

Experiment NO : 07

EFFECT OF AWGN OF AM AND FM

Objective: To study the transmission amplitude modulated (AM) and frequency modulated (FM) signal under the additive Gaussian noise signal using the Matlab/Simulink and draw the distorted waveforms for different signal to noise (SNR) values.

Software: Matlab/Simulink

Theory: AWGN is a basic noise model used to mimic the effect of many random process that occurs in nature.

Channel produces Additive white Gaussian Noise.

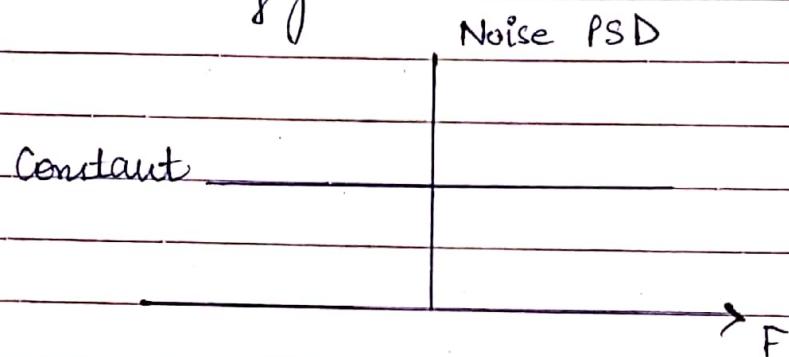
Additive - The received signal equals the transmit signal plus some noise, where the noise is statistically independent of the signal.

$$x(t) = s(t) + w(t)$$

↓ ↓
 message noise
 signal

White: It refers to the noise has some power distribution at every frequency or it has uniform power across the frequency band for the information system.

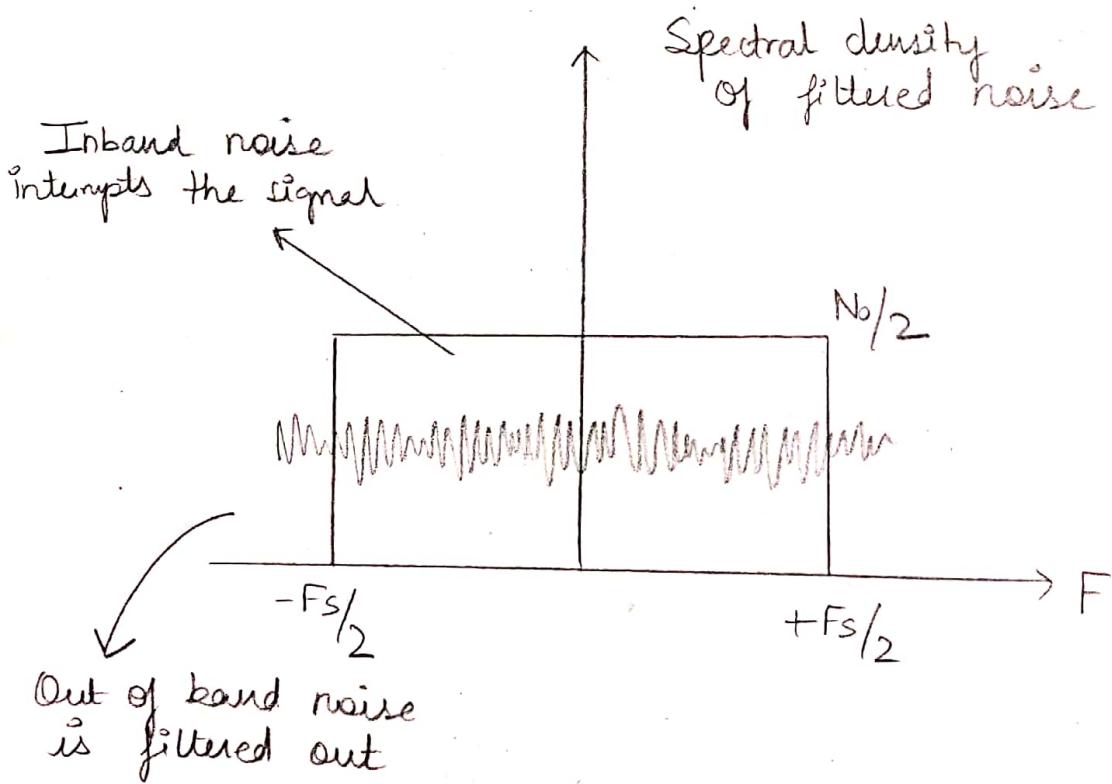
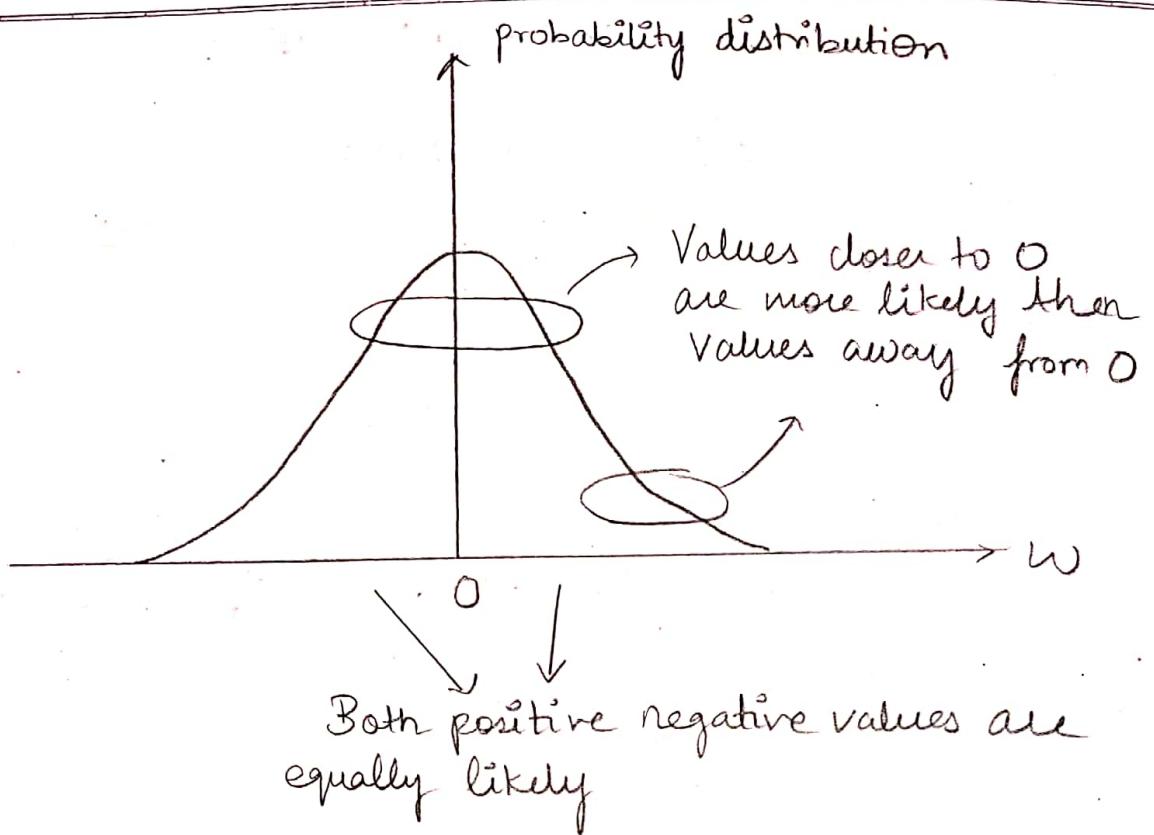
It is an analogy to the color white which has uniform emission at all frequency in the visible spectrum. If we focus a beam of light for each color on the visible spectrum onto a single spot whose combination would result in a beam of white light, as consequence, power spectral density (PSD) of white noise is constant for all frequency ranging from $-\infty$ to $+\infty$ as shown in figure.



Gaussian \rightarrow Gaussian distribution, or a normal distribution, has an average of zero in time domain, and is represented as a bell-shaped curve. The probability distribution of the noise sample is Gaussian with a zero mean.

The value close to zero has a higher chance of occurrence while the values far away from zero are less likely to appear.

In reality, the ideal flat spectrum from $-\infty$ to ∞ is true for frequency of interest in wireless communication (a few KHz to hundreds of GHz) but not for higher frequency.



Signal-to-Noise Ratio:

The SNR or S/N is a measure used in science and engineering that compare the level of a desired signal to the level of background noise. It is defined as the ratio of signal to power to noise power, often expressed in decibel (dB). A ratio higher than 1:1 (greater than 0 dB) indicate more signal than noise.

SNR, bandwidth, and channel capacity of communication channel are connected by Shannon-Hartley theorem.

$$\text{SNR}_{\text{dB}} = 10 \log_{10} \left(\frac{P_{\text{signal}}}{P_{\text{noise}}} \right)$$

Shannon - Hartley theorem: It indicates that channel capacity (bits per second) or information rate of data that can be communicated at low error rate using an average received signal power through communication channel subject to AWGN of power.

$$C = B \log_2 \left(1 + \frac{S}{N} \right)$$

where B is bandwidth of channel in Hertz.

We can see that it is related to SNR.

Different case for SNR values.

5 dB - 10 dB → is minimum level to establish a connection, due to noise level being nearly indistinguishable from desired signal

25 dB - 40 dB → is deemed to be good.

41dB or higher \rightarrow is considered to be excellent.

AWGN over AM (Amplitude Modulation)

Let $E_m(t) = E_m \sin(\omega_m t)$ be message signal

and $E_c(t) = E_c \sin(\omega_c t)$ be carrier signal

then we know that,

$$e_m(t) = (E_c + E_m \sin(\omega_m t)) \sin(\omega_c t)$$

$$e_{am}(t) = (E_c + E_m \sin(\omega_m t)) \sin(\omega_c t)$$

MATLAB code:

For performing AWGN effects over AM -

clc;

clear all;

$t = 0 : 0.001 : 1$

$V_m = 6$;

$V_c = 12$;

$f_m = 5$;

$f_c = 30$;

$m = V_m * \sin(2 * \pi * f_m * t)$;

$c = V_c * \sin(2 * \pi * f_c * t)$;

$amp = V_c + V_m * \sin(2 * \pi * f_m * t)$;

$am = amp * \sin(2 * \pi * f_c * t)$;

$y = awgn(am, 15; 'measured')$;

subplot (4, 1, 1);

plot (t, m);

xlabel ('time');

```

ylabel('amplitude');
title('Carrus Signal');
subplot(4, 1, 3);
plot(t, am);
xlabel('time');
ylabel('amplitude');
title('amplitude modulated signal');
subplot(4, 1, 4);
plot(t, y);
xlabel('time');
ylabel('amplitude');
title('amplitude modulated signal with AWGN');

```

Matlab Code for AWGN effect on different functions
(Sine, Cosine, Sawtooth)

```

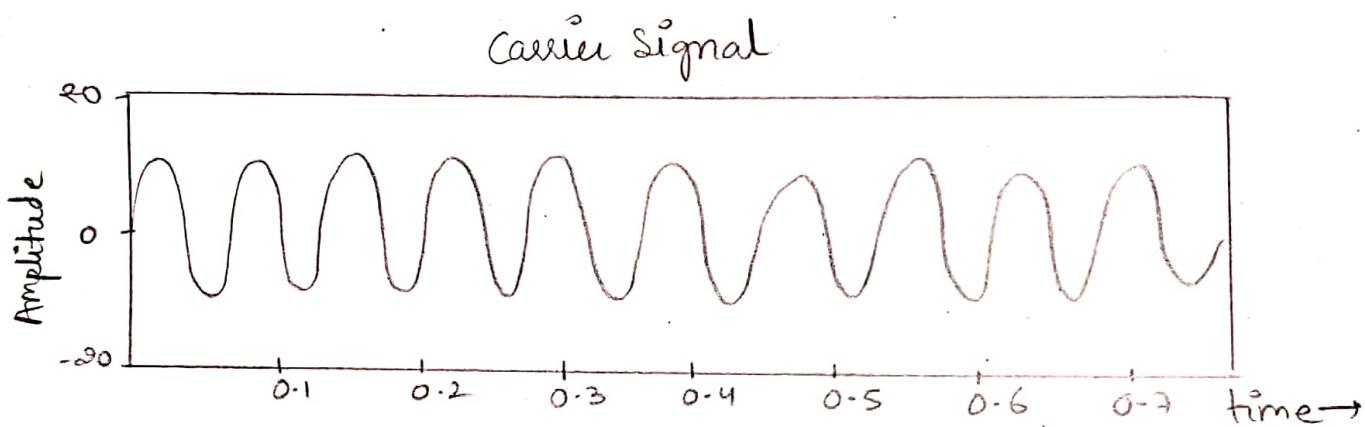
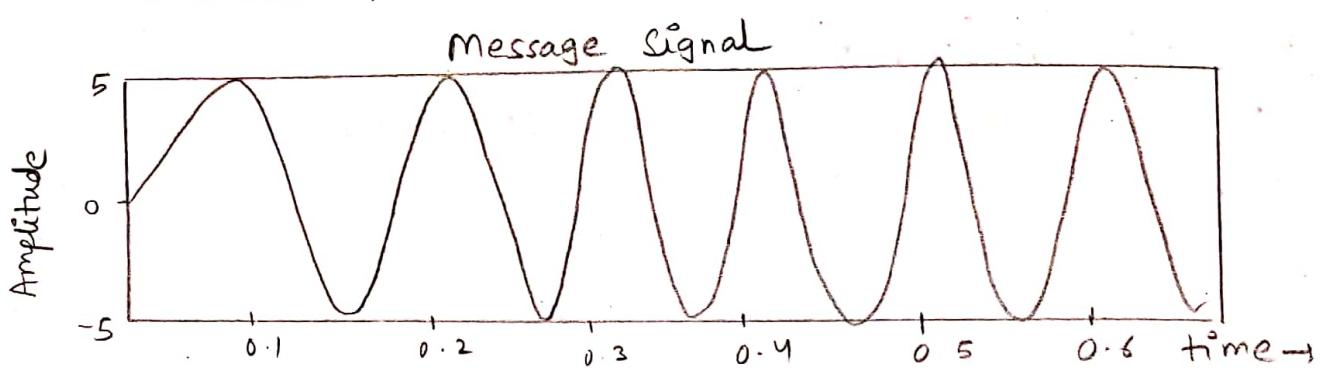
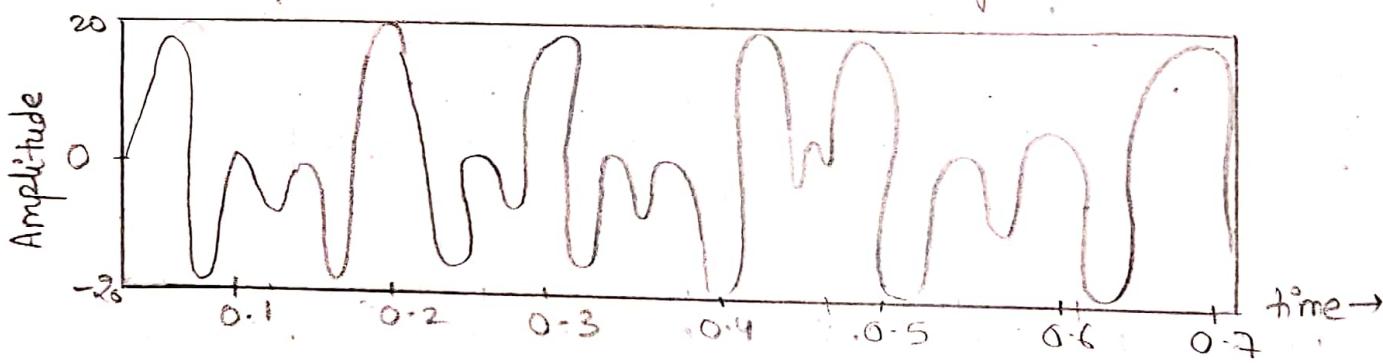
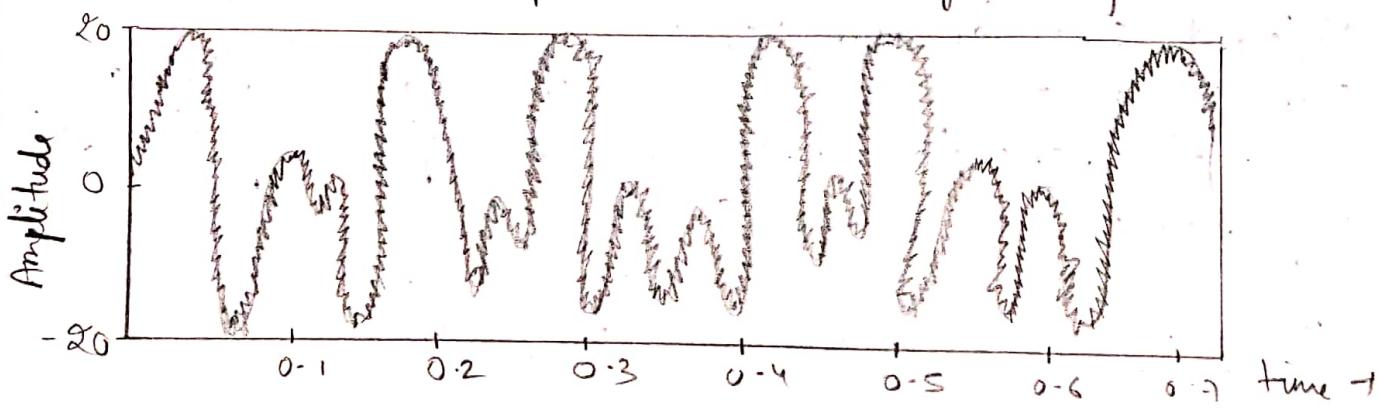
clc;
clear all;
t = (0:0.1:10);
x = sawtooth(t);
y = awgn(x, 10, 'measured');
plot(t, [x y]);
legend('Original Signal', 'Signal with AWGN')

```

```

clc;
clear all;
t = (0:0.1:10);
x = sin(t);

```

AWGN Effect over AM**Amplitude Modulated Signal****Amplitude Modulated Signal Using AWGN**

```
y = awgn(x, 10, 'measured');
plot(t, [x y])
legend('Original Signal', 'Signal with AWGN');
```

clc;

clear all;

t = (0:0.1:10);

x = cos(t);

```
y = awgn(x, 10, 'measured');
```

```
plot(t, [x y])
```

```
legend('Original Signal', 'Signal with AWGN')
```

MATLAB CODE FOR AM WITH DIFFERENT SNR VALUES

clc;

clear all;

t = 0:0.001:1;

Vm = 5;

Vc = 10

fm = 2;

fc = 25;

m = Vm * sin(2 * pi * fm * t);

c = Vc * sin(2 * pi * fc * t);

Amp = Vc + Vm * sin(2 * pi * fm * t);

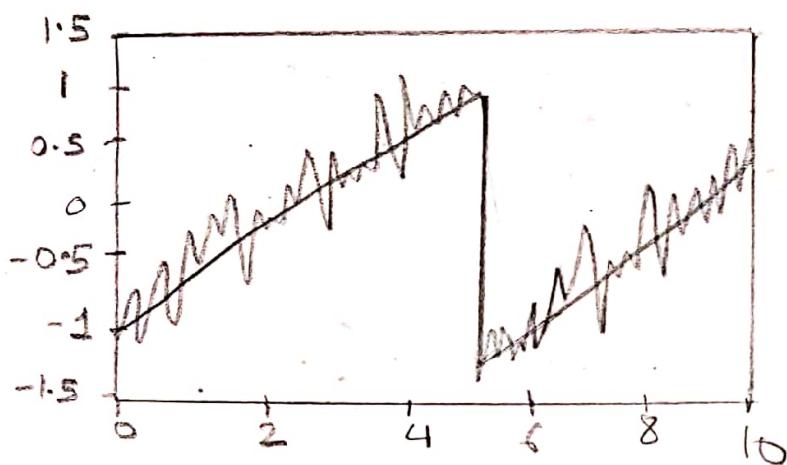
Am = Amp * sin(2 * pi * fc * t);

y1 = awgn(am, 10, 'measured');

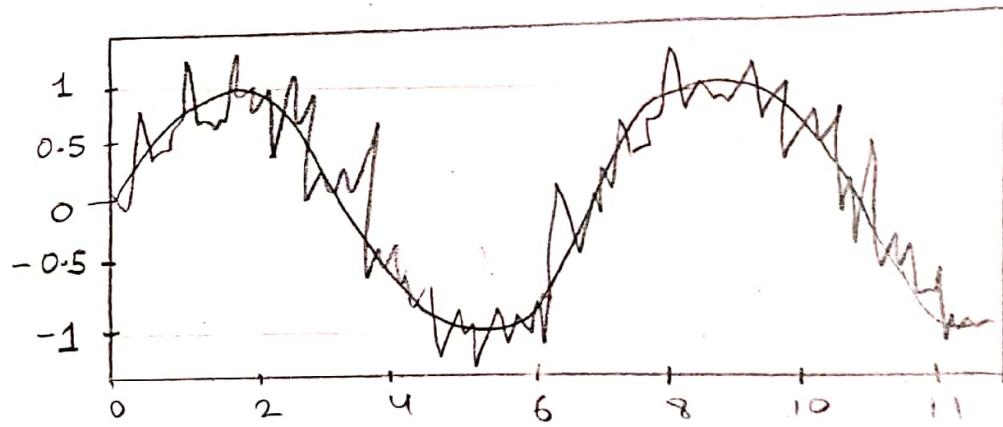
y2 = awgn(am, 100, 'measured');

AWGN effect on different functions

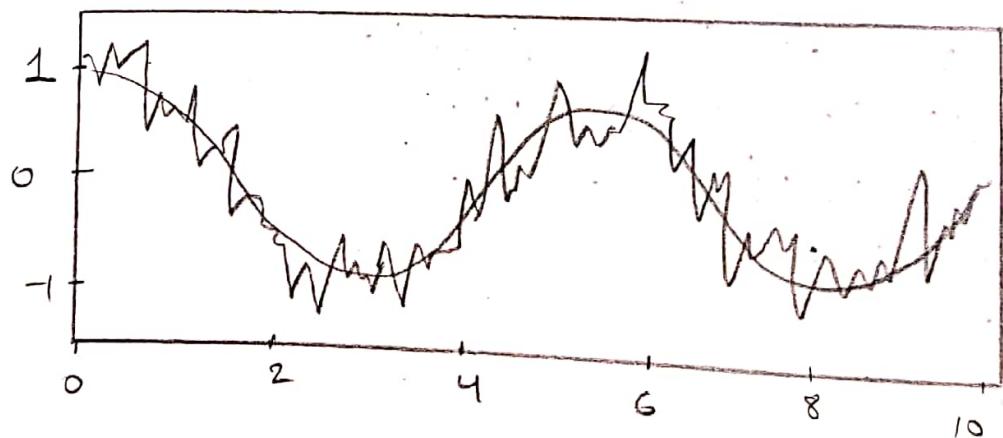
- Sawtooth:



- Sine:



- Cosine:



```

y3 = awgn ( am , 1000 , 'measured' );
Subplot ( 4 , 1 , 1 );
plot ( t , am );
xlabel ( 'time' );
ylabel ( 'amplitude' );
title ( 'amplitude modulated signal' );
Subplot ( 4 , 1 , 2 );
plot ( t , y1 );
xlabel ( 'time' );
ylabel ( 'amplitude' );
title ( 'Amplitude modulated signal with AWGN [snr 10]' );
Subplot ( 4 , 1 , 4 );
plot ( t , y3 );
xlabel ( 'time' );
ylabel ( 'amplitude' );
title ( 'amplitude modulated signal with AWGN [snr 1000]' );

```

MATLAB CODE FOR FM SIGNAL UNDER AWGN

```

clc;
clear all;

```

$t = 0 : 0.001 : 1;$

$$V_m = 5;$$

$$V_c = 5;$$

$$f_m = 2$$

$$f_c = 25$$

$$f_d = 5;$$

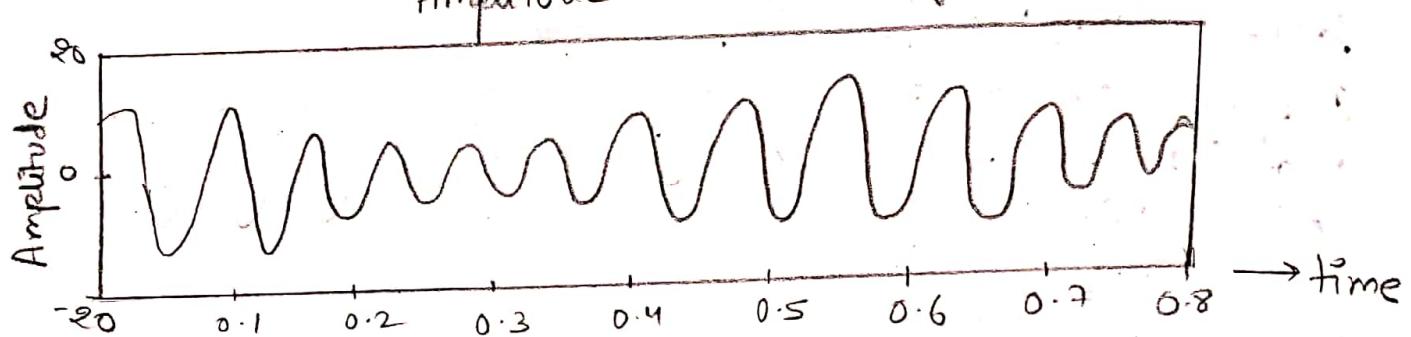
$$msg = V_m * \sin(2 * \pi * f_m * t);$$

$$C = V_c * \sin(2 * \pi * f_c * t);$$

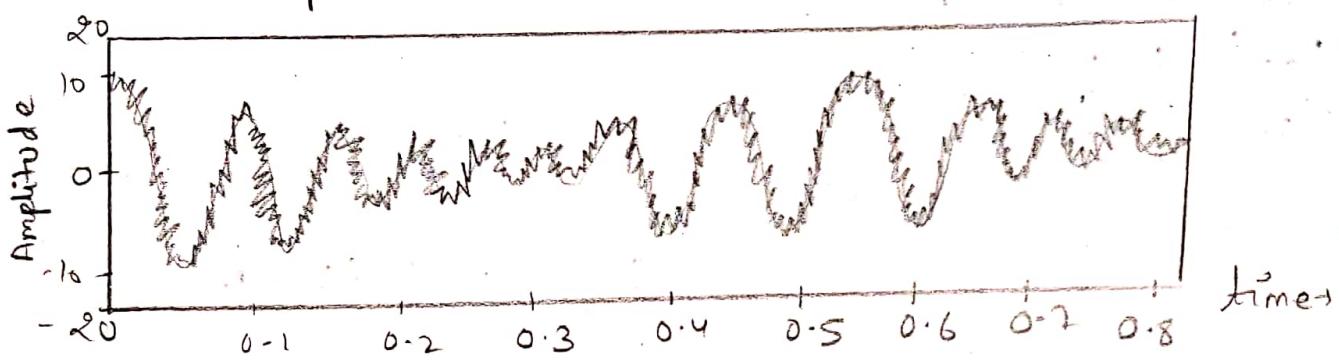
$$y = V_c * \sin(2 * \pi * f_c * t + f_d) * \cos(2 * \pi * f_m * t);$$

AM With Different SNR Values

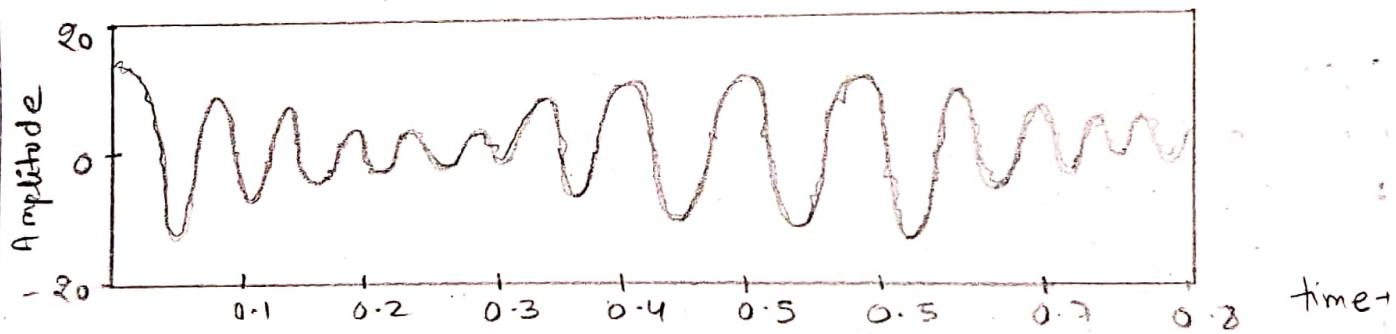
Amplitude Modulated Signal



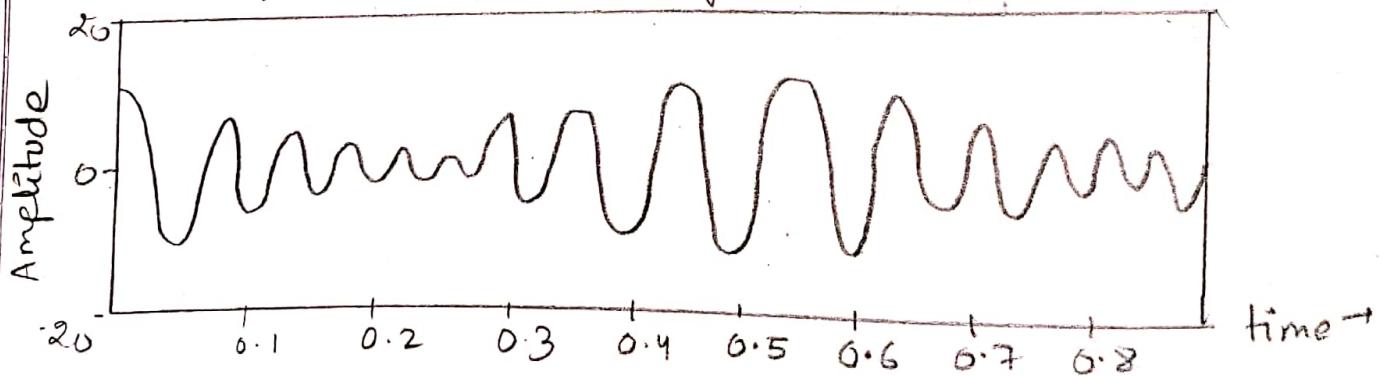
Amplitude Modulated Signal with AWGN [Snr 10]



Amplitude Modulated Signal with AWGN [Snr 100]



Amplitude Modulated Signal with AWGN [Snr 1000]



```

Z = awgn(y, 5, 'measured');
subplot(4, 1, 1);
plot(t, msg);
xlabel('time');
ylabel('amplitude');
title('message signal');
subplot(4, 1, 2);
plot(t, c);
xlabel('time');
ylabel('amplitude');
title('carrier signal');
subplot(4, 1, 3);
plot(t, y);
xlabel('time');
ylabel('amplitude');
title('frequency modulated signal');
subplot(4, 1, 4);
plot(t, z);
xlabel('time');
ylabel('amplitude');
title('Frequency modulated signal with AWGN');

```

Matlab Code for Different SNR in FM

```

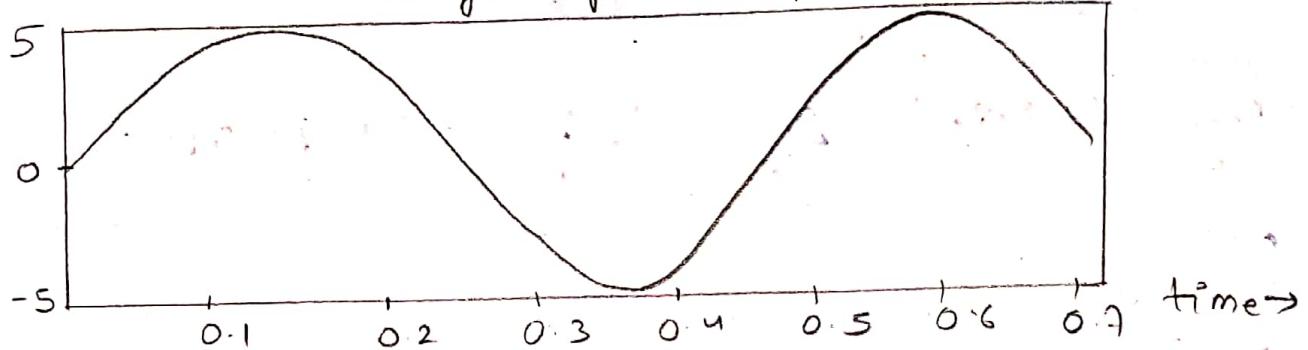
dc;
clear all;
t = 0:0.001:1;
Vm = 10
Vc = 5
fm = 2
fc = 25

```

FM Under AWGN

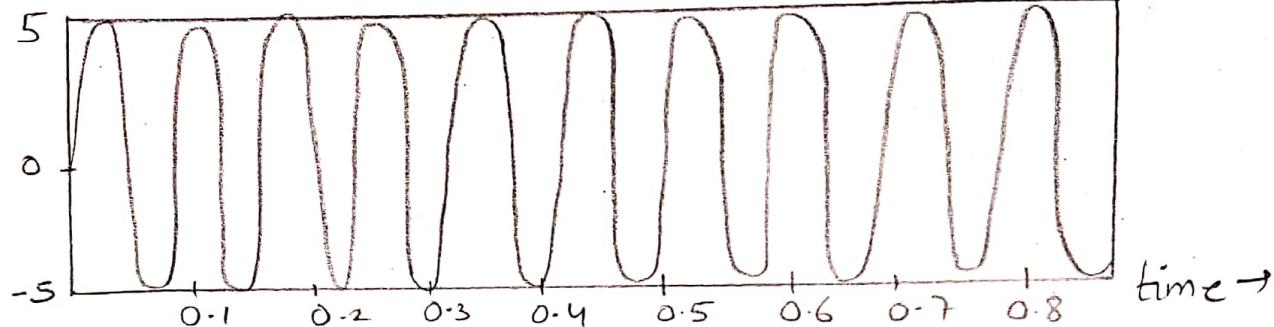
Message Signal

Amplitude



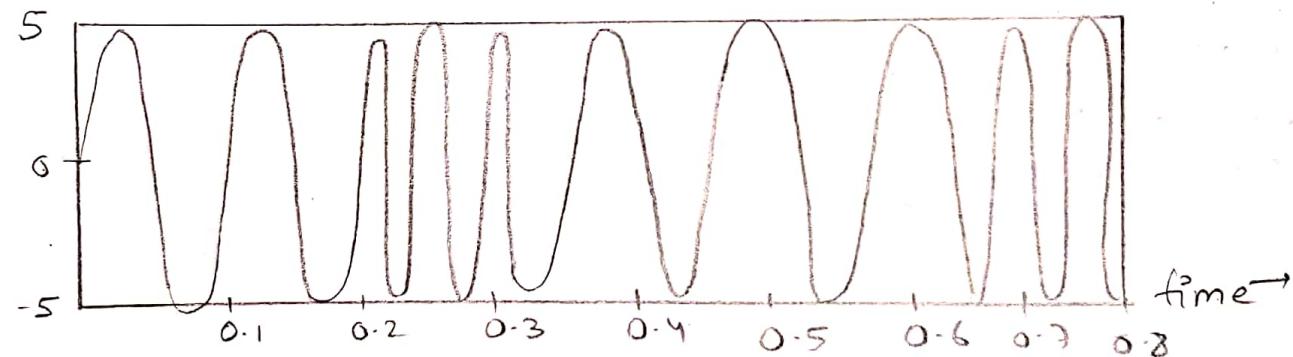
Carrier Signal

Amplitude



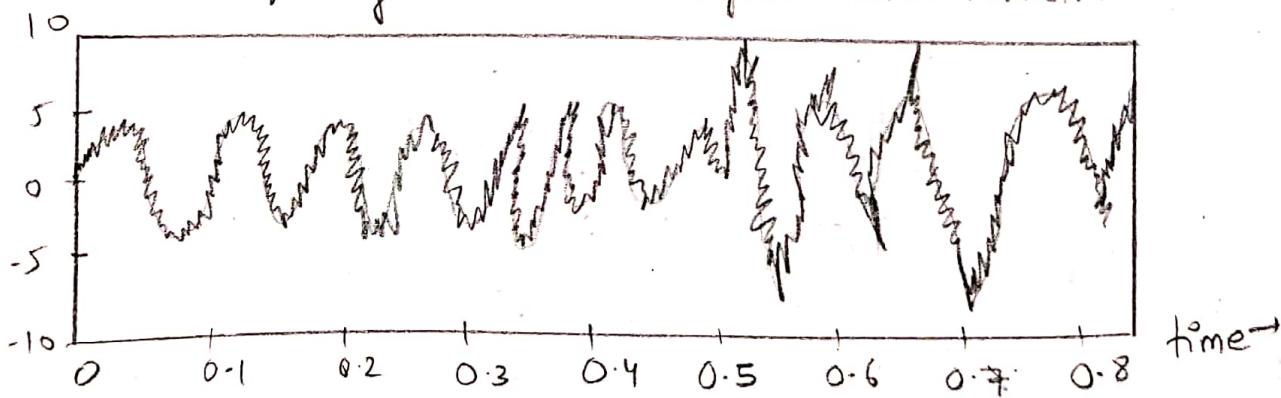
Frequency Modulated Signal

Amplitude



Frequency Modulated Signal With AWGN

Amplitude



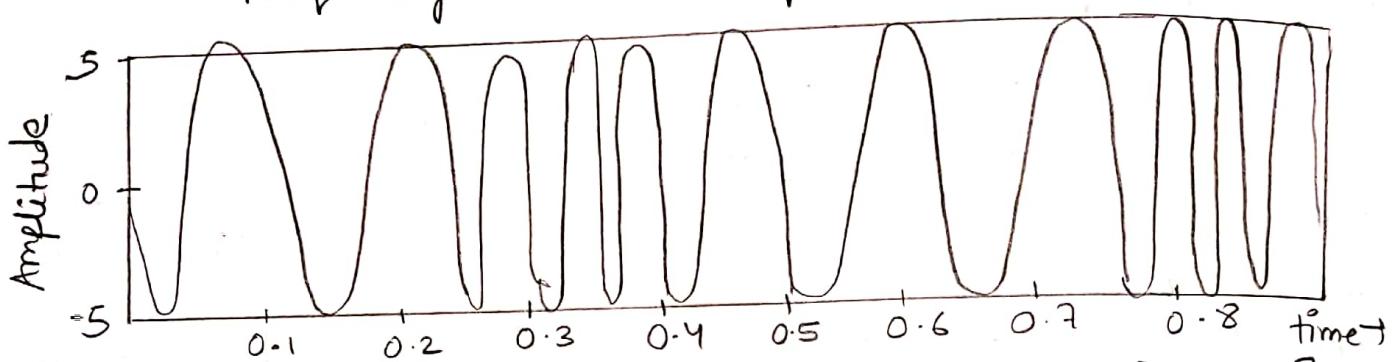
```

 $f_d = 10$ 
 $m = V_m * \sin(2 * \pi * f_m * t);$ 
 $C = V_c * \sin(2 * \pi * f_c * t);$ 
 $ampl = V_c + V_m * \sin(2 * \pi * f_c * t + f_d);$ 
 $y = V_c + \sin(2 * \pi * f_c * t + f_d) * \cos(2 * \pi * f_m * t);$ 
 $y_1 = awgn(y, 1, 'measured');$ 
 $y_2 = awgn(y, 10, 'measured');$ 
 $y_3 = awgn(y, 100, 'measured');$ 
 $subplot(4, 1, 1);$ 
 $plot(t, y);$ 
 $xlabel('time');$ 
 $ylabel('amplitude');$ 
 $title('Frequency modulated Signal');$ 
 $subplot(4, 1, 2);$ 
 $plot(t, y);$ 
 $xlabel('time');$ 
 $ylabel('amplitude');$ 
 $title('Frequency modulated Signal with AWGN [snr 1]');$ 
 $subplot(4, 1, 3);$ 
 $plot(t, y_2);$ 
 $xlabel('time');$ 
 $ylabel('amplitude');$ 
 $title('Frequency modulated Signal with AWGN [snr 10]');$ 
 $subplot(4, 1, 4);$ 
 $plot(t, y_3);$ 
 $xlabel('time');$ 
 $ylabel('amplitude');$ 
 $title('Frequency modulated Signal with AWGN [snr 100]');$ 

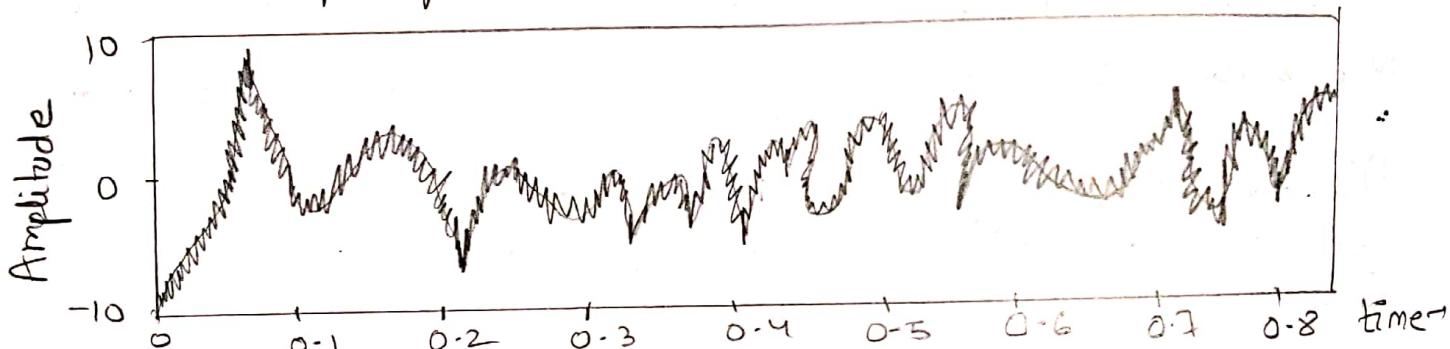
```

AWGN for different SNR in FM

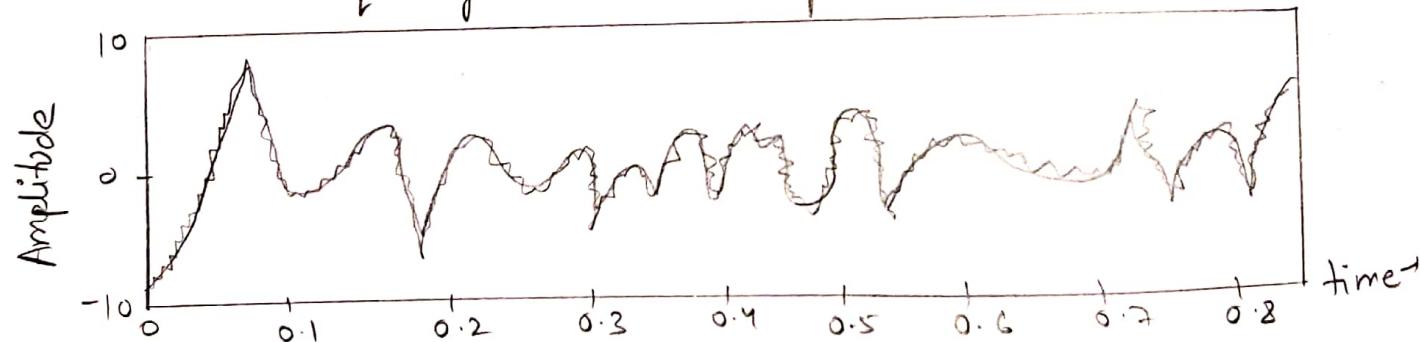
Frequency Modulated Signal



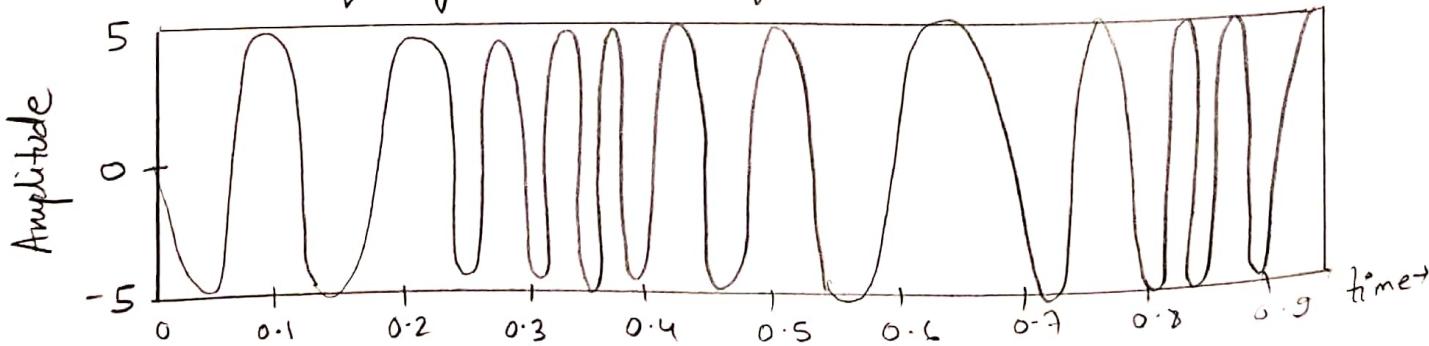
Frequency modulated signal with AWGN [snr 1]



Frequency modulated signal with AWGN [snr 10]



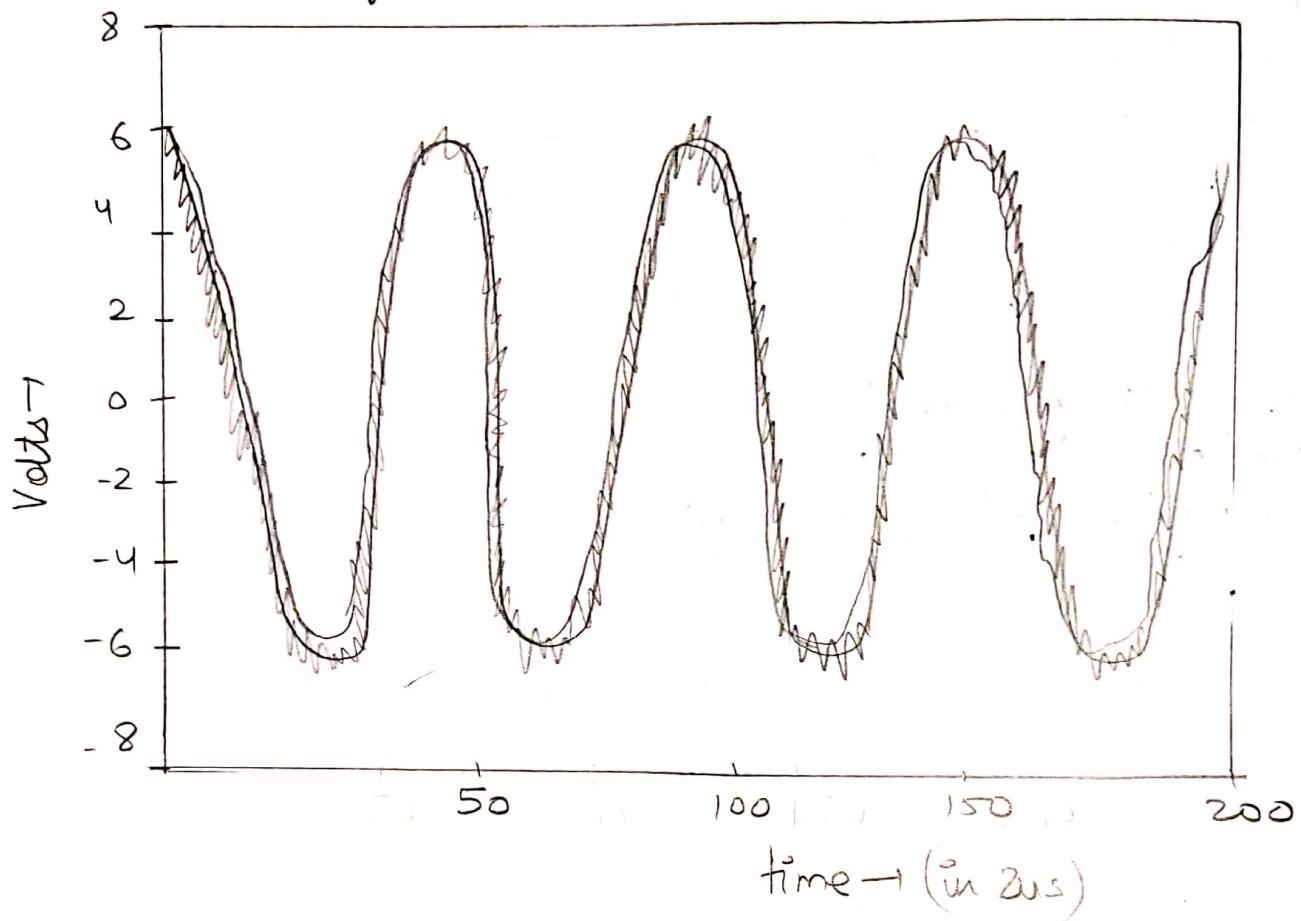
Frequency modulated signal with AWGN [snr 100]



Matlab Code for Moving Average Filter to retrieve the Signal by Averaging the Noise Fluctuation

```
% moving average filter
clear all;
close all;
dc;
fs = 500000;
fm = 10000;
t = 1:200;
x = 5 * cos(2 * pi * (fm/fs) * t);
z = awgn(x, 5); % average while Gaussian noise to the
                  input with S/N = 5
plot(x, 'g', 'LineWidth', 1.5);
hold on;
plot(z)
hold on;
for i = 1:194;
y(i) = (z(i) + z(i+1) + z(i+2) + z(i+3) + z(i+4) + z(i+6))/6,
end
plot(y, 'r', 'LineWidth', 1.5);
legend('Actual', 'Noisy', 'Filtered');
title('moving Average filter', 'FontSize', 12);
xlabel('--> time in 2 us');
ylabel('--> Volts');
```

Moving Average Filter



Noise

Actual

Filtered

Advantages of AWGN:

- The noise is additive i.e the received signal is equal to the transmitted signal plus noise. This gives the most widely used equality in communication systems.
- The result of summing a large number of different & independent factors which allows us to apply an important result from probability and statistics, called the central limit theorem

Applications:

It is often used as a channel model in which the only impairment to communication is a linear addition of wideband or white noise with a constant spectral density (expressed as watts per hertz of bandwidth) and a gaussian distribution of amplitude.

Conclusion:

Successfully observed the AM and FM under AWGN using Matlab software and drew the waveforms for different signal to noise values.