss: 1.398200
(Epoch 4 / 10) train acc: 0.486500; val acc: 0.476000
(Iteration 1001 / 2450) loss: 1.304034
(Iteration 1051 / 2450) loss: 1.336680
(Iteration 1101 / 2450) loss: 1.232518
(Iteration 1151 / 2450) loss: 1.414879
(Iteration 1201 / 2450) loss: 1.383723
(Epoch 5 / 10) train acc: 0.528000; val acc: 0.492000
(Iteration 1251 / 2450) loss: 1.256974
(Iteration 1301 / 2450) loss: 1.439812
(Iteration 1351 / 2450) loss: 1.387156
(Iteration 1401 / 2450) loss: 1.376448
(Iteration 1451 / 2450) loss: 1.261169
(Epoch 6 / 10) train acc: 0.522500; val acc: 0.490000
(Iteration 1501 / 2450) loss: 1.282738
(Iteration 1551 / 2450) loss: 1.355038
(Iteration 1601 / 2450) loss: 1.334716
(Iteration 1651 / 2450) loss: 1.291129
(Iteration 1701 / 2450) loss: 1.295876
(Epoch 7 / 10) train acc: 0.555500; val acc: 0.501000
(Iteration 1751 / 2450) loss: 1.127626
(Iteration 1801 / 2450) loss: 1.205444
(Iteration 1851 / 2450) loss: 1.181347
(Iteration 1901 / 2450) loss: 1.177063
(Iteration 1951 / 2450) loss: 1.312735
(Epoch 8 / 10) train acc: 0.552000; val acc: 0.514000
(Iteration 2001 / 2450) loss: 1.190539
```

```
(Iteration 2051 / 2450) loss: 1.299826
(Iteration 2101 / 2450) loss: 1.255337
(Iteration 2151 / 2450) loss: 1.130772
(Iteration 2201 / 2450) loss: 1.365917
(Epoch 9 / 10) train acc: 0.574000; val acc: 0.512000
(Iteration 2251 / 2450) loss: 1.238973
(Iteration 2301 / 2450) loss: 1.208276
(Iteration 2351 / 2450) loss: 1.249342
(Iteration 2401 / 2450) loss: 1.313017
(Epoch 10 / 10) train acc: 0.571000; val acc: 0.523000
# Run this cell to visualize training loss and train / val accuracy
plt.subplot(2, 1, 1)
plt.title('Training loss')
plt.plot(solver.loss history, '-')
plt.xlabel('Iteration')
plt.subplot(2, 1, 2)
plt.title('Accuracy')
plt.plot(solver.train_acc_history, '-o', label='train')
plt.plot(solver.val_acc_history, '-o', label='val')
plt.plot([0.5] * len(solver.val acc history), 'k--')
plt.xlabel('Epoch')
plt.legend(loc='lower right')
plt.gcf().set size inches(15, 12)
plt.show()
```



Multilayer Neural Network

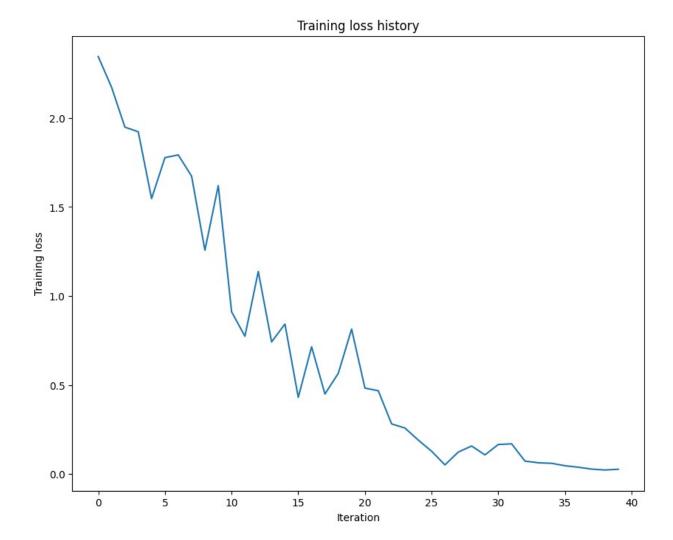
Now, we implement a multi-layer neural network.

Read through the FullyConnectedNet class in the file nndl/fc net.py.

Implement the initialization, the forward pass, and the backward pass. There will be lines for batchnorm and dropout layers and caches; ignore these all for now. That'll be in HW #4.

```
loss, grads = model.loss(X, y)
  print('Initial loss: {}'.format(loss))
  for name in sorted(grads):
    f = lambda : model.loss(X, y)[0]
    grad num = eval numerical gradient(f, model.params[name],
verbose=False, h=1e-5)
    print('{} relative error: {}'.format(name, rel error(grad num,
grads[name])))
Running check with reg = 0
Initial loss: 2.3029647255985943
W1 relative error: 7.25474992251241e-06
W2 relative error: 1.3653886594193302e-06
W3 relative error: 4.016447031312336e-07
b1 relative error: 4.3744119680732e-08
b2 relative error: 3.242335147561271e-09
b3 relative error: 7.450748227701268e-11
Running check with reg = 3.14
Initial loss: 6.78836760928242
W1 relative error: 2.698213332263102e-08
W2 relative error: 1.9675435737221835e-08
W3 relative error: 1.1067262553151193e-08
b1 relative error: 2.5741770601558084e-08
b2 relative error: 1.3450279529674712e-08
b3 relative error: 3.217926375348156e-10
# Use the three layer neural network to overfit a small dataset.
num train = 50
small data = {
  'X train': data['X train'][:num train],
  'y_train': data['y_train'][:num_train],
  'X val': data['X val'],
  'y_val': data['y_val'],
#### !!!!!!
# Play around with the weight scale and learning rate so that you can
overfit a small dataset.
# Your training accuracy should be 1.0 to receive full credit on this
part.
weight scale = 1e-2
learning rate = 1e-2
model = FullyConnectedNet([100, 100],
              weight scale=weight scale, dtype=np.float64)
solver = Solver(model, small_data,
                print every=10, num epochs=20, batch size=25,
```

```
update rule='sqd',
                optim config={
                  'learning rate': learning rate,
solver.train()
plt.plot(solver.loss history, '-')
plt.title('Training loss history')
plt.xlabel('Iteration')
plt.ylabel('Training loss')
plt.show()
(Iteration 1 / 40) loss: 2.344782
(Epoch 0 / 20) train acc: 0.340000; val acc: 0.123000
(Epoch 1 / 20) train acc: 0.180000; val acc: 0.120000
(Epoch 2 / 20) train acc: 0.480000; val acc: 0.137000
(Epoch 3 / 20) train acc: 0.560000; val acc: 0.153000
(Epoch 4 / 20) train acc: 0.620000; val acc: 0.161000
(Epoch 5 / 20) train acc: 0.660000; val acc: 0.191000
(Iteration 11 / 40) loss: 0.911175
(Epoch 6 / 20) train acc: 0.700000; val acc: 0.191000
(Epoch 7 / 20) train acc: 0.800000; val acc: 0.204000
(Epoch 8 / 20) train acc: 0.880000; val acc: 0.200000
(Epoch 9 / 20) train acc: 0.860000; val acc: 0.176000
(Epoch 10 / 20) train acc: 0.860000; val acc: 0.161000
(Iteration 21 / 40) loss: 0.482494
(Epoch 11 / 20) train acc: 0.940000; val acc: 0.185000
(Epoch 12 / 20) train acc: 0.980000; val acc: 0.203000
(Epoch 13 / 20) train acc: 1.000000; val acc: 0.198000
(Epoch 14 / 20) train acc: 1.000000; val_acc: 0.213000
(Epoch 15 / 20) train acc: 1.000000; val acc: 0.193000
(Iteration 31 / 40) loss: 0.165924
(Epoch 16 / 20) train acc: 1.000000; val acc: 0.186000
(Epoch 17 / 20) train acc: 1.000000; val acc: 0.191000
(Epoch 18 / 20) train acc: 1.000000; val_acc: 0.200000
(Epoch 19 / 20) train acc: 1.000000; val acc: 0.193000
(Epoch 20 / 20) train acc: 1.000000; val acc: 0.200000
```



This is the 2-layer neural network notebook for ECE C147/C247 Homework #3

Please follow the notebook linearly to implement a two layer neural network.

Please print out the notebook entirely when completed.

The goal of this notebook is to give you experience with training a two layer neural network.

```
import random
import numpy as np
from utils.data_utils import load_CIFAR10
import matplotlib.pyplot as plt

%matplotlib inline
%load_ext autoreload
%autoreload 2

def rel_error(x, y):
    """ returns relative error """
    return np.max(np.abs(x - y) / (np.maximum(le-8, np.abs(x) + np.abs(y))))

The autoreload extension is already loaded. To reload it, use:
    %reload_ext autoreload
```

Toy example

Before loading CIFAR-10, there will be a toy example to test your implementation of the forward and backward pass. Make sure to read the description of TwoLayerNet class in neural_net.py file, understand the architecture and initializations

```
from nndl.neural_net import TwoLayerNet

# Create a small net and some toy data to check your implementations.
# Note that we set the random seed for repeatable experiments.
input_size = 4
hidden_size = 10
num_classes = 3
num_inputs = 5

def init_toy_model():
    np.random.seed(0)
    return TwoLayerNet(input_size, hidden_size, num_classes, std=1e-1)

def init_toy_data():
    np.random.seed(1)
    X = 10 * np.random.random.random.inputs, input_size)
```

```
y = np.array([0, 1, 2, 2, 1])
return X, y

net = init_toy_model()
X, y = init_toy_data()
```

Compute forward pass scores

```
## Implement the forward pass of the neural network.
## See the loss() method in TwoLayerNet class for the same
# Note, there is a statement if y is None: return scores, which is why
# the following call will calculate the scores.
scores = net.loss(X)
print('Your scores:')
print(scores)
print()
print('correct scores:')
correct scores = np.asarray([
    [-1.07260209, 0.05083871, -0.87253915],
[-2.02778743, -0.10832494, -1.52641362],
    [-0.74225908, 0.15259725, -0.39578548],
    [-0.38172726, 0.10835902, -0.17328274],
    [-0.64417314, -0.18886813, -0.41106892]])
print(correct scores)
print()
# The difference should be very small. We get < 1e-7
print('Difference between your scores and correct scores:')
print(np.sum(np.abs(scores - correct scores)))
Your scores:
[[-1.07260209 0.05083871 -0.87253915]
 [-2.02778743 -0.10832494 -1.52641362]
 [-0.74225908 0.15259725 -0.39578548]
 [-0.38172726 0.10835902 -0.17328274]
 [-0.64417314 -0.18886813 -0.41106892]]
correct scores:
[[-1.07260209 0.05083871 -0.87253915]
 [-2.02778743 -0.10832494 -1.52641362]
 [-0.74225908  0.15259725  -0.39578548]
 [-0.38172726 0.10835902 -0.17328274]
 [-0.64417314 -0.18886813 -0.41106892]]
Difference between your scores and correct scores:
3.381231233889892e-08
```

Forward pass loss

```
loss, _ = net.loss(X, y, reg=0.05)
correct_loss = 1.071696123862817

# should be very small, we get < 1e-12
print("Loss:",loss)
print('Difference between your loss and correct loss:')
print(np.sum(np.abs(loss - correct_loss)))

Loss: 1.071696123862817
Difference between your loss and correct loss:
0.0</pre>
```

Backward pass

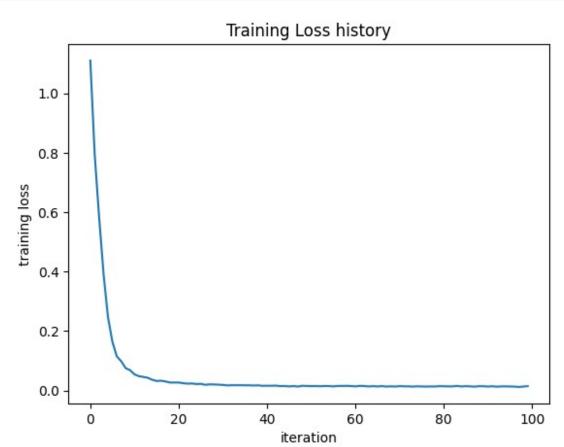
Implements the backwards pass of the neural network. Check your gradients with the gradient check utilities provided.

```
from utils.gradient check import eval numerical gradient
# Use numeric gradient checking to check your implementation of the
backward pass.
# If your implementation is correct, the difference between the
numeric and
# analytic gradients should be less than 1e-8 for each of W1, W2, b1,
and b2.
loss, grads = net.loss(X, y, reg=0.05)
# these should all be less than 1e-8 or so
for param name in grads:
    f = lambda W: net.loss(X, y, reg=0.05)[0]
    param grad num = eval numerical gradient(f,
net.params[param name], verbose=False)
    print('{} max relative error: {}'.format(param name,
rel error(param grad num, grads[param name])))
W2 max relative error: 2.9632227682005116e-10
b2 max relative error: 1.2482660547101085e-09
W1 max relative error: 1.2832874456864775e-09
bl max relative error: 3.1726806716844575e-09
```

Training the network

Implement neural_net.train() to train the network via stochastic gradient descent, much like the softmax and SVM.

```
net = init_toy_model()
stats = net.train(X, y, X, y,
```



Classify CIFAR-10

Do classification on the CIFAR-10 dataset.

```
from utils.data_utils import load_CIFAR10

def get_CIFAR10_data(num_training=49000, num_validation=1000,
num_test=1000):
```

```
0.00
    Load the CIFAR-10 dataset from disk and perform preprocessing to
prepare
    it for the two-layer neural net classifier.
    # Load the raw CIFAR-10 data
    cifar10 dir =
'/Users/krishpatel/Desktop/HW3 code/utils/datasets/cifar-10-batches-
py' # remember to use correct path
    X train, y train, X test, y test = load CIFAR10(cifar10 dir)
    # Subsample the data
    mask = list(range(num_training, num training + num validation))
    X val = X train[mask]
    y_val = y_train[mask]
    mask = list(range(num training))
    X train = X train[mask]
    y train = y train[mask]
    mask = list(range(num test))
    X \text{ test} = X \text{ test[mask]}
    y test = y test[mask]
    # Normalize the data: subtract the mean image
    mean image = np.mean(X train, axis=0)
    X train -= mean image
    X val -= mean image
    X test -= mean image
    # Reshape data to rows
    X train = X train.reshape(num training, -1)
    X val = X val.reshape(num validation, -1)
    X test = X test.reshape(num test, -1)
    return X train, y train, X val, y val, X test, y test
# Invoke the above function to get our data.
X_train, y_train, X_val, y_val, X_test, y_test = get_CIFAR10_data()
print('Train data shape: ', X_train.shape)
print('Train labels shape: ', y_train.shape)
print('Validation data shape: '
print('Validation data shape: ', X_val.shape)
print('Validation labels shape: ', y_val.shape)
print('Test data shape: ', X_test.shape)
print('Test labels shape: ', y test.shape)
Train data shape: (49000, 3072)
Train labels shape: (49000,)
Validation data shape: (1000, 3072)
Validation labels shape: (1000,)
```

```
Test data shape: (1000, 3072)
Test labels shape: (1000,)
```

Running SGD

If your implementation is correct, you should see a validation accuracy of around 28-29%.

```
input size = 32 * 32 * 3
hidden size = 50
num classes = 10
net = TwoLayerNet(input size, hidden size, num classes)
# Train the network
stats = net.train(X train, y train, X val, y val,
            num iters=1000, batch size=200,
            learning_rate=le-4, learning_rate_decay=0.95,
            reg=0.25, verbose=True)
# Predict on the validation set
val acc = (net.predict(X val) == y val).mean()
print('Validation accuracy: ', val acc)
# Save this net as the variable subopt net for later comparison.
subopt net = net
iteration 0 / 1000: loss 2.302757518613176
iteration 100 / 1000: loss 2.302120159207236
iteration 200 / 1000: loss 2.2956136007408703
iteration 300 / 1000: loss 2.2518259043164135
iteration 400 / 1000: loss 2.188995235046776
iteration 500 / 1000: loss 2.1162527791897747
iteration 600 / 1000: loss 2.064670827698217
iteration 700 / 1000: loss 1.9901688623083942
iteration 800 / 1000: loss 2.002827640124685
iteration 900 / 1000: loss 1.9465176817856502
Validation accuracy: 0.283
```

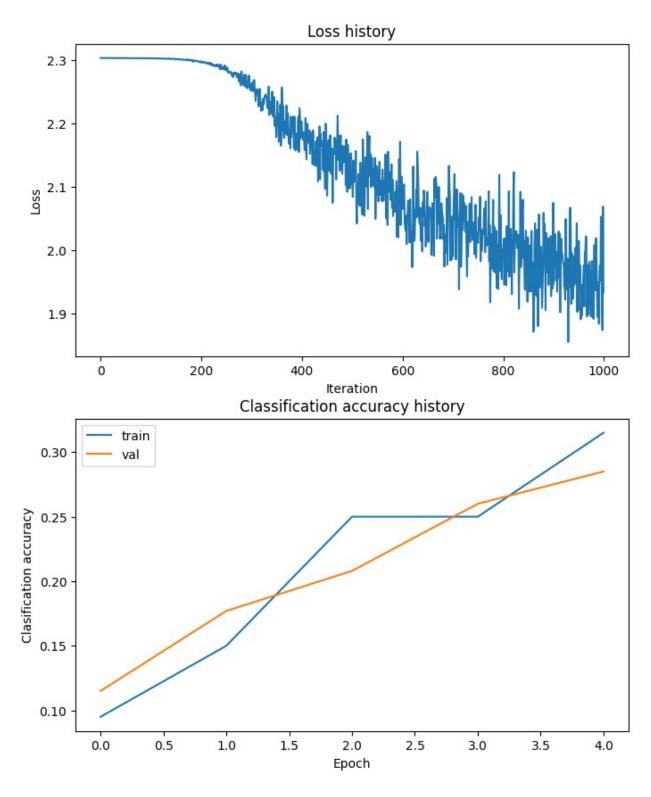
Questions:

The training accuracy isn't great.

- (1) What are some of the reasons why this is the case? Take the following cell to do some analyses and then report your answers in the cell following the one below.
- (2) How should you fix the problems you identified in (1)?

```
stats['train_acc_history']
[0.095, 0.15, 0.25, 0.25, 0.315]
```

```
# YOUR CODE HERE:
 Do some debugging to gain some insight into why the optimization
  isn't great.
# ================= #
# Plot the loss function and train / validation accuracies
fig, ax = plt.subplots(2, 1, figsize=(8, 10))
ax[0].plot(stats['loss history'])
ax[0].set title('Loss history')
ax[0].set_xlabel('Iteration')
ax[0].set_ylabel('Loss')
ax[1].plot(stats['train acc history'], label='train')
ax[1].plot(stats['val acc history'], label='val')
ax[1].set_title('Classification accuracy history')
ax[1].set xlabel('Epoch')
ax[1].set ylabel('Clasification accuracy')
ax[1].legend()
plt.show()
# ================= #
# END YOUR CODE HERE
```



Answers:

(1) According to the Loss Vs Iteration graph, it appears that the loss doesn't decrease by a large factorand instead stays almost flat, hinting that the learning rate might be too low. Also, both

the training and validation sets show similar but poor accuracy, and haven't reached convergence or stability. This suggests we might need more iterations to see improvements.

(2) To improve accuracy, we need to adjust certain settings such as our learning rate parameter, the iteration count, how much we penalize complex models (regularization coefficient), and the number of samples per batch (batch size).

Optimize the neural network

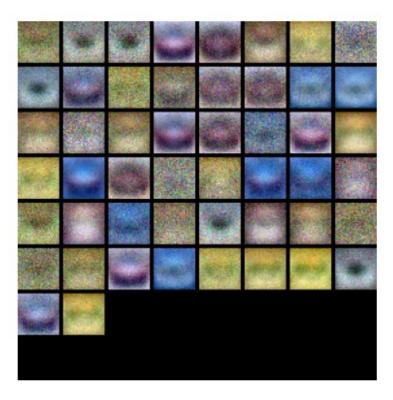
Use the following part of the Jupyter notebook to optimize your hyperparameters on the validation set. Store your nets as best_net.

```
best net = None # store the best model into this
# YOUR CODE HERE:
  Optimize over your hyperparameters to arrive at the best neural
   network. You should be able to get over 50% validation accuracy.
  For this part of the notebook, we will give credit based on the
    accuracy you get. Your score on this question will be multiplied
by:
#
       min(floor((X - 28\%)) / \%22, 1)
    where if you get 50% or higher validation accuracy, you get full
   points.
#
  Note, you need to use the same network structure (keep hidden size
= 50)!
input size = 32 * 32 * 3
hidden size = 50
num classes = 10
iteration numbers = np.arange((2, 4) * 10**3
reg coefs = np.arange(0.1, 0.25, 0.05)
learning rates = np.power(10, -np.arange(3.0, 4.1, 0.1))
batch sizes = np.arange(200, 260, 10)
best val= 0
for iteration_number in iteration_numbers:
    for reg coef in reg coefs:
        for batch size in batch sizes:
            for learning rate in learning rates:
                net = TwoLayerNet(input size, hidden size,
num classes)
                stats = net.train(X train, y train, X val,
y val, num iters=iteration number, batch size=batch size,
learning rate=learning rate, learning_rate_decay=0.95, reg=reg_coef,
verbose=False)
                val acc = (net.predict(X val)==y val).mean()
```

```
print("Training accuracy for this iteration:",
(net.predict(X train) == y train).mean())
               print("Validation accuracy for this iteration:",
val acc)
               print("n iteration:", iteration number)
               print("reg_coef:", reg_coef)
               print("batch size:", batch size)
               print("learning_rate:", learning_rate)
               if best val < val acc:</pre>
                  best val = val acc
               if val acc \geq 0.5:
                  best net = net
                  break
           else:
               continue
           break
       else:
           continue
       break
   else:
       continue
   break
# =========== #
# END YOUR CODE HERE
# ======== #
if best net is not None:
   val acc = (best net.predict(X val) == y val).mean()
   print('Validation accuracy: ', val acc)
else:
   print("No best network found.")
Training accuracy for this iteration: 0.5378979591836734
Validation accuracy for this iteration: 0.492
n iteration: 2000
reg coef: 0.1
batch size: 200
learning rate: 0.001
Training accuracy for this iteration: 0.5268979591836734
Validation accuracy for this iteration: 0.493
n iteration: 2000
rea coef: 0.1
batch size: 200
learning rate: 0.0007943282347242813
Training accuracy for this iteration: 0.5143469387755102
Validation accuracy for this iteration: 0.484
n iteration: 2000
reg coef: 0.1
batch size: 200
```

```
learning rate: 0.000630957344480193
Training accuracy for this iteration: 0.5006734693877551
Validation accuracy for this iteration: 0.494
n iteration: 2000
reg coef: 0.1
batch size: 200
learning rate: 0.000501187233627272
Training accuracy for this iteration: 0.48653061224489796
Validation accuracy for this iteration: 0.465
n iteration: 2000
reg_coef: 0.1
batch size: 200
learning_rate: 0.0003981071705534969
Training accuracy for this iteration: 0.467734693877551
Validation accuracy for this iteration: 0.454
n iteration: 2000
reg_coef: 0.1
batch size: 200
learning rate: 0.0003162277660168376
Training accuracy for this iteration: 0.4459183673469388
Validation accuracy for this iteration: 0.443
n iteration: 2000
reg coef: 0.1
batch size: 200
learning rate: 0.0002511886431509577
Training accuracy for this iteration: 0.42675510204081635
Validation accuracy for this iteration: 0.429
n iteration: 2000
reg coef: 0.1
batch size: 200
learning rate: 0.00019952623149688769
Training accuracy for this iteration: 0.4018775510204082
Validation accuracy for this iteration: 0.392
n iteration: 2000
reg coef: 0.1
batch size: 200
learning rate: 0.0001584893192461111
Training accuracy for this iteration: 0.3798979591836735
Validation accuracy for this iteration: 0.38
n iteration: 2000
reg coef: 0.1
batch size: 200
learning_rate: 0.0001258925411794165
Training accuracy for this iteration: 0.35612244897959183
Validation accuracy for this iteration: 0.362
n iteration: 2000
reg coef: 0.1
batch size: 200
learning rate: 9.9999999999998e-05
```

```
Training accuracy for this iteration: 0.5289795918367347
Validation accuracy for this iteration: 0.497
n iteration: 2000
reg coef: 0.1
batch size: 210
learning_rate: 0.001
Training accuracy for this iteration: 0.5319795918367347
Validation accuracy for this iteration: 0.508
n_iteration: 2000
reg coef: 0.1
batch size: 210
learning_rate: 0.0007943282347242813
Validation accuracy: 0.508
from utils.vis utils import visualize grid
# Visualize the weights of the network
def show net weights(net):
    W1 = net.params['W1']
    W1 = W1.T.reshape(32, 32, 3, -1).transpose(3, 0, 1, 2)
    plt.imshow(visualize_grid(W1, padding=3).astype('uint8'))
    plt.gca().axis('off')
    plt.show()
show net weights(subopt net)
show net weights(best net)
```





Question:

(1) What differences do you see in the weights between the suboptimal net and the best net you arrived at?

Answer:

(1) The best net seems to preserve more features about the visual charactersistics. However in the subopt, all of the features seem to be much more blurred(looks like a gaussian blue), thus suggesting that the latesr don't do well at preserving the features.

Evaluate on test set

```
test_acc = (best_net.predict(X_test) == y_test).mean()
print('Test accuracy: ', test_acc)
Test accuracy: 0.489
```

```
import numpy as np
from .layers import *
from .layer_utils import *
class TwoLayerNet(object):
 A two-layer fully-connected neural network with ReLU nonlinearity and
 softmax loss that uses a modular layer design. We assume an input dimension
 of D, a hidden dimension of H, and perform classification over C classes.
 The architecure should be affine - relu - affine - softmax.
 Note that this class does not implement gradient descent; instead, it
 will interact with a separate Solver object that is responsible for running
 optimization.
 The learnable parameters of the model are stored in the dictionary
 self.params that maps parameter names to numpy arrays.
 def init (self, input dim=3*32*32, hidden dims=100, num classes=10,
             dropout=0, weight scale=1e-3, reg=0.0):
   Initialize a new network.
   Inputs:
   - input dim: An integer giving the size of the input
   - hidden dims: An integer giving the size of the hidden layer
   - num classes: An integer giving the number of classes to classify
   - dropout: Scalar between 0 and 1 giving dropout strength.
   - weight scale: Scalar giving the standard deviation for random
     initialization of the weights.
   - reg: Scalar giving L2 regularization strength.
   self.params = {}
   self.reg = reg
   # YOUR CODE HERE:
      Initialize W1, W2, b1, and b2. Store these as self.params['W1'],
     self.params['W2'], self.params['b1'] and self.params['b2']. The
     biases are initialized to zero and the weights are initialized
     so that each parameter has mean 0 and standard deviation weight scale.
     The dimensions of W1 should be (input dim, hidden dim) and the
      dimensions of W2 should be (hidden dims, num classes)
   # ----- #
   self.params['W1'] = np.random.normal(0, weight scale, (input dim, hidden dims))
   self.params['W2'] = np.random.normal(0, weight_scale, (hidden_dims, num_classes))
   self.params['b1'] = np.zeros(hidden_dims)
   self.params['b2'] = np.zeros(num classes)
   # END YOUR CODE HERE
   def loss(self, X, y=None):
   Compute loss and gradient for a minibatch of data.
   Inputs:
   - X: Array of input data of shape (N, d 1, ..., d k)
   - y: Array of labels, of shape (N,). y[i] gives the label for X[i].
   Returns:
```

```
If y is None, then run a test-time forward pass of the model and return:
   - scores: Array of shape (N, C) giving classification scores, where
    scores[i, c] is the classification score for X[i] and class c.
   If y is not None, then run a training-time forward and backward pass and
   return a tuple of:
   - loss: Scalar value giving the loss
   - grads: Dictionary with the same keys as self.params, mapping parameter
    names to gradients of the loss with respect to those parameters.
   scores = None
   # ----- #
   # YOUR CODE HERE:
     Implement the forward pass of the two-layer neural network. Store
     the class scores as the variable 'scores'. Be sure to use the layers
     you prior implemented.
   hidden, cache hidden = affine relu forward(X, self.params['W1'], self.params['b1'])
   scores, cache scores = affine forward(hidden, self.params['W2'], self.params['b2'])
   # ----- #
   # END YOUR CODE HERE
   # If y is None then we are in test mode so just return scores
   if y is None:
    return scores
   loss, grads = 0, {}
   # ----- #
   # YOUR CODE HERE:
   # Implement the backward pass of the two-layer neural net. Store
   # the loss as the variable 'loss' and store the gradients in the
    'grads' dictionary. For the grads dictionary, grads['W1'] holds
     the gradient for W1, grads['b1'] holds the gradient for b1, etc.
      i.e., grads[k] holds the gradient for self.params[k].
     Add L2 regularization, where there is an added cost 0.5*self.reg*W^2
    for each W. Be sure to include the 0.5 multiplying factor to
     match our implementation.
     And be sure to use the layers you prior implemented.
   # ----- #
   loss, dout = softmax loss(scores, y)
   loss += 0.5 * self.reg * (np.sum(self.params['W1'] ** 2) + np.sum(self.params['W2'] ** 2))
   dh, dw2, db2 = affine backward(dout, cache scores)
   dx, dw1, db1 = affine relu backward(dh, cache hidden)
   grads['W1'] = dw1 + self.reg * self.params['W1']
   grads['b1'] = db1
   grads['W2'] = dw2 + self.reg * self.params['W2']
   qrads['b2'] = db2
   # END YOUR CODE HERE
   return loss, grads
class FullyConnectedNet(object):
 A fully-connected neural network with an arbitrary number of hidden layers,
```

ReLU nonlinearities, and a softmax loss function. This will also implement

```
dropout and batch normalization as options. For a network with L layers,
 the architecture will be
 \{affine - [batch norm] - relu - [dropout]\} x (L - 1) - affine - softmax
 where batch normalization and dropout are optional, and the {...} block is
 repeated L - 1 times.
 Similar to the TwoLayerNet above, learnable parameters are stored in the
 self.params dictionary and will be learned using the Solver class.
 def init (self, hidden dims, input dim=3*32*32, num classes=10,
             dropout=0, use batchnorm=False, reg=0.0,
             weight scale=1e-2, dtype=np.float32, seed=None):
   Initialize a new FullyConnectedNet.
   Inputs:
   - hidden dims: A list of integers giving the size of each hidden layer.
   - input dim: An integer giving the size of the input.
   - num classes: An integer giving the number of classes to classify.
   - dropout: Scalar between 0 and 1 giving dropout strength. If dropout=0 then
     the network should not use dropout at all.
   - use batchnorm: Whether or not the network should use batch normalization.
   - reg: Scalar giving L2 regularization strength.
   - weight scale: Scalar giving the standard deviation for random
     initialization of the weights.
   - dtype: A numpy datatype object; all computations will be performed using
     this datatype. float32 is faster but less accurate, so you should use
     float64 for numeric gradient checking.
   - seed: If not None, then pass this random seed to the dropout layers. This
     will make the dropout layers deteriminstic so we can gradient check the
   11 11 11
   self.use_batchnorm = use_batchnorm
   self.use dropout = dropout > 0
   self.reg = reg
   self.num layers = 1 + len(hidden dims)
   self.dtype = dtype
   self.params = {}
   # ----- #
   # YOUR CODE HERE:
     Initialize all parameters of the network in the self.params dictionary.
     The weights and biases of layer 1 are W1 and b1; and in general the
      weights and biases of layer i are Wi and bi. The
      biases are initialized to zero and the weights are initialized
     so that each parameter has mean 0 and standard deviation weight scale.
   # ----- #
   for i in np.arange(self.num layers):
     if(i == 0):
       self.params['W' + str(i+1)] = np.random.normal(0, weight scale, (input dim,
hidden dims[i]))
       self.params['b' + str(i+1)] = np.zeros(hidden dims[i])
     elif(i == self.num layers - 1):
       self.params['W' + str(i+1)] = np.random.normal(0, weight_scale, (hidden_dims[i-1],
num classes))
       self.params['b' + str(i+1)] = np.zeros(num classes)
       self.params['W' + str(i+1)] = np.random.normal(0, weight scale, (hidden dims[i-1],
hidden dims[i]))
      self.params['b' + str(i+1)] = np.zeros(hidden dims[i])
   # ------ #
   # END YOUR CODE HERE
```

```
# When using dropout we need to pass a dropout param dictionary to each
   # dropout layer so that the layer knows the dropout probability and the mode
   # (train / test). You can pass the same dropout_param to each dropout layer.
   self.dropout param = {}
   if self.use dropout:
     self.dropout param = {'mode': 'train', 'p': dropout}
     if seed is not None:
       self.dropout param['seed'] = seed
   # With batch normalization we need to keep track of running means and
   # variances, so we need to pass a special bn_param object to each batch
   # normalization layer. You should pass self.bn params[0] to the forward pass
   # of the first batch normalization layer, self.bn_params[1] to the forward
   # pass of the second batch normalization layer, etc.
   self.bn params = []
   if self.use batchnorm:
     self.bn params = [{'mode': 'train'} for i in np.arange(self.num layers - 1)]
   # Cast all parameters to the correct datatype
   for k, v in self.params.items():
     self.params[k] = v.astype(dtype)
 def loss(self, X, y=None):
   Compute loss and gradient for the fully-connected net.
   Input / output: Same as TwoLayerNet above.
   11 11 11
   X = X.astype(self.dtype)
   mode = 'test' if y is None else 'train'
   # Set train/test mode for batchnorm params and dropout param since they
   # behave differently during training and testing.
   if self.dropout param is not None:
     self.dropout param['mode'] = mode
   if self.use batchnorm:
     for bn param in self.bn params:
       bn param[mode] = mode
   scores = None
   # YOUR CODE HERE:
      Implement the forward pass of the FC net and store the output
       scores as the variable "scores".
   H = []
   H cache = []
   for i in range(self.num layers):
     H app = None
     H cache app = None
     if(i == 0):
       H app, H cache app = affine relu forward(X, self.params['W' + str(i+1)],
self.params['b' + str(i+1)])
       H.append(H app)
       H cache.append(H cache app)
     elif(i == self.num layers - 1):
       scores, H_cache_app = affine_forward(H[i-1], self.params['W' + str(i+1)],
self.params['b' + str(i+1)])
       H cache.append(H cache app)
     else:
       H app, H cache app = affine relu forward(H[i-1], self.params['W' + str(i+1)],
self.params['b' + str(i+1)])
       H.append(H app)
```

```
H_cache.append(H_cache_app)
   # END YOUR CODE HERE
    ______#
   # If test mode return early
   if mode == 'test':
    return scores
   loss, grads = 0.0, {}
   # ----- #
   # YOUR CODE HERE:
   # Implement the backwards pass of the FC net and store the gradients
    in the grads dict, so that grads[k] is the gradient of self.params[k]
     Be sure your L2 regularization includes a 0.5 factor.
   loss, dhidden = softmax loss(scores, y)
   for i in range(self.num layers, 0, -1):
    loss += 0.5*self.reg*np.sum(self.params['W{}'.format(i)]*self.params['W{}'.format(i)])
    if i == self.num layers:
      dH1, dW, db = affine backward(dhidden, H cache[i-1])
      grads['W{}'.format(i)] = dW + self.reg*self.params['W{}'.format(i)]
      grads['b{}'.format(i)] = db
    else:
      dH1, dW, db = affine relu backward(dH1,H cache[i-1])
      grads['W{}'.format(i)] = dW + self.reg*self.params['W{}'.format(i)]
      grads['b{}'.format(i)] = db
   # loss, dout = softmax loss(H[self.num layers - 1], y)
   # for i in np.arange(self.num layers):
       loss += 0.5 * self.reg * np.sum(self.params['W' + str(i+1)] * self.params['W' +
str(i+1)])
   # for i in np.arange(self.num layers - 1, -1, -1):
      if(i == self.num layers - 1):
           dx, grads['W' + str(i+1)], grads['b' + str(i+1)] = affine backward(dout,
cache[i])
      else:
          dx, grads['W' + str(i+1)], grads['b' + str(i+1)] = affine relu backward(dx,
cache[i])
        grads['W' + str(i+1)] += self.reg * self.params['W' + str(i+1)]
   # END YOUR CODE HERE
   # ------ #
   return loss, grads
```

```
import pdb
def affine forward(x, w, b):
 Computes the forward pass for an affine (fully-connected) layer.
 The input x has shape (N, d_1, ..., d_k) and contains a minibatch of N
 examples, where each example x[i] has shape (d_1, \ldots, d_k). We will
 reshape each input into a vector of dimension D = d 1 * ... * d k, and
 then transform it to an output vector of dimension M.
 Inputs:
 - x: A numpy array containing input data, of shape (N, d 1, ..., d k)
 - w: A numpy array of weights, of shape (D, M)
 - b: A numpy array of biases, of shape (M,)
 Returns a tuple of:
 - out: output, of shape (N, M)
 - cache: (x, w, b)
 # YOUR CODE HERE:
 # Calculate the output of the forward pass. Notice the dimensions
   of w are D x M, which is the transpose of what we did in earlier
 # assignments.
 # ----- #
 X = x.reshape((x.shape[0], -1))
 out = np.dot(X, w) + b
 # END YOUR CODE HERE
 cache = (x, w, b)
 return out, cache
def affine backward(dout, cache):
 Computes the backward pass for an affine layer.
 Inputs:
 - dout: Upstream derivative, of shape (N, M)
 - cache: Tuple of:
   - x: Input data, of shape (N, d 1, \ldots d k)
   - w: Weights, of shape (D, M)
 Returns a tuple of:
 - dx: Gradient with respect to x, of shape (N, d1, ..., dk)
 - dw: Gradient with respect to w, of shape (D, M)
 - db: Gradient with respect to b, of shape (M,)
 11 11 11
 x, w, b = cache
 dx, dw, db = None, None, None
 # ----- #
 # YOUR CODE HERE:
   Calculate the gradients for the backward pass.
 # ----- #
 X = x.reshape((x.shape[0], -1))
 db = np.sum(dout,axis=0)
 dw = np.dot(X.T, dout)
```

import numpy as np

```
# dout is N x M
 \# dx should be N x d1 x ... x dk; it relates to dout through multiplication with w, which is
 \# dw should be D x M; it relates to dout through multiplication with x, which is N x D after
reshaping
 # db should be M; it is just the sum over dout examples
 # ----- #
 # END YOUR CODE HERE
 # ----- #
 return dx, dw, db
def relu forward(x):
 Computes the forward pass for a layer of rectified linear units (ReLUs).
 Input:
 - x: Inputs, of any shape
 Returns a tuple of:
 - out: Output, of the same shape as x
 - cache: x
 # ============= #
 # YOUR CODE HERE:
   Implement the ReLU forward pass.
 # ------ #
 out = np.maximum(0,x)
 # END YOUR CODE HERE
 # ----- #
 cache = x
 return out, cache
def relu backward(dout, cache):
 Computes the backward pass for a layer of rectified linear units (ReLUs).
 - dout: Upstream derivatives, of any shape
 - cache: Input x, of same shape as dout
 Returns:
 - dx: Gradient with respect to x
 ** ** **
 x = cache
 # ------ #
 # YOUR CODE HERE:
   Implement the ReLU backward pass
 # ============= #
 # ReLU directs linearly to those > 0
 dx = dout*(x>0)
 # END YOUR CODE HERE
```

dx = np.dot(dout, w.T).reshape(x.shape)

return dx

```
def softmax loss(x, y):
  Computes the loss and gradient for softmax classification.
  Inputs:
  - x: Input data, of shape (N, C) where x[i, j] is the score for the jth class
   for the ith input.
  - y: Vector of labels, of shape (N,) where y[i] is the label for x[i] and
   0 \le y[i] < C
  Returns a tuple of:
  - loss: Scalar giving the loss
  - dx: Gradient of the loss with respect to x
  probs = np.exp(x - np.max(x, axis=1, keepdims=True))
  probs /= np.sum(probs, axis=1, keepdims=True)
  N = x.shape[0]
  loss = -np.sum(np.log(probs[np.arange(N), y])) / N
  dx = probs.copy()
  dx[np.arange(N), y] = 1
  dx /= N
  return loss, dx
```

```
import numpy as np
import matplotlib.pyplot as plt
class TwoLayerNet(object):
 A two-layer fully-connected neural network. The net has an input dimension of
 D, a hidden layer dimension of H, and performs classification over C classes.
 We train the network with a softmax loss function and L2 regularization on the
 weight matrices. The network uses a ReLU nonlinearity after the first fully
 connected layer.
 In other words, the network has the following architecture:
  input - fully connected layer - ReLU - fully connected layer - softmax
  The outputs of the second fully-connected layer are the scores for each class.
      __init__(self, input_size, hidden_size, output_size, std=1e-4):
 def
   Initialize the model. Weights are initialized to small random values and
   biases are initialized to zero. Weights and biases are stored in the
   variable self.params, which is a dictionary with the following keys:
   W1: First layer weights; has shape (H, D)
   b1: First layer biases; has shape (H,)
   W2: Second layer weights; has shape (C, H)
   b2: Second layer biases; has shape (C,)
   Inputs:
   - input size: The dimension D of the input data.
   - hidden size: The number of neurons H in the hidden layer.
   - output size: The number of classes C.
   11 11 11
   self.params = {}
   self.params['W1'] = std * np.random.randn(hidden size, input size)
   self.params['b1'] = np.zeros(hidden size)
   self.params['W2'] = std * np.random.randn(output size, hidden size)
   self.params['b2'] = np.zeros(output size)
  def loss(self, X, y=None, reg=0.0):
   Compute the loss and gradients for a two layer fully connected neural
   network.
   Inputs:
   - X: Input data of shape (N, D). Each X[i] is a training sample.
   - y: Vector of training labels. y[i] is the label for X[i], and each y[i] is
     an integer in the range 0 \le y[i] \le C. This parameter is optional; if it
     is not passed then we only return scores, and if it is passed then we
     instead return the loss and gradients.
   - reg: Regularization strength.
   Returns:
   If y is None, return a matrix scores of shape (N, C) where scores[i, c] is
   the score for class c on input X[i].
   If y is not None, instead return a tuple of:
   - loss: Loss (data loss and regularization loss) for this batch of training
     samples.
    - grads: Dictionary mapping parameter names to gradients of those parameters
     with respect to the loss function; has the same keys as self.params.
    # Unpack variables from the params dictionary
   W1, b1 = self.params['W1'], self.params['b1']
```

```
W2, b2 = self.params['W2'], self.params['b2']
N, D = X.shape
# Compute the forward pass
scores = None
h1 = np.dot(X, W1.T) + b1
h1[h1 <= 0] = 0
h2 = np.dot(h1, W2.T) +b2
# YOUR CODE HERE:
  Calculate the output scores of the neural network. The result
 should be (N, C). As stated in the description for this class,
 there should not be a ReLU layer after the second FC layer.
 The output of the second FC layer is the output scores. Do not
  use a for loop in your implementation.
# ------ #
real scores = h2
scores = h2 - np.max(h2, axis=1, keepdims=True)
exp scores = np.exp(scores)
probs = exp scores / np.sum(exp scores, axis=1, keepdims=True)
# ------ #
# END YOUR CODE HERE
 ______ #
# If the targets are not given then jump out, we're done
if y is None:
 return real scores
# Compute the loss
loss = None
# ----- #
# YOUR CODE HERE:
 Calculate the loss of the neural network. This includes the
 softmax loss and the L2 regularization for W1 and W2. Store the
 total loss in teh variable loss. Multiply the regularization
  loss by 0.5 (in addition to the factor reg).
# ----- #
# scores is num examples by num classes
num examples = X.shape[0]
correct logprobs = -np.log(probs[range(num examples), y])
data loss = np.sum(correct logprobs) / num examples
reg_loss = 0.5*reg*(np.sum(W1 * W1) + np.sum(W2 * W2))
loss = data_loss + reg_loss
# ----- #
# END YOUR CODE HERE
# ----- #
qrads = \{\}
# ----- #
# YOUR CODE HERE:
  Implement the backward pass. Compute the derivatives of the
 weights and the biases. Store the results in the grads
# dictionary. e.g., grads['W1'] should store the gradient for
 W1, and be of the same size as W1.
# ----- #
dscores = probs
dscores[range(N), y] = 1
dscores /= N
grads['W2'] = np.dot(dscores.T, h1) + reg * W2
grads['b2'] = np.sum(dscores, axis=0)
```

```
dh1 = np.dot(dscores, W2)
 dh1[h1 <= 0] = 0
 grads['W1'] = np.dot(dh1.T, X) + reg * W1
 grads['b1'] = np.sum(dh1, axis=0)
 # ============= #
 # END YOUR CODE HERE
 return loss, grads
def train(self, X, y, X_val, y_val,
        learning rate=1e-3, learning rate decay=0.95,
        reg=1e-5, num iters=100,
       batch size=200, verbose=False):
 Train this neural network using stochastic gradient descent.
 Inputs:
 - X: A numpy array of shape (N, D) giving training data.
 - y: A numpy array f shape (N,) giving training labels; y[i] = c means that
  X[i] has label c, where 0 <= c < C.
 - X_val: A numpy array of shape (N_val, D) giving validation data.
 - y val: A numpy array of shape (N val,) giving validation labels.
 - learning rate: Scalar giving learning rate for optimization.
 - learning rate decay: Scalar giving factor used to decay the learning rate
   after each epoch.
 - reg: Scalar giving regularization strength.
 - num iters: Number of steps to take when optimizing.
 - batch size: Number of training examples to use per step.
 - verbose: boolean; if true print progress during optimization.
 num train = X.shape[0]
 iterations per epoch = max(num train / batch size, 1)
 # Use SGD to optimize the parameters in self.model
 loss history = []
 train acc history = []
 val acc history = []
 for it in np.arange(num iters):
   X batch = None
   y_batch = None
   # ------ #
   # YOUR CODE HERE:
    Create a minibatch by sampling batch size samples randomly.
   indexes = np.random.choice(num_train,batch_size)
   X \text{ batch} = X[\text{indexes}]
   y_batch = y[indexes]
   # ----- #
   # END YOUR CODE HERE
   # Compute loss and gradients using the current minibatch
   loss, grads = self.loss(X batch, y=y_batch, reg=reg)
   loss history.append(loss)
   # ----- #
   # YOUR CODE HERE:
     Perform a gradient descent step using the minibatch to update
     all parameters (i.e., W1, W2, b1, and b2).
   self.params['W1'] -= learning rate*grads['W1']
```

```
self.params['W2'] -= learning_rate*grads['W2']
    self.params['b1'] -= learning_rate*grads['b1']
    self.params['b2'] -= learning rate*grads['b2']
    # ----- #
    # END YOUR CODE HERE
    if verbose and it % 100 == 0:
      print('iteration {} / {}: loss {}'.format(it, num_iters, loss))
    # Every epoch, check train and val accuracy and decay learning rate.
    if it % iterations per epoch == 0:
      # Check accuracy
      train acc = (self.predict(X batch) == y batch).mean()
      val acc = (self.predict(X val) == y val).mean()
      train acc history.append(train acc)
      val _acc_history.append(val_acc)
      # Decay learning rate
      learning rate *= learning rate decay
   return {
    'loss history': loss history,
    'train acc history': train acc history,
     'val acc history': val acc history,
   }
 def predict(self, X):
   Use the trained weights of this two-layer network to predict labels for
   data points. For each data point we predict scores for each of the C
   classes, and assign each data point to the class with the highest score.
   Inputs:
   - X: A numpy array of shape (N, D) giving N D-dimensional data points to
    classify.
   Returns:
   - y pred: A numpy array of shape (N,) giving predicted labels for each of
    the elements of X. For all i, y pred[i] = c means that X[i] is predicted
    to have class c, where 0 \le c < C.
   y pred = None
   # YOUR CODE HERE:
     Predict the class given the input data.
   something = np.dot(np.maximum(0, np.dot(X, self.params['W1'].T) + self.params['b1']),
self.params['W2'].T) + self.params['b2']
   y pred = np.argmax(something, axis=1)
   # ----- #
   # END YOUR CODE HERE
   # ----- #
   return y_pred
```