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O If then & o(g,(n) and t_2(n) & (g_2(n)), then t_1(n)+t_2(n) & o (maxdg,(n); g_2(n) y). Prove that assertions.

We need to show that $t_i(n) + t_i(n) \in O(\max_i (g_i(n); g_i(n)))$.
This means there exists a positive constant cand no such that $t_i(n) + t_i(n) \le C$.

ticn) < cigicn), for all nzn.

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let no=max (ni,nig for all nzno.

consider $t_1(n)+t_2(n)$ for all $n \ge n_0$ $t_1(n)+t_2(n) \le c_1g_1(n)+c_2g_2(n)$

we need to relate $g_i(n)$ and $g_i(n)$ to $\max dg_i(n); g_i(n) y$: $g_i(n) \leq \max dg_i(n); g_i(n) y \text{ and}$

9, cn) < max (9, cn); 9, cn) 4

Thus,

c,9,(n) ≤ c, max (9,(n); 9, (n) y c,9,(n) ≤ c, max (9,(n); 9, (n) y

(19,(n) + (19,(n) & c, max (9,(n); 9,(n)) + (1, max (9,(n); 9,(n)))

cig(n) + cig2(n) < (ci+ci) mand g(n); g2(n) 4

E((n)+ +2(n) = (c+c2) max (9,(n); 92 cn) y for all n zno

By the defination of Big-O Notation

E(n) + t2(n) E0(max (g, (n); g, (n) y, then

6,(n)+ 6,(n) €0 (max (g,(n); g,(n))

Thus, the assertion is proved.

Find the time complexity of the recurrence equation.

Let us consider such that the recurrence for merge

Sort .

 $T(n) = \lambda T(n/\lambda) + n$

By using the master's theorem

 $T(n) = \alpha T(\gamma_b) + f(n)$

where, azi; bzi and fini is a positive constant function.

Ex: T(n) = 2T(n/2) +n

a=2; b=2; f(n)=0

By comparing of f(n) with n'096

1096 = 1092 =1

compare f(n) with n 109 b.

6(0) ((()) = n

n 1096 = n'=n

 $*f(n) = O(n^{1096})$, then $t(n) = O(n^{1096} \log n)$

In our case:

1096 = 1

 $T(n) = O(n'\log n) = O(n\log n)$

Then time complexity of the recurrence relation

is TCn) = 2T (N2) +n is O(nlogn).

 $T(n) = \int dT (n/2) + 1$ if n > 1otherwise By applying of master's theorem T(n)=aT(n/b)+f(n) where az1 621 TCn)=27 (1/2)+1 Here a=a; b=a; f(n)=1 By comparision of f(n) and nings if f(n) = O(nc) where c < log b, then T(n) = O(nlogb) if f(n) = 0 (n'09b), then T(n) = 0 (n'09b 109n) if f(n) = 12 (nc), where c>109 & then T(n)=0(f(n)) Let us calculate 109,a: 1096a = 109, =1 f(n) = 1 n'egg = n'= n' audorat monthe f(n)= O(nc) with c = log a (case 1) in this case c=0 and log q =1 C<1,50 T(n) = D(n'096) = 0 (n') = 0(n)

.. The time complexity of recurrence relation is T(n) = 2T(n/s) + 1 is O(n).

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T(n) = d 2T(n-1) if n>0

Otherwise
  Here,
       where n=0
       T(0) = 1
   recurrance relation analysis
       for nou!
     T(n) = 2T(n-1)
     T(n)=2T(n-1)
     T(n-1)= 27(n-2)
     T(n-2)=2T(n-3)
 T(1)= 27(0)
                  ) (ar and (100 a) ( - (a)) 1
   From this above pattern
   T(n) = 2 \cdot 2 \cdot 2 \cdot \dots \cdot 2 \cdot T(0) = 2^n \cdot T(0)
 Since,
      T(0) = 1; we have
          T(n) = 20
   .: The recurrance relation is
         T(n)= 2T(n-1) for n>0 and T(0)=1 is
              T(n) = 2n.
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3) Big-O-Notation show that f(n) = na+3n+5 is 0(n2).

f(n)=O(g(n)) means c>o and no 20 f(n) < c.g(n) for all n 2no

Given,

f(n) = n + 3n + 5

c>0, no zo such that f(n) < c.n2

f(n)=n+3n+5

lets

choose c=2

f(n) < 2. n2

f(n) = n2+3n+5 4 n2+3n2+5n2

=902

so, c=9; no=1; f(n) <9n2 for all n21

f(n) = n2+3n+5 is O(n2).