

Roll No. \_\_\_\_\_

21/1085

**B.C.A. Examination, 2021****(First Semester)****Fifth Paper****Mathematics - I**

Time : 1½ Hours / Maximum Marks : 75

**Note :** Answer any **five** questions. **All** questions carry equal marks.

1. Find the inverse of the matrix 15

$$A = \begin{bmatrix} 0 & 1 & 2 \\ 1 & 2 & 3 \\ 3 & 1 & 1 \end{bmatrix}$$

2. For the two matrices A and B where 15

$$A = \begin{bmatrix} 2 & 3 & 4 \\ 1 & 2 & 3 \\ -1 & 1 & 2 \end{bmatrix}, B = \begin{bmatrix} 1 & 3 & 0 \\ -1 & 2 & 1 \\ 0 & 0 & 2 \end{bmatrix}$$

**P.T.O.****21/1085**Compute AB and BA and show that  $AB \neq BA$ 

3. Evaluate 15

$$\lim_{x \rightarrow 0} \frac{(1+x)^n - 1}{x}$$

4. A function
- $f(x)$
- is defined as follows: 15

$$f(x) = \begin{cases} (x^2/a) - a, & \text{when } x < a \\ 0, & \text{when } x = a \\ a - (a^2/x), & \text{when } x > a \end{cases}$$

Prove that the function  $f(x)$  is continuous at  $x=a$ .

5. If
- $x\sqrt{1-y^2} + y\sqrt{1-x^2} = a$
- 15

$$\text{Show that } \frac{d^2y}{dx^2} = -\frac{a}{(1-x^2)^{3/2}}$$

6. Find the maximum value of
- $(x-1)(x-2)(x-3)$
- 15

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✓ 7. Evaluate :  $\int \frac{x^2 + x + 2}{(x-2)(x-1)} dx$  15

8. Evaluate :  $\int \frac{x}{(x-3)\sqrt{x+1}} dx$  15