



Power Model:

$$P_{\text{total}} = P_{\text{dyn}} + P_{\text{leak}}$$

P_{dyn} :

$$P_{\text{dyn}} = C_{\text{eff}} \cdot V^2 \cdot f \cdot \alpha(w)$$

\downarrow \downarrow \downarrow
 $\ln F$ V_{dd} $\alpha(w)$
Switching Activity

$$\alpha(w) = 0.5 + 0.5 \cdot w$$



$\alpha(w)=1 \Rightarrow \text{compute}$
 $\alpha(w)=0.5 \Rightarrow \text{memory}$

P_{leak} :

$$P_{\text{leak}} = P_{\text{leak}\phi} \cdot e^{a(V-0.8)} \cdot e^{b(T-25)}$$

\downarrow \downarrow \downarrow
 $0.6W @ 25^\circ\text{C}$ Sensitive to Volt. ($a=2$) Sensitive to temp. ($b=0.04$)

$$P_{\text{total}} = P_{\text{dyn}} + P_{\text{leak}}$$

Thermal Model:

$$T_{\text{ss}} = T_{\text{amb}} + (P_{\text{total}} \cdot R_{\text{th}})$$

Thermal RC Model: (1st order RC model)

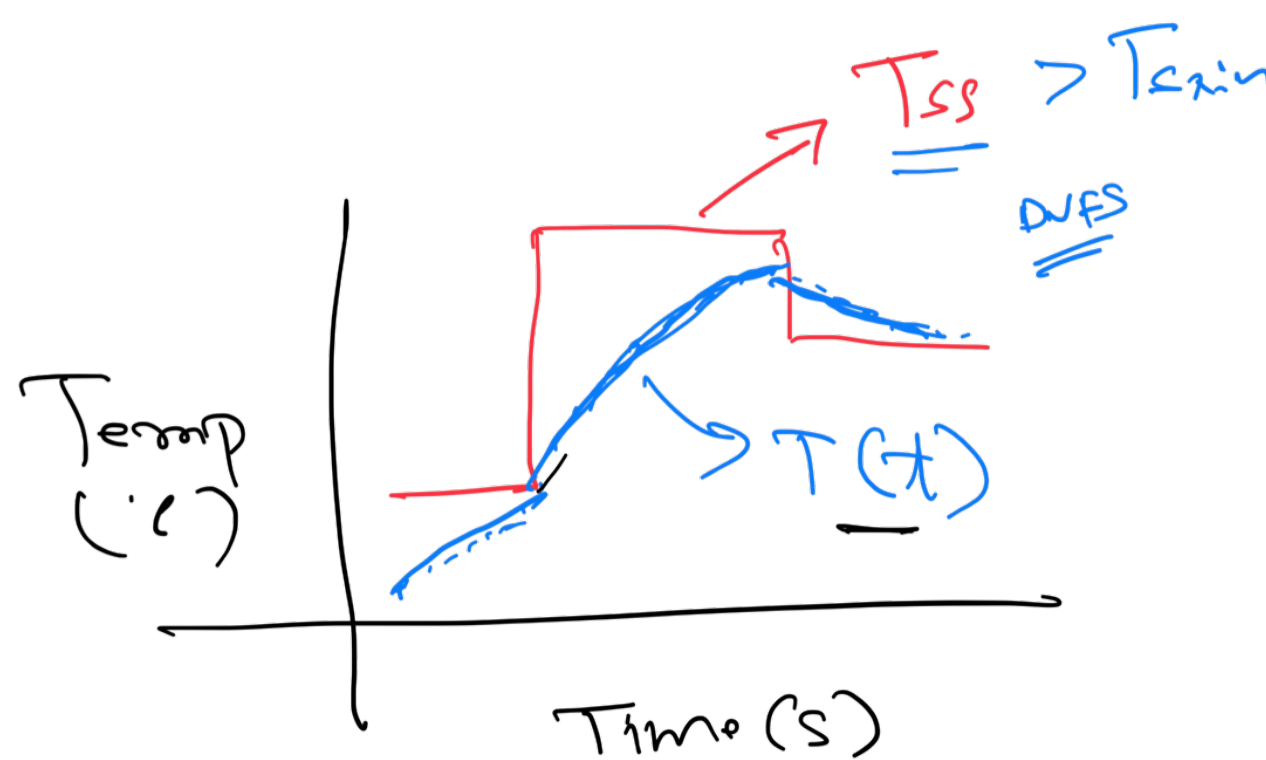
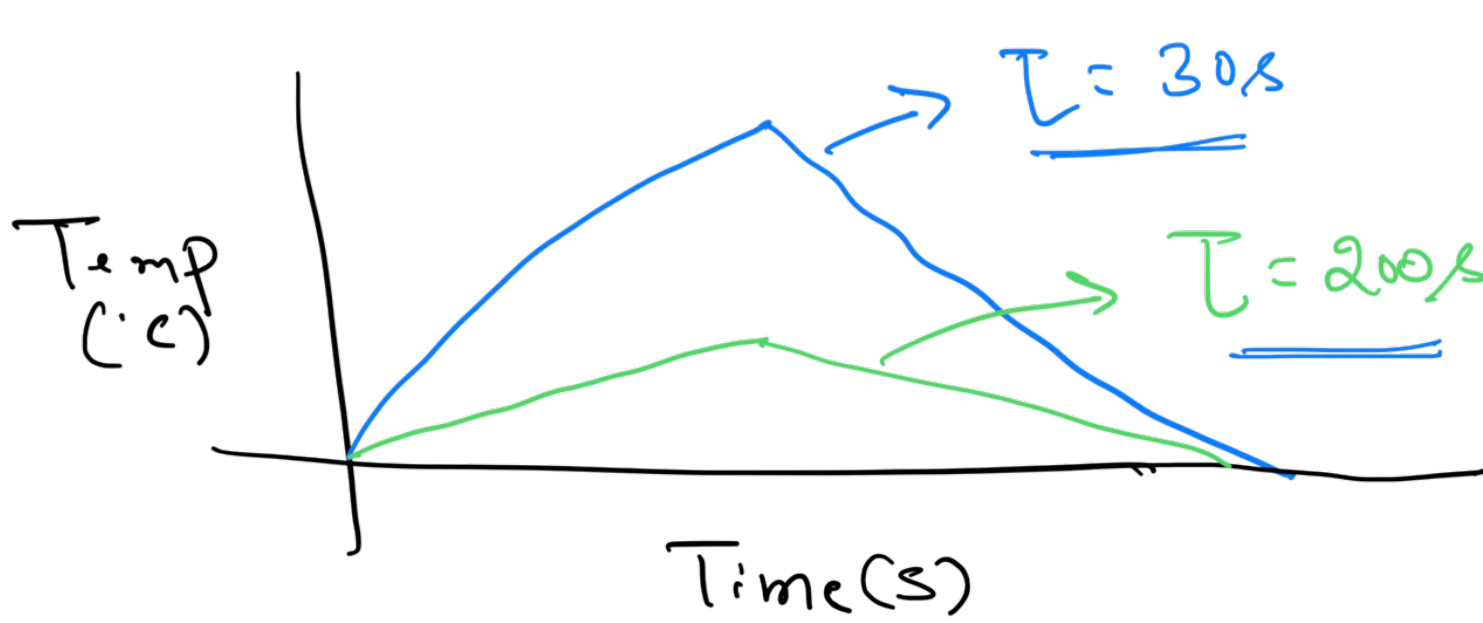
$$T(t+dt) = T(t) + (T_{\text{ss}} - T(t))(1 - e^{-dt/R_c})$$

\Downarrow simplify

$$T_{\text{new}} = T_{\text{old}} + (T_{\text{ss}} - T_{\text{old}}) \cdot (1 - e^{-t/R_c})$$

$$T = R_{\text{th}} \cdot C_{\text{th}} \begin{cases} \text{Large} \Rightarrow \text{slow temp. change} \\ \text{Small} \Rightarrow \text{fast temp. change} \end{cases}$$

$T(t) \rightarrow T_{\text{ss}}$ as $t \rightarrow \infty$ but will be capped by DVFS



Performance Model:

$$P_{\text{perf}} = \text{IPC}(w) \times \text{freq. (GHz)}$$

$$\text{IPC}(w) = \text{IPC}_{\text{min}} + (\text{IPC}_{\text{max}} - \text{IPC}_{\text{min}}) \cdot w$$

\downarrow \downarrow \downarrow
 (0.5) (2) $w = \text{workload mix}$
 \downarrow \downarrow
 (memory bound $w=0$) (compute bound $w=1$)

Energy:

$$E = P \cdot t \quad (\text{J})$$

$$E = \frac{P \cdot t}{3600} \quad (\text{Wh}) \rightarrow \text{watt-hour}$$

$$E(t) \leftarrow E(t) + dE$$

→ Energy curve is cumulative; never goes down

→ Battery drops as energy accumulates

$$\rightarrow \text{Battery \% (Wh)} = \left[\frac{\text{Battery} - \text{Energy}}{\text{Battery}} \right] \times 100$$