

## MODULE - A

### SLABS

one way slab:-

$$\left[ \frac{L_y}{L_x} > 2 \right]$$

1. Simply supported
2. Continuous
3. Cantilever

two way slab

$$\left[ \frac{L_y}{L_x} \leq 2 \right]$$

main steel

This is the type of reinforcement which is provided to resist bending moment.

The diameters of the bar usually provided are 8mm, 10mm & 12mm.

Usually main steel is provided in the shorter span.

The clear cover for the main steel is 20mm  
The spacing provided is maximum 3 times the dia of bars (or) 300mm

### Distribution Steel

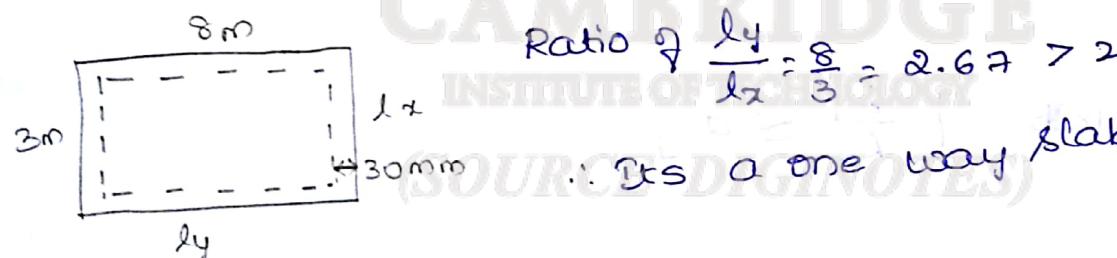
This Steel is provided to prevent surface cracks which is caused due to temperature Expansion + Contraction. It is also used to hold the main bar in one position.

Area of distribution steel should always be 0.12% of the gross area.

Maximum Spacing of distribution steel should be 5 times the dia of bars (or) 450mm

Usually 8mm dia bars are provided for distribution steel.

1. Design a slab for the room dimension 8m x 3m simply supported on 230mm thick wall. The live load on the slab is 2kN/m<sup>2</sup> & floor finishing 0.5kN/m<sup>2</sup> use M<sub>20</sub> & Fe 415. [only 20 grade for a slab].



### Step ②: Load calculation

Take  $\frac{l}{d} = 20 \times MF$  [length should always be shorter span.]

$$\frac{3000}{d} = d$$

$$20 \times 1.85$$

$$d = 120\text{mm}$$

Overall depth effective cover  $D = 20\text{mm} + \left(\frac{10}{2}\right) = 25\text{mm}$  D<sub>90</sub> 9 bars.

overall depth  $D = 120 + 25 = 145\text{mm}$

$b = 1\text{m} = 1000\text{mm}$  — Assumption.

$$DL = 1 \times 0.145 \times 25$$

$$DL = 3.625 \text{ kN/m}$$

$$FF = 0.5 \times 1 = 0.5 \text{ kN/m}$$

$$L = 2 \times 1 \rightarrow 2 \text{ kN/m}$$

$$\text{Total load } w = 6.125 \text{ kN/m}$$

$$w_u = 9.187 \text{ kN/m}$$

$$\text{Effective span [le]} = 3 + 0.23 = 3.23$$

$$le = 3 + \frac{0.145}{0.145} = 3.187$$

$$\text{Taking least } le = 3.187 \text{ m}$$

$$M_u = \frac{w_u le^2}{8} = \frac{9.187 \times (3.12)^2}{8} = 11.17 \text{ kN-m}$$

$$V_u = \frac{w_u le}{2} = 14.33 \text{ kN}$$

Check for depth.

$$M_u = 0.36 \frac{f_y b d}{d} \left[ 1 - 0.42 \frac{x_{u \max}}{d} \right] f_{ck} b d^2$$

$$11.17 \times 10^6 = 0.36 \times 0.48 \left[ 1 - 0.42 \times 0.48 \right] \times 20 \times 1000 \times d^2$$

$$d = 63.62 \text{ mm} \quad d \text{ is less than effective depth}$$

∴ d is safe

$$M_u = 0.87 f_y A_{st} d \left[ 1 - \frac{A_{st} f_y}{f_{ck} b d} \right]$$

$$11.17 \times 10^6 = 0.87 \times 115 \times A_{st} \times 120 \left[ 1 - \frac{A_{st} \times 415}{20 \times 1000 \times 120} \right]$$

$$11.17 \times 10^6 = 433.26 A_{st} - 1.49 A_{st}^2 \quad A_{st} = 270.45 \text{ mm}^2$$

$$\text{Spacing } \# = 10\text{ mm} ; \quad \frac{\text{Area of 1 bar}}{\text{Ast}} \times 1000$$

$$= \frac{\pi (10)^2}{4} \times 1000$$

$$\text{Ast}$$

$$= 290.4 \text{ mm}$$

Provide 10φ @ 290 mm c/c.

### Area of distribution bars

$$\text{Area} = 0.12\% \times B D$$

$$= \frac{0.12}{100} \times 1000 \times 145$$

A = 174 mm<sup>2</sup>

$$\text{Provide Spacing} = \frac{\pi (8)^2}{\frac{4}{174}} \times 1000 = 288.3 \text{ mm}$$

Provide 8φ bars @ 288 mm c/c

### Check for Shear

$$\tau_v = \frac{V_u}{bd} = \frac{14.33 \times 10^3}{1000 \times 120} = 0.119 \text{ kN/mm}^2$$

$$\tau_c = \frac{100 \text{ Ast}}{bd} = \frac{100 \times 290.45}{1000 \times 120} = 0.22$$

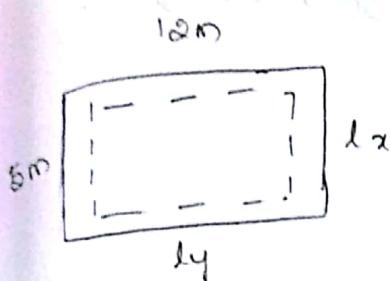
$$\tau_c = 0.336 \text{ N/mm}^2$$

only for slabs

If  $\tau_c > \tau_v$ , shear design is safe

Note: If  $\tau_v > \tau_c$ , increase the depth (solve from first)

② Design a slab for an internal room dimension 12m x 15m by using M20 & Fe415 which carries a live load of 0.25 kN/m<sup>2</sup>. & Simply supported on 200mm thick wall.



$$\frac{L_y}{d} = \frac{12}{4} = 3 > 2$$

∴ It's one way slab

### Step ② Load calculation

$$\text{Take } \frac{l}{d} = 20 \times \text{M.F}$$

$$\frac{5000}{20 \times 1.25} = d$$

$$d = 200 \text{ mm} \quad \text{= Effective depth.}$$

$$\text{Effective Cover } d' = 20 \text{ mm} + \frac{10}{2} = 25 \text{ mm}$$

$$\text{Overall depth } D = 200 + 25 = 225 \text{ mm}$$

$$b = 1 \text{ m} = 1000 \text{ mm}$$

$$DL = 1 \times 0.225 \times 25 = 5.625 \text{ kN/m}$$

$$FF = 0.5 \times 1 = 0.5 \text{ kN/m}$$

$$LK = 0.225 \times 1 = 0.225 \text{ kN/m}$$

$$\text{Total load } w = 8.375 \text{ kN/m}$$

$$w_u = 12.56 \text{ kN/m}$$

$$\text{Effective Span } [l_e] = 5 + 0.23 = 5.23$$

$$l_e = 5 + 0.125 = 5.125$$

Taking least 5.2 m

$$M_u = \frac{w_u l_e^2}{8} = \frac{12.56 \times (5.2)^2}{8} = 40.45 \text{ kN-m}$$

$$V_u = \frac{w_u l_e}{2} = \frac{12.56 \times 5.2}{2} = 32.16 \text{ kN}$$

Check for depth

$$M_u = 0.36 \frac{x_{u\max}}{d} \left[ 1 - 0.42 \frac{x_{u\max}}{d} \right] f_{ck} b d^2$$

$$42.45 \times 10^6 = 0.36 \frac{10.098}{d} \left[ 1 - 0.42 \times 0.48 \right] 200 \times 1000 \times d^2$$

$$d = 124.03 \text{ mm}$$

$$M_u = 0.87 f_y A_{st} d \left[ 1 - \frac{f_y A_{st}}{bd f_{ck}} \right]$$

$$42.45 \times 10^6 = 0.87 \times 415 \times A_{st} \times 200 \left[ 1 - \frac{415 A_{st}}{1000 \times 200 \times 20} \right]$$

$$42.45 \times 10^6 = f_{2210} A_{st} \left[ 1 - 1.0375 \times 10^{-4} A_{st} \right]$$

$$42.45 \times 10^6 = f_{2210} A_{st} - 1.49 A_{st}^2$$

$$A_{st} = 628.89 \text{ mm}^2$$

$$\text{Spacing} \# 10 \text{ mm} @ 120 \text{ mm c/c} = \frac{\pi(10)^2}{4} \times 1000 \\ = 184.88 \text{ mm}$$

Provide 10φ @ 120 mm c/c

Area of distribution bar

$$A = 0.12\% \times B \times D$$

$$= \frac{0.12}{100} \times 1000 \times 225$$

$$A = 270 \text{ mm}^2$$

$$\text{provide spacing} = \frac{\pi(8)^2 + C}{\frac{4}{270}} \times 1000 = 186.16 \text{ mm}$$

Provide 8φ bars @ 180 mm

### check for shear

$$\tau_v = \frac{v_u}{bd} = \frac{8.164 \times 10^3}{1000 \times 200} = 0.040 \text{ kN/mm}^2$$

$$\tau_c = \frac{100 A_{st}}{bd} = \frac{100 \times 628.89}{1000 \times 200} = 0.314$$

$$\tau_c = 0.38 \text{ N/mm}^2$$

$\tau_c > \tau_v$  shear design is safe

$$0.5 \rightarrow 0.48$$

$$0.3 \rightarrow ,$$

$$0.25 \rightarrow 0.32$$

$$0.38$$

3. In an elevated highway bridge the slab span bw 2 columns is 21m & It is a 2 lane highway along with extra widening of 2.5m. The concrete used is 25 MPa with Fe500 Steel. If there is a single truck of 4 kN/m<sup>2</sup>. Design the slab.

$$\frac{l}{d} = 20 \times MF \quad \text{per lane} = 3.45 \text{ m}$$

$$d = \frac{9400}{20 \times 10^{25}} = 376 \text{ mm} \quad \text{2 lane} = 3.45 \text{ m}$$

$$\frac{ly}{lx} = \frac{21}{9.4} = 2.23 > L \quad (3.45 \times 2) + 2.5 = 9.4 \text{ m}$$

hence 21 x 9.4 m

$$C.C = 20 \text{ mm}$$

$$D = 376 + 20 + \frac{30}{2}$$

$$= 411 \text{ mm}$$

$$b = 1 \text{ m} \quad \text{stop} = 1000 \text{ mm}$$

$$l_e = 9.4 + 0.376$$

$$= 9.77$$

$$D.L = 1 \times 0.411 \times 25 = 10.275$$

$$F.L = 1 \times 4 = 4 \text{ kN/m}$$

$$F.F = 1 \text{ kN/m}$$

$$W = 15.27 \text{ kN/m}$$

$$W_u = 18.91 \text{ kN/m}$$

$$M_u = \frac{W_u l e^2}{8} = \frac{22.9 \times 9.77^2}{8} = 273.3 \text{ kN-m}$$

$$V_u = \frac{W_u l e}{2} = 111.9 \text{ kN}$$

Check for depth

$$M_u = 0.36 \frac{x_{umax}}{d} [1 - 0.42 \frac{x_{umax}}{d}] f_{ck} bd^2$$

$$273.3 \times 10^6 = 0.36 \times 0.46 [1 - 0.42 \times 0.46] 25 \times 1000 \times d^2$$

$$\boxed{d = 286.04 \text{ mm}}$$

$$M_u = 0.87 f_y A_{st} d \left[ 1 - \frac{f_y A_{st}}{bd f_{ck}} \right]$$

$$273.3 \times 10^6 = 0.87 \times 500 \times A_{st} d \left[ 1 - \frac{500 A_{st}}{1000 \times 376 \times 25} \right]$$

$$273.3 \times 10^6 = 163560 A_{st} \left[ 1 - 5.319 \times 10^{-5} A_{st} \right]$$

$$273.3 \times 10^6 = 163560 A_{st} - 8.7 A_{st}^2$$

$$\boxed{A_{st} = 1853.7 \text{ mm}^2}$$

$$\text{spacing } \#30\phi @ 120 \text{ mm clc} = \frac{\pi (30)^2}{4} \times 1000 - A_{st}$$

$$(SOURCE DIGINOTES) = 381.32$$

provide 30φ @ 380 mm clc

Area of distribution bar

$$A = \frac{0.12}{1000} \times 1000 \times 411 = 493.2 \text{ mm}^2$$

$$\text{provide spacing} = \frac{\pi (10)^2}{4} \times 1000 = 159.84 \text{ mm}$$

provide 10φ bars of 150 mm

check for shear

$$C_v = \frac{V_u}{bd} = \frac{111.9 \times 10^3}{1000 \times 376} = 0.29 \text{ kN/m}^2$$

$$\tau_c = \frac{100 A_{st}}{bd} = \frac{100 \times 1853.7}{1000 \times 376} = 0.49$$

$$\tau_c = 0.48$$

$$\begin{aligned} 0.25 &\rightarrow 0.36 \\ 0.49 &\rightarrow \\ 0.55 &\rightarrow 0.49 \end{aligned}$$

$\tau_c > \tau_s \therefore$  Design is safe.

Job Job

(de) Effective span is given by = centre to centre distance of the beam - width of the beam

Ultimate moment of resistance  $(M_u) = \frac{wq l^2}{10} - \frac{wq l^2}{9}$

for continuous beam

$$V_u = 0.6 le \times [wq + w_g]$$

① Design an RC slab for a room of dimension 7m x 14m <sup>beam</sup> spaced at 3.5 m interval. If width of the beam is 300mm & super imposed load is 2kN/m<sup>2</sup> floor finish 1kN/m<sup>2</sup>. Use M<sub>20</sub> & Fe<sub>415</sub>.

calculation of effective length: step ① Depth effective depth

$$l_e = 3.5 - 0.23 = 3.27 \text{ m} \rightarrow \text{for clear span}$$

$$d = \left( \frac{\text{span}}{30} \right) \text{ [Assume]} \quad \text{on spacing}$$

$$d = \left( \frac{3500}{30} \right) = 116.67 \text{ mm} \quad = 0.116 \text{ m}$$

$$l_e = l + \text{wall thickness (d)}$$

$$l_e = 3.27 + 0.116 \quad \text{+ wall thickness (d)}$$

$$\begin{aligned} l &= \text{spacing} - w_b \\ &= 3.5 - 0.23 \end{aligned}$$

$$l = 3.27 \text{ m}$$

$$l_e = 3.38 \text{ m}$$

## Load calculation

$$\text{Main bar dia} = 10 \quad \left. \begin{array}{l} \\ \end{array} \right\} D = 120 + 20 + (10/2)$$

$$\text{Clear cover} = 20 \quad \boxed{D = 145 \text{ mm}}$$

for slab

(Assumed breadth)

$$DL = 0.145 \times 1 \times 25 = 3.625 \text{ kN/m}$$

$$FF = 0$$

$$I = \pm 1 \text{ kNm}$$

$$W = 4.625 \text{ kN/m}$$

$$W_0 = 1.5 \times 4.625 = 6.93 \text{ kN/m}$$

$$\rightarrow N_g = 6.93 \text{ kN/m}$$

$$W_Q = 1.5 \times 3 = 4.5 \text{ kN/m}$$

$$M_U = \frac{W_0 le^2}{10} + \frac{W_Q le^2}{9}$$

$$= \frac{6.93 \times 3.38^2}{10} + \frac{4.5 \times 3.38^2}{9}$$

$$\boxed{M_U = 13.62 \text{ kN-m}}$$

$$N_U = 0.6 le [W_g + W_Q]$$

$$= 0.6 \times 3.38 [6.93 + 4.5]$$

$$\boxed{V_U = 23.18 \text{ kN}}$$

$$M_U = 0.87 f_y A_{st} d \left[ 1 - \frac{f_y A_{st}}{bd f_{ck}} \right]$$

$$13.62 \times 10^6 = 0.87 \times 415 \times A_{st} \times 120 \left[ 1 - \frac{415 A_{st}}{1000 \times (120) \times 80} \right]$$

$$13.62 \times 10^6 = 43326 A_{st} \left[ 1 - \frac{415 A_{st}}{1000 \times (120) \times 80} \right]$$

$$13.62 \times 10^6 = 43326 A_{st} - 0.415 A_{st}^2$$

$$\boxed{A_{st} = 333.60 \text{ mm}^2}$$

$$\text{spacing} = \frac{\frac{A_{st}}{\pi(10)}}{f} \times 1000 = 235.43 \text{ mm}$$

provide 10φ @ 235 mm c/c - main bar

$$\text{spacing of 8m = m} = \frac{\frac{\pi(8)}{4}}{f} \times 1000 = 150.67$$

$$\text{Distribution bar} = \frac{0.12}{100} \times 1000 \times 145$$

$$A_{bd} = 174 \text{ mm}^2$$

$$\text{spacing} = \frac{\frac{\pi \times 8}{4}}{174} \times 1000 = 288.8 \text{ mm}$$

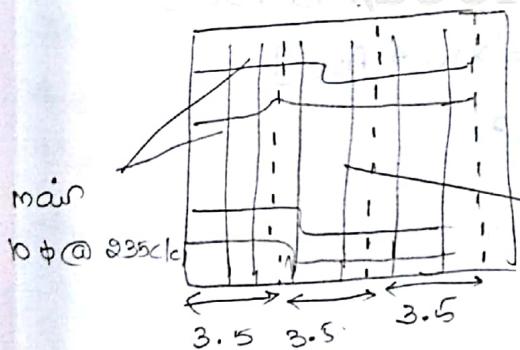
provide 8φ @ 280 mm c/c - distribution bar

check for shear

$$\tau_v = \frac{V_u}{b d} = \frac{23.22 \times 10^3}{1000 \times 120} = 0.1935 \text{ N/mm}^2$$

$$\frac{100 A_{st}}{bd} = \frac{100 \times 333.6}{1000 \times 120} = 0.278 \quad \tau_c \rightarrow 0.278$$

$$\tau_c > \tau_v$$



D bars 8φ @ 280 c/c.

- ② For a commercial parking lot of dimensions 14x27 m as a beam spacing 4.5m centre to centre and width of the beam is 230mm placed inside the wall thickness of 250mm Use M<sub>20</sub> & F<sub>415</sub> & Super Imposed load 3.5 kN/m<sup>2</sup>

$$d = \frac{4500}{30} = 150\text{mm}$$

10a/17

$$D = 150 + 20 + (10\%) \\ = 175\text{mm}$$

$$\text{length} = 4.5 - 0.03 \\ = 4.47\text{m}$$

$$l_e = 4.47 + 0.25 = 4.52 \quad (\text{or}) \quad 4.47 + 0.15 = 4.42$$

Considering least of both  $\therefore l_e = 4.42\text{m}$

### Load calculation

$$DL = 0.175 \times 1 \times 25 = 437.5 \text{ kNm}$$

$$FF = 15 \text{ kNm}, \quad w_g = 1.5 \times 5.375 = 8.06 \text{ kNm} \\ w = 5.375$$

$$w_g = 1.5 \times 3.5 = 3.25 \text{ kNm}$$

$$M_U = \frac{w_g l_e^2}{10} + \frac{w_g l_e^2}{9} \\ = 27.14 \text{ kNm}$$

$$V_U = 0.6 l_e (w_g + w_2) \\ = 35.29 \text{ kN}$$

$$\text{But } M_U = 0.87 f_y A_{st} d \left[ 1 - \frac{f_y A_{st}}{bd f_{ck}} \right]$$

$$27.14 \times 10^6 = 0.87 \times 415 \times A_{st} \times 150 \left[ 1 - \frac{415 A_{st}}{1000 \times 150 \times 20} \right]$$

$$27.14 \times 10^6 = 54157.5 A_{st} \left[ 1 - 1.38 \times 10^{-4} A_{st} \right]$$

$$27.14 \times 10^6 = 54157.5 A_{st} - 7.49 A_{st}^2$$

$$A_{st} = 541.71 \text{ mm}^2$$

$$\text{Spacing} = \frac{\pi (10)^2}{A_{st}}$$

$$\uparrow \times 1000 = 144.9 \text{ mm}$$

Provide 10@140mm clc main bar

## Distribution bar

$$\frac{0.12}{100} \times 1000 \times 175 = 210 \text{ mm}$$

spacing 8mm  $\phi = \frac{\pi(8)^2}{4} \times 1000 = 239.35 \text{ mm}$

provide 8φ @ 235 mm c/c

$$\tau_v = \frac{VU}{bd} = \frac{35.29 \times 10^3}{1000 \times 150} = 0.23$$

$$\frac{100 \text{ Ast}}{bd} = \frac{100 \times 541.7}{1000 \times 150} = 0.36$$

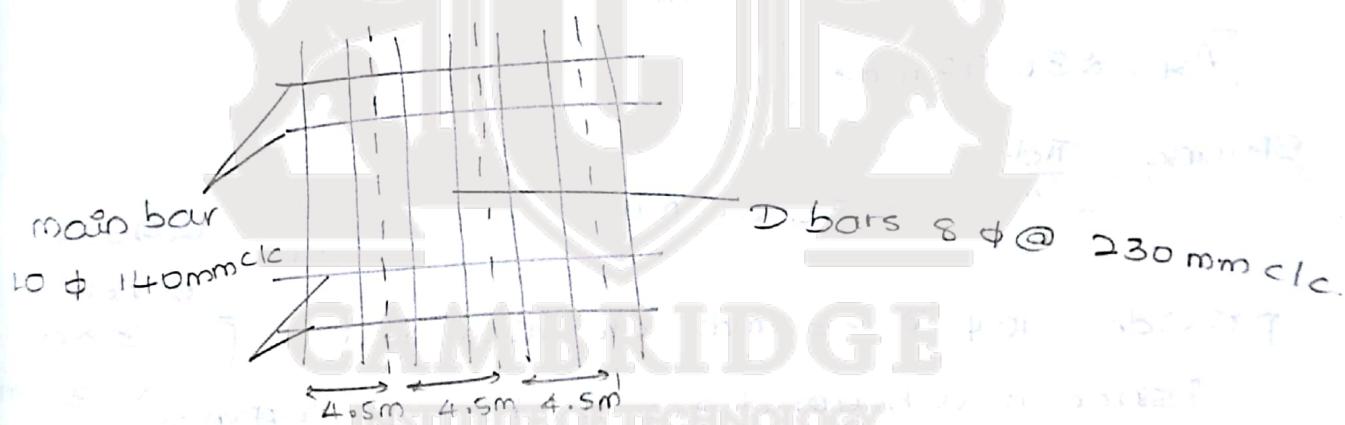
$$0.25 \rightarrow 0.36$$

$$0.36 \rightarrow ?$$

$$0.5 \rightarrow 0.48$$

$$\tau_c = 0.41$$

$\tau_c > \tau_v$  : design is safe



③ for a residential building Internal room dia is 8x16m as the room spacing 3m centre to centre where width of the beam is 200mm lying on the wall of thickness 230 mm Use M<sub>00</sub> & F<sub>ck</sub> & take Super Imposed load as 2.5 kN/m<sup>2</sup> & check for the deflection control.

$$d = \frac{3000}{30} = 100 \text{ mm}$$

$$\text{length} = 3m - 0.23$$

$$= 2.8 \text{ m}$$

$$D = 100 + 20 + \left(\frac{10}{2}\right)$$

$$I_e = 2.8 + 0.23 = 3.03 \text{ (wall thickness)}$$

$$D = 125 \text{ mm}$$

$$l_c = 2.8 + 0.1 = 2.9 \text{ (ds)}$$

Considering least value.

$$f_c = 2.9$$

## Load calculation

$$DL = 0.125 \times 25 = 3.125 \text{ kNm}$$

$$FF = 0.5 \text{ kNm} \quad \text{[since it's a residential building]}$$

$$Wq = 1.5 \times 3.625 = 5.437 \text{ kNm}$$

$$Wq = 1.5 \times 2.5 = 3.75 \text{ kNm}$$

$$M_u = \frac{w_g l_e^2}{10} + \frac{w_q l_e^2}{90} \quad V_u = 0.6 l_e (w_g + w_q)$$

$$M_u = 8.07 \text{ kNm} \quad V_u = 15.98 \text{ kN}$$

$$M_u = 0.87 f_y A_{st} d \left[ 1 - \frac{f_y A_{st}}{bd f_{ck}} \right]$$

$$8.07 \times 10^6 = 0.87 \times 415 \times A_{st} \times 100 \left[ 1 - \frac{415 A_{st}}{1000 \times 100 \times 20} \right]$$

$$8.07 \times 10^6 = 36105 A_{st} \left[ 1 - 2.075 \times 10^{-4} \right]$$

$$8.07 \times 10^6 = 36105 A_{st} - 7.49 A_{st}^2$$

$$A_{st} = 234.97 \text{ mm}^2$$

$$\text{Spacing} = \frac{\frac{\pi d^2}{4}}{A_{st}} = 334.25 \text{ mm}$$

provide 10 φ @ 330 mm c/c main bar

[since it is beyond 300 it shouldn't happen so] = 300mm \*

Provide 10 φ @ 300 mm c/c main bar

$$\text{Distribution bar} : \frac{0.12}{100} \times 1000 \times D = 150 \text{ mm} = A_{st}$$

$$\text{Spacing 8mm} \phi \frac{\frac{\pi (8)^2}{4}}{150} \approx 1000 \text{ mm} = 335.1 \text{ mm}$$

provide 8 φ @ 335 mm c/c

$$T_{fix} = \frac{V_u}{bd} = \frac{15.98 \times 10^3}{1000 \times 100} = 0.159$$

$$\frac{100 A_{st}}{bd} = \frac{100 \times 234.97}{1000 \times 100} = 0.23$$

$$0.25 \rightarrow 0.36$$

0.23 → ?

$$0.5 \rightarrow 0.48$$

$$\tau_c = 0.35$$

$$\tau_c > \tau_v$$

∴ Design is safe.

check for deflection

$$\frac{L}{R} = 26 \text{ mF}$$

$$\frac{3000}{100} = 30$$

from page 38 graph Fig(4)

$$\text{modification factor } F_i = \frac{100 \text{ Ast}}{\text{bd}} = 0.23$$

$$f_{sc} = 0.58 f_y \left( \frac{A_{st}}{A_c A_{st}} \right)$$

$$\text{Act Ast} = \frac{\pi(10)^2}{4} \times 1000$$

$\leftarrow 300$

$$A_{ct} A_{st} = 261.7 \text{ mm}^2$$

$$f_{SC} = 0.58 \times 415 \left[ \frac{234.97}{261.7} \right]$$

$$f_{sc} = 216.11 \text{ N/mm}^2$$

0.23 on MF &  $f_{sc} = 216.11$  so  $\text{RF}_1$

$$MF = 1.9 \times 26 = 49.5$$

↓  
formula

$\frac{1}{d} < M_F \therefore$  Hence def is under Continuous

④ Design a cantilever slab of span 1.2 m from beam bearing a live load of  $1.25 \text{ kN/m}^2$ . Use  $M_{20}$  &

Fe<sub>4</sub>V

For Cantilever  $\frac{l}{d} = \frac{1}{2}$

$$d = \frac{1200}{7} = 171.4 \approx 175 \text{ mm}$$

$$D = 175 + 20 + \left(\frac{10}{2}\right)$$

$$\boxed{D = 200 \text{ mm}}$$

$$L_e = 1.2 + 0.23 \quad (\text{or}) \quad 1.2 + 0.175 \\ = 1.43 \quad (\text{or}) \quad 1.375$$

Taking the least  $L_e = 1.37$

$$M_u = \frac{w_u L_e^2}{2} \quad N_u = w_u L_e$$

$$w_u = D_L + L_L$$

$$D_L = 0.2 \times 25 = 5$$

$$L_L = 1.25 = 1.25$$

$$FF = 0.5$$

$$W = 6.75 \text{ kNm}$$

$$w_u = 1.5 \times W = 10.125 \text{ kNm}$$

$$M_u = \frac{w_u L_e^2}{2} = \frac{10.125 \times 1.37^2}{2} = 9.5 \text{ KN-m}$$

$$V_u = w_u L_e = 13.87 \text{ KN}$$

check for depth

$$M_u = 0.36 \frac{x_{u\max}}{d} \left[ 1 - 0.42 \frac{x_{u\max}}{d} \right] b d^2 f_{ck}$$

$$9.5 \times 10^6 = 0.36 \times 0.48 \left[ 1 - 0.42 \times 0.48 \right] \times 1000 \times d^2 \times 20$$

$$\boxed{d = 158.67 \text{ mm}} < 175 \text{ mm} \text{ so it is safe}$$

Ast for main steel.

$$M_u = 0.87 f_y A_{st} \left[ 1 - \frac{f_y A_{st}}{bd f_{ck}} \right]$$

$$9.5 \times 10^6 = 0.87 \times 415 A_{st} \left[ 1 - \frac{415 A_{st}}{1000 \times 175 \times 20} \right]$$

$$9.5 \times 10^6 = 63183.75 \text{ Ast} - 7.49 \text{ Ast}^2$$

$$\boxed{\text{Ast} = 153.13 \text{ mm}^2}$$

spacing for 10 mm dia

$$\frac{\pi(10)^2}{4} \times 1000$$

$$\text{Ast}$$

$$= 512.89$$

~~efficiency~~

Its more than 300 so take 300 from clc

provide 10φ @ 300 mm clc main bar

Distribution steel

$$\text{Ast} = \frac{0.12}{100} \times 1000 \times 300 = 240 \text{ mm}^2$$

provide 8φ at 240mm

$$\text{spacing} = \frac{\pi(8)^2}{4} \times 1000 = 209.43 \text{ clc band width}$$

so take it as 205

provide 8φ @ 205 mm clc

(page 48)

Development Length of Bars.

$$L_d = \frac{\phi \sigma_s}{f_t \tau_{bd}}$$

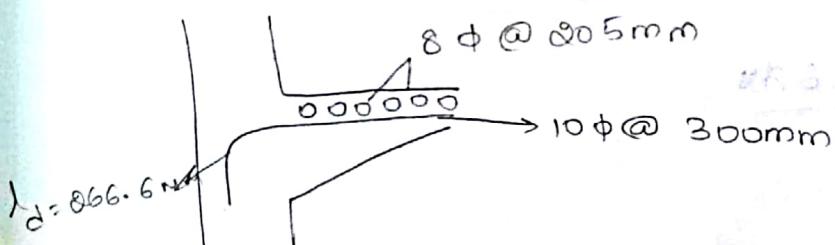
$$= \frac{10 \times 0.128}{4 \times 1.02}$$

$$\sigma_s = \frac{\omega_u}{A} = \frac{10.125}{\pi(10)^2 / 4}$$

$$\sigma_s = 0.128$$

$$L_d = 0.26 \text{ m}$$

$$\boxed{L_d = 266.6 \text{ mm}}$$



$$\tau_v = \frac{VU}{bd} = \frac{13.87 \times 10^3}{1000 \times 175} = 0.079 \text{ kN/m}$$

$$2. \frac{100 \text{ ast}}{bd} = \frac{100 \times 153.13}{1000 \times 175} = 0.087 \text{ kN/m}$$

$$\tau_c = 0.087$$

$$\tau_c > \tau_v$$

12/10/17

## TWO WAY SLAB

If the ratio of longer span by shorter spans is less than (or) equal to 2 then it will be designed as two way slab i.e.  $\frac{l_1}{l_2} \leq 2$ .

### Simply Supported Slab:

- For a room of Internal dimension  $4m \times 5m$ , carries a live load of  $2.5 \text{ kN/m}^2$ . Use M<sub>20</sub> & Fe<sub>415</sub>.

$$\frac{l_1}{l_2} = \frac{5}{4} = 1.25 < 2 \text{ Hence it is two way slab.}$$

$$\frac{l}{d} = 20$$

$$\frac{4000}{20} = d$$

$$d = 200 \text{ mm}$$

$$D = 200 + 20 + \frac{10}{2}$$

$$D = 225 \text{ mm}$$

$$l_e = 4 + 0.23 = 4.23 \quad (\text{OR}) \quad 4 + 0.2 = 4.2$$

$$\text{Taking least value } l_e = 4.2$$

$$\frac{(l_e)_y}{(l_e)_x} = \frac{5.2}{4.2} = 1.24$$

For simply supported all the four sides of beam is free

By page 91 :- 9th condition :- For simply supported slab all 4 edges are discontinuous.

$$1.2 \rightarrow 0.072 \quad \alpha_x = 0.074$$

$$1.04 \rightarrow x \quad \alpha_y = 0.056$$

$$1.3 \rightarrow 0.079$$

$$M_x = \alpha_x w l_x^2$$

$$M_y = \alpha_y w l_x^2$$

Load calculation :-

$$\text{D.L} \rightarrow 1 \times D = 1 \times 0.825 \times 1 \times 2.5 = 5.625 \text{ kNm}$$

$$= 0.5 \text{ kNm}$$

FF →

$$L_d \rightarrow = 10.2 \text{ kNm}^2$$

$$W = 8.125 \text{ kNm}$$

$$W_u = 1.5 \times W = 12.18 \text{ kNm}$$

$$M_x = \alpha_x w l_x^2 \\ = 0.074 \times 12.18 \times (4.2)^2$$

$$M_x = 15.89 \text{ kNm}$$

$$M_y = \alpha_y w l_x^2 \\ = 0.056 \times 12.18 \times (4.2)^2$$

$$M_y = 18.03 \text{ kNm}$$

Area of steel in x-direction

Check for depth

$$M_u = 0.36 \frac{x_{umax}}{d} \left[ 1 - \frac{x_{umax}}{d} \times 0.42 \right] b d^2 f_{ck}$$

$$M_x = 0.36 (0.48) \left[ 1 - (0.48) (0.42) \times 1000 \times d^2 \times 20 \right]$$

$$d_s = 75.88 \text{ mm} \quad \therefore 'd' is safe.$$

For simply supported all the four sides of beam is free

By page 91 :- 9th condition :- For simply supported slab all 4 edges are discontinuous.

$$1.2 \rightarrow 0.072 \quad \alpha_x = 0.074$$

$$1.84 \rightarrow x \quad \alpha_y = 0.056$$

$$1.3 \rightarrow 0.079$$

$$M_x = \alpha_x w l_x^2$$

$$M_y = \alpha_y w l_x^2$$

Load calculation :-

$$\text{D.L} \rightarrow 1 \times 0.825 \times 1 \times 2.5 = 5.625 \text{ kN/m}$$

$$= 0.5 \text{ kN/m}$$

FF →

$$\text{L.R} \rightarrow = 10.2 \text{ kN/m}^2$$

$$w = 8.125 \text{ kN/m}$$

$$w_u = 1.5 \times w = 12.18 \text{ kN/m}$$

$$M_x = \alpha_x w_u l_x^2$$

$$= 0.074 \times 12.18 \times (4.2)^2$$

$$M_x = 15.89 \text{ kN-m}$$

$$M_y = \alpha_y w l_x^2$$

$$= 0.056 \times 12.18 \times (4.2)^2$$

$$M_y = 12.03 \text{ kN-m}$$

Area of steel in x-direction

Check for depth

$$dM_u = 0.36 \frac{x_{\text{umax}}}{d} \left[ 1 - \frac{x_{\text{umax}}}{d} \times 0.42 \right] b d^2 f_{ck}$$

$$M_x = 0.36 (0.48) \left[ 1 - (0.48) (0.42) \times 1000 \times d^2 \times 20 \right]$$

$$d_s = 75.88 \text{ mm}$$

$\therefore d'$  is safe.

Ast for shorter spans

$$M_u = 0.87 f_y A_{st} d \left[ 1 - \frac{f_y A_{st}}{bd f_{ck}} \right]$$

$$15.89 \times 10^6 = 0.87 \times 415 \times A_{st} \left[ 1 - \frac{415 A_{st}}{1000 \times 200 \times 20} \right]$$

$$15.89 \times 10^6 = \frac{72210}{366405} A_{st} \left[ 1 - \frac{1.037}{4.488 \times 10^4} A_{st} \right]$$

$$15.89 \times 10^6 = \frac{72210}{366405} A_{st} - 0.488 A_{st}^2$$

$$A_{st} = 225.3 \text{ mm}^2$$

Provide Spacing

$$\frac{\pi d^2}{4} \times 1000 = 348.6 \times 1000 = 348600$$

Provide 10φ @ 300mm c/c in x-direction

Ast)<sub>long</sub>

$$M_u = 0.86 \frac{x_{u\max}}{d} \left[ 1 - \frac{x_{u\max}}{d} \times 0.42 \right] bd^2 f_{ck}$$

$$12.03 \times 10^6 = 0.36 \times 0.48 \left[ 1 - 0.48 \times 0.42 \right] 1000 \times 200$$

$$M_u = 0.87 f_y A_{st} d \left[ 1 - \frac{f_y A_{st}}{bd f_{ck}} \right]$$

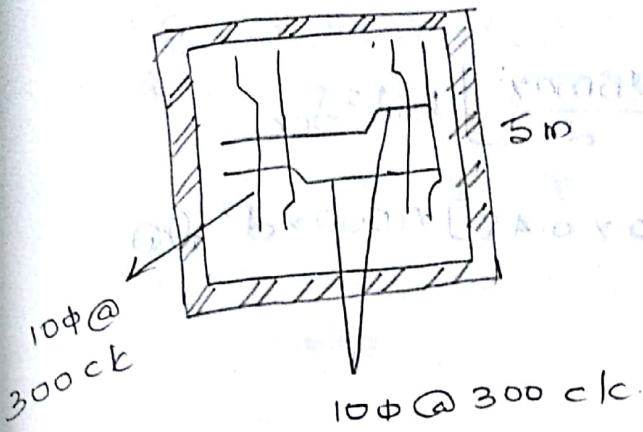
$$12.03 \times 10^6 = 0.87 \times 415 \times A_{st} \times 200 \left[ 1 - \frac{415 A_{st}}{1000 \times 200 \times 20} \right]$$

$$A_{st} = 169.57 \text{ mm}^2$$

Spacing

$$\frac{\pi d^2}{4} \times 1000 = 463.17 \text{ mm}$$

Since it is more than 300,  
take only 300



② Design a slab for a room dimension of 8m x 10m carrying a live load of 2.5 kN/m<sup>2</sup> & check for the deflection using M<sub>20f</sub> & Fe<sub>415</sub>.

$$\frac{d}{l_x} = \frac{10}{8} = 1.25 \text{ m} < 2 \text{ m} \quad \text{Hence 2 way slab.}$$

$$\frac{l}{d} = 20$$

$$\frac{8000}{20} = d$$

$$d = 400 \text{ mm}$$

$$D = 400 + 20 + \frac{10}{2}$$

$$D = 425 \text{ mm}$$

$$l_e = 8 + 0.23 = 8.23 \text{ (ORD) } 8 + (d) = 8 + 0.4 = 8.4$$

$$\text{so least is } 8.23 \quad l_e = 8.23$$

$$\alpha_2 = 0.074 \\ \alpha_4 = 0.056$$

$$\frac{(l_e)_y}{(l_e)_x} = \frac{10.23}{8.23} = 1.24$$

$$DL = 0.425 \times 1 \times 2.5 = 10.625 \text{ kN/m}$$

$$FF =$$

$$= 0.5 \text{ kN/m}$$

$$LK =$$

$$= 2.5 \text{ kN/m}$$

$$w = 13.625 \quad w_u = 20.43 \text{ kN/m}$$

$$M_x = \alpha_x w_u l_x^2$$

$$= (0.074) \times (20.43) (0.074)^2$$

$$M_x = 102.39 \text{ kN-m}$$

$$M_y = \alpha_y w_u l_x^2$$

$$M_y = 77.49 \text{ kN-m}$$

### check for depth

$$M_u = 0.36 \frac{\pi d^2}{d} \left[ 1 - 0.42 \times \frac{\pi d^2}{d} \right] bd^2 f_{ck}$$

$$102.39 \times 10^6 = 0.36 \times 0.48 \left[ 1 - 0.42 \times 0.48 \right] \times 1000 \times d^2 \quad \text{20}$$

$$\boxed{d = 192.63 \text{ mm}}$$

spacing

$$\frac{\pi d^2}{4}$$

Ast for shorter span

$$M_u = 0.87 \times f_y \times Ast \times d \left[ 1 - \frac{f_y \ Ast}{bd \ f_{ck}} \right]$$

$$102.39 \times 10^6 = 0.87 \times 415 \times Ast \times 100 \left[ 1 - \frac{415 \ Ast}{1000 \times 400 \times 20} \right]$$

$$102.39 \times 10^6 = 144420 \ Ast - 7.49 \ Ast^2$$

$$\boxed{Ast = 552.38 \text{ mm}^2}$$

$$\boxed{Ast = 737.155 \text{ mm}^2}$$

$$\frac{\pi d^2}{4} \times 1000 = 144420 \quad 106.54$$

provide 10φ @ 105 mm clc in x-direction

$$M_u = 0.87 f_y \ Ast \ d \left[ 1 - \frac{f_y \ Ast}{bd \ f_{ck}} \right]$$

$$102.39 \times 10^6 = 0.87 \times 415 \times Ast \times 100 \left[ 1 - \frac{415 \ Ast}{1000 \times 400 \times 20} \right]$$

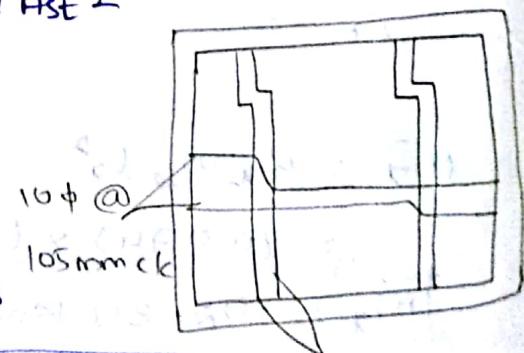
$$102.39 \times 10^6 = 144420 \ Ast - 7.49 \ Ast^2$$

$$\boxed{Ast = 552.38 \text{ mm}^2}$$

spacing

$$\frac{\pi d^2}{4}$$

$$\times 1000 = 144420 \quad 106.54$$



provide 10φ @ 140 clc in y-direction

## Deflection

$$f_{sc} = \frac{0.58 f_y}{\text{Act Ast}} \quad \text{shorter span Ast}$$

$$= \frac{0.58 \times 415 \times 737.15}{747.99} = 237.2.$$

$$\frac{100}{100} \quad \text{Act Ast} = \frac{\pi (10)^2}{4} = \underline{\underline{747.99}}$$

$$\frac{100 \text{ Ast}}{bd} = \frac{100 \times 737.15}{1000 \times 400} = 0.18$$

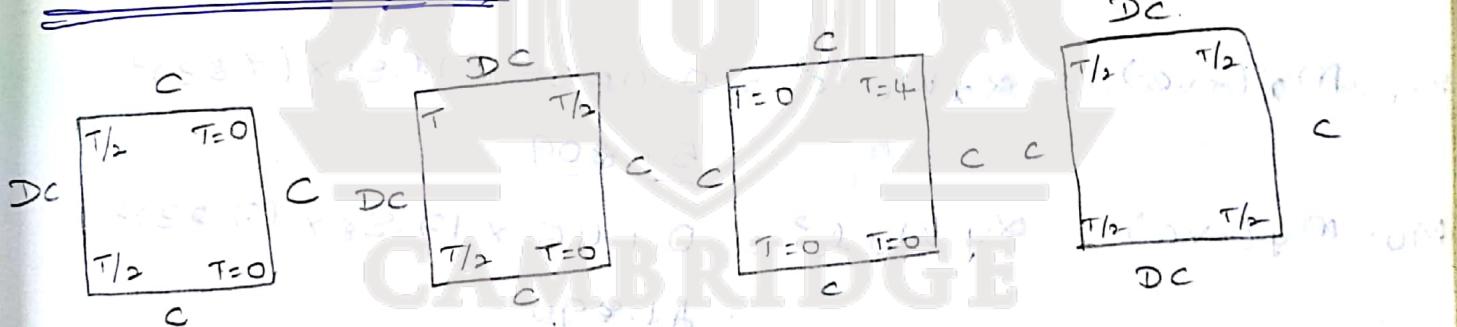
$$f_1 = 2$$

$$\frac{l}{d} = \frac{8000}{400} = 20$$

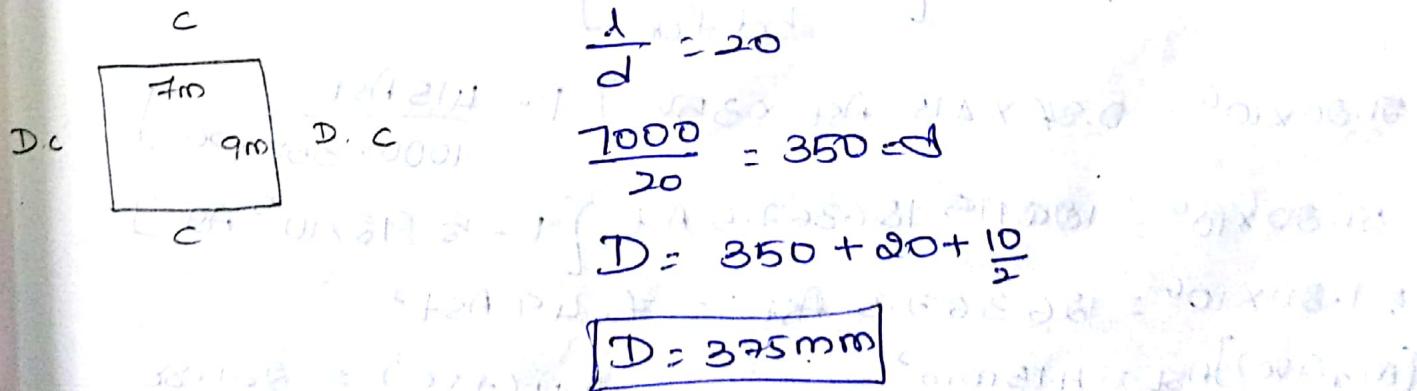
$$MF = F_1 \times f_2 \times f_3 \times 20$$

$$= 2 \times 20 = 40$$

## Restrained Slabs



① Design a slab for a room internal dimension 7m x 9m where two adjacent sides of slab span are discontinuous & carrying a TL of 2 kN/m<sup>2</sup>. Use M<sub>so</sub> & f<sub>A15</sub>



Load calculation :-

$$DL = 1 \times D \times 25 = 1 \times 0.325 \times 25 = 9.325 \text{ kNm}$$

0.5 kNm

EF =

$$LF = 0.5 \times 25 = 12.5 \text{ kNm}$$

$$w = 11.8 \text{ kNm}$$

$$WU = 17.81 \text{ kNm}$$

PP EF

$$l_e = 7 + 0.23 = 7.23 \text{ (or) } 7 + 0.35 = 7.35$$

least  $l_e = 7.23$

$$\frac{(l_e)y}{(l_e)x} = \frac{7.23}{7.23} = 1.07$$

$$\alpha_x(-ve) = 0$$

$$\alpha_x(+ve) = 0.0055$$

$$\alpha_y(-ve) = 0.0045$$

$$\alpha_y(+ve) = 0.0035$$

$$M_x(-ve) = 0$$

$$M_x(+ve) = 100$$

$$M_y(-ve)$$

$$M_y(+ve)$$

$$M_u = M_x(+ve) = \alpha_x W_u l_e^2 = 0.0055 \times 17.81 \times (7.23)^2 \\ = \underline{\underline{51.809}}$$

$$M_u = M_y(-ve) = \alpha_y W_u l_e^2 = 0.0045 \times 17.81 \times (7.23)^2 \\ = \underline{\underline{41.895}}$$

$$M_u = M_y(+ve) = \alpha_y W_u l_e^2 = 0.0035 \times 17.81 \times (7.23)^2 = \underline{\underline{32.58}}$$

$$51.80 \times 10^6 = 0.87 f_y A_{st} d \left[ 1 - \frac{f_y A_{st}}{bd f_{cr}} \right]$$

$$51.80 \times 10^6 = 186367.5 A_{st} \left[ 1 - \frac{415 A_{st}}{1000 \times 350 \times 20} \right]$$

$$51.80 \times 10^6 = 186367.5 A_{st} - 4.49 A_{st}^2$$

$$[M_x(+ve)]_{A_{st}} = 415 \text{ mm}^2$$

$$M_y(+ve) = 261.88$$

$$[M_y(-ve)]_{A_{st}} = 338.77 \text{ mm}^2$$

$$\frac{M_2(+ve)}{Ast} = \frac{\pi d^2 / 4}{Ast} \times 1000$$

$$M_2(+ve) = 189.25 \approx 180$$

$$M_4(+ve) = 299.9$$

$$(M_y(-ve)) = \frac{\pi d^2 / 4}{Ast} \times 1000$$

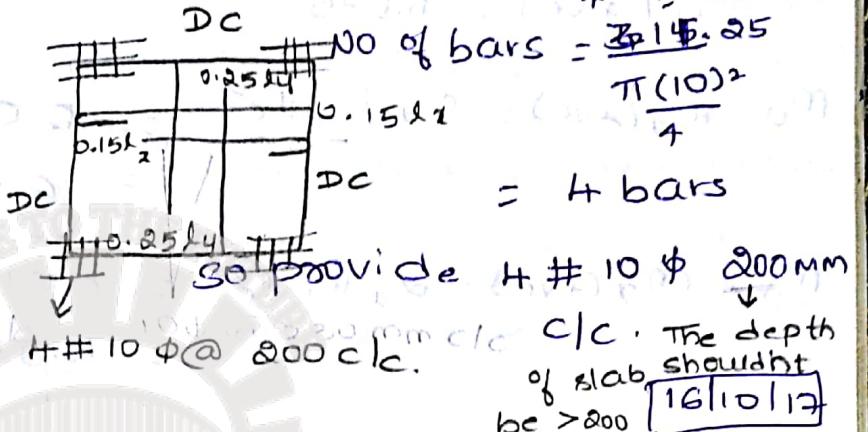
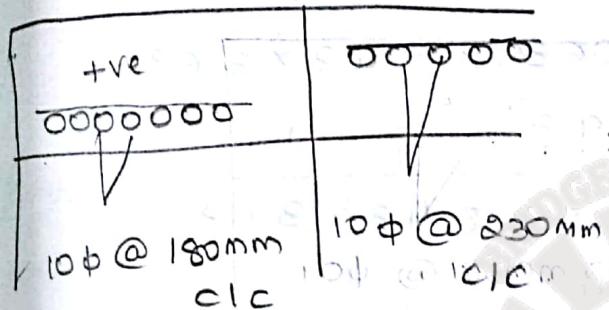
$$= 31.83 \approx 30$$

For top bars

$$\frac{M_2(+ve)}{Ast} = \frac{\pi d^2 / 4}{Ast} = 31.83$$

$$No. of bars = \frac{31.83}{14.25} = 2.21 \approx 2$$

$$\frac{\pi (10)^2}{4} = 78.54 \text{ mm}^2$$



① Design a slab for a room of Internal dimension  $3.5 \times 6\text{m}$  where the two short edges are discontinuous carrying a live load of  $2\text{ kN/m}^2$ . Used  $M_{20} + Fe_{415}$  slab lies on the beam's width of  $250\text{mm}$ .

$$\frac{l}{D} = 35 \times 0.8 \rightarrow \text{for two way slab } l < 3.5\text{m span} \\ \text{should multiply with 0.8.}$$

$$D = 125\text{mm}$$

$$d = 125 - 25 \\ = 100\text{mm}$$

Load calculation:

$$D.L = (0.125 \times 1) \times 2.5 = 3.125 \text{ kN/m} \\ = 0.5 \text{ kN/m}$$

$$F.F =$$

$$L.L =$$

$$W = 5.625 \text{ kN/m}$$

$$W_u = 1.5 \times W = 8.43 \text{ kN/m}$$

$$l_c = 3.5 + 0.25 = 3.75 \text{ m}$$

(or) small a value  $\div 1000$

$$l_c = 3.5 + 0.1 \rightarrow 3.6 \text{ m}$$

$$\frac{\alpha_e(y)}{\alpha_e(x)} = \frac{6.1}{3.6} = 1.69$$

(b)  $\alpha_x(-ve) = 0.0638$

$\alpha_y(+ve) = 0.048$

$\alpha$	$y$
0.15	0.06
1.75	0.065

$$\alpha_y(-ve) = 0$$

$$\alpha_y(+ve) = 0.035$$

$$M_u = M_x(+ve) = \alpha_x W_u l e^2 = 0.0638 \times 8.43 \times 3.6^2 = 6.97$$

$$M_u = M_y(+ve) = \alpha_y W_u l e^2 = 0.048 \times 8.43 \times 3.6^2 = 5.84$$

$$M_y(-ve) = \alpha_y W_u l e^2 = 0$$

$$M_y(+ve) = 0.035 \times 8.43 \times 3.6^2 = 3.82$$

$$M_x \rightarrow \text{reqd } M_u = 0.87 f_y A_{st} d \left[ 1 - \frac{f_y P_s +}{bd f_{ck}} \right]$$

$$M_x(-ve) = 6.97 \times 10^6 = 0.87 \times 415 A_{st} \times 100 \left[ 1 - \frac{415 A_{st}}{100 \times 1000 \times 20} \right]$$

$$6.97 \times 10^6 = 36105 A_{st} \left[ 1 - 2.075 \times 10^{-4} A_{st} \right]$$

$$6.97 \times 10^6 = 36105 A_{st} - 7.49 A_{st}^2$$

$$M_x(-ve) = A_{st} = 201.46 \text{ mm}^2$$

$$M_x(+ve) = 149.78 = A_{st}$$

$$M_y(+ve) = 0$$

$$M_y(-ve) = 108.23 = A_{st}$$

### Spacing

$$\text{spacing for +ve steel} = \frac{\pi \times 10^2}{4} \times 1000 \\ = 149.78$$

$$= 1524.36 \text{ mm}$$

Provide 10φ @ 300 mm c/c

$$\text{spacing for top steel} = \frac{T \times 10^2}{f} = \frac{198.75}{1000} \times 1000 = 395.16 \text{ mm}$$

Provide 10φ @ 300mm c/c.

For top bar

$$A_{st} = (M_x + ve) = 149.78$$

$$\text{no of bars} = \frac{149.78}{\frac{T \times (10)^2}{4}} = 1.4 \approx 2 \text{ bars}$$

provide 2# 10φ @ 185mm c/c.

- ③ Design a slab for a room dimension 3x5m whose one long edge is continuous carrying a live load of 1.5 KN/m<sup>2</sup>

$$\frac{l}{D} = 3.5 \times 0.8$$

$$D = 107.14 \text{ mm} \approx 108 \text{ mm}$$

$$d = 110 - 25 = 85 \text{ mm}$$

$$l_{e(y)} = \frac{\text{load calculation}}{0.11 \times 1} \times 25 = 2.75 \text{ KN/m}$$

$$DL = (0.11 \times 1) \times 25 = 0.5 \text{ KN/m}$$

$$FF =$$

$$LL = \frac{1.5 \text{ KN/m}}{0.11 \times 1}$$

$$W = 4.75$$

$$WU = 7.125 \text{ KN/m}$$

$$l_{e(y)} = 3 \times 0.85 = 2.55 \quad (\text{or}) \quad 2.55 = 2.3 \text{ m}$$

$$3 + 0.085 = 3.085$$

$$\frac{l_{e(y)}}{l_{e(x)}} = \frac{2.085}{3.085} = 1.64$$

$$\text{Condition (1): } \alpha_2(-ve) = 0.087$$

$$\alpha_2(+ve) = 0.0648$$

$$\alpha_y(-ve) = 0$$

$$\alpha_y(+ve) = 0.043$$

$$M_U = (M_x)_{+ve} = \alpha_x W_u l e^2 = 0.088 \times 4.125 \times 3085^2$$

$$M_x (-ve) = 5.899$$

$$M_x (+ve) = 4.643$$

$$M_y (-ve) = 0$$

$$M_y (+ve) = 2.915$$

$$M_U = 0.87 f_y A_{st} d \left[ 1 - \frac{f_y A_{st}}{bd f_{ck}} \right]$$

$$5.89 \times 10^6 = 0.87 \times 415 \times A_{st} \times 85 \left[ 1 - \frac{415 A_{st}}{1000 \times 85 \times 20} \right]$$

$$5.89 \times 10^6 = 30689.25 A_{st} \left[ 1 - 2.44 \times 10^{-4} A_{st} \right]$$

$$5.89 \times 10^6 = 30689.25 A_{st} - 7.49 A_{st}^2$$

$$A_{st_1} = 201.86 \text{ mm}^2$$

$$A_{st_2} = 153.7 \text{ mm}^2$$

$$A_{st_3} = 0$$

$$A_{st_4} = 97.29 \text{ mm}^2$$

Check for depth

$$M_U = 0.36 \left( \frac{x_{umax}}{d} \right) \left[ 1 - 0.42 \left( \frac{x_{umax}}{d} \right) \right] \times f_{ck} \cdot b \times d^2$$

$$5.89 \times 10^6 = 0.36 \times 0.48 \left[ 1 - 0.42 \times 0.48 \right] \times 205 \times 1000 \times d^2$$

$$\underline{d = 46.2 \text{ mm}} \quad \text{is less than taken } d' = 50 \text{ mm.}$$

$$M_U = 0.87 f_y A_{st} d \left[ 1 - \frac{f_y A_{st}}{bd f_{ck}} \right]$$

$$5.89 \times 10^6 = 0.87 \times 415 \times A_{st} \times 85 \left[ 1 - \frac{415 A_{st}}{1000 \times 85 \times 20} \right]$$

$$5.89 \times 10^6 = 30689.25 A_{st} \left[ 1 - 2.44 \times 10^{-4} A_{st} \right]$$

$$5.89 \times 10^6 = 30689.25 A_{st} - 7.49 A_{st}^2$$

$$A_{st} = 201.85 \text{ mm}^2$$

$$A_{st} = 153.7$$

$$A_{st} = 204.4 \text{ mm}^2$$

$$A_{st} = 97.12 \text{ mm}^2$$

min  $A_{st}$

$$\frac{As}{bd} = \frac{0.85}{f_y}$$

$$As = \frac{0.85 \times 85 \times 1000}{415}$$

$$As = 174.09 \text{ mm}^2$$

For (+ve) take  $A_{st}$  as this value

spacing for 10mm  $\phi$

$$\frac{\pi (10)^2}{4}$$

$$= 451.14 \text{ mm}$$

$$\frac{\pi (10)^2}{204.4} = 384.12 \text{ mm}$$

provide 300m clc

Theoretically

$$\frac{0.12}{100} \times b \times D$$

$$\frac{0.12}{100} \times 1000 \times 110 = 132 \text{ mm}$$

- ④ Design a slab of 200ms interior dimensions  $5 \times 8 \text{ m}$  whose any two adjacent sides are discontinuous carrying a live load of  $2.25 \text{ kN/m}^2$ . Use M20 & Fe415.

$$\frac{l}{d} = 80$$

$$\frac{5000}{d} = 80$$

$$d = 250 \text{ mm}$$

$$D = 250 + 25$$

$$D = 275 \text{ mm}$$

Load calculation

$$DL = 0.275 \times 25 = 6.875$$

$$LL = 2.25$$

$$FP = 0.5$$

$$W = 9.625 \text{ kN/m}^2$$

$$W_u = 14.43 \text{ kN/m}$$

$$l_e = 5 + \frac{d}{0.25} = 5.25$$

$$5 + (0.23) = 5.23$$

$$\frac{l_e(y)}{l_e(x)} = \frac{8.23}{5.23} = 1.57$$

$$\alpha_2(-ve) = 0.077$$

$$M_u = \alpha_2 w_u l_e^2 = 30.39$$

$$\alpha_2(+ve) = 0.057$$

$$M_u = 22.49$$

$$\alpha_4(-ve) = 0.047$$

$$M_u = 18.55$$

$$\alpha_4(+ve) = 0.035$$

$$M_u = 13.81$$

$$M_u = 0.87 f_y A_{st} d \left[ 1 - \frac{f_y A_{st}}{bd f_{ck}} \right]$$

$$30.39 \times 10^6 = 0.87 \times 415 A_{st} \times 250 \left[ 1 - \frac{415 A_{st}}{1000 \times 250 \times 20} \right]$$

$$30.39 \times 10^6 = 90262.5 A_{st} \left[ 1 - 8.3 \times 10^{-5} A_{st} \right]$$

$$30.39 \times 10^6 = 90262.5 A_{st} - 7.49 A_{st}^2$$

$$A_{st} = 346.30 \rightarrow -ve$$

$$A_{st} = 254.53 \rightarrow +ve$$

$$A_{st} = 209.14 \rightarrow -ve$$

$$A_{st} = 154.99 \rightarrow +ve$$

check for depth

$$M_u = 0.36 \left( \frac{\alpha_{umax}}{d} \right) \left[ 1 - 0.42 \left( \frac{\alpha_{umax}}{d} \right) \right] bd^2 f_{ck}$$

$$30.39 \times 10^6 = 0.36 \times 0.48 \left[ 1 - 0.42 \times 0.48 \right] \times 1000 \times d^2 \times 20$$

$$d = 104.94 \text{ mm}$$

$\therefore d$  is safe.

$F_r$	$M_u$	Ast	Min Ast
X (-ve)	30.39	346.65	330
(+ve)	22.49	257.53	330
Y (-ve)	18.55	209.14	330
(+ve)	13.81	154.9	330

$$\text{min } \text{Ast} = 0.12 \times b \times d$$

$$= \frac{0.12}{100} \times 1000 \times 275$$

spacing

$$\cancel{\frac{\pi(10)^2}{4}}$$

(+ve) Spacing.

$$\frac{0.12}{100} \times b \times d$$

$$\frac{0.12}{100} \times 1000 \times 275$$

$$= 330$$

$$\frac{\pi d^2}{4} \times 1000$$

$$= \frac{\pi(10)^2}{4} \times 1000 = 237.99$$

$$= 230 \text{ mm c/c.}$$

For (-ve spacing) which is bigger

$$\frac{0.12}{100} \times \frac{\pi d^2}{4} \times 1000 = \frac{\pi(10)^2}{4} \times 1000$$

$$346.3$$

$$= 226.7 \approx 220 \text{ mm c/c.}$$

check for deflection

$$\text{Act Ast} = \frac{\pi d^2}{4} \times 1000$$

Ast  $\rightarrow$  +ve steel value.

$$= \frac{\pi(10)^2}{4} \times 1000$$

230

$$\boxed{\text{Act Ast} = 341.47 \text{ mm}^2}$$

$$\frac{l}{d} = \frac{6000}{250} = 20 < 40 \therefore \text{deflection under control}$$

$$f_{sc} = 0.58 f_y \frac{A_{st}}{A_{ct}}$$

$$\text{Formation of } 0.58$$

$$= 0.58 \times 415 \times \frac{330}{341.37}$$

$$f_{sc} = 232.66 \text{ N/mm}^2$$

$$\frac{100 A_{st}}{bd} = \frac{100 \times 330}{250 \times 1000} = 0.13$$

$$F_1 = 2$$

$$F_2 = 1$$

$$F_3 = 1$$

$$\frac{5000}{250} = 40$$

$$20 < 40$$

Hence deflection is under control

$$P_t = \frac{100 A_{st}}{bd} = \frac{100 \times 346.65}{1000 \times 250} = 0.13$$

$$f_y = 0.58 f_y \frac{A_{st}}{A_{ct}} = 0.58 \times 415 \times \frac{330}{341.49} = 232.6 \text{ N/mm}^2$$

$$A_{ct} A_{st} = \frac{\pi \times 10^2}{4} \times 1000 = \frac{\pi \times 10^2}{4} \times 1000 = 341.44 \text{ mm}^2$$

## COLUMNS

There are three types of column:

1. Square column

2. Rectangular column

3. Circular column

Column can be differentiated into two types based on length by breadth ratio

If  $\frac{l}{b} \leq 12$  short column

If  $\frac{l}{b} > 12$  long column