

# Normalp

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```
library('normalp')

#Let's compute the density for a x value with mu=0, sigmap=2 and p=2
dnormp(2, p=2)

## [1] 0.05399097

#Let's compute the distribution for a q value with mu=1, sigmap=2 and p=2
pnormp(0.7, mu=1, sigmap=2, p=2)

## [1] 0.4403823

#Let's compute the quantile for a probability value pr=0.4 with mu=3, sigmap=2 and
p=2
qnormp(0.4, mu=3, sigmap=2, p=1.5)

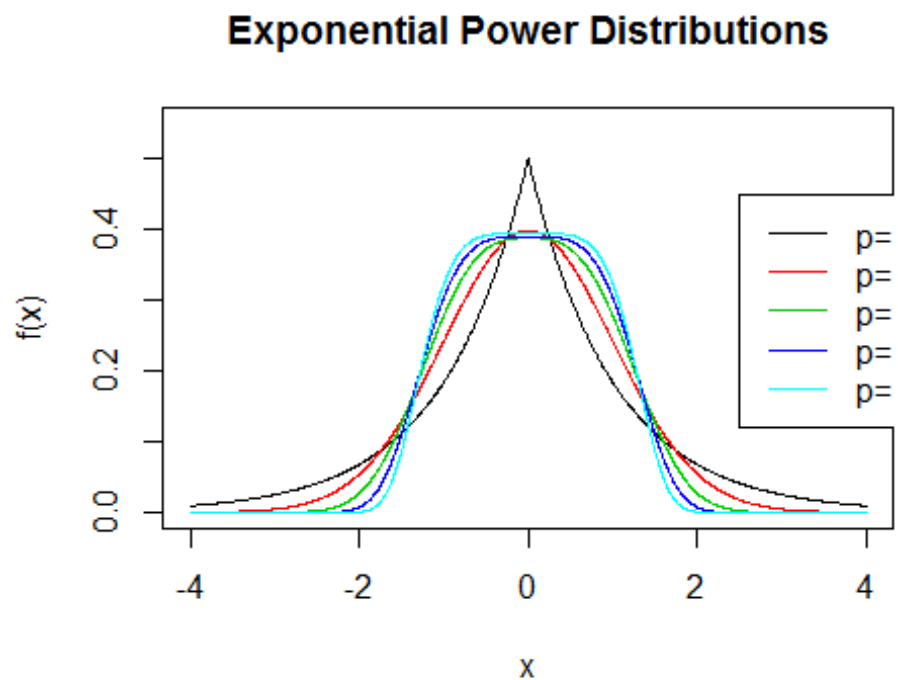
## [1] 2.51149

#In the following example, we generate a random sample of size n=30 from an
exponential power distribution
#with mu=2, sigmap=3 and p=1.5
rnormp(30,2,3,1.5)

## [1] 8.0053821 8.1042743 -2.3606352 5.2568087 1.9550047 2.8596691
## [7] 1.7795360 3.6183377 1.1902721 6.9011483 4.8606972 3.5129063
## [13] 3.3935536 1.4716770 6.4289855 1.1359680 -4.6231760 2.3544251
## [19] -2.8170461 3.9082953 3.3320523 -1.3695038 -2.3745950 8.2578143
## [25] 6.7712646 2.6541339 -0.3799379 -1.1570932 -2.2119725 -2.2464491

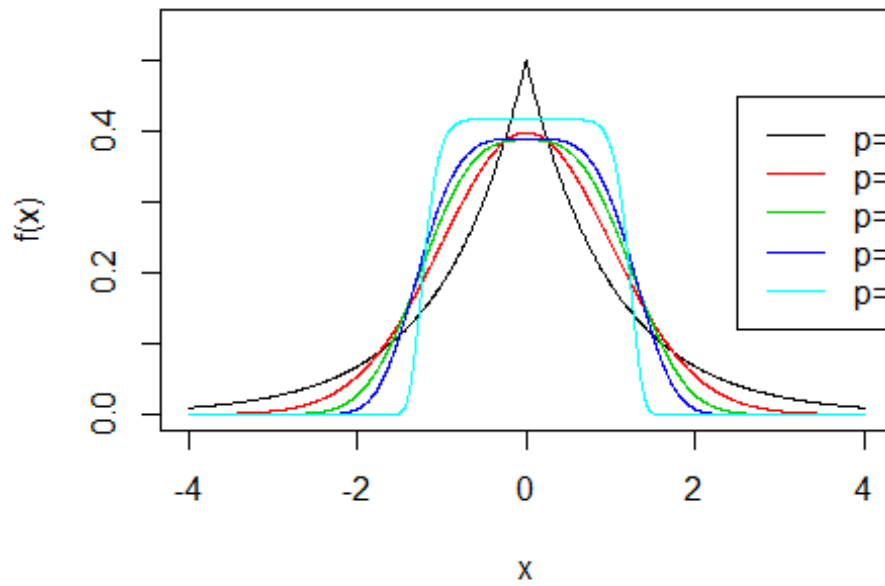
#With the following command, we plot 5 different distributions with p=1, 2, 3, 4,
5, 10, 20, 30, 50 (the last one will be the
```

```
#uniform distribution)  
graphnp(c(1:4,5))
```



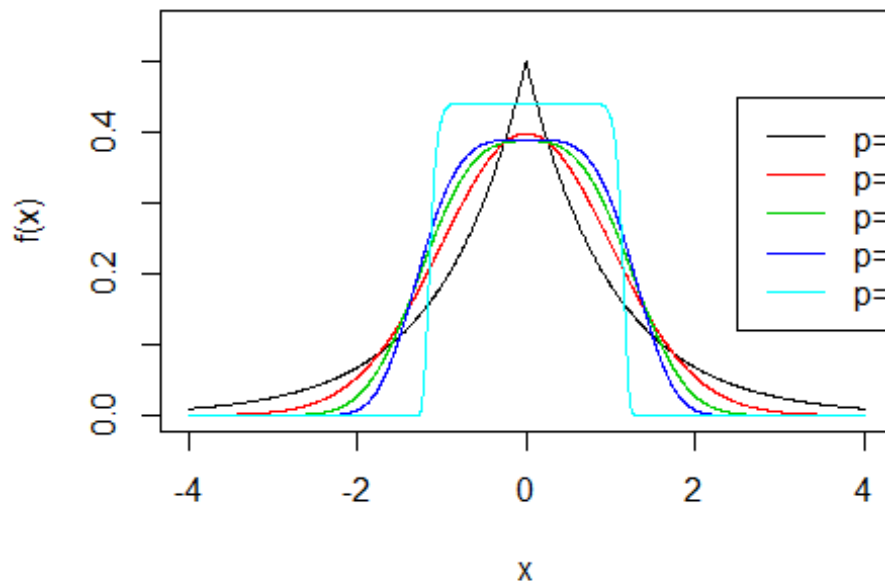
```
graphnp(c(1:4,10))
```

### Exponential Power Distributions



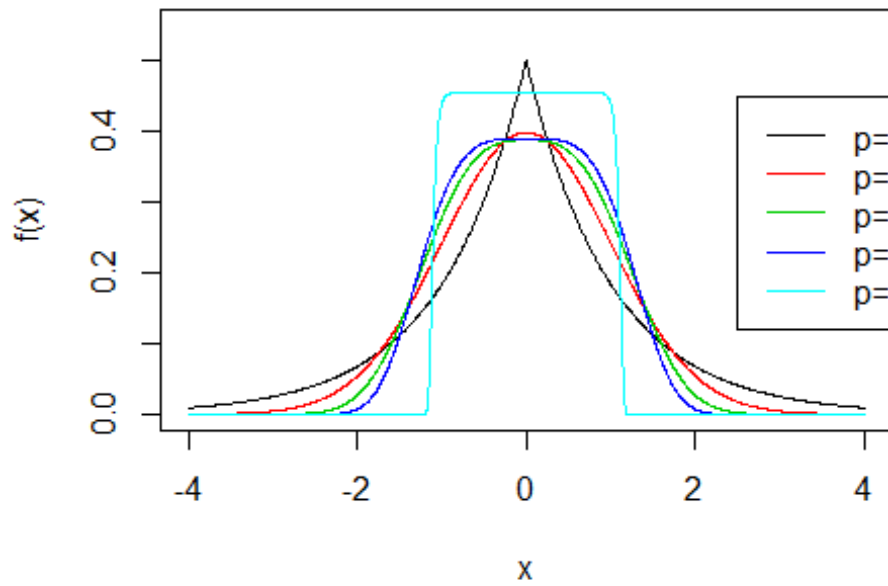
```
graphnp(c(1:4,20))
```

### Exponential Power Distributions



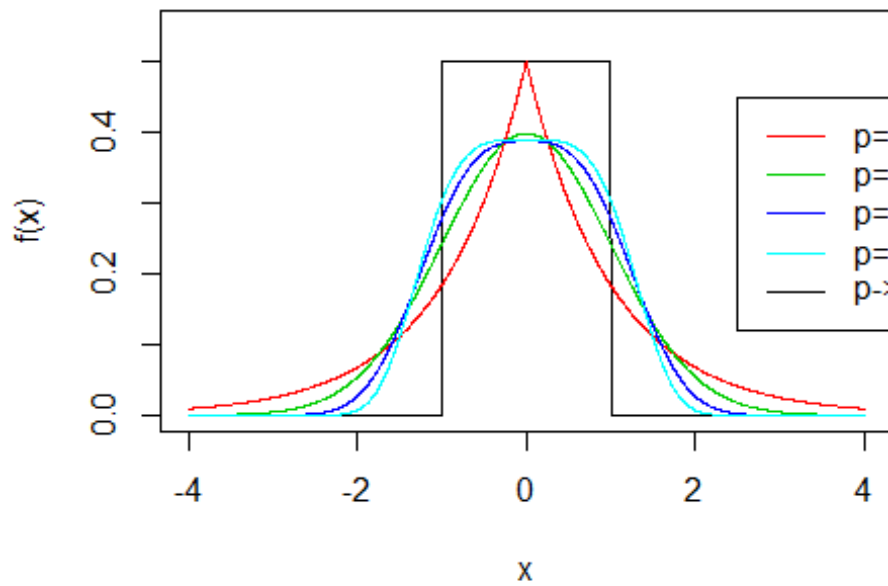
```
graphnp(c(1:4,30))
```

## Exponential Power Distributions



```
graphnp(c(1:4,50))
```

## Exponential Power Distributions

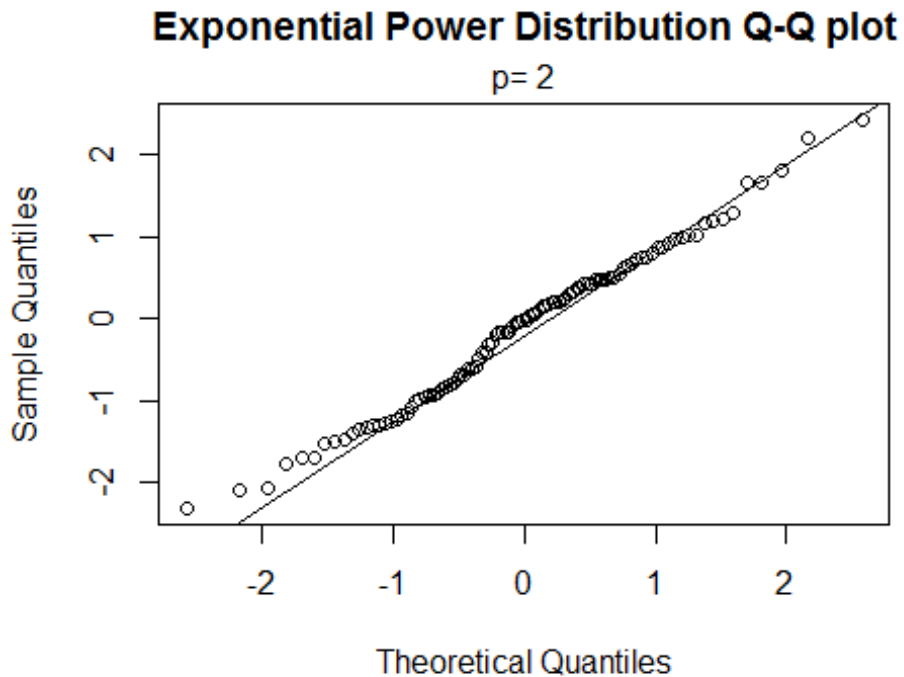


*#and an exponential power distribution Q-Q plot for a sample of size n=100:*

```
x=rnormp(100, p=2)
```

```
qqnormp(x, p=2)
```

```
qqlinep(x, p=2)
```



###Estimating the exponential power distribution parameters###

*#Let's estimate the shape parameter p from a vector of observations:*

```
x=rnormp(200,1,2,4)
```

```
p=estimatep(x, 1, 2)
```

```
p
```

```
## [1] 3.127864
```

*#Let's estimate {inserir mu, sigmap } and p from a vector of observations:*

```
x=rnormp(200,1,2,3)
```

```
parameters=paramp(x)
```

```
parameters
```

```

##      Mean      Mp      Sd      Sp      p
## 1.004110 1.030457 1.794412 2.004770 2.855000
##
## no.conv = FALSE

#Let's compute the values of theoretical and empirical indices of kurtosis, with p known or estimated
kurtosis(p=1.5)

##      VI      B2      Bp
## 1.303127 3.761954 2.500000

kurtosis(x, p=1.5, value='parameter')

##      VI      B2      Bp
## 1.208993 2.355632 1.852478

kurtosis(x)

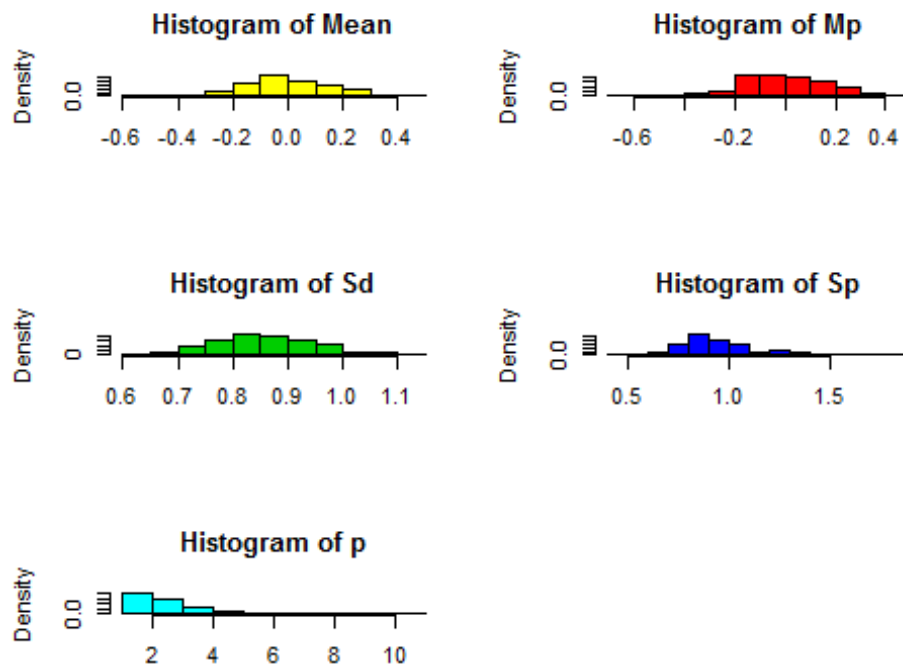
##      VI      B2      Bp
## 1.207764 2.345899 3.503474

#Let's perform a simulation plan for m=200 samples of size n=30, with mu=0, sigmap=1, p=3, by showing the histogram for each set of estimates
sim=simul.mp(30, 200, p=3)
sim

##      Mean      Mp      Sd      Sp      p
## Mean      0.001880339 -0.007492459 0.85687655 0.95915706 3.374070
## Variance 0.024985574 0.027781130 0.00868146 0.04562682 7.531195
##
## Number of samples with a difficult convergence: 10

par(mfrow=c(3,2))
plot(sim)
par(mfrow=c(1,1))

```



```
###Fitting a linear regression model with random errors distributed according to
an exponential power distribution###
```

```
#We consider an example that has the only purpose to show the use of the
implemented functions to fit a
#linear regression model when we have to assume that the random errors are
distributed according to an exponential
#power distribution
```

```
dataset
```

```
##      Gross Videos
## 1    1.10  57.18
## 2    1.13  26.17
## 3    1.18  92.79
## 4    1.25  61.60
## 5    1.44  46.50
## 6    1.53  85.06
## 7    1.53 103.52
```

```
## 8    1.69  30.88
## 9    1.74  49.29
## 10   1.77  24.14
## 11   2.42 115.31
## 12   5.34  87.04
## 13   5.70 128.45
## 14   6.43 126.64
## 15   8.59 107.28
## 16   9.36 190.80
## 17   9.89 121.57
## 18  12.66 183.30
## 19  15.35 204.72
## 20  17.55 112.47
## 21  17.91 162.95
## 22  18.25 109.20
## 23  23.13 280.79
## 24  27.62 229.51
## 25  37.09 277.68
## 26  40.73 226.73
## 27  45.55 365.14
## 28  46.62 218.64
## 29  57.70 286.31
## 30  58.51 254.58
```

```
attach(dataset)
```

```
res.lmp=lmp(Videos~Gross)
```

```
res.lmp
```

```
##
```

```
## Call:
```

```
## lmp(formula = Videos ~ Gross)
```

```
##
```

```
## Coefficients:
```

```
## (Intercept)      Gross
```

```
##      78.235      4.317
```



*#Let's report a summary of the mian results with a plot showing the 2 straight lines derived by using the  
#OLS methods and the Lmp() method:*

```
summary(res.lmp)
```

```
##
```

```
## Call:
```

```
## lmp(formula = Videos ~ Gross)
```

```
##
```

```
## Residuals:
```

```
##      Min       1Q   Median       3Q      Max  
## -76.224 -40.236  -3.907   26.374 102.710
```

```
##
```

```
## Coefficients:
```

```
## (Intercept)      Gross  
##      78.235       4.317
```

```
##
```

```
## Estimate of p
```

```
## `2.471869`
```

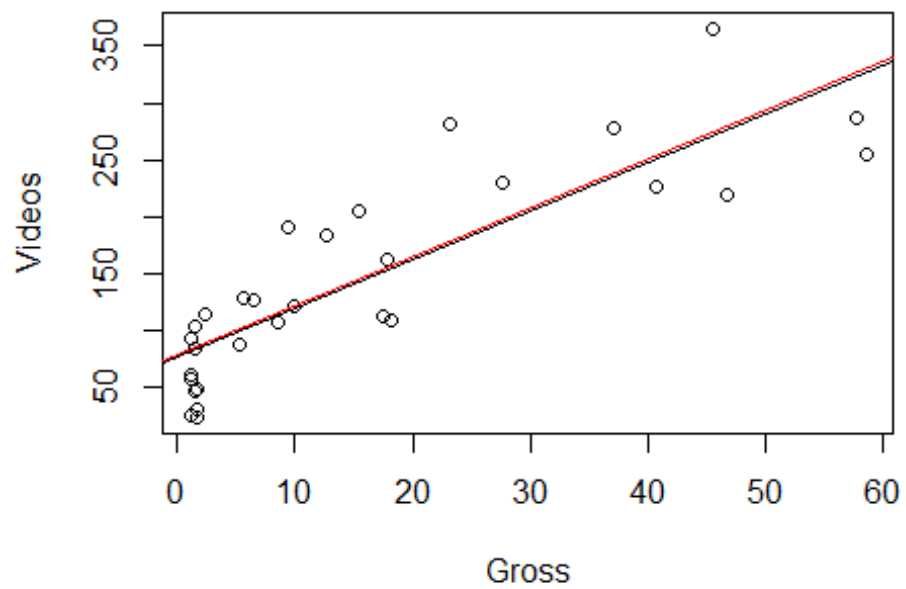
```
##
```

```
## Power deviation of order p: 51.69
```

```
plot(Videos~Gross)
```

```
abline(lm(Videos~Gross))
```

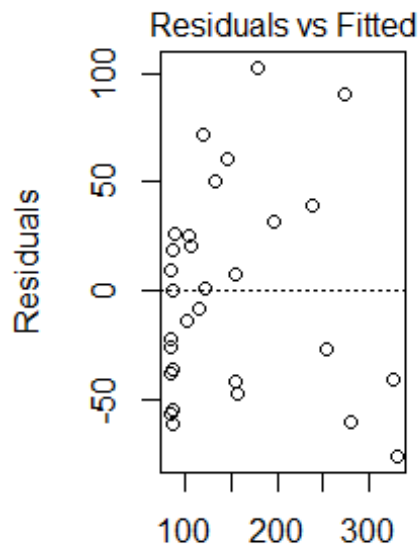
```
abline(res.lmp, col='red')
```



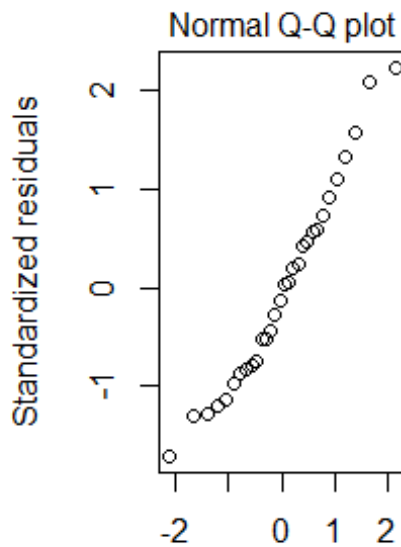
*#Let's perform an analysis of residuals:*

```
par(mfrow=c(1.5,2))
```

```
plot(res.lmp)
```



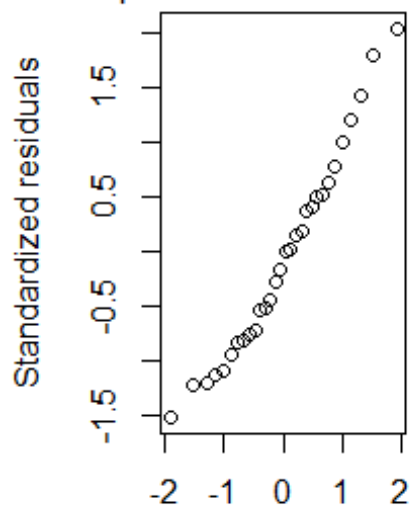
Fitted values  
Imp(formula = Videos ~ Gross



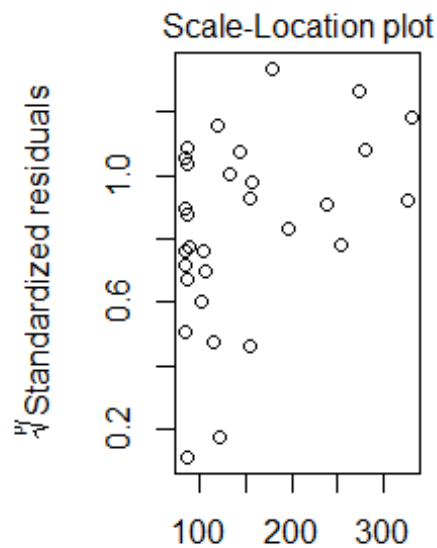
Theoretical Quantiles  
Imp(formula = Videos ~ Gross

## ponential Power Distribution

p= 2.47186949233502



Theoretical Quantiles  
Imp(formula = Videos ~ Gross



Fitted values  
Imp(formula = Videos ~ Gross

#Let's perform a simulation plan for  $m=200$  samples of size  $n=30$  for a linear regression model with only one regressor, by showing the histogram for each set of estimates

```

sim=simul.lmp(30,200,1,2,1,1,3)
sim

##           (intercept)          x1          Sp          p
## Mean          1.0264802  1.9712919  0.91180743  3.012432
## Variance      0.1151872  0.3411297  0.03726107  6.326452
##
## Number of samples with a difficult convergence: 1

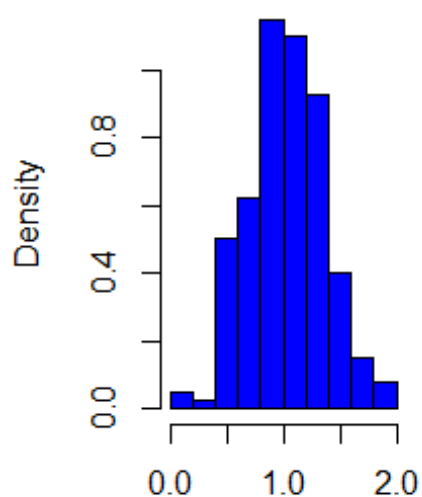
summary(sim)

## Results:
##           (intercept)          x1          Sp          p
## Mean          1.0264802  1.9712919  0.91180743  3.012432
## Variance      0.1151872  0.3411297  0.03726107  6.326452
##
## Coefficients:
## (intercept)          x1
##           1          2
##
## Formula:
## y ~ +x1
## <environment: 0x0000000073de4b0>
##
## Number of samples:
## `200`
##
## Value of p:
## `3`
##
## Number of samples with problems on convergence
## `1`

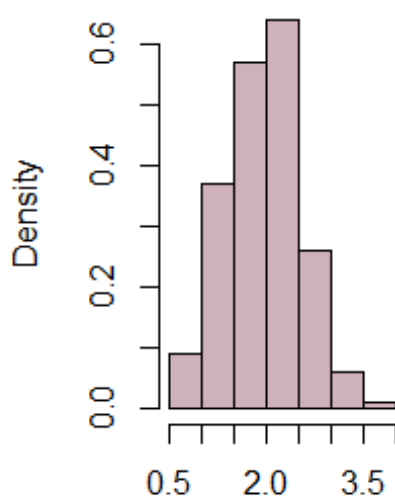
par(mfrow=c(1.5,2))
plot(sim)

```

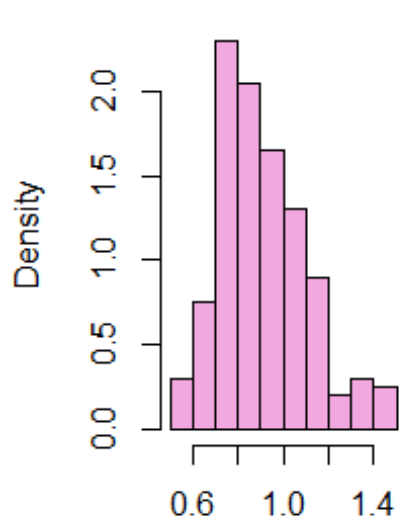
**Histogram of intercept**



**Histogram of x1**



**Histogram of Sp**



**Histogram of p**

