# Social network Graph Link Prediction - Facebook Challenge

#### **Problem statement:**

Given a directed social graph, have to predict missing links to recommend users (Link Prediction in graph)

#### **Data Overview**

Taken data from facebook's recruting challenge on kaggle <a href="https://www.kaggle.com/c/FacebookRecruiting">https://www.kaggle.com/c/FacebookRecruiting</a>) data contains two columns source and destination eac edge in graph

- Data columns (total 2 columns):

source\_node int64destination\_node int64

#### Mapping the problem into supervised learning problem:

- Generated training samples of good and bad links from given directed graph and for each link got some features like no of followers, is he followed back, page rank, katz score, adar index, some svd fetures of adj matrix, some weight features etc. and trained ml model based on these features to predict link.
- Some reference papers and videos :
  - https://www.cs.cornell.edu/home/kleinber/link-pred.pdf (https://www.cs.cornell.edu/home/kleinber/link-pred.pdf)
  - https://www3.nd.edu/~dial/publications/lichtenwalter2010new.pdf (https://www3.nd.edu/~dial/publications/lichtenwalter2010new.pdf)
  - https://kaggle2.blob.core.windows.net/forum-message-attachments/2594/supervised\_link\_prediction.pdf (https://kaggle2.blob.core.windows.net/forum-message-attachments/2594/supervised\_link\_prediction.pdf)
  - https://www.youtube.com/watch?v=2M77Hgy17cg (https://www.youtube.com/watch?v=2M77Hgy17cg)

#### Performance metric for supervised learning:

- Both precision and recall is important so F1 score is good choice
- Confusion matrix

# **Importing Libraries and Pre Processing**

```
In [0]: #Importing Libraries
        # please do go through this python notebook:
        import warnings
        warnings.filterwarnings("ignore")
        import csv
        import pandas as pd#pandas to create small dataframes
        import datetime #Convert to unix time
        import time #Convert to unix time
        # if numpy is not installed already : pip3 install numpy
        import numpy as np#Do aritmetic operations on arrays
        # matplotlib: used to plot graphs
        import matplotlib
        import matplotlib.pylab as plt
        import seaborn as sns#Plots
        from matplotlib import rcParams#Size of plots
        from sklearn.cluster import MiniBatchKMeans, KMeans#Clustering
        import math
        import pickle
        import os
        # to install xgboost: pip3 install xgboost
        import xgboost as xgb
        import warnings
        import networkx as nx
        import pdb
        import pickle
        from pandas import read hdf
        from pandas import HDFStore,DataFrame
        from tqdm import tqdm
        from scipy.sparse.linalg import svds, eigs
        from sklearn.ensemble import RandomForestClassifier
        from sklearn.metrics import f1_score
        import seaborn as sns#Plots
        import xgboost as xgb
        from sklearn.metrics import accuracy score
        from sklearn.metrics import precision_score
        from sklearn.metrics import recall_score
        from sklearn.metrics import f1_score
        from sklearn.metrics import confusion matrix
```

# In [0]: # Load the Drive helper and mount from google.colab import drive # This will prompt for authorization. drive.mount('/content/drive')

Go to this URL in a browser: https://accounts.google.com/o/oauth2/auth?client\_id=947318989803-6bn6qk8qdgf4n4g3pfee6491hc0brc4i.apps.googleusercontent.com&redirect\_uri=urn%3Aietf% 3Awg%3Aoauth%3A2.0%3Aoob&scope=email%20https%3A%2F%2Fwww.googleapis.com%2Fauth%2Fdocs.test%20https%3A%2F%2Fwww.googleapis.com%2Fauth%2Fdrive.photos.readonly%20https%3A%2F%2Fwww.googleapis.com%2Fauth%2Fpeopleapi.readonly&response\_type=code

Enter your authorization code:
.....
Mounted at /content/drive

# In [0]: **%%time**

#reading graph with filtered file
g=nx.read\_edgelist('/content/drive/My Drive/Colab Notebooks/data\_facebook/facebook\_train\_woheader.csv',delimiter=',',create\_using=nx.DiGraph(),nodetype=int)
print(nx.info(g))

Name:

Type: DiGraph

Number of nodes: 1862220 Number of edges: 9437519 Average in degree: 5.0679 Average out degree: 5.0679

CPU times: user 1min 13s, sys: 4.49 s, total: 1min 17s

Wall time: 1min 18s

# In [0]: %%time #Displaying a sub graph with 50 rows pd.read\_csv('/content/drive/My Drive/Colab Notebooks/data\_facebook/train.csv', nrows=50).to\_csv('/content/drive/My Drive/Colab Notebooks/data\_facebook/train\_woheader\_sample.csv', header=False,index=False) subgraph=nx.read\_edgelist('/content/drive/My Drive/Colab Notebooks/data\_facebook/train\_woheader\_sample.csv',delimiter=',',create\_using=nx.DiGraph(),nodetype=int) # https://stackoverflow.com/questions/9402255/drawing-a-huge-graph-with-networkx-and-matplotlib pos=nx.spring\_layout(subgraph) nx.draw(subgraph,pos,node\_color='#A0CBE2',edge\_color='#00bb5e',width=1,edge\_cmap=plt.cm.Blues,with\_labels=True) plt.savefig("graph\_sample.pdf") print(nx.info(subgraph))

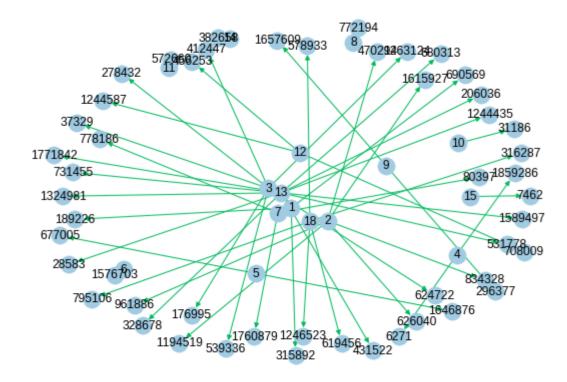
Name:

Type: DiGraph
Number of nodes: 66
Number of edges: 50

Average in degree: 0.7576 Average out degree: 0.7576

CPU times: user 366 ms, sys: 113 ms, total: 479 ms

Wall time: 946 ms



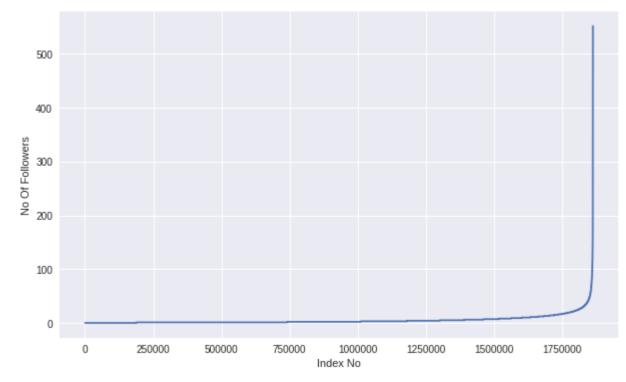
# 1. Exploratory Data Analysis

In [0]: # No of Unique persons
print("The number of unique persons",len(g.nodes()))

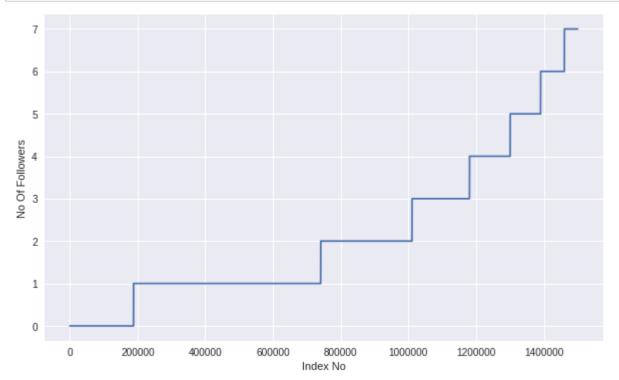
The number of unique persons 1862220

# 1.1 No of followers for each person

```
In [0]: indegree_dist = list(dict(g.in_degree()).values())
    indegree_dist.sort()
    plt.figure(figsize=(10,6))
    plt.plot(indegree_dist)
    plt.xlabel('Index No')
    plt.ylabel('No Of Followers')
    plt.show()
```



```
In [0]: #ploting at some index
    indegree_dist = list(dict(g.in_degree()).values())
    indegree_dist.sort()
    plt.figure(figsize=(10,6))
    plt.plot(indegree_dist[0:1500000])
    plt.xlabel('Index No')
    plt.ylabel('No Of Followers')
    plt.show()
    #indegree_dist
```



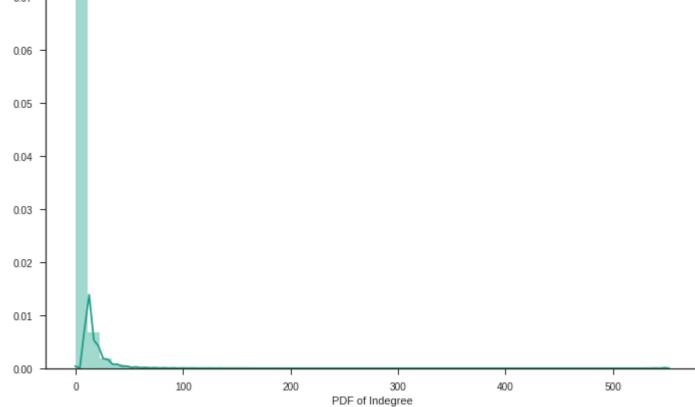
```
In [0]: ### 90-100 percentile
for i in range(0,11):
    print(90+i, 'percentile value is',np.percentile(indegree_dist,90+i))

90 percentile value is 12.0
91 percentile value is 13.0
92 percentile value is 14.0
93 percentile value is 15.0
94 percentile value is 17.0
95 percentile value is 19.0
96 percentile value is 21.0
97 percentile value is 21.0
```

99% of data having followers of 40 only.

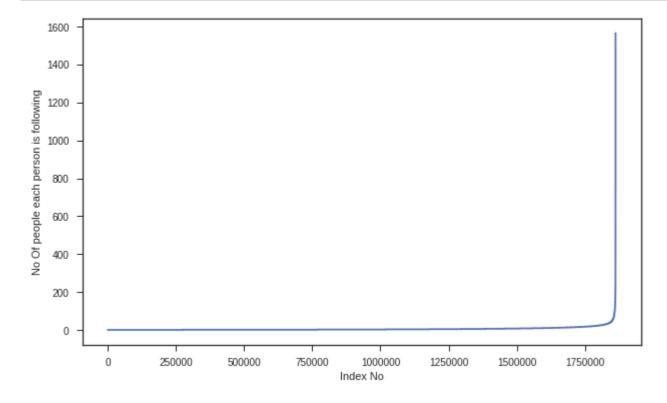
98 percentile value is 29.0 99 percentile value is 40.0 100 percentile value is 552.0

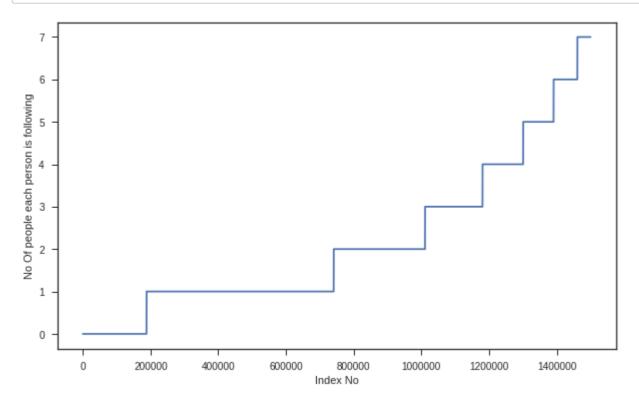
```
In [0]: ### 99-100 percentile
        for i in range(10,110,10):
            print(99+(i/100), 'percentile value is', np.percentile(indegree_dist, 99+(i/100)))
        99.1 percentile value is 42.0
        99.2 percentile value is 44.0
        99.3 percentile value is 47.0
        99.4 percentile value is 50.0
        99.5 percentile value is 55.0
        99.6 percentile value is 61.0
        99.7 percentile value is 70.0
        99.8 percentile value is 84.0
        99.9 percentile value is 112.0
        100.0 percentile value is 552.0
In [0]: %matplotlib inline
        sns.set_style('ticks')
        fig, ax = plt.subplots()
        fig.set_size_inches(11.7, 8.27)
        sns.distplot(indegree_dist, color='#16A085')
        plt.xlabel('PDF of Indegree')
        sns.despine()
        #plt.show()
         0.08
         0.07
```



# 1.2 No of people each person is following

```
In [0]: outdegree_dist = list(dict(g.out_degree()).values())
    outdegree_dist.sort()
    plt.figure(figsize=(10,6))
    plt.plot(outdegree_dist)
    plt.xlabel('Index No')
    plt.ylabel('No Of people each person is following')
    plt.show()
```

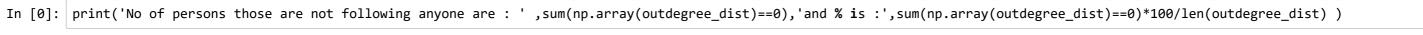




```
In [0]: ### 90-100 percentile
for i in range(0,11):
    print(90+i,'percentile value is',np.percentile(outdegree_dist,90+i))
```

90 percentile value is 12.0
91 percentile value is 13.0
92 percentile value is 14.0
93 percentile value is 15.0
94 percentile value is 17.0
95 percentile value is 19.0
96 percentile value is 21.0
97 percentile value is 24.0
98 percentile value is 29.0
99 percentile value is 40.0
100 percentile value is 552.0

```
In [0]: ### 99-100 percentile
        for i in range(10,110,10):
            print(99+(i/100), 'percentile value is',np.percentile(outdegree_dist,99+(i/100)))
        99.1 percentile value is 42.0
        99.2 percentile value is 44.0
        99.3 percentile value is 47.0
        99.4 percentile value is 50.0
        99.5 percentile value is 55.0
        99.6 percentile value is 61.0
        99.7 percentile value is 70.0
        99.8 percentile value is 84.0
        99.9 percentile value is 112.0
        100.0 percentile value is 552.0
In [0]: sns.set_style('ticks')
        fig, ax = plt.subplots()
        fig.set_size_inches(11.7, 8.27)
        sns.distplot(outdegree_dist, color='#16A085')
        plt.xlabel('PDF of Outdegree')
        sns.despine()
         0.08
         0.07
         0.06
         0.05
```



500

400

No of persons those are not following anyone are : 188043 and % is : 10.097786512871734

300

PDF of Outdegree

In [0]: print('No of persons having zero followers are : ',sum(np.array(indegree\_dist)==0),'and % is : ',sum(np.array(indegree\_dist)==0)\*100/len(indegree\_dist) )

No of persons having zero followers are: 188043 and % is: 10.097786512871734

200

100

0.04

0.03

0.02

0.01

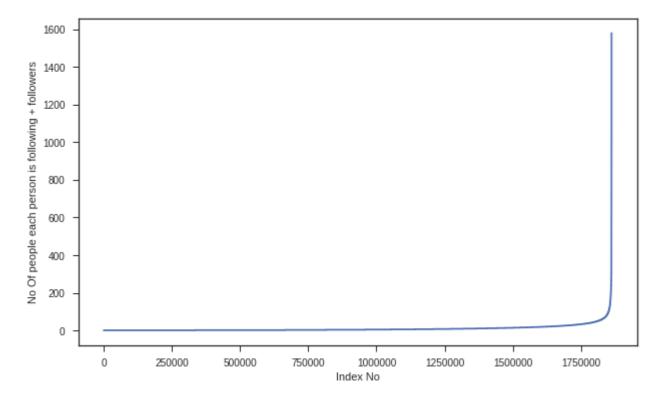
0.00

0

# 1.3 both followers + following

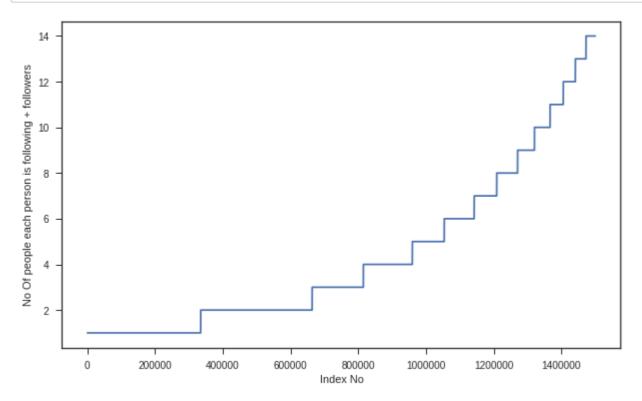
```
In [0]: from collections import Counter
    dict_in = dict(g.in_degree())
    dict_out = dict(g.out_degree())
    d = Counter(dict_in) + Counter(dict_out)
    in_out_degree = np.array(list(d.values()))
```

```
In [0]: in_out_degree_sort = sorted(in_out_degree)
    plt.figure(figsize=(10,6))
    plt.plot(in_out_degree_sort)
    plt.xlabel('Index No')
    plt.ylabel('No Of people each person is following + followers')
    plt.show()
```



No of persons those are not following anyone and also not having any followers are : 0

```
In [0]: in_out_degree_sort = sorted(in_out_degree)
    plt.figure(figsize=(10,6))
    plt.plot(in_out_degree_sort[0:1500000])
    plt.xlabel('Index No')
    plt.ylabel('No Of people each person is following + followers')
    plt.show()
```



```
In [0]: ### 90-100 percentile
for i in range(0,11):
    print(90+i,'percentile value is',np.percentile(in_out_degree_sort,90+i))
```

90 percentile value is 24.0
91 percentile value is 26.0
92 percentile value is 28.0
93 percentile value is 31.0
94 percentile value is 33.0
95 percentile value is 37.0
96 percentile value is 41.0
97 percentile value is 48.0
98 percentile value is 58.0
99 percentile value is 79.0
100 percentile value is 1579.0

```
In [0]: ### 99-100 percentile
        for i in range(10,110,10):
            print(99+(i/100), 'percentile value is',np.percentile(in_out_degree_sort,99+(i/100)))
        99.1 percentile value is 83.0
        99.2 percentile value is 87.0
        99.3 percentile value is 93.0
        99.4 percentile value is 99.0
        99.5 percentile value is 108.0
        99.6 percentile value is 120.0
        99.7 percentile value is 138.0
        99.8 percentile value is 168.0
        99.9 percentile value is 221.0
        100.0 percentile value is 1579.0
In [0]: print('Min of no of followers + following is',in out degree.min())
        print(np.sum(in_out_degree==in_out_degree.min()),' persons having minimum no of followers + following')
        Min of no of followers + following is 1
        334291 persons having minimum no of followers + following
In [0]: print('Max of no of followers + following is',in_out_degree.max())
        print(np.sum(in_out_degree==in_out_degree.max()),' persons having maximum no of followers + following')
        Max of no of followers + following is 1579
        1 persons having maximum no of followers + following
In [0]: print('No of persons having followers + following less than 10 are',np.sum(in_out_degree<10))</pre>
        No of persons having followers + following less than 10 are 1320326
In [0]: print('No of weakly connected components',len(list(nx.weakly_connected_components(g))))
        for i in list(nx.weakly_connected_components(g)):
            if len(i)==2:
                count+=1
        print('weakly connected components wit 2 nodes',count)
        No of weakly connected components 45558
```

# 1.4 Posing a problem as classification problem

weakly connected components wit 2 nodes 32195

```
In [0]: | %%time
         ###generating bad edges from given graph
         import random
        if not os.path.isfile('/content/drive/My Drive/Colab Notebooks/data facebook/missing edges final.p'):
            #getting all set of edges
          r = csv.reader(open('/content/drive/My Drive/Colab Notebooks/data_facebook/train_woheader_sample.csv','r'))
            edges = dict()
            for edge in r:
                 edges[(edge[0], edge[1])] = 1
            missing_edges = set([])
            while (len(missing_edges)<9437519):</pre>
                 a=random.randint(1, 1862220)
                b=random.randint(1, 1862220)
                 tmp = edges.get((a,b),-1)
                if tmp == -1 and a!=b:
                    try:
                         if nx.shortest_path_length(g,source=a,target=b) > 2:
                             missing_edges.add((a,b))
                         else:
                             continue
                    except:
                             missing_edges.add((a,b))
                 else:
                     continue
            pickle.dump(missing_edges,open('data/after_eda/missing_edges_final.p','wb'))
         else:
          print("b")
          missing_edges = pickle.load(open('/content/drive/My Drive/Colab Notebooks/data_facebook/missing_edges_final.p','rb'))
        CPU times: user 2.41 s, sys: 1.61 s, total: 4.02 s
        Wall time: 7.24 s
In [0]: len(missing_edges)
```

# 1.5 Training and Test data split:

Out[0]: 9437519

Removed edges from Graph and used as test data and after removing used that graph for creating features for Train and test data

```
In [0]: from sklearn.model selection import train test split
        if (not os.path.isfile('/content/drive/My Drive/Colab Notebooks/data_facebook/train_pos_after_eda.csv')) and (not os.path.isfile('/content/drive/My Drive/Colab Notebooks/data_facebook/train_pos_after_eda.csv'))
        ebook/test_pos_after_eda.csv')):
            #reading total data df
            print("New file")
            df pos = pd.read csv('/content/drive/My Drive/Colab Notebooks/data facebook/facebook train.csv')
            df_neg = pd.DataFrame(list(missing_edges), columns=['source_node', 'destination_node'])
            print("Number of nodes in the graph with edges", df_pos.shape[0])
            print("Number of nodes in the graph without edges", df neg.shape[0])
            #Trian test split
            #Spiltted data into 80-20
            #positive links and negative links seperatly because we need positive training data only for creating graph
            #and for feature generation
            X_train_pos, X_test_pos, y_train_pos, y_test_pos = train_test_split(df_pos,np.ones(len(df_pos)),test_size=0.2, random_state=9)
            X_train_neg, X_test_neg, y_train_neg, y_test_neg = train_test_split(df_neg,np.zeros(len(df_neg)),test_size=0.2, random_state=9)
            print('='*60)
            print("Number of nodes in the train data graph with edges", X_train_pos.shape[0],"=",y_train_pos.shape[0])
            print("Number of nodes in the train data graph without edges", X_train_neg.shape[0],"=", y_train_neg.shape[0])
            print('='*60)
            print("Number of nodes in the test data graph with edges", X_test_pos.shape[0],"=",y_test_pos.shape[0])
            print("Number of nodes in the test data graph without edges", X_test_neg.shape[0],"=",y_test_neg.shape[0])
            #removing header and saving
            X_train_pos.to_csv('data/after_eda/train_pos_after_eda.csv',header=False, index=False)
            X test pos.to csv('data/after eda/test pos after eda.csv',header=False, index=False)
            X_train_neg.to_csv('data/after_eda/train_neg_after_eda.csv',header=False, index=False)
            X_test_neg.to_csv('data/after_eda/test_neg_after_eda.csv',header=False, index=False)
        else:
            #Graph from Traing data only
            print("Already Existed")
            del missing_edges
```

Already Existed

```
In [0]: if (os.path.isfile('/content/drive/My Drive/Colab Notebooks/data facebook/train pos after eda.csv')) and (os.path.isfile('/content/drive/My Drive/Colab Notebooks/data facebook/te
        st pos after eda.csv')):
            train_graph=nx.read_edgelist('/content/drive/My Drive/Colab Notebooks/data_facebook/train_pos_after_eda.csv',delimiter=',',create_using=nx.DiGraph(),nodetype=int)
            test graph=nx.read edgelist('/content/drive/My Drive/Colab Notebooks/data facebook/test pos after eda.csv',delimiter=',',create using=nx.DiGraph(),nodetype=int)
            print(nx.info(train graph))
            print(nx.info(test graph))
            # finding the unique nodes in the both train and test graphs
            train_nodes_pos = set(train_graph.nodes())
            test nodes pos = set(test graph.nodes())
            trY teY = len(train nodes pos.intersection(test nodes pos))
            trY_teN = len(train_nodes_pos - test_nodes_pos)
            teY_trN = len(test_nodes_pos - train_nodes_pos)
            print('no of people common in train and test -- ',trY teY)
            print('no of people present in train but not present in test -- ',trY teN)
            print('no of people present in test but not present in train -- ',teY trN)
            print(' % of people not there in Train but exist in Test in total Test data are {} %'.format(teY_trN/len(test_nodes_pos)*100))
        Name:
        Type: DiGraph
        Number of nodes: 1780722
        Number of edges: 7550015
        Average in degree: 4.2399
        Average out degree: 4.2399
```

we have a cold start problem here

Name:

Type: DiGraph

Number of nodes: 1144623 Number of edges: 1887504 Average in degree: 1.6490 Average out degree: 1.6490

no of people common in train and test -- 1063125

no of people present in train but not present in test -- 717597 no of people present in test but not present in train -- 81498

% of people not there in Train but exist in Test in total Test data are 7.1200735962845405 %

```
In [0]: #final train and test data sets
        if (not os.path.isfile('/content/drive/My Drive/Colab Notebooks/data_facebook/train_after_eda.csv')) and \
        (not os.path.isfile('/content/drive/My Drive/Colab Notebooks/data_facebook/test_after_eda.csv')) and \
        (not os.path.isfile('/content/drive/My Drive/Colab Notebooks/data facebook/train y.csv')) and \
        (not os.path.isfile('/content/drive/My Drive/Colab Notebooks/data facebook/test y.csv')) and \
        (os.path.isfile('/content/drive/My Drive/Colab Notebooks/data facebook/train pos after eda.csv')) and \
        (os.path.isfile('/content/drive/My Drive/Colab Notebooks/data_facebook/test_pos_after_eda.csv')) and \
        (os.path.isfile('/content/drive/My Drive/Colab Notebooks/data facebook/train neg after eda.csv')) and \
        (os.path.isfile('/content/drive/My Drive/Colab Notebooks/data_facebook/test_neg_after_eda.csv')):
            X_train_pos = pd.read_csv('/content/drive/My Drive/Colab Notebooks/data_facebook/train_pos_after_eda.csv', names=['source_node', 'destination_node'])
            X_test_pos = pd.read_csv('/content/drive/My Drive/Colab Notebooks/data_facebook/test_pos_after_eda.csv', names=['source_node', 'destination_node'])
            X_train_neg = pd.read_csv('/content/drive/My Drive/Colab Notebooks/data_facebook/train_neg_after_eda.csv', names=['source_node', 'destination_node'])
            X_test_neg = pd.read_csv('/content/drive/My Drive/Colab Notebooks/data_facebook/test_neg_after_eda.csv', names=['source_node', 'destination_node'])
             print('='*60)
             print("Number of nodes in the train data graph with edges", X_train_pos.shape[0])
             print("Number of nodes in the train data graph without edges", X_train_neg.shape[0])
             print('='*60)
             print("Number of nodes in the test data graph with edges", X_test_pos.shape[0])
             print("Number of nodes in the test data graph without edges", X_test_neg.shape[0])
            X_train = X_train_pos.append(X_train_neg,ignore_index=True)
            y_train = np.concatenate((y_train_pos,y_train_neg))
            X_test = X_test_pos.append(X_test_neg,ignore_index=True)
            y_test = np.concatenate((y_test_pos,y_test_neg))
            X train.to csv('/content/drive/My Drive/Colab Notebooks/data facebook/train after eda.csv',header=False,index=False)
            X_test.to_csv('/content/drive/My Drive/Colab Notebooks/data_facebook/test_after_eda.csv',header=False,index=False)
             pd.DataFrame(y train.astype(int)).to csv('/content/drive/My Drive/Colab Notebooks/data facebook/train y.csv',header=False,index=False)
             pd.DataFrame(y_test.astype(int)).to_csv('/content/drive/My Drive/Colab Notebooks/data_facebook/test_y.csv',header=False,index=False)
        else:
          print("testing")
```

Number of nodes in the train data graph with edges 7550015

Number of nodes in the train data graph without edges 7550015

----
Number of nodes in the test data graph with edges 1887504

Number of nodes in the test data graph without edges 1887504

#### **Featurization**

# 1. Reading Data

Type: DiGraph
Number of nodes: 1780722
Number of edges: 7550015
Average in degree: 4.2399
Average out degree: 4.2399
CPU times: user 1min 2s, sys: 3.43 s, total: 1min 6s

### 2. Similarity measures

Wall time: 1min 7s

#### 2.1 Jaccard Distance:

http://www.statisticshowto.com/jaccard-index/ (http://www.statisticshowto.com/jaccard-index/)

$$j = \frac{|X \cap Y|}{|X \cup Y|}$$

```
In [0]: print(jaccard_for_followers(273084,470294))
0
```

#### 2.2 Cosine distance

$$CosineDistance = \dfrac{|X \cap Y|}{|X| \cdot |Y|}$$

```
In [0]: #for followees
        def cosine_for_followees(a,b):
            try:
                if len(set(train_graph.successors(a))) == 0 | len(set(train_graph.successors(b))) == 0:
                sim = (len(set(train_graph.successors(a)).intersection(set(train_graph.successors(b)))))/\
                                            (math.sqrt(len(set(train_graph.successors(a)))*len((set(train_graph.successors(b))))))
                return sim
            except:
                return 0
In [0]: print(cosine_for_followees(273084,1505602))
        0.0
In [0]: def cosine_for_followers(a,b):
             try:
                if len(set(train_graph.predecessors(a))) == 0 | len(set(train_graph.predecessors(b))) == 0:
                sim = (len(set(train_graph.predecessors(a)).intersection(set(train_graph.predecessors(b)))))/\
                                              (math.sqrt(len(set(train_graph.predecessors(a))))*(len(set(train_graph.predecessors(b)))))
                return sim
            except:
                return 0
In [0]: print(cosine_for_followers(2,470294))
```

# 3. Ranking Measures

0.02886751345948129

https://networkx.github.io/documentation/networkx-1.10/reference/generated/networkx.algorithms.link\_analysis.pagerank\_alg.pagerank.html (https://networkx.github.io/documentation/networkx-1.10/reference/generated/networkx.algorithms.link\_analysis.pagerank\_html)

PageRank computes a ranking of the nodes in the graph G based on the structure of the incoming links.

Mathematical PageRanks for a simple network, expressed as percentages. (Google uses a logarithmic scale.) Page C has a higher PageRank than Page E, even though there are fewer links to C; the one link to C comes from an important page and hence is of high value. If web surfers who start on a random page have an 85% likelihood of choosing a random link from the page they are currently visiting, and a 15% likelihood of jumping to a page chosen at random from the entire web, they will reach Page E 8.1% of the time. (The 15% likelihood of jumping to an arbitrary page corresponds to a damping factor of 85%.) Without damping, all web surfers would eventually end up on Pages A, B, or C, and all other pages would have PageRank zero. In the presence of damping, Page A effectively links to all pages in the web, even though it has no outgoing links of its own.

#### 3.1 Page Ranking

https://en.wikipedia.org/wiki/PageRank (https://en.wikipedia.org/wiki/PageRank)

```
In [0]: if not os.path.isfile('/content/drive/My Drive/Colab Notebooks/data_facebook/fea_sample/page_rank.p'):
             pr = nx.pagerank(train_graph, alpha=0.85)
             pickle.dump(pr,open('/content/drive/My Drive/Colab Notebooks/data_facebook/fea_sample/page_rank.p','wb'))
        else:
            print("b")
             pr = pickle.load(open('/content/drive/My Drive/Colab Notebooks/data_facebook/fea_sample/page_rank.p','rb'))
        b
In [0]: print('min',pr[min(pr, key=pr.get)])
        print('max',pr[max(pr, key=pr.get)])
        print('mean',float(sum(pr.values())) / len(pr))
        min 1.6556497245737814e-07
        max 2.7098251341935827e-05
        mean 5.615699699389075e-07
In [0]: | #for imputing to nodes which are not there in Train data
        mean_pr = float(sum(pr.values())) / len(pr)
        print(mean_pr)
        5.615699699389075e-07
```

# 4. Other Graph Features

#### 4.1 Shortest path:

Getting Shortest path between two nodes, if nodes have direct path i.e directly connected then we are removing that edge and calculating path.

```
In [0]: #if has direct edge then deleting that edge and calculating shortest path
def compute_shortest_path_length(a,b):
    p=-1
    try:
        if train_graph.has_edge(a,b):
            train_graph.remove_edge(a,b)
            p= nx.shortest_path_length(train_graph,source=a,target=b)
            train_graph.add_edge(a,b)
    else:
        p = nx.shortest_path_length(train_graph,source=a,target=b)
        return p
    except:
    return -1
```

```
In [0]: #testing
compute_shortest_path_length(77697, 826021)
```

Out[0]: 10

```
In [0]: #testing
    compute_shortest_path_length(669354,1635354)
Out[0]: -1
```

4.2 Checking for same community

```
In [0]: | #getting weekly connected edges from graph
        wcc=list(nx.weakly_connected_components(train_graph))
        def belongs_to_same_wcc(a,b):
            index = []
            if train_graph.has_edge(b,a):
                return 1
            if train_graph.has_edge(a,b):
                    for i in wcc:
                        if a in i:
                            index= i
                            break
                    if (b in index):
                        train_graph.remove_edge(a,b)
                        if compute_shortest_path_length(a,b)==-1:
                            train_graph.add_edge(a,b)
                            return 0
                        else:
                            train_graph.add_edge(a,b)
                            return 1
                    else:
                        return 0
            else:
                    for i in wcc:
                        if a in i:
                            index= i
                            break
                    if(b in index):
                        return 1
                    else:
                        return 0
```

```
In [0]: belongs_to_same_wcc(861, 1659750)
Out[0]: 0
```

#### 4.3 Adamic/Adar Index:

Adamic/Adar measures is defined as inverted sum of degrees of common neighbours for given two vertices.

$$A(x,y) = \sum_{u \in N(x) \cap N(y)} rac{1}{log(|N(u)|)}$$

```
In [0]: calc_adar_in(1,189226)
```

Out[0]: 0

#### 4.4 Is persion was following back:

```
In [0]: def follows_back(a,b):
    if train_graph.has_edge(b,a):
        return 1
    else:
        return 0
```

```
In [0]: follows_back(1,189226)
Out[0]: 1
```

#### 4.5 Katz Centrality:

https://en.wikipedia.org/wiki/Katz\_centrality\_(https://en.wikipedia.org/wiki/Katz\_centrality\_)

https://www.geeksforgeeks.org/katz-centrality-measure/ (https://www.geeksforgeeks.org/katz-centrality-measure/)

Katz centrality computes the centrality for a node based on the centrality of its neighbors. It is a generalization of the eigenvector centrality. The Katz centrality for node i is

 $x_i = lpha \sum_j A_{ij} x_j + eta,$ 

where A is the adjacency matrix of the graph G with eigenvalues

λ

The parameter

 $\beta$ 

controls the initial centrality and

$$lpha < rac{1}{\lambda_{max}}$$
.

```
In [0]: if not os.path.isfile('/content/drive/My Drive/Colab Notebooks/data_facebook/fea_sample/katz.p'):
    katz = nx.katz.katz_centrality(train_graph,alpha=0.005,beta=1)
    pickle.dump(katz,open('/content/drive/My Drive/Colab Notebooks/data_facebook/fea_sample/katz.p','wb'))
else:
    katz = pickle.load(open('/content/drive/My Drive/Colab Notebooks/data_facebook/fea_sample/katz.p','rb'))

In [0]: print('min',katz[min(katz, key=katz.get)])
    print('max',katz[max(katz, key=katz.get)])
    print('mean',float(sum(katz.values())) / len(katz))

In [0]: mean_katz = float(sum(katz.values())) / len(katz)
    print(mean_katz)
    0.0007483800935562018
```

#### 4.6 Hits Score

The HITS algorithm computes two numbers for a node. Authorities estimates the node value based on the incoming links. Hubs estimates the node value based on outgoing links.

https://en.wikipedia.org/wiki/HITS\_algorithm (https://en.wikipedia.org/wiki/HITS\_algorithm)

```
In [0]: if not os.path.isfile('/content/drive/My Drive/Colab Notebooks/data_facebook/fea_sample/hits.p'):
    hits = nx.hits(train_graph, max_iter=100, tol=1e-08, nstart=None, normalized=True)
    pickle.dump(hits,open('/content/drive/My Drive/Colab Notebooks/data_facebook/fea_sample/hits.p','wb'))
else:
    hits = pickle.load(open('/content/drive/My Drive/Colab Notebooks/data_facebook/fea_sample/hits.p','rb'))

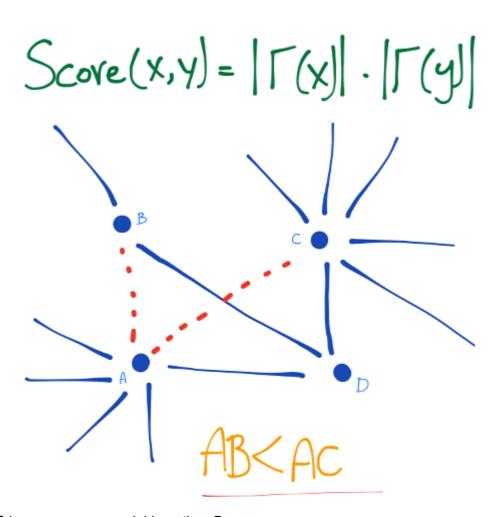
In [0]: print('min',hits[0][min(hits[0], key=hits[0].get)])
    print('max',hits[0][max(hits[0], key=hits[0].get)])
    print('mean',float(sum(hits[0].values())) / len(hits[0]))

min 0.0
max 0.004868653378780953
mean 5.615699699344123e-07
```

#### 5. Preferential Attachment (Similarity measures)

Preferential Attachment One well-known concept in social networks is that users with many friends tend to create more connections in the future. This is due to the fact that in some social networks, like in finance, the rich get richer. We estimate how "rich" our two vertices are by calculating the multiplication between the number of friends ( $|\Gamma(x)|$ ) or followers each vertex has. It may be noted that the similarity index does not require any node neighbor information; therefore, this similarity index has the lowest computational complexity.

$$j = |X|. |Y|$$



The link between A and C is more probable than the link between A and B as C have many more neighbors than B

```
In [0]: #working code
        #G= nx.barabasi_albert_graph(20,10)
        #nx.draw(G, with_labels=True)
        #plt.show()
In [0]: #preferential attachment
        def preferential_attachment(a,b):
                if len(set(train_graph.successors(a))) == 0 | len(set(train_graph.successors(b))) == 0:
                    #print("a")
                    return 0
                #print("d")
                sim = ((math.sqrt(len(set(train_graph.successors(a)))*len(set(train_graph.successors(b))))))
                #print("c")
            except:
                #print("b")
                return 0
            return sim
```

```
In [0]: preferential_attachment(200,320)
Out[0]: 3.7416573867739413
```

#### 5. Featurization

In [0]: import random

#### 5.1 Reading a sample of Data from both train and test

```
if os.path.isfile('/content/drive/My Drive/Colab Notebooks/data_facebook/train_after_eda.csv'):
            filename = "/content/drive/My Drive/Colab Notebooks/data facebook/train after eda.csv"
             # you uncomment this line, if you don't know the lentgh of the file name
            # here we have hardcoded the number of lines as 15100030
             # n_train = sum(1 for line in open(filename)) #number of records in file (excludes header)
             n train = 15100028
            s = 100000 #desired sample size
             skip_train = sorted(random.sample(range(1,n_train+1),n_train-s))
             #https://stackoverflow.com/a/22259008/4084039
In [0]: if os.path.isfile('/content/drive/My Drive/Colab Notebooks/data facebook/test after eda.csv'):
             filename = "/content/drive/My Drive/Colab Notebooks/data_facebook/test_after_eda.csv"
             # you uncomment this line, if you dont know the lentgh of the file name
            # here we have hardcoded the number of lines as 3775008
            # n_test = sum(1 for line in open(filename)) #number of records in file (excludes header)
            n test = 3775006
            s = 50000 #desired sample size
            skip_test = sorted(random.sample(range(1,n_test+1),n_test-s))
            #https://stackoverflow.com/a/22259008/4084039
In [0]: print("Number of rows in the train data file:", n_train)
        print("Number of rows we are going to elimiate in train data are",len(skip_train))
        print("Number of rows in the test data file:", n_test)
        print("Number of rows we are going to elimiate in test data are",len(skip_test))
        Number of rows in the train data file: 15100028
        Number of rows we are going to elimiate in train data are 15000028
        Number of rows in the test data file: 3775006
        Number of rows we are going to elimiate in test data are 3725006
In [0]: df final train = pd.read csv('/content/drive/My Drive/Colab Notebooks/data facebook/train after eda.csv', skiprows=skip train, names=['source node', 'destination node'])
        df_final_train['indicator_link'] = pd.read_csv('/content/drive/My Drive/Colab Notebooks/data_facebook/train_y.csv', skiprows=skip_train, names=['indicator_link'])
        print("Our train matrix size ",df_final_train.shape)
        df_final_train.head(2)
        Our train matrix size (100002, 3)
Out[0]:
```

Our test matrix size (50002, 3)

Out[0]:

	source_node	destination_node	indicator_link			
0	848424	784690	1			
1	1446582	1393749	1			

#### 5.2 Adding a set of features

we will create these each of these features for both train and test data points

- 1. jaccard followers
- 2. jaccard followees
- 3. cosine followers
- 4. cosine followees
- 5. num followers s
- 6. num followees s
- 7. num followers d
- 8. num followees d
- 9. inter followers
- 10. inter followees

```
In [0]: if not os.path.isfile('/content/drive/My Drive/Colab Notebooks/data_facebook/fea_sample/storage_sample_stage1.h5'):
    #mapping jaccrd followers to train and test data
    df_final_train['jaccard_followers'] = df_final_train.apply(lambda row:jaccard_for_followers(row['source_node'],row['destination_node']),axis=1)
    df_final_test['jaccard_followers'] = df_final_test.apply(lambda row:jaccard_for_followers(row['source_node'],row['destination_node']),axis=1)
    #mapping jaccrd followees to train and test data
    df_final_train['jaccard_followees'] = df_final_test.apply(lambda row:jaccard_for_followees(row['source_node'],row['destination_node']),axis=1)
    df_final_test['jaccard_followers'] = df_final_test.apply(lambda row:cosine_for_followers(row['source_node'],row['destination_node']),axis=1)
    df_final_test['cosine_followers'] = df_final_test.apply(lambda row:cosine_for_followers(row['source_node'],row['destination_node']),axis=1)
    #mapping jaccrd followees to train and test data
    df_final_test['cosine_followees'] = df_final_test.apply(lambda row:cosine_for_followees(row['source_node'],row['destination_node']),axis=1)
    df_final_train['cosine_followees'] = df_final_train.apply(lambda row:cosine_for_followees(row['source_node'],row['destination_node']),axis=1)
    df_final_test['cosine_followees'] = df_final_train.apply(lambda row:cosine_for_followees(row['source_node'],row['destination_node']),axis=1)
```

```
In [0]: def compute features stage1(df final):
             #calculating no of followers followees for source and destination
             #calculating intersection of followers and followees for source and destination
             num followers s=[]
            num followees s=[]
             num followers d=[]
             num_followees_d=[]
            inter followers=[]
            inter_followees=[]
            for i,row in df final.iterrows():
                try:
                    s1=set(train graph.predecessors(row['source node']))
                    s2=set(train_graph.successors(row['source_node']))
                 except:
                     s1 = set()
                    s2 = set()
                 try:
                    d1=set(train_graph.predecessors(row['destination_node']))
                    d2=set(train_graph.successors(row['destination_node']))
                except:
                    d1 = set()
                    d2 = set()
                num_followers_s.append(len(s1))
                num_followees_s.append(len(s2))
                num_followers_d.append(len(d1))
                num_followees_d.append(len(d2))
                inter_followers.append(len(s1.intersection(d1)))
                inter_followees.append(len(s2.intersection(d2)))
             return num_followers_s, num_followees_s, num_followers_d, num_followees_d, inter_followers, inter_followees
```

```
In [0]: %%time
        if not os.path.isfile('/content/drive/My Drive/Colab Notebooks/data_facebook/fea_sample/storage_sample_stage1.h5'):
            df_final_train['num_followers_s'], df_final_train['num_followees_s'], \
            df_final_train['num_followers_d'], df_final_train['num_followees_d'], \
            df_final_train['inter_followers'], df_final_train['inter_followees'] = compute_features_stage1(df_final_train)
            df_final_test['num_followers_s'], df_final_test['num_followees_s'], \
            df_final_test['num_followers_d'], df_final_test['num_followees_d'], \
            df_final_test['inter_followers'], df_final_test['inter_followees'] = compute_features_stage1(df_final_test)
            hdf = HDFStore('/content/drive/My Drive/Colab Notebooks/data facebook/storage sample stage1.h5')
            hdf.put('train_df',df_final_train, format='table', data_columns=True)
            hdf.put('test_df',df_final_test, format='table', data_columns=True)
            hdf.close()
        else:
            print("b")
            df final train = read hdf('/content/drive/My Drive/Colab Notebooks/data facebook/fea sample/storage sample stage1.h5', 'train df',mode='r')
            df_final_test = read_hdf('/content/drive/My Drive/Colab Notebooks/data_facebook/fea_sample/storage_sample_stage1.h5', 'test_df',mode='r')
```

CPU times: user 158 ms, sys: 26 ms, total: 184 ms Wall time: 221 ms

#### 5.3 Adding new set of features

#### we will create these each of these features for both train and test data points

- 1. adar index
- 2. is following back
- 3. belongs to same weakly connect components
- 4. shortest path between source and destination

```
In [0]: if not os.path.isfile('/content/drive/My Drive/Colab Notebooks/data facebook/fea sample/storage sample stage2.h5'):
           #mapping adar index on train
           df final train['adar index'] = df final train.apply(lambda row: calc adar in(row['source node'],row['destination node']),axis=1)
           #mapping adar index on test
           df_final_test['adar_index'] = df_final_test.apply(lambda row: calc_adar_in(row['source_node'],row['destination_node']),axis=1)
           #-----
           #mapping followback or not on train
           df_final_train['follows_back'] = df_final_train.apply(lambda row: follows_back(row['source_node'],row['destination_node']),axis=1)
           #mapping followback or not on test
           df_final_test['follows_back'] = df_final_test.apply(lambda row: follows_back(row['source_node'],row['destination_node']),axis=1)
           #-----
           #mapping same component of wcc or not on train
           df final train['same comp'] = df final train.apply(lambda row: belongs to same wcc(row['source node'],row['destination node']),axis=1)
           ##mapping same component of wcc or not on train
           df final test['same comp'] = df final test.apply(lambda row: belongs to same wcc(row['source node'],row['destination node']),axis=1)
           #-----
           #mapping shortest path on train
           df final train['shortest path'] = df final_train.apply(lambda row: compute_shortest_path_length(row['source_node'],row['destination_node']),axis=1)
           #mapping shortest path on test
           df final test['shortest path'] = df final test.apply(lambda row: compute shortest path length(row['source node'],row['destination node']),axis=1)
           hdf = HDFStore('/content/drive/My Drive/Colab Notebooks/data facebook/fea sample/storage sample stage2.h5')
           hdf.put('train_df',df_final_train, format='table', data_columns=True)
           hdf.put('test_df',df_final_test, format='table', data_columns=True)
           hdf.close()
       else:
           print("Already Existed")
           df_final_train = read_hdf('/content/drive/My Drive/Colab Notebooks/data_facebook/fea_sample/storage_sample_stage2.h5', 'train_df',mode='r')
           df final test = read hdf('/content/drive/My Drive/Colab Notebooks/data facebook/fea sample/storage sample stage2.h5', 'test df',mode='r')
```

Already Existed

#### 5.4 Adding new set of features

#### we will create these each of these features for both train and test data points

- 1. Weight Features
  - weight of incoming edges
  - weight of outgoing edges
  - weight of incoming edges + weight of outgoing edges
  - weight of incoming edges \* weight of outgoing edges
  - 2\*weight of incoming edges + weight of outgoing edges
  - weight of incoming edges + 2\*weight of outgoing edges
- 2. Page Ranking of source
- 3. Page Ranking of dest

#

- 4. katz of source
- 5. katz of dest
- 6. hubs of source
- 7. hubs of dest
- 8. authorities s of source
- 9. authorities\_s of dest

#### Weight Features

In order to determine the similarity of nodes, an edge weight value was calculated between nodes. Edge weight decreases as the neighbor count goes up. Intuitively, consider one million people following a celebrity on a social network then chances are most of them never met each other or the celebrity. On the other hand, if a user has 30 contacts in his/her social network, the chances are higher that many of them know each other. credit - Graph-based Features for Supervised Link Prediction William Cukierski, Benjamin Hamner, Bo Yang

$$W=rac{1}{\sqrt{1+|X|}}$$

it is directed graph so calculated Weighted in and Weighted out differently

```
In [0]: | %%time
        #weight for source and destination of each link
        Weight_in = {}
        Weight out = {}
        for i in tqdm(train_graph.nodes()):
            s1=set(train graph.predecessors(i))
            w_{in} = 1.0/(np.sqrt(1+len(s1)))
            Weight_in[i]=w_in
            s2=set(train graph.successors(i))
            w_out = 1.0/(np.sqrt(1+len(s2)))
            Weight_out[i]=w_out
        #for imputing with mean
        mean_weight_in = np.mean(list(Weight_in.values()))
        mean_weight_out = np.mean(list(Weight_out.values()))
        100% | 1780722/1780722 [00:17<00:00, 99947.76it/s]
        CPU times: user 17.8 s, sys: 362 ms, total: 18.2 s
        Wall time: 18.2 s
In [0]: if not os.path.isfile('/content/drive/My Drive/Colab Notebooks/data_facebook/fea_sample/storage_sample_stage3.h5'):
            #mapping to pandas train
            df final train['weight in'] = df final train.destination node.apply(lambda x: Weight in.get(x,mean weight in))
            df_final_train['weight_out'] = df_final_train.source_node.apply(lambda x: Weight_out.get(x,mean_weight_out))
            #mapping to pandas test
            df_final_test['weight_in'] = df_final_test.destination_node.apply(lambda x: Weight_in.get(x,mean_weight_in))
            df final test['weight out'] = df final test.source node.apply(lambda x: Weight out.get(x,mean weight out))
            #some features engineerings on the in and out weights
            df_final_train['weight_f1'] = df_final_train.weight_in + df_final_train.weight_out
            df_final_train['weight_f2'] = df_final_train.weight_in * df_final_train.weight_out
            df final train['weight f3'] = (2*df final train.weight in + 1*df final train.weight out)
            df_final_train['weight_f4'] = (1*df_final_train.weight_in + 2*df_final_train.weight_out)
            #some features engineerings on the in and out weights
            df_final_test['weight_f1'] = df_final_test.weight_in + df_final_test.weight_out
            df_final_test['weight_f2'] = df_final_test.weight_in * df_final_test.weight_out
            df_final_test['weight_f3'] = (2*df_final_test.weight_in + 1*df_final_test.weight_out)
            df_final_test['weight_f4'] = (1*df_final_test.weight_in + 2*df_final_test.weight_out)
        else:
          print("Already Existed")
```

Already Existed

```
In [0]: if not os.path.isfile('/content/drive/My Drive/Colab Notebooks/data facebook/fea sample/storage sample stage3.h5'):
           #page rank for source and destination in Train and Test
           #if anything not there in train graph then adding mean page rank
           df final train['page rank s'] = df final train.source node.apply(lambda x:pr.get(x,mean pr))
           df final train['page rank d'] = df final train.destination node.apply(lambda x:pr.get(x,mean pr))
           df final test['page rank s'] = df final test.source node.apply(lambda x:pr.get(x,mean pr))
           df_final_test['page_rank_d'] = df_final_test.destination_node.apply(lambda x:pr.get(x,mean_pr))
           #Katz centrality score for source and destination in Train and test
           #if anything not there in train graph then adding mean katz score
           df final train['katz s'] = df final train.source node.apply(lambda x: katz.get(x,mean katz))
           df_final_train['katz_d'] = df_final_train.destination_node.apply(lambda x: katz.get(x,mean_katz))
           df final test['katz s'] = df final test.source node.apply(lambda x: katz.get(x,mean katz))
           df final test['katz d'] = df final test.destination node.apply(lambda x: katz.get(x,mean katz))
           #Hits algorithm score for source and destination in Train and test
           #if anything not there in train graph then adding 0
           df final train['hubs s'] = df final train.source node.apply(lambda x: hits[0].get(x,0))
           df final train['hubs d'] = df final train.destination node.apply(lambda x: hits[0].get(x,0))
           df_final_test['hubs_s'] = df_final_test.source_node.apply(lambda x: hits[0].get(x,0))
           df_final_test['hubs_d'] = df_final_test.destination_node.apply(lambda x: hits[0].get(x,0))
           #Hits algorithm score for source and destination in Train and Test
           #if anything not there in train graph then adding 0
           df final train['authorities s'] = df final train.source node.apply(lambda x: hits[1].get(x,0))
           df_final_train['authorities_d'] = df_final_train.destination_node.apply(lambda x: hits[1].get(x,0))
           df final test['authorities s'] = df final test.source node.apply(lambda x: hits[1].get(x,0))
           df final test['authorities d'] = df final test.destination node.apply(lambda x: hits[1].get(x,0))
           hdf = HDFStore('data/fea_sample/storage_sample_stage3.h5')
           hdf.put('train df',df final train, format='table', data columns=True)
           hdf.put('test df',df final test, format='table', data columns=True)
           hdf.close()
       else:
           hdf.close()
           df final train = read hdf('/content/drive/My Drive/Colab Notebooks/data facebook/fea sample/storage sample stage3.h5', 'train df',mode='r')
           df final test = read hdf('/content/drive/My Drive/Colab Notebooks/data facebook/fea sample/storage sample stage3.h5', 'test df',mode='r')
           hdf.close()
```

#### 5.5 Adding new set of features

we will create these each of these features for both train and test data points

1. SVD features for both source and destination

```
In [0]: def svd(x, S):
            try:
                z = sadj_dict[x]
                return S[z]
            except:
                return [0,0,0,0,0,0]
In [0]: #for svd features to get feature vector creating a dict node val and index in svd vector
        sadj_col = sorted(train_graph.nodes())
        sadj_dict = { val:idx for idx,val in enumerate(sadj_col)}
In [0]: Adj = nx.adjacency_matrix(train_graph,nodelist=sorted(train_graph.nodes())).asfptype()
In [0]: U, s, V = svds(Adj, k = 6)
        print('Adjacency matrix Shape',Adj.shape)
        print('U Shape',U.shape)
        print('V Shape', V.shape)
        print('s Shape',s.shape)
        Adjacency matrix Shape (1780722, 1780722)
        U Shape (1780722, 6)
        V Shape (6, 1780722)
        s Shape (6,)
```

```
In [0]: if not os.path.isfile('/content/drive/My Drive/Colab Notebooks/data facebook/fea sample/storage sample stage4.h5'):
         df final train[['svd u s 1', 'svd u s 2','svd u s 3', 'svd u s 4', 'svd u s 5', 'svd u s 6']] = \
         df final train.source node.apply(lambda x: svd(x, U)).apply(pd.Series)
         df_final_train[['svd_u_d_1', 'svd_u_d_2', 'svd_u_d_3', 'svd_u_d_4', 'svd_u_d_5','svd_u_d_6']] = \
         df final train.destination node.apply(lambda x: svd(x, U)).apply(pd.Series)
         df_final_train[['svd_v_s_1', 'svd_v_s_2', 'svd_v_s_3', 'svd_v_s_4', 'svd_v_s_5', 'svd_v_s_6',]] = 
         df final train.source node.apply(lambda x: svd(x, V.T)).apply(pd.Series)
         df_final_train[['svd_v_d_1', 'svd_v_d_2', 'svd_v_d_3', 'svd_v_d_4', 'svd_v_d_5','svd_v_d_6']] = \
         df_final_train.destination_node.apply(lambda x: svd(x, V.T)).apply(pd.Series)
         df_final_test[['svd_u_s_1', 'svd_u_s_2', 'svd_u_s_3', 'svd_u_s_4', 'svd_u_s_5', 'svd_u_s_6']] = \
         df final test.source node.apply(lambda x: svd(x, U)).apply(pd.Series)
         df final test.destination node.apply(lambda x: svd(x, U)).apply(pd.Series)
         df_final_test[['svd_v_s_1','svd_v_s_2', 'svd_v_s_3', 'svd_v_s_4', 'svd_v_s_5', 'svd_v_s_6',]] = \
         df_final_test.source_node.apply(lambda x: svd(x, V.T)).apply(pd.Series)
         df_final_test[['svd_v_d_1', 'svd_v_d_2', 'svd_v_d_3', 'svd_v_d_4', 'svd_v_d_5','svd_v_d_6']] = \
         df final test.destination node.apply(lambda x: svd(x, V.T)).apply(pd.Series)
         hdf = HDFStore('/content/drive/My Drive/Colab Notebooks/data_facebook/fea_sample/storage_sample_stage4.h5')
         hdf.put('train df',df final train, format='table', data columns=True)
         hdf.put('test df',df final test, format='table', data columns=True)
         hdf.close()
      else:
       print("Already Existed")
```

Already Existed

#### 5.6 Adding New Feature preferential attachment

```
In [0]: #reading from file
    from pandas import read_hdf

df_final_train = read_hdf('/content/drive/My Drive/Colab Notebooks/data_facebook/fea_sample/storage_sample_stage4.h5', 'train_df',mode='r')

df_final_test = read_hdf('/content/drive/My Drive/Colab Notebooks/data_facebook/fea_sample/storage_sample_stage4.h5', 'test_df',mode='r')
```

```
In [0]: #creating new file
with open('/content/drive/My Drive/Colab Notebooks/data_facebook/storage_sample_stage5.h5', 'w') as f:
    f.write('content')
```

```
In [0]: #adding new features

df_final_train['preferential_attachment'] = df_final_train.apply(lambda row:preferential_attachment(row['source_node'],row['destination_node']),axis=1)

df_final_test['preferential_attachment'] = df_final_test.apply(lambda row:preferential_attachment(row['source_node'],row['destination_node']),axis=1)

hdf = HDFStore('/content/drive/My Drive/Colab Notebooks/data_facebook/storage_sample_stage5.h5',mode='w')
hdf.put('train_df',df_final_train, format='table', data_columns=True)
hdf.put('test_df',df_final_test, format='table', data_columns=True)
hdf.close()
```

In [0]: df\_final\_train.head(2)

Out[0]:

	S	source_node	destination_node	indicator_link	jaccard_followers	jaccard_followees	cosine_followers	cosine_followees	num_followers_s	num_followees_s	num_followees_d		svd_v_s_4	svd_v_
C	2	273084	1505602	1	0	0.000000	0.000000	0.000000	6	15	8	:	1.545075e- 13	8.10843 13
1	1 8	332016	1543415	1	0	0.187135	0.028382	0.343828	94	61	142		1.345726e- 02	3.70347 12

2 rows × 55 columns

Adding SVD DOT features (source node \* destination node)

.

```
In [0]: #Appling SVD DOT in source and destination nodes
        df final train['svd u 1 dot'] = df final train['svd u s 1']*(df final train['svd u d 1'])
        df final test['svd u 1 dot'] = df final test['svd u s 1']*(df final test['svd u d 1'])
        df final train['svd v 1 dot'] = df final train['svd v s 1']*(df final train['svd v d 1'])
        df final test['svd v 1 dot'] = df final test['svd v s 1']*(df final test['svd v d 1'])
        df final train['svd u 2 dot'] = df final train['svd u s 2']*(df final train['svd u d 2'])
        df_final_test['svd_u_2_dot'] = df_final_test['svd_u_s_2']*(df_final_test['svd_u_d_2'])
        df final train['svd v 2 dot'] = df final train['svd v s 2']*(df final train['svd v d 2'])
        df_final_test['svd_v_2_dot'] = df_final_test['svd_v_s_2']*(df_final_test['svd_v_d_2'])
        df_final_train['svd_u_3_dot'] = df_final_train['svd_u_s_3']*(df_final_train['svd_u_d_3'])
        df_final_test['svd_u_3_dot'] = df_final_test['svd_u_s_3']*(df_final_test['svd_u_d_3'])
        df_final_train['svd_v_3_dot'] = df_final_train['svd_v_s_3']*(df_final_train['svd_v_d_3'])
        df_final_test['svd_v_3_dot'] = df_final_test['svd_v_s_3']*(df_final_test['svd_v_d_3'])
        df_final_train['svd_u_4_dot'] = df_final_train['svd_u_s_4']*(df_final_train['svd_u_d_4'])
        df final test['svd u 4 dot'] = df final test['svd u s 4']*(df final test['svd u d 4'])
        df_final_train['svd_v_4_dot'] = df_final_train['svd_v_s_4']*(df_final_train['svd_v_d_5'])
        df_final_test['svd_v_4_dot'] = df_final_test['svd_v_s_4']*(df_final_test['svd_v_d_5'])
        df final train['svd u 5 dot'] = df final train['svd u s 5']*(df final train['svd u d 5'])
        df_final_test['svd_u_5_dot'] = df_final_test['svd_u_s_5']*(df_final_test['svd_u_d_5'])
        df_final_train['svd_v_5_dot'] = df_final_train['svd_v_s_5']*(df_final_train['svd_v_d_5'])
        df_final_test['svd_v_5_dot'] = df_final_test['svd_v_s_5']*(df_final_test['svd_v_d_5'])
        df final train['svd u 6 dot'] = df final train['svd u s 6']*(df final train['svd u d 6'])
        df_final_test['svd_u_6_dot'] = df_final_test['svd_u_s_6']*(df_final_test['svd_u_d_6'])
        df final train['svd v 6 dot'] = df final train['svd v s 6']*(df final train['svd v d 6'])
        df_final_test['svd_v_6_dot'] = df_final_test['svd_v_s_6']*(df_final_test['svd_v_d_6'])
        #creating new file
        hdf = HDFStore('/content/drive/My Drive/Colab Notebooks/data facebook/storage sample stage6.h5',mode='w')
        hdf.put('train df',df final train, format='table', data columns=True)
        hdf.put('test_df',df_final_test, format='table', data_columns=True)
```

hdf.close()

```
Out[0]:
            source_node | destination_node | indicator_link | jaccard_followers | jaccard_followees | cosine_followers | cosine_followees | num_followers_s | num_followees_s | num_followees_d
                                                                                                                                                                                              svd_u_2_dot svd
                                                                                                                                                                                              2.490079e-
          0 273084
                           1505602
                                                                             0.000000
                                                                                                0.000000
                                                                                                                  0.000000
                                                                                                                                                      15
                                                                                                                                                                                                            1.835
                                                                                                                                                                                              25
          1 832016
                                                                                                0.028382
                                                                                                                  0.343828
                                                                                                                                    94
                                                                                                                                                      61
                                                                                                                                                                        142
                           1543415
                                                           0
                                                                             0.187135
                                                                                                                                                                                              1.689511e-20 5.429
          2 1325247
                                                                                                                                                                        22
                                                                             0.369565
                                                                                                0.156957
                                                                                                                  0.566038
                                                                                                                                    28
                                                                                                                                                      41
                                                                                                                                                                                              7.011467e-37
                                                                                                                                                                                                           2.092
                           760242
```

11

11

0.000000

0.000000

0.000000

0.000000

0.000000

0.000000

0

5.825985e-

2.728218e-

24

26

1.798

0.000

5 rows × 67 columns

1006992

1708748

In [0]: y\_train = df\_final\_train.indicator\_link

y\_test = df\_final\_test.indicator\_link

**3** | 1368400

**4** 140165

In [0]: df final train.head()

**Implementing Models** 

#### RandomForestClassifier

```
In [0]: #reading
        from pandas import read hdf
        df_final_train = read_hdf('/content/drive/My Drive/Colab Notebooks/data_facebook/storage_sample_stage6.h5', 'train_df',mode='r')
        df_final_test = read_hdf('/content/drive/My Drive/Colab Notebooks/data_facebook/storage_sample_stage6.h5', 'test_df',mode='r')
In [0]: df_final_train.columns
Out[0]: Index(['source_node', 'destination_node', 'indicator_link',
                'jaccard_followers', 'jaccard_followees', 'cosine_followers',
                'cosine_followees', 'num_followers_s', 'num_followees_s',
               'num_followees_d', 'inter_followers', 'inter_followees', 'adar_index',
                'follows_back', 'same_comp', 'shortest_path', 'weight_in', 'weight_out',
                'weight_f1', 'weight_f2', 'weight_f3', 'weight_f4', 'page_rank_s',
                'page_rank_d', 'katz_s', 'katz_d', 'hubs_s', 'hubs_d', 'authorities_s',
                'authorities_d', 'svd_u_s_1', 'svd_u_s_2', 'svd_u_s_3', 'svd_u_s_4',
                'svd_u_s_5', 'svd_u_s_6', 'svd_u_d_1', 'svd_u_d_2', 'svd_u_d_3',
                'svd_u_d_4', 'svd_u_d_5', 'svd_u_d_6', 'svd_v_s_1', 'svd_v_s_2',
                'svd_v_s_3', 'svd_v_s_4', 'svd_v_s_5', 'svd_v_s_6', 'svd_v_d_1',
                'svd_v_d_2', 'svd_v_d_3', 'svd_v_d_4', 'svd_v_d_5', 'svd_v_d_6',
               'preferential_attachment', 'svd_u_1_dot', 'svd_v_1_dot', 'svd_u_2_dot',
                'svd_v_2_dot', 'svd_u_3_dot', 'svd_v_3_dot', 'svd_u_4_dot',
               'svd_v_4_dot', 'svd_u_5_dot', 'svd_v_5_dot', 'svd_u_6_dot',
               'svd_v_6_dot'],
              dtype='object')
```

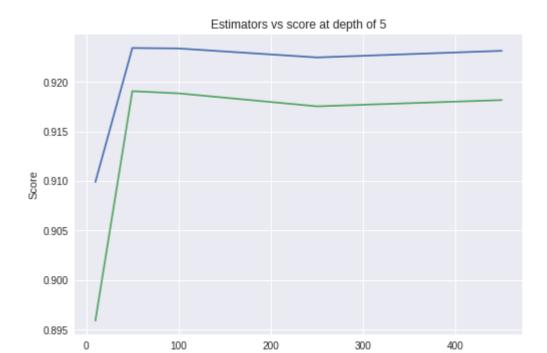
'authorities\_d', 'svd\_u\_s\_1', 'svd\_u\_s\_2', 'svd\_u\_s\_3', 'svd\_u\_s\_4', 'svd\_u\_s\_5', 'svd\_u\_s\_6', 'svd\_u\_d\_1', 'svd\_u\_d\_2', 'svd\_u\_d\_3', 'svd\_u\_d\_4', 'svd\_u\_d\_5', 'svd\_u\_d\_6', 'svd\_v\_s\_1', 'svd\_v\_s\_2', 'svd\_v\_s\_3', 'svd\_v\_s\_4', 'svd\_v\_s\_5', 'svd\_v\_s\_6', 'svd\_v\_d\_1', 'svd\_v\_d\_2', 'svd\_v\_d\_3', 'svd\_v\_d\_4', 'svd\_v\_d\_5', 'svd\_v\_d\_6',

'preferential\_attachment', 'svd\_u\_1\_dot', 'svd\_v\_1\_dot', 'svd\_u\_2\_dot',

'svd\_v\_2\_dot', 'svd\_u\_3\_dot', 'svd\_v\_3\_dot', 'svd\_u\_4\_dot', 'svd\_v\_4\_dot', 'svd\_u\_5\_dot', 'svd\_v\_5\_dot', 'svd\_u\_6\_dot',

'svd\_v\_6\_dot'], dtype='object')

```
In [0]: %%time
                       #estimator wise
                       estimators = [10,50,100,250,450]
                       train scores = []
                       test scores = []
                       for i in estimators:
                                  clf = RandomForestClassifier(bootstrap=True, class_weight=None, criterion='gini', max_depth=5, max_features='auto', max_leaf_nodes=None, min_impurity_decrease=0.0, min_impurity_decrea
                       _split=None,
                                                                                                                 min_samples_leaf=52, min_samples_split=120,min_weight_fraction_leaf=0.0, n_estimators=i, n_jobs=-1,random_state=25,verbose=0,warm_start=False)
                                 clf.fit(df_final_train,y_train)
                                 train_sc = f1_score(y_train,clf.predict(df_final_train))
                                 test_sc = f1_score(y_test,clf.predict(df_final_test))
                                 test_scores.append(test_sc)
                                 train_scores.append(train_sc)
                                 print('Estimators = ',i,'Train Score',train_sc,'test Score',test_sc)
                       #ploting graph
                       plt.plot(estimators,train_scores,label='Train Score')
                       plt.plot(estimators,test_scores,label='Test Score')
                       plt.xlabel('Estimators')
                       plt.ylabel('Score')
                       plt.title('Estimators vs score at depth of 5')
                      Estimators = 10 Train Score 0.9099031396125584 test Score 0.8959235857230405
                       Estimators = 50 Train Score 0.9234163581989668 test Score 0.9190653146060338
```



Estimators

CPU times: user 4min 11s, sys: 859 ms, total: 4min 12s

Wall time: 2min 8s

Estimators = 100 Train Score 0.9233729295633262 test Score 0.9188439889103587 Estimators = 250 Train Score 0.9224650422841834 test Score 0.917535305985205 Estimators = 450 Train Score 0.9231348198325336 test Score 0.918167695343662

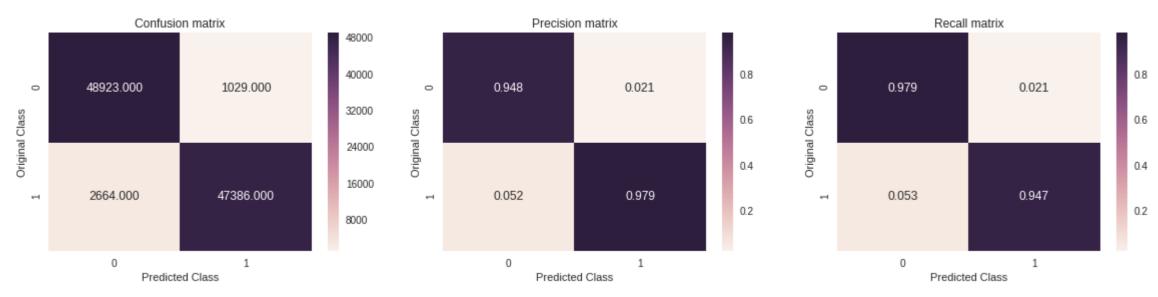
```
In [0]: | %%time
        from sklearn.metrics import f1_score
        from sklearn.ensemble import RandomForestClassifier
        from sklearn.metrics import f1 score
        from sklearn.model selection import RandomizedSearchCV
        from scipy.stats import randint as sp randint
        from scipy.stats import uniform
        param_dist = {"n_estimators":sp_randint(105,125),
                       "max depth": sp randint(10,15),
                       "min_samples_split": sp_randint(110,190),
                       "min_samples_leaf": sp_randint(25,65)}
        clf = RandomForestClassifier(random_state=25,n_jobs=-1)
        rf_random = RandomizedSearchCV(clf, param_distributions=param_dist,n_iter=5,cv=10,scoring='f1',random_state=25)
        rf_random.fit(df_final_train,y_train)
        print('mean test scores',rf_random.cv_results_['mean_test_score'])
        print('mean train scores',rf_random.cv_results_['mean_train_score'])
        mean test scores [0.96141322 0.96087341 0.9596804 0.960717 0.96220727]
        mean train scores [0.96214874 0.96141099 0.95976391 0.96118062 0.96303008]
        CPU times: user 2min 45s, sys: 5.78 s, total: 2min 51s
        Wall time: 20min 12s
In [0]: print(rf_random.best_estimator_)
        RandomForestClassifier(bootstrap=True, class weight=None, criterion='gini',
                    max_depth=14, max_features='auto', max_leaf_nodes=None,
                    min_impurity_decrease=0.0, min_impurity_split=None,
                    min_samples_leaf=28, min_samples_split=111,
                    min_weight_fraction_leaf=0.0, n_estimators=121, n_jobs=-1,
                    oob score=False, random state=25, verbose=0, warm start=False)
In [0]: | %%time
        #fitting and predicting through model
        clf = RandomForestClassifier(bootstrap=True, class_weight=None, criterion='gini',
                    max depth=14, max features='auto', max leaf nodes=None,
                    min_impurity_decrease=0.0, min_impurity_split=None,
                    min_samples_leaf=28, min_samples_split=111,
                    min weight fraction leaf=0.0, n estimators=121, n jobs=-1,
                    oob_score=False, random_state=25, verbose=0, warm_start=False)
        clf.fit(df_final_train,y_train)
        y_train_pred = clf.predict(df_final_train)
        y test pred = clf.predict(df final test)
        CPU times: user 54.8 s, sys: 193 ms, total: 55 s
```

Wall time: 28 s

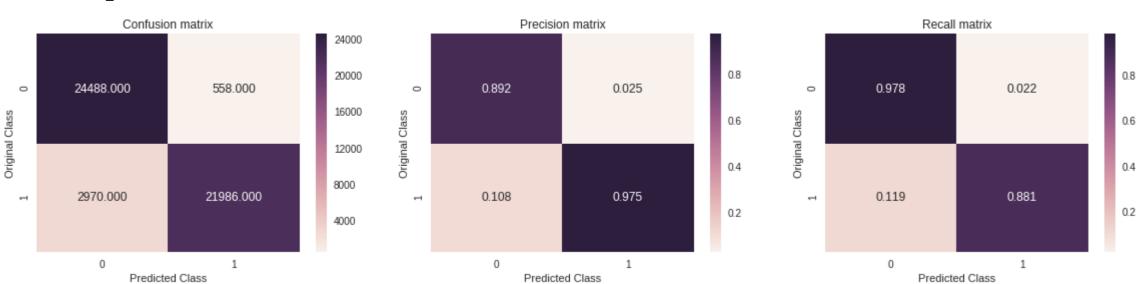
```
In [0]: from sklearn.metrics import confusion_matrix
        def plot_confusion_matrix(test_y, predict_y):
            C = confusion_matrix(test_y, predict_y)
            A = (((C.T)/(C.sum(axis=1))).T)
            B = (C/C.sum(axis=0))
            plt.figure(figsize=(20,4))
            labels = [0,1]
            # representing A in heatmap format
            plt.subplot(1, 3, 1)
            sns.heatmap(C, annot=True, fmt=".3f", xticklabels=labels, yticklabels=labels)
            plt.xlabel('Predicted Class')
            plt.ylabel('Original Class')
            plt.title("Confusion matrix")
            plt.subplot(1, 3, 2)
            sns.heatmap(B, annot=True, fmt=".3f", xticklabels=labels, yticklabels=labels)
            plt.xlabel('Predicted Class')
            plt.ylabel('Original Class')
            plt.title("Precision matrix")
            plt.subplot(1, 3, 3)
            # representing B in heatmap format
            sns.heatmap(A, annot=True, fmt=".3f", xticklabels=labels, yticklabels=labels)
            plt.xlabel('Predicted Class')
            plt.ylabel('Original Class')
            plt.title("Recall matrix")
            plt.show()
```

In [0]: print('Train confusion\_matrix')
 plot\_confusion\_matrix(y\_train,y\_train\_pred)
 print('Test confusion\_matrix')
 plot\_confusion\_matrix(y\_test,y\_test\_pred)

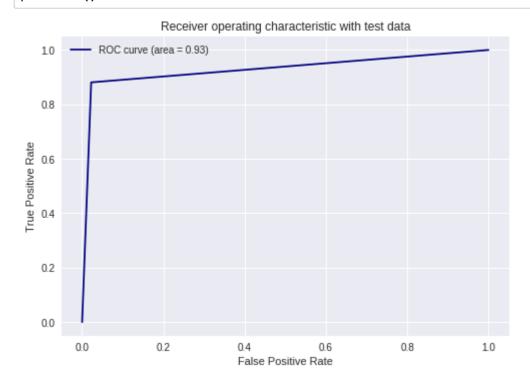
Train confusion\_matrix



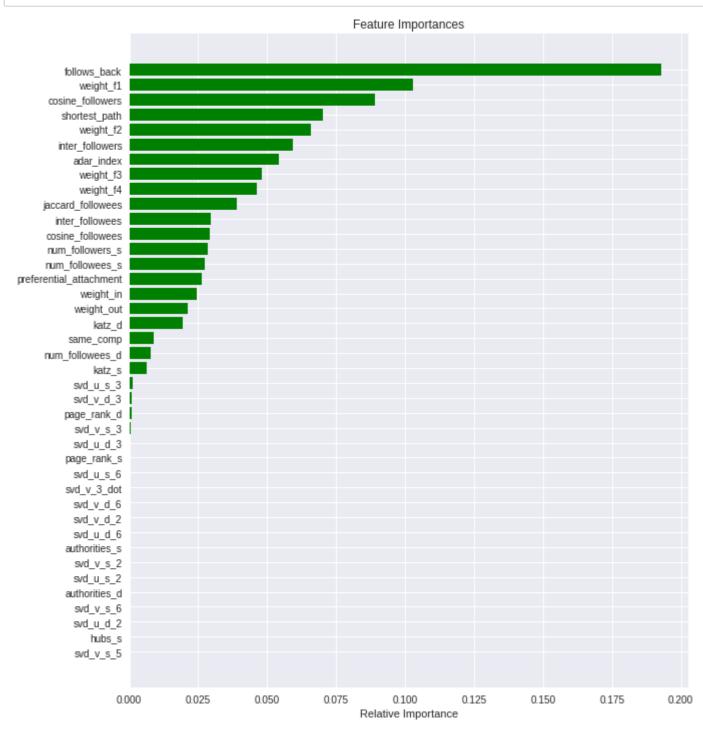
## Test confusion\_matrix



In [0]: from sklearn.metrics import roc\_curve, auc
 fpr,tpr,ths = roc\_curve(y\_test,y\_test\_pred)
 auc\_sc = auc(fpr, tpr)
 plt.plot(fpr, tpr, color='navy',label='ROC curve (area = %0.2f)' % auc\_sc)
 plt.xlabel('False Positive Rate')
 plt.ylabel('True Positive Rate')
 plt.title('Receiver operating characteristic with test data')
 plt.legend()
 plt.show()



```
In [0]: features = df_final_train.columns
    importances = clf.feature_importances_
    indices = (np.argsort(importances))[-40:]
    plt.figure(figsize=(10,12))
    plt.title('Feature Importances')
    plt.barh(range(len(indices)), importances[indices], color='g', align='center')
    plt.yticks(range(len(indices)), [features[i] for i in indices])
    plt.xlabel('Relative Importance')
    plt.show()
```

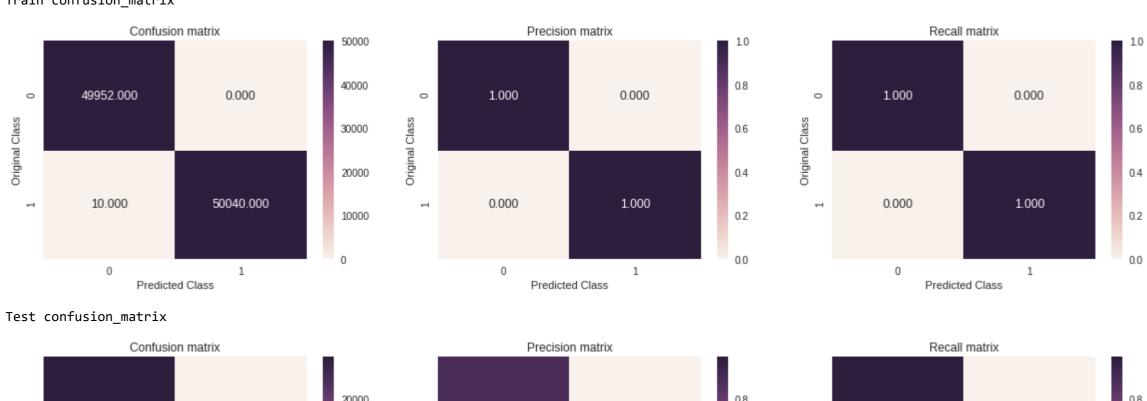


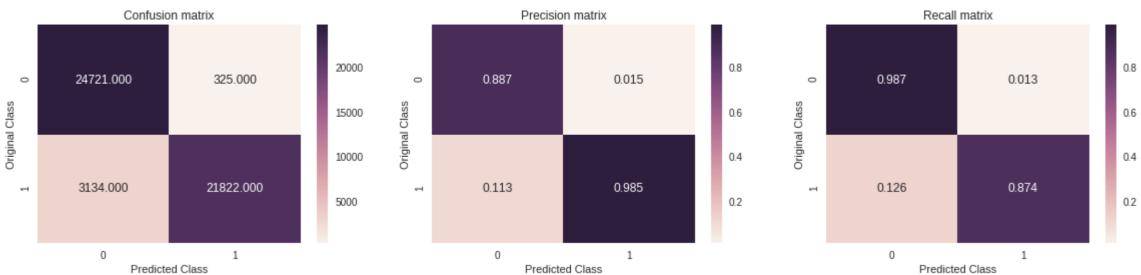
```
In [0]: #reading
        from pandas import read_hdf
        df_final_train = read_hdf('/content/drive/My Drive/Colab Notebooks/data_facebook/storage_sample_stage6.h5', 'train_df',mode='r')
        df final test = read hdf('/content/drive/My Drive/Colab Notebooks/data facebook/storage sample stage6.h5', 'test df',mode='r')
In [0]: df_final_train.columns
Out[0]: Index(['source_node', 'destination_node', 'indicator_link',
                'jaccard followers', 'jaccard followees', 'cosine followers',
                'cosine_followees', 'num_followers_s', 'num_followees_s',
                'num_followees_d', 'inter_followers', 'inter_followees', 'adar_index',
                'follows_back', 'same_comp', 'shortest_path', 'weight_in', 'weight_out',
                'weight_f1', 'weight_f2', 'weight_f3', 'weight_f4', 'page_rank_s',
                'page_rank_d', 'katz_s', 'katz_d', 'hubs_s', 'hubs_d', 'authorities_s',
                'authorities_d', 'svd_u_s_1', 'svd_u_s_2', 'svd_u_s_3', 'svd_u_s_4',
                'svd_u_s_5', 'svd_u_s_6', 'svd_u_d_1', 'svd_u_d_2', 'svd_u_d_3',
                'svd_u_d_4', 'svd_u_d_5', 'svd_u_d_6', 'svd_v_s_1', 'svd_v_s_2',
                'svd_v_s_3', 'svd_v_s_4', 'svd_v_s_5', 'svd_v_s_6', 'svd_v_d_1',
                'svd_v_d_2', 'svd_v_d_3', 'svd_v_d_4', 'svd_v_d_5', 'svd_v_d_6',
               'preferential_attachment', 'svd_u_1_dot', 'svd_v_1_dot', 'svd_u_2_dot',
                'svd_v_2_dot', 'svd_u_3_dot', 'svd_v_3_dot', 'svd_u_4_dot',
               'svd_v_4_dot', 'svd_u_5_dot', 'svd_v_5_dot', 'svd_u_6_dot',
                'svd_v_6_dot'],
               dtype='object')
In [0]: y_train = df_final_train.indicator_link
        y_test = df_final_test.indicator_link
In [0]: #droping source code, destination code and indicator link
        df_final_train.drop(['source_node', 'destination_node', 'indicator_link'],axis=1,inplace=True)
        df_final_test.drop(['source_node', 'destination_node', 'indicator_link'],axis=1,inplace=True)
In [0]: | %%time
        from sklearn.metrics import f1_score
        from sklearn.metrics import f1_score
        from sklearn.model_selection import RandomizedSearchCV
        from scipy.stats import randint as sp_randint
        from scipy.stats import uniform
        param_dist = {"n_estimators":sp_randint(105,125),
                       "max_depth": sp_randint(10,15)}
        xgb_clf= xgb.XGBClassifier(random_state=25,n_jobs=-1)
        rf_random = RandomizedSearchCV(xgb_clf, param_distributions=param_dist,n_iter=5,cv=10,scoring='f1',random_state=25)
        rf_random.fit(df_final_train,y_train)
        print('mean test scores',rf_random.cv_results_['mean_test_score'])
        print('mean train scores',rf_random.cv_results_['mean_train_score'])
        mean test scores [0.98029406 0.98025694 0.97989429 0.98006164 0.98012339]
        mean train scores [0.99994339 0.99997558 0.99286112 0.99557341 0.99591635]
        CPU times: user 1h 40min 48s, sys: 2.86 s, total: 1h 40min 51s
```

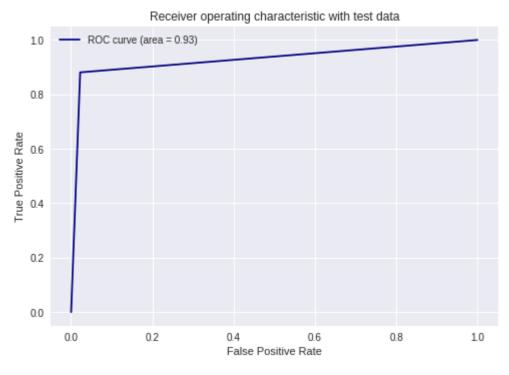
Wall time: 1h 40min 52s

In [0]: #confusion matrix
 print('Train confusion\_matrix')
 plot\_confusion\_matrix(y\_train,y\_train\_pred)
 print('Test confusion\_matrix')
 plot\_confusion\_matrix(y\_test,y\_test\_pred)

Train confusion\_matrix

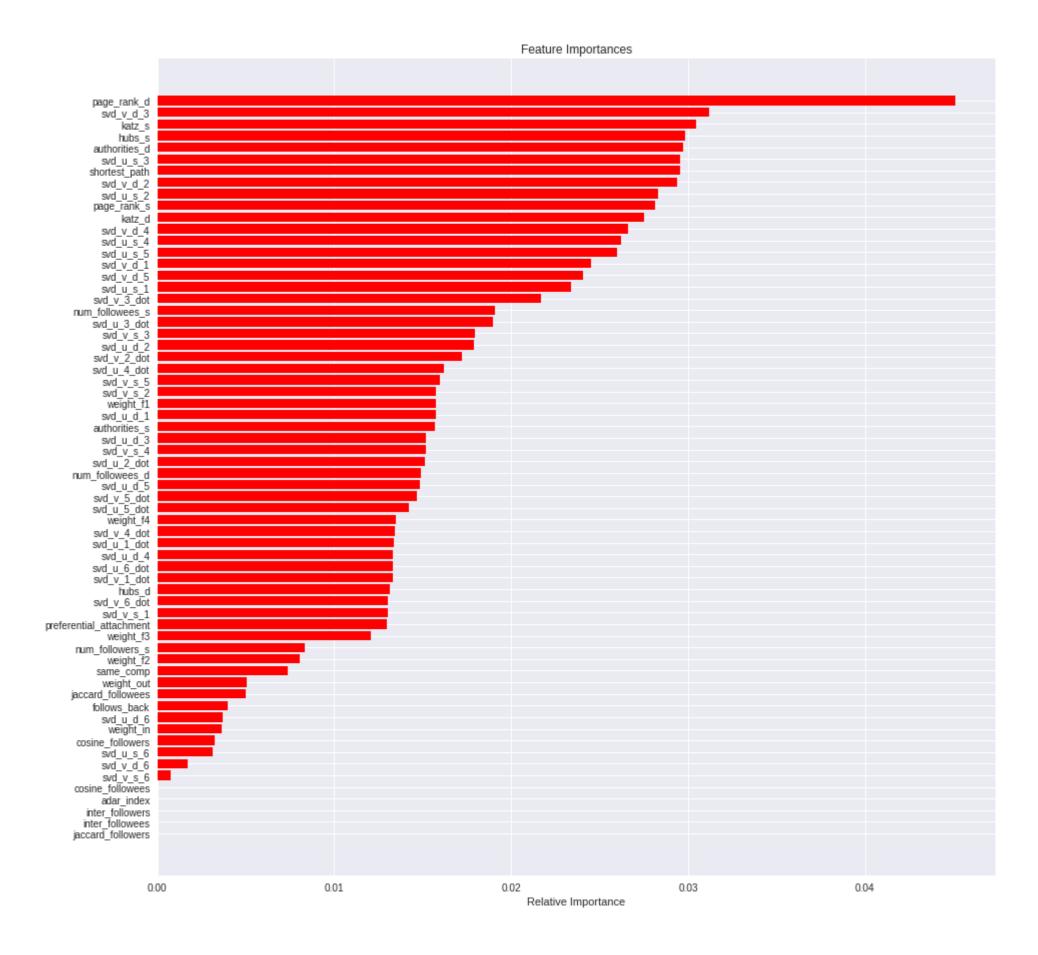






## Feature importance

```
In [0]: #Feature importance
    features = df_final_train.columns
    importances = xgb_clf.feature_importances_
    indices = (np.argsort(importances))[-70:]
    plt.figure(figsize=(15,15))
    plt.title('Feature Importances')
    plt.barh(range(len(indices)), importances[indices], color='r', align='center')
    plt.yticks(range(len(indices)), [features[i] for i in indices])
    plt.xlabel('Relative Importance')
    plt.show()
```



## Conclution

Sno	+   Model +	Scoring	Accuracy	Precision	Recall	F1-Score
1.	Random Forest XG Boost	f1 f1	92.94% 93.08%	97.52% 98.53%	88.09% 87.44%	92.57%   92.65%

1. XG Boost shows best performance.
2. We have added Preferential Attachn

2. We have added Preferential Attachment feature, it shows great result in linking nodes.

3. SVD DOT features also played good role we can see in feature importance graph.

Steps for solving this approch:

1. Fislty we must perform finest EDA on raw data, so that we could get simple or filtered data for processing.

2. After EDA we should perform all basics algos related to graph theory and pridictions. like we have used

```
a)Follow back well scroedb)Cosine followers also well.c)SVD is also perform welld)Shortest path. etc etc
```

- 3. After going through all basics algo test them in best classifier like Random forest or Xgboost, we have done both random forest and xgboost where xgboost stood best.
- 4. After modeling it will give feature importance by which we came to know which algo is best and worst.

```
So on random forest(best algo):

a) follow back

b) weight

c) Shortest path

d) cosine followers

So on Xgboost(best algo):

a)Page rank

b)SVD

c)Katz

d)Hits Score
```

5. At the end i will conclude XgBoost gives best results for this type of approch.