

## Assessment\_1 - One Neuron -Tech Neuron- Statistics Assessments

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1. Two unbiased dice are thrown. Find the probability that
- Both dice show same number
  - First die show 6
  - Total number on dice is 8
  - Total number on dice is  $>8$
  - Total number on dice is 13 and total number on dice is between 2 to 12 both inclusive

Sol:

- Both dice show same number  
 $= 1/6$
- First die show 6  
 $= 1/6$
- Total number on dice is 8  
 $= 5/36$
- Total number on dice is  $>8$   
 $= 5/18$
- Total number on dice is 13 and total number on dice is between 2 to 12 both inclusive  
Total number on dice 13 is  $= 0$   
total number on dice is between 2 to 12 both inclusive  $= 1$

2. Four cards are drawn at random from a pack of 52. Find the probability that
- They are king, queen jack and ace
  - Two kings and two queens
  - Two black or two red
  - Two hearts or two diamonds

Sol :

a.They are king, queen jack and ace  
$$P = \frac{4C1 \cdot 4C1 \cdot 4C1 \cdot 4C1}{52C4} = 0.000945$$

- b.Two kings and two queens

$$P = \frac{4C2 \cdot 4C2}{52C4} = 0.00013$$

- c.Two black or two red

$$P = \frac{26C2 \cdot 26C2}{52C4} = 0.394$$

- d.Two hearts or two diamonds

$$P = \frac{13C2 \cdot 13C2}{52C4} = 0.0224$$

3. An urn contains 6 white, 4 red, 9 black balls. If 3 balls are drawn at random find the probability of
- 2 are white
  - One of each colour
  - None is red
  - At Least 1 is white

Sol:

3 Balls are drawn

19 balls total

Number of ways at 3 balls can be drawn is  ${}^{19}C_3 = 969$

- 2 are white =  ${}^6C_2 \times {}^{13}C_1 = 195$ , so  
Probability =  $195/969$
- One of each colour  
 ${}^6C_1 \times {}^4C_1 \times {}^9C_1 = 216$   
Probability =  $216/969$
- None is red =  
 ${}^{15}C_3 = 455$   
Probability =  $455/969 = 65/323$
- At Least 1 is white=  
Non white balls can draw  ${}^{13}C_3 = 286$   
Probability for none of 3 balls white is =  $286/969 = 65/323$

So

Probability that at least one for three balls drawn is white is =  $1 - 286/969$   
 $= 686/969$

4. The odds against manager X settling the wage dispute with the workers are 8:6 and odds in favour of manager Y settling the same dispute are 14:16
- Chance that neither will settle the dispute if they try independently
  - What is the probability that the dispute will be settled?

Sol:

The probability that it is dispute not settled by manager X is =  $8/14$

The probability that it is dispute settled by manager X is =  $1 - 8/14 = 6/14$

The probability that it is dispute not settled by manager Y is =  $14/30$

The probability that it is dispute settled by manager Y is =  $1 - 14/30 = 6/30$

a. Chance that neither will settle the dispute if they try independently

$$\begin{aligned} &\text{Probability settling disputes if they try independently} \\ &= 6/14 \times 8/14 + 6/30 \times 14/30 + 6/14 \times 6/30 \\ &= 48/196 + 84/900 + 36/900 \end{aligned}$$

b. what is the probability that the dispute will be settled?

$$6/14 \times 6/30 = 36/420$$

5. The odds that person X speaking truth are 3:2 and the odds of the person Y speaks truth are 5:3. In what percentage of the cases are they likely to contradict each other?

Sol:

A : 3 : 2 means that in 5 situation,  
A told the True 3 times; as a fraction  $3/5$ ;  
A told the lies in  $(5 - 3)/5 = 2/5$ ,

B : 5 : 3 means that  $5 + 3 = 8$  situation,  
B told the True; in 5 out of 8.  
As a fraction  $5/8$  and  
B told lies in 3 out of 8 situations.  
As a fraction  $3/8$

Both contradict each other when A told the True and B lied.  
 $= 3/5 \times 3/8 = 9/40 = 22.5\%$

Or A lied and B told the True. As fractions:  $2/5 \times 5/8 = 10/40 = 25\%$

Probability of Contradiction:  $22.5 + 25 = 47.5\%$ :

6. A problem in statistics is given to three students A, B and C whose chances of solving it are  $\frac{1}{2}$ ,  $\frac{3}{4}$  and  $\frac{1}{4}$ , respectively. What is the probability that the problem will be solved if all of them try independently.

Sol:

$$A = 1/2$$

$$B = 3/4$$

$$C = 1/4$$

$$\begin{aligned} &\text{Probability that the problem will be solved if all of them try independently} = \\ &P(A \cup B \cup C) = P(A) + P(B) + P(C) - P(A \cap B) - P(A \cap C) - P(B \cap C) + P(A \cap B \cap C) \\ &= 1/2 + 3/4 + 1/4 - 1/2 \times 3/4 - 3/4 \times 1/4 - 1/2 \times 1/4 - 1/2 \times 3/4 \times 1/4 \end{aligned}$$

7. In a certain town there are equal numbers of male and female residents. It is known that 5% and 20% are unemployed. If any unemployed person is picked up at random, what is the probability that:

a. It is a female

b. It is a male

**Sol:** Males = 5%

Female = 20%

$E_1$  = Person being male  $P(E_1) = \frac{1}{2}$

$E_2$  = Person being female  $P(E_2) = \frac{1}{2}$

$P(E/E_1) = 5\% = 0.05$

$P(E/E_2) = 20\% = 0.2$

$P(E_2/E) \text{ female} = P(E) \times P(E/E_2) / \sum P(E_2) \times P(E/E_i)$

$P(E) \times P(E/E_2) = P(E_1) \times P(E/E_1) + P(E_2) \times P(E/E_2)$   
 $= P(E) = \frac{1}{2} \times 0.05 + \frac{1}{2} \times 0.2 = 0.125$

$P(E_2/E) \text{ female} = \frac{1}{2} \times 0.2 / 0.125 = \frac{4}{5} = 0.8$

$P(E_2/E) \text{ male} = \frac{1}{2} \times 0.05 / 0.125 = 0.025 / 0.125 = 0.2$