

$f: A \rightarrow B$

$A \leftarrow B : g$

$f \circ g = g \circ f = i_{\text{dom } f}$

$\cancel{g = f^{-1}}$

$f: Z \rightarrow Z$

$f(x) = 2x + 1$

$y = 2x + 1$

$f^{-1}(x) = \frac{x-1}{2}$

$\frac{y-1}{2} = x$

## Computer Representations of Sets

$\{1, 2, 3\}$

$\downarrow$   
 $\{1, 3, 2\}$

Set  
unordered

Union  
Intersection  
subset

*in Comp  
order*

Let  $a_1, a_2, \dots, a_n$  be the arbitrary ordering of the elements of  $U$ .

$$f: N \rightarrow U \quad \text{where } N = \{1, \dots, n\}$$

$$f(i) = a_i$$

Now, to represent a subset  $A$  of  $U$  with the bit string of length  $n$ , we follow:

→  $i^{\text{th}}$  bit in this string is 1,  
if  $a_i \in A$  and  
0 if  $a_i \notin A$ .

example

$$U = \{1, 2, 3, 4, \dots, 10\}$$

and give arbitrary ordering in increasing order.

$$f(i) = a_i = i \quad : \quad f(1) = 1$$

$$f(2) = 2$$

$$f(3) = 3$$

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etc

$$f(10) = 10$$

$$\begin{aligned} U &= \{1, 2, \dots, 10\} \\ A &= \{1, 3, 5, 7, 9\} \\ B &= \{2, 4, 6, 8, 10\} \\ C &= \{1, 2, 3, 4, 5\} \end{aligned}$$

Q: What bit string represents the subset of all odd integers in  $U$ , the subset of all even integers in  $U$ , and the subset of integers not exceeding 5 in  $U$ .

A: The bit string that represents the set of odd integers in  $U(\{1, 3, 5, 7, 9\})$ , has a one bit in first, 3<sup>rd</sup>, 5<sup>th</sup>, 7<sup>th</sup>, 9<sup>th</sup> positions and zero elsewhere.

It is: 1 0 1 0 1 0 1 0

== = - - - -

Similar: the bit string represent representation of set of even integers in  $\mathbb{N}$ .  
↳ :

0101010101 ✓  $\rightarrow \{2, 4, 6, 8, 10\}$

And  
== 1111000000 ↲  $\{1, 2, 3, 4, 5\}$

#  $\mathcal{N} = \{1, 2, \dots, 10\} \leftrightarrow 111111111_2$

$\neg A = \{1, 3, 5, 7, 9\} \leftrightarrow \underline{1010101010}$

$\neg B = \{2, 4, 6, 8, 10\} \leftrightarrow 0101010101$

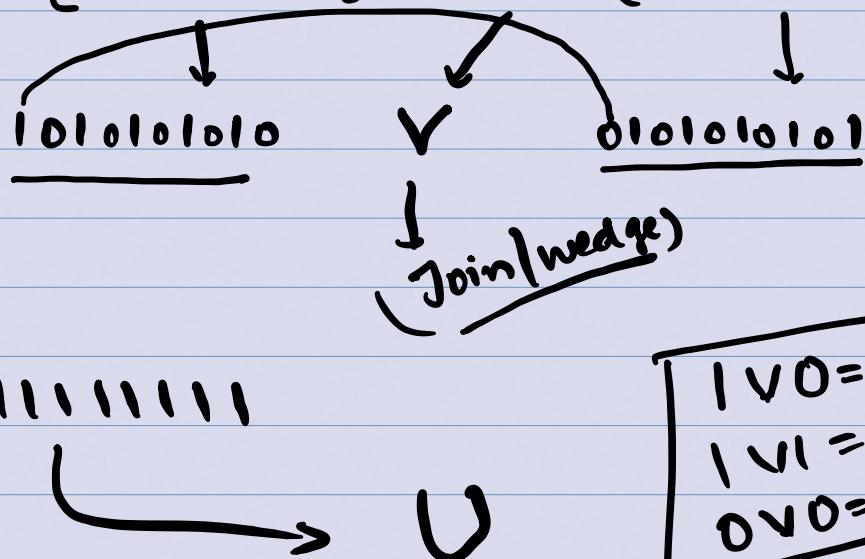
$\neg C = \{1, 2, 3, 4, 5\} \leftrightarrow 1111100000$

$A^C = \underline{0101010101} = B$


 Simply  
 replacing  $1 \leftrightarrow 0$   
 $0 \leftrightarrow 1$

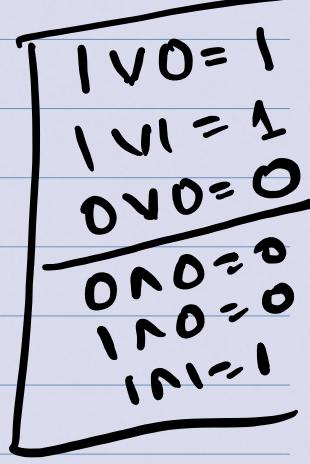
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A ∪ B :  $\{1, 3, 5, 7, 9\}$   $\cup$   $\{2, 4, 6, 8, 10\}$

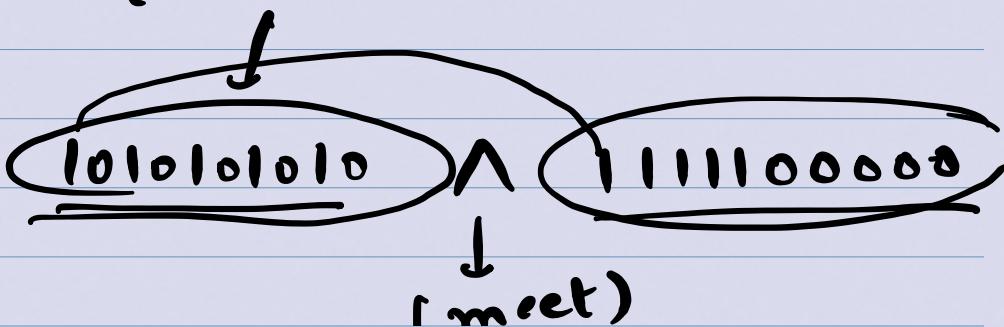


$= 1111111111$





A ∩ C :  $A \cap \{1, 3, 5, 7, 9\} \cap \{1, 2, 3, 4, 5\}$



1010100000

{1, 3, 5}

Graphs of function

#

Cryptograph

Error Correction

3000

CD

1960

(A), f.

(f: A → B)

A function  $f$  from  $A$  to  $B$  can be represented as a subset of  $A \times B$ .

if  $f: A \rightarrow B$ , then

$$f = \{(a, b) : a \in A \text{ and } b = f(a)\}$$

$$\{(a, b) : a \in A \text{ and } b \in B\}$$

Ex:

$$A = \{1, 2, 3, 4\}$$

$$B = \{1, 2, -1, 0, 3\}$$

$$f: A \rightarrow B$$

$$\begin{aligned} f(1) &= 1 \\ f(2) &= 4 \\ f(3) &= 9 \\ f(4) &= 16 \end{aligned}$$

$$f = \{(1, 1), (2, 4), (3, 9), (4, 16)\}$$

$$f(x)$$

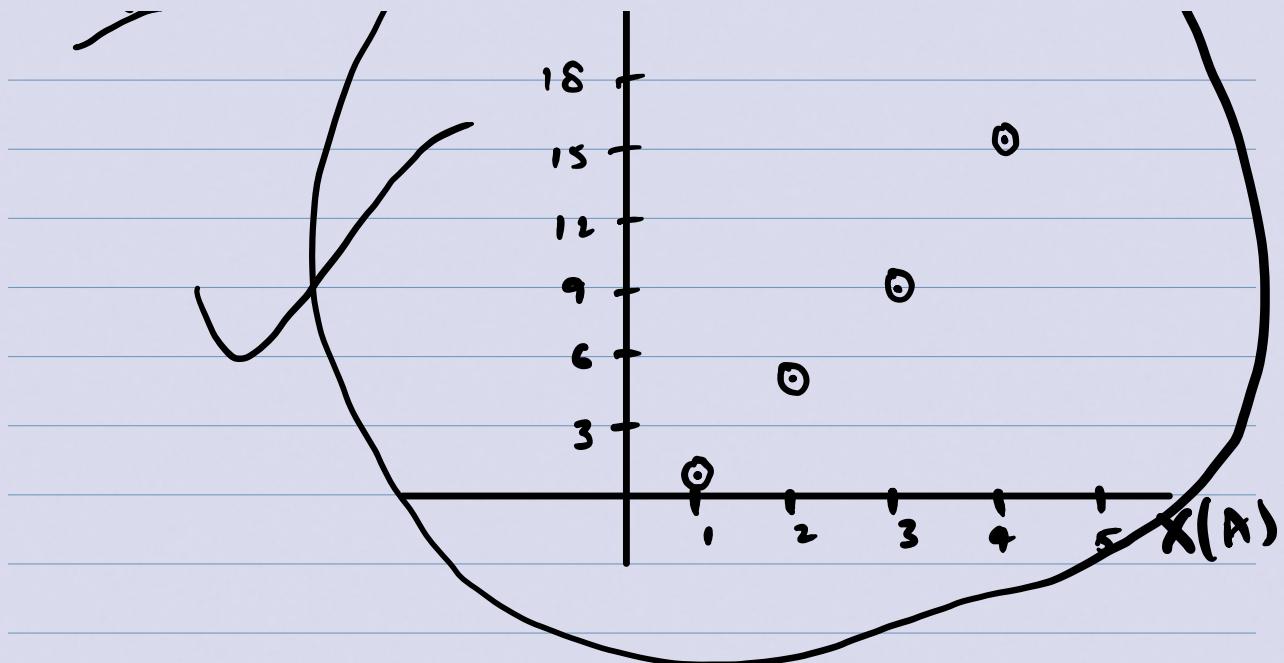
Graph

$$\{ \}$$

$$<$$

$$\{ \}$$

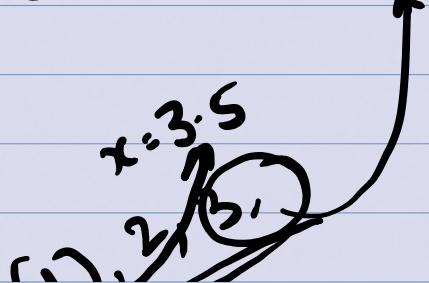
$$>$$



## Ceiling and Floor functions.

Floor function: assigns to the real no.  $x$ , the largest integer that is less than or equal to  $x$ . It is denoted by  $\lfloor x \rfloor$

$$\lfloor 3.5 \rfloor = 3$$



W//

Ceiling function - assigns \_\_\_\_\_

the smallest integer  
that is greater than  
or equal to  $x$

$\lceil x \rceil$

$$\lceil 3.5 \rceil = 4$$

$$\lceil 4 \rceil = 4$$

$$3.5 \leq \underline{4, 5, 6, 7}$$

W