

Assessment 2 - One Neuron -Tech Neuron- Statistics Assessments

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1. An urn contains 4 tickets numbered 1, 2, 3, 4 and another contains 6 tickets numbered 2, 6, 7, 8, 9. If one of the two urns is chosen at random and a ticket is drawn at random from a chosen urn, find the probabilities that the ticket drawn bears

- a. 2 or 4
- b. 3
- c. 1 or 9

Sol:

Let's

consider Bag A contains = 4 tickets

consider Bag B contains = 6 tickets

Probability of choosing the Bag = $\frac{1}{2}$

- a. The probabilities that the ticket drawn 2 or 4 = $\frac{1}{2} [1/4 + 1/6] = 10/48 = 5/24$
- b. The probabilities that the ticket drawn 3 is = $\frac{1}{2} [1/4 + 0] = 1/8$
- c. The probabilities that the ticket drawn 1 or 9 = $\frac{1}{2} [1/4 + 1/6] = 10/48 = 5/24$

2. A box contains 6 red, 4 white and 5 black balls. A person draws 4 balls at random from the box at random. Find the probability that among the balls drawn there is at least one ball of each colour.

Sol :

② Let
A = at least one of the ball of each color
 \bar{A} = Red, White, Black
 $P(\bar{A})$ = total possible outcomes
 $P(A) = 1 - P(\bar{A})$
total possibility = ${}^{15}C_4$
 $P(\bar{A}) = \frac{{}^9C_4 + {}^{10}C_4 + {}^{11}C_4}{{}^{15}C_4}$
 $P(A) = 1 - P(\bar{A}) = 1 - \frac{{}^9C_4 + {}^{10}C_4 + {}^{11}C_4}{{}^{15}C_4}$

Prob at least one ball of each color

3. The odds that a book on statistics will be favourably reviewed by 3 independent critics are 3 to 2, 4 to 3 and 2 to 3 respectively. What is the probabilities that the reviews:

- All will be favourable
- Majority of the reviews will be favourable
- Exactly one review will be favourable
- Exactly two reviews will be favourable
- At Least one of the reviews will be favourable

Sol :

③ Let P_1, P_2, P_3 prob of favorable reviews

Let $\bar{P}_1, \bar{P}_2, \bar{P}_3$ " " non "

Three critics are $3 \rightarrow 2, 4 \rightarrow 3, 2 \rightarrow 3$

$$P_1 = \frac{3}{5} ; \bar{P}_1 = \frac{2}{5}$$

$$P_2 = \frac{4}{7} ; \bar{P}_2 = \frac{3}{7}$$

$$P_3 = \frac{2}{5} ; \bar{P}_3 = \frac{3}{5}$$

④ Prob of all favorable = $P_1 \times P_2 \times P_3$

$$= \frac{3}{5} \times \frac{4}{7} \times \frac{2}{5} = \frac{24}{175}$$

⑤ at least two favorable =

$$P(P_1, P_2, \bar{P}_3) + P(P_1, P_3, \bar{P}_2) + P(P_2, P_3, \bar{P}_1)$$

$$= \left(\frac{3}{5} \times \frac{4}{7} \times \frac{3}{5} \right) + \frac{3}{5} \times \frac{2}{5} \times \frac{3}{7} + \left(\frac{4}{7} \times \frac{2}{5} \times \frac{3}{5} \right)$$

⑥ at least one favorable =

$$= P(P_1, \bar{P}_2, \bar{P}_3) + P(P_2, \bar{P}_1, \bar{P}_3) + P(P_3, \bar{P}_1, \bar{P}_2)$$

$$= \left(\frac{3}{5} \times \frac{3}{7} \times \frac{3}{5} \right) + \frac{4}{7} \times \frac{2}{5} \times \frac{3}{5} + \left(\frac{2}{5} \times \frac{2}{7} \times \frac{3}{5} \right)$$

⑦ Majority =

$$P(P_1, P_2, \bar{P}_3) + P(P_2, P_3, \bar{P}_1) + P(P_1, P_3, \bar{P}_2) + P(P_1, P_2, P_3)$$

$$= \left(\frac{3}{5} \times \frac{4}{7} \times \frac{3}{5} \right) + \frac{3}{5} \times \frac{2}{5} \times \frac{3}{7} + \left(\frac{4}{7} \times \frac{2}{5} \times \frac{3}{5} \right) + \frac{3}{5} \times \frac{4}{7} \times \frac{2}{5}$$