

## MODULE - 3

### FLOW THROUGH SOILS

water strongly affects engineering behaviour of most kind of soils and water is an important factor. In most geotechnical engineering problems Hence it is essential to understand basic principles of flow of water through soil medium.

→ Flow of water takes place through interconnected pores between soil particles considered in one direction.

- \* Flow of water through soils may be laminar flow or a turbulent flow.
- \* In laminar flow, each fluid particle travels along a definite path which never process the path of any other particle.
- \* In turbulent flow, the paths are irregular and twisting, crossing and the crossing and twisting, crossing and the crossing problems the flow.
- \* In most soil mechanics problems the flow is considered laminar.

## permeability :-

The ease with which the water can flow through soil mass is permeable.

The study of seepage of water is important for the following engineering properties

- ① determination of settlement of a saturated compressible soil layer.
- ② calculation of seepage through the body of earthdams, and stability of source.
- ③ calculation of uplift pressure under hydraulic structures and their safety against piping.
- ④ Ground water flow towards walls and drainage of soils.

## DARCY'S LAW (French Scientist)

(H.P.G. Darcy)

The theory of seepage flow in porous media is based on generalization of Darcy's law.

\* Darcy's law is stated as "Velocity of

flow in porous media is proportional to the hydraulic gradient. [Flow is laminar]

$$Q = k i A$$

$Q$  = Discharge per unit time

$k$  = co-efficient of permeability ( $\text{mm/s}$ )

$i$  = Hydraulic gradient

$A$  = Total cross section area of soil

mass perpendicular to direction of flow.

Hydraulic gradient ( $i$ ) :-

It is defined as the loss of head per unit length of flow.

$$i = \frac{\Delta h}{L}$$

co-efficient of permeability :- [ $k$ ] :-

co-efficient of permeability of soil describes how easily a liquid will move through a soil hence it is also referred to as hydraulic conductivity.

\* This factor can be affected by the viscosity or thickness (fluidity) of a liquid and its density.

Water is also called neutronion fluid or ideal fluid.

SOIL TYPE	CO-EFFICIENT OF PERMEABILITY (mm/s)
① Coarse	$10 - 10^3$
② Fine Gravel, coarse and medium sand	$10^{-2} - 10$
③ Fine sand, loose silt	$10^{-4} - 10^{-2}$
④ Dense silt, clayey silt	$10^{-5} - 10^{-4}$
⑤ Silty clay, clay	$10^{-8} - 10^{-5}$

### Assumptions of Darcy's law :-

- \* The flow is laminar i.e. flow of fluids is described as laminar if a fluid particle flow follows a definite path and does not cross the path of other particles.
- \* Water in soil are incompressible i.e. continuity equation is assumed to be valid.
- \* The soil is saturated
- \* The flow is steady i.e. flow condition do not change with time.

### VALIDITY OR LIMITATIONS OF DARCY'S LAW

According to Darcy's law, the velocity of flow through soil mass is directly

proportional to the hydraulic gradient for laminar flow conditions only.

\* In practice one can expect the flow through to be always laminar in the case of fine grained soil deposits because of flow permeability. and hence low velocity of flow.

\* However in the case of sands and gravels flow will be laminar up to a certain value of velocity for each deposit and investigations have been carried out to find the limit of application of Darcy's law.

\* According to experimental investigation, flow through sands will be laminar and Darcy's law is valid as long as the Reynold's number expressed in the form shown below is less than or equal to unity.

$$\frac{V D_a \gamma_w}{\eta g} \leq 1$$

$V$  = velocity of flow in cm/s

$D_a$  = size of particles (avg) in cm

- \* It is found that the limiting value of Reynold's number taken as one is very approximate as its actual value can have wide variation.
- \* Depending partly on the characteristic size of particle used in the equation.

- \* The upper limit of effective size of particles can be taken as 3mm for Darcy's law to be valid.

### Factors affecting permeability :-

- ① Particle size :- Permeability of coarse soil is less than the fine soil.
- ② Structure of soil mass :-
- ③ Shape of particles :- Angular particles have less permeability than rounded particles.
- ④ Void ratio :- For higher void ratio, higher is the coefficient of permeability or hydraulic conductivity.

⑥ Properties of water :- Unit weight of water and viscosity affects permeability. Viscosity varies with temperature.

⑦ Degree of saturation :- Partially saturated soils have less permeability than fully saturated soils.

⑧ Absorbed water :- Absorbed water layer on particles is not free to move and this layer affects permeability.

⑨ Impurities in water :- Impurities in water tend to block or plug the flow passage of water and reduce the permeability of soil.

Determination of coefficient of permeability

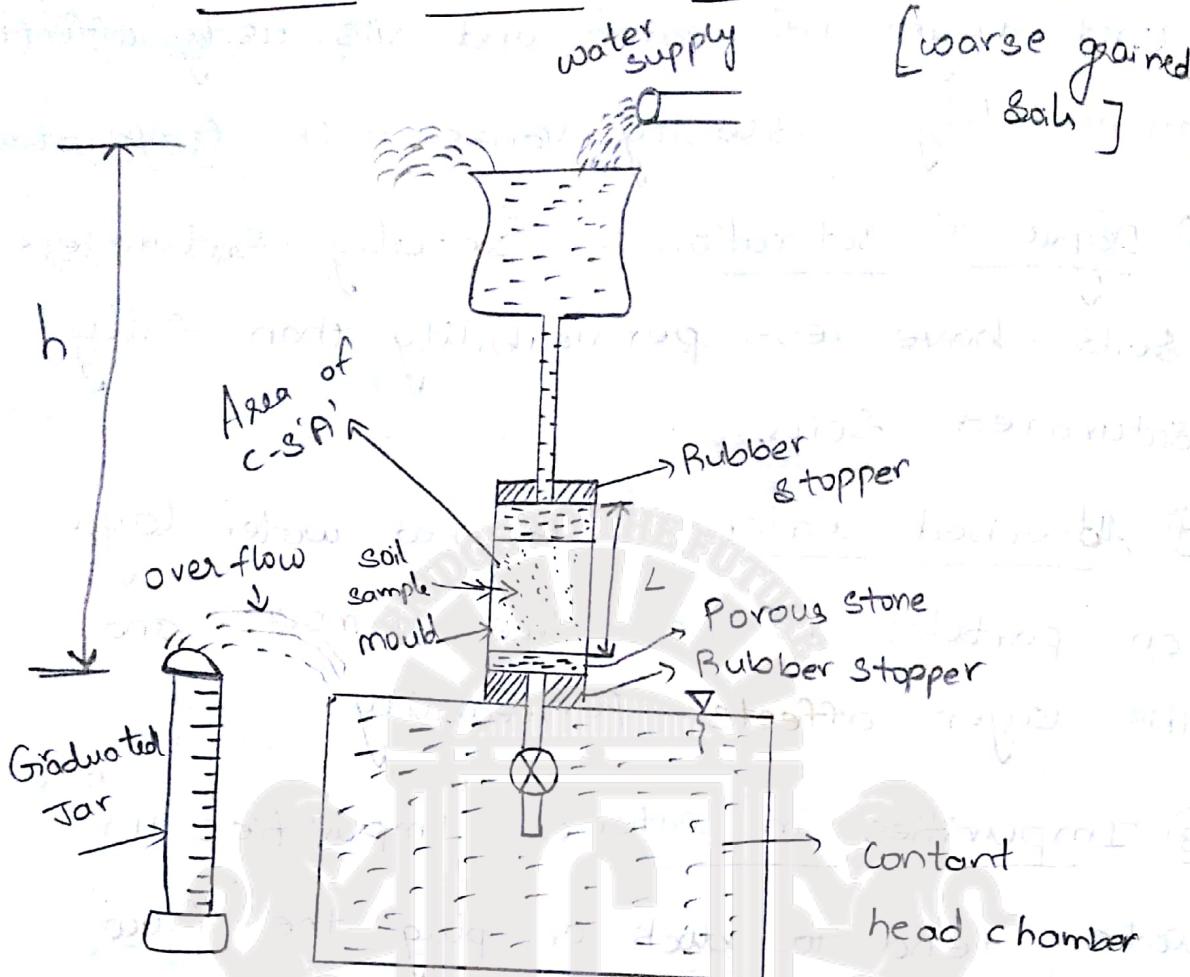
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LABORATORY TESTS :-

① Constant Head permeability

② Varying or Falling Head permeability

## CONSTANT HEAD PERMEABILITY



The constant head test is suitable for more permeable coarse grained soils. The basic laboratory test is shown in figure.

- \* The soil specimen is placed in cylindrical mould and constant head 'h' of water flowing through the soil is maintained by adjusting the supply.
- \* The out flow water is collected in a measuring cylinder and the duration of collection period is noted.

- \* Repeat the procedure of discharge of water through the Soil Sample for a Specific time period three times.
- \* From Darcy's law, The total quantity of flow 'Q' in time 't' can be given by

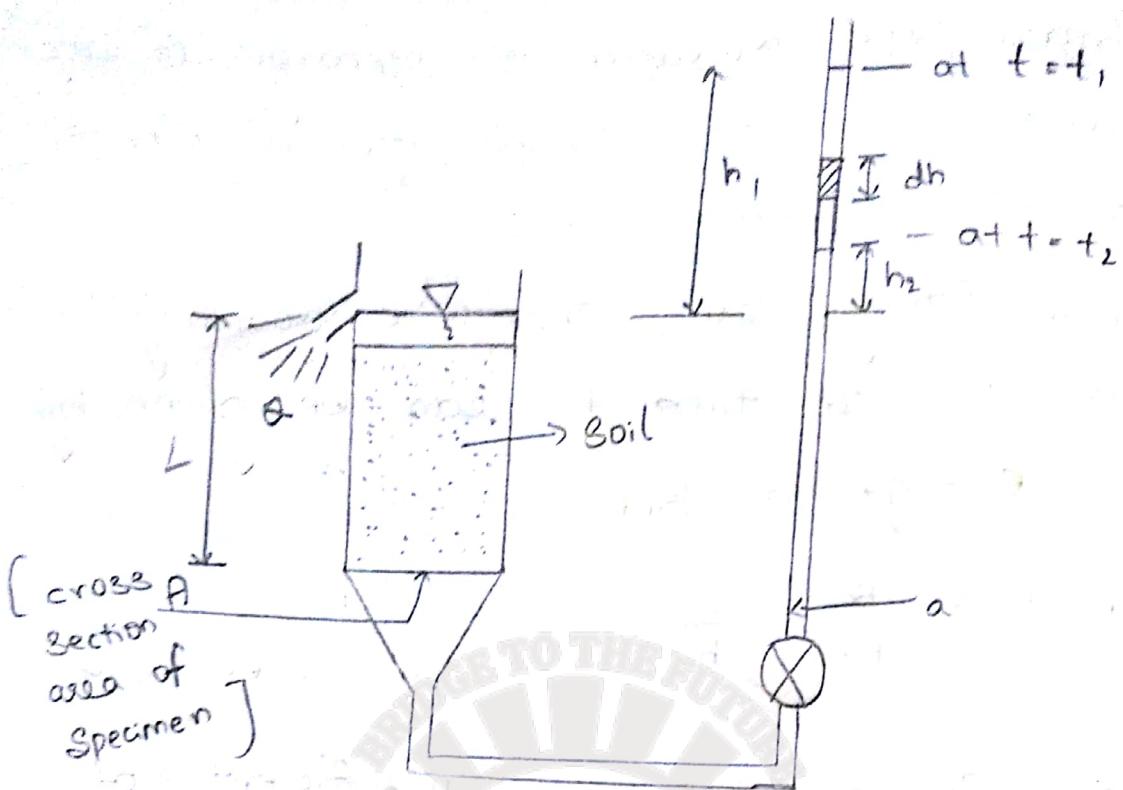
$$Q = q_t = k_i A t$$

$$\therefore k = \frac{Q}{A t} \cdot \frac{L}{h}$$

Note :- The knowledge of coefficient of permeability or hydraulic conductivity is much essential in solving problems involving yield of water bearing strata, Seepage through earthen dams and embankments of canal bank affected by seepage, settlement etc.,

Varying Variable or falling Head permeability

(Suitable for fine grained soils)



- \* The falling head permeability test is most suitable for fine grained soil.
- \* The figure shows the general laboratory arrangement for the test.
- \* The soil Specimen is placed inside the cube or mould and a stand pipe is attached to the top of the Specimen.
- \* water is allowed to flow through the soil Specimen.
- \* The initial head  $h_1$  at time  $t_1$  is recorded and water is allowed to flow through such that the final predetermined head ' $h_2$ ' at time ' $t_2$ ' is recorded.
- \* 3 or 4 trials are conducted.

\* The rate of flow of soil is

$$K = 2.303 \frac{aL}{At} \log_{10} \left( \frac{h_1}{h_2} \right)$$

$a$  = cross section area of pipe

$h_1$  = Initial head

$h_2$  = Final head

$$t = t_2 - t_1$$

$A$  = cross section area of the Specimen

$L$  = Length of Soil Specimen

Note - For a constant  $t$ , at two instances

let water level fall from  $h_1$  to  $h_2$  and

$h_2$  to  $h_3$  then  $h_2 = \sqrt{h_1 h_3}$

Need and scope of the experiment:-

- ① To estimate ground water flow
- ② To calculate seepage through dams
- ③ To find out rate of consolidation and settlement of structures
- ④ To plan the method of lowering the ground water table.
- ⑤ To calculate the uplift pressure and piping
- ⑥ To design the grouting
- ⑦ It is used for soil freezing test
- ⑧ To design sewage pits for recharging.

For very fine grained soils, capillarity permeability test is recommended.

### Determination of coefficient of permeability

#### FIELD TESTS

The co-efficient of permeability or hydraulic conductivity of a permeable layer can be determined by pumping from a well at a constant rate and observing the steady state water table in nearby observation wells. The steady state is established when the water levels in the test well and observation wells becomes constant.

\* when the water is pumped out from the well the aquifer gets depleted of water and the water table is lowered resulting in a circular depression in the phreatic surface, this is to refer to as drawdown curve or zone of depression.

Aquifer - A body of permeable rock which can contain or transulate ground water. An aquifer is an underground layer of water bearing

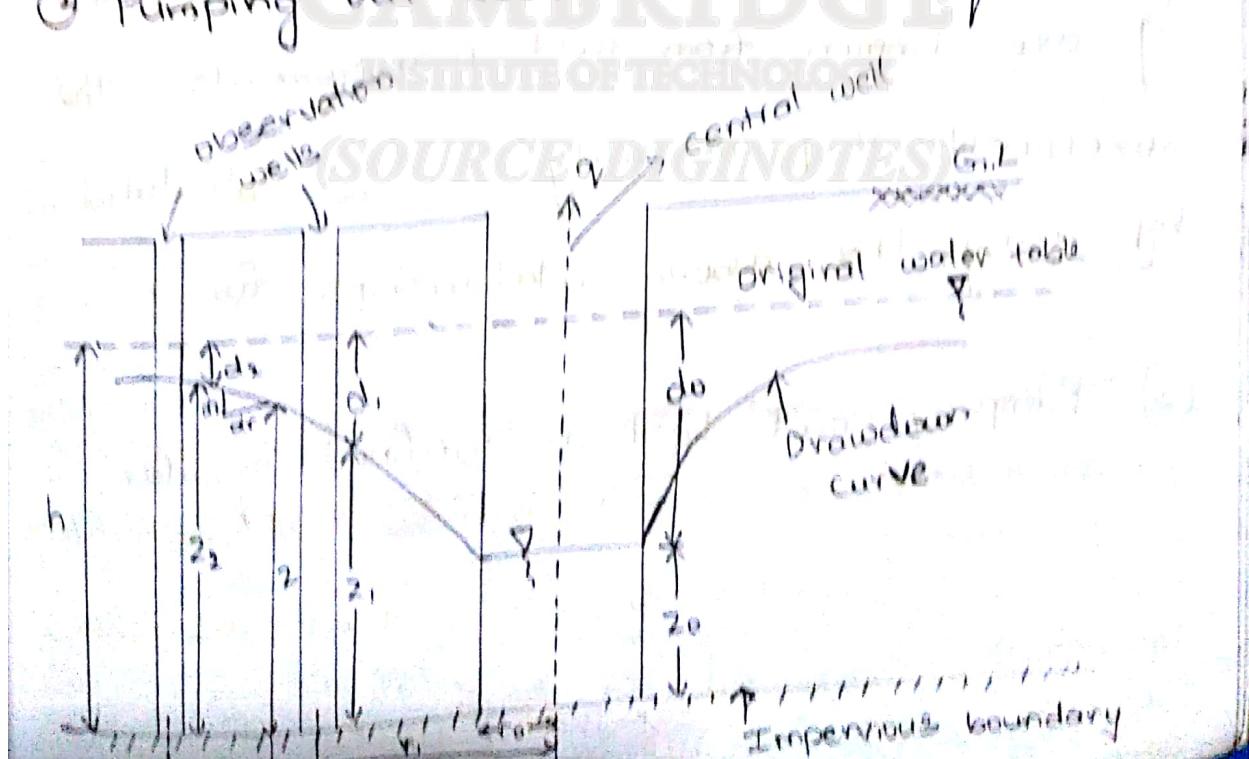
permeable rock, rock structures or unconsolidated materials from which ground water can be extracted using the water well.

### Assumptions made in field permeability test (in-situ)

- \* The aquifer is homogeneous
- \* Darcy's law is valid
- \* The flow is horizontal
- \* The well penetrates the entire thickness of the aquifer
- \* Natural ground water regime [confined] remains constant with time

### FIELD PERMEABILITY TEST

- ① Pumping out test in unconfined aquifer
- ② Pumping out test in confined aquifer



Let  $r$  and  $z$  be the radial distance and height above the impervious boundary at any point on the draw down curve as shown in figure. At steady state the rate of discharge due to pumping can be expressed as  $q = kia$ .

\* Hydraulic gradient at any point is given by Dupuit theory.

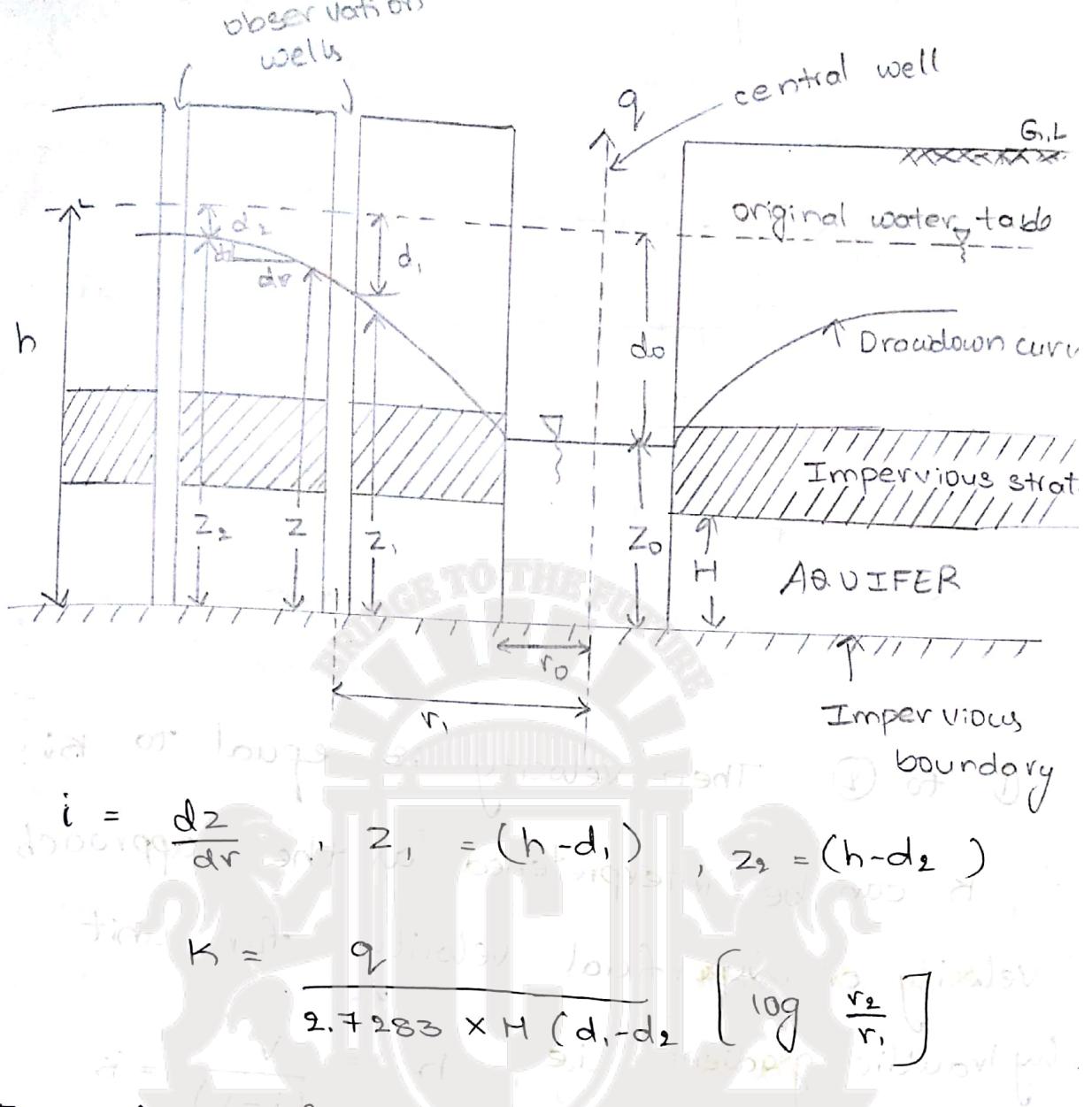
$$i = \frac{dz}{dr}$$

$$z_1 = (h - d_1), \quad z_2 = (h - d_2)$$

$$k = \frac{2.303 q}{\pi \left[ (d_1 - d_2) (2h - d_1 - d_2) \right] \left[ \log_{10} \frac{r_2}{r_1} \right]}$$

If the values of  $r_1$ ,  $r_2$  and  $z_1$ ,  $z_2$  and 'q' are known from field measurements, the co-efficient of permeability can be calculated by using the above relationships for 'k'.

② Pumping out test in confined aquifer



$$i = \frac{dz}{dr} \text{ and } z_1 = (h - d_1), z_2 = (h - d_2)$$

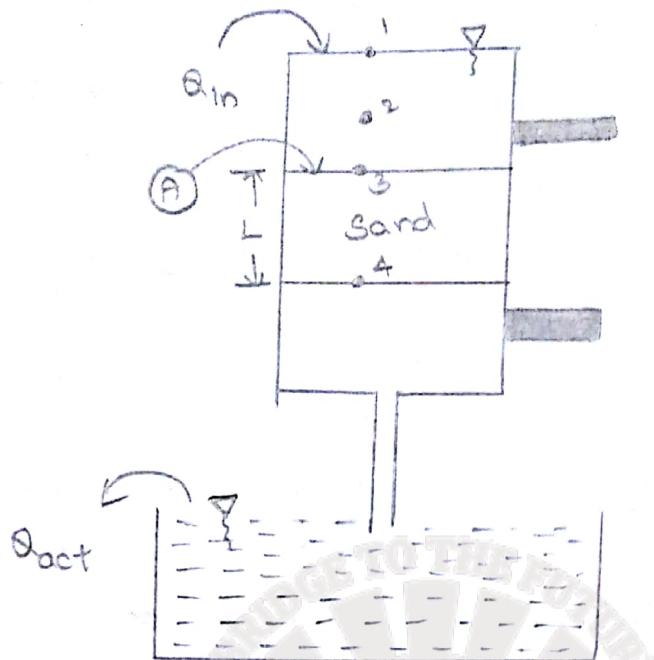
$$K = \frac{q}{2.7283 \times H (d_1 - d_2)} \left[ \log \frac{r_2}{r_1} \right]$$

The values of  $r_1, r_2, z_1, z_2$  and  $q$  are known from field measurements, the co-efficient of permeability can be calculated by using above relationship for  $K$ .

### Seepage velocity and Superficial velocity

Consider flow of water through soil medium of length ' $L$ ' and cross-sectional area ' $A'$ ' as shown in figure.

If ' $v_{seep}$ ' is the velocity of downward movement of drop of water from position



① to ② . Then velocity is equal to  $k_i$ .

$\therefore k$  can be interpreted as the approach velocity or superficial velocity for unit hydraulic gradient. i.e.,  $k = \frac{V}{(i=1)} = k$

Drop of water flow from position ③ to ④ at faster rate than it thus from positions ① to ② because the average area of flow through the soil is smaller. The actual velocity of water flowing through the voids is termed as Seepage velocity.

By the principle of continuity, the velocity of approach 'V' may be related to the seepage velocity or average effective velocity of flow  $V_s$ , by equating  $Q_{in}$

and  $Q_{out}$ .

$$Q_{out} = A_{out} V_s = A_{out} \frac{V}{n} = A_{out} \frac{AL}{AvL} = A_{out} \frac{V}{V_n}$$

$$V_s = \frac{V}{n} = \frac{A}{Av} = \frac{AL}{AvL} = \frac{V}{V_n}$$

$$V_s = \frac{V}{n} = \frac{1+e}{e} V = \frac{k_i}{n}$$

$V_s$  = Seepage velocity

$V$  = total volume of soil

$V_n$  = Volume of voids

$e$  = void ratio

$n$  = porosity

Thus Seepage velocity is the superficial velocity divided by the porosity. Above equations

indicates that the Seepage velocity is also proportional to the hydraulic gradient.

$$V_s = \frac{k_i}{n} i = \frac{(1+e)}{e} k_i$$

$$= k_p i$$

$$V_s \propto k_p$$

$k_p$  = coefficient of percolation

$$k_p = \frac{k}{n} \frac{(1+e)}{e} k$$

co-efficient of percolation: It is the

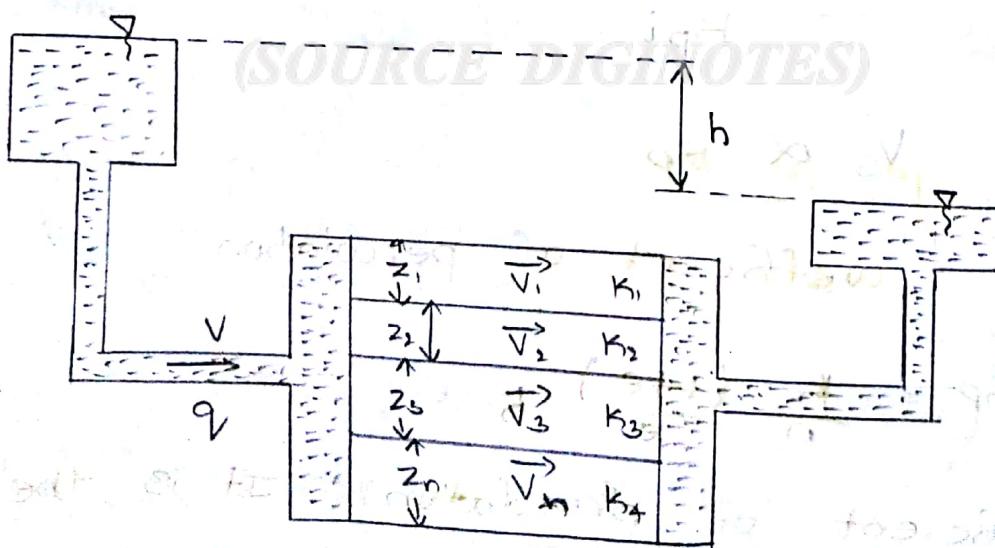
ratio of coefficient of permeability to the porosity.

## PERMEABILITY OF STRATIFIED SOILS

In nature soil mass may consist of several layers deposited one above the other. Their bedding planes may be horizontal, inclined or vertical. Each layer assumed to be homogeneous and isotropic, as its own value of permeability.

The average permeability of the whole deposit will depend upon the direction of flow with relation to the direction of bedding plane. We shall consider the cases of flow.

- ① Parallel to the bedding planes
- ② Perpendicular to the bedding planes
- ③ Average permeability parallel to the bedding planes



FLOW PARALLEL TO BEDDING PLANE

Let  $z_1, z_2, \dots, z_n$  is the thickness of the layers

$k_1, k_2, \dots, k_n$  = permeability of layers

For flow to be parallel to the bedding planes, the hydraulic gradient 'i' will be the same for all the layers. However since  $V = ki$  and since  $k$  is different, the velocity of flow will be different in different layers.

Let  $K_{oc}$  = average permeability of soil deposit parallel to the bedding plane.

Total discharge through the soil deposit is equal to sum of discharge through the individual layers.

$$dq/dz = q_1 + q_2 + \dots + q_n$$

$$q = K_{oc} iz = k_1 iz_1 + k_2 iz_2 + \dots + k_n iz_n$$

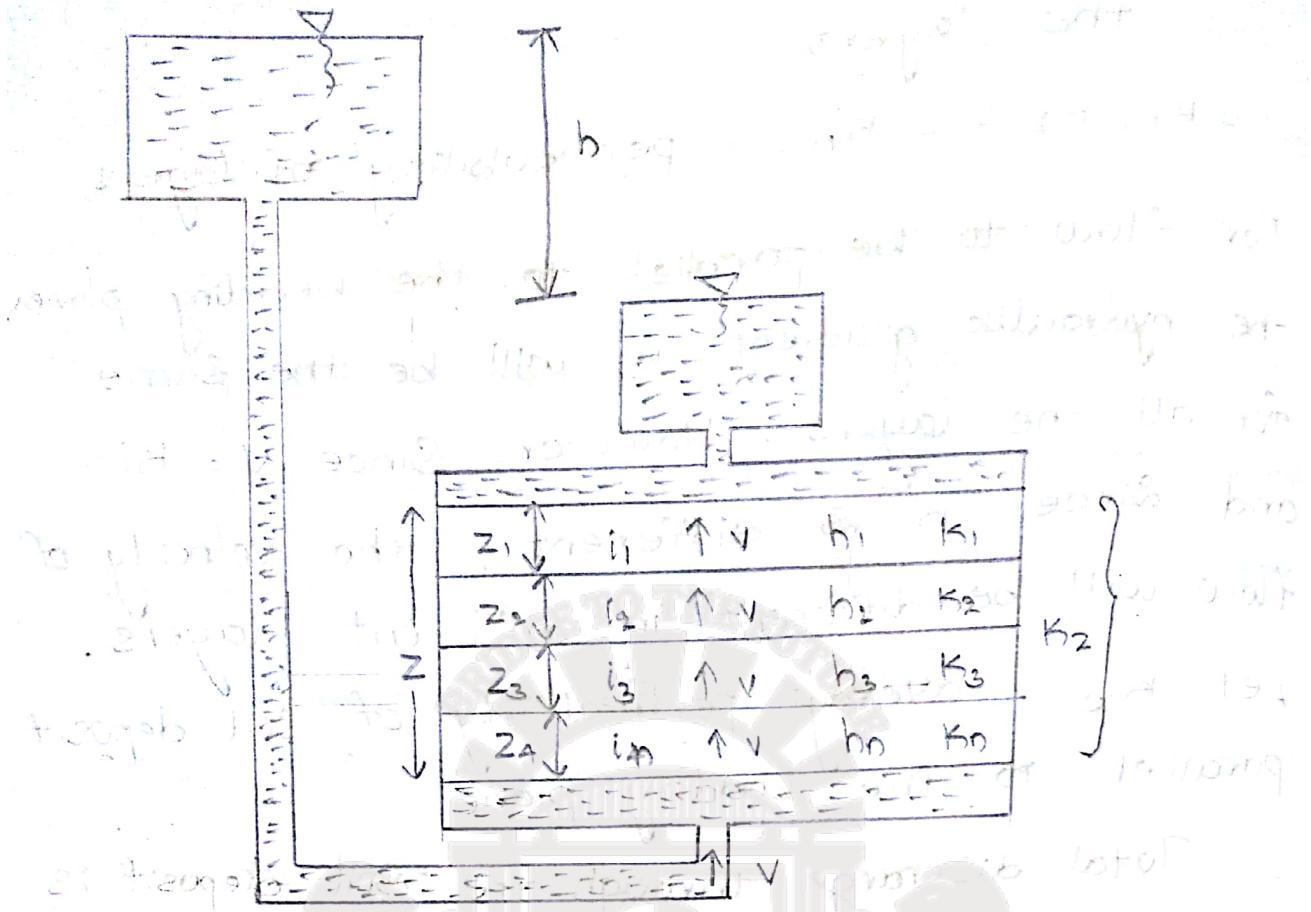
$$K_{oc} = \frac{k_1 z_1 + k_2 z_2 + \dots + k_n z_n}{z}$$

② Average permeability perpendicular to the bedding planes

$$\frac{d}{\sum} = i \Rightarrow \sum d = id$$

$$\frac{\sum d}{n} = id$$

$$\frac{n}{n} id = id$$



In this case the velocity of flow and hence the unit discharge will be the same through each layer. However the hydraulic gradient and hence the head loss through each layer will be different. Denoting the head loss through the layers  $h_1, h_2 + \dots + h_n$

$$h = h_1, h_2 + \dots + h_n$$

$$h = \text{total head} \quad i = \frac{h}{Z}$$

$$h_1 = i_1 z_1$$

$$h_2 = i_2 z_2$$

$$h_n = i_n z_n$$

$$h = i_1 z_1 + i_2 z_2 + \dots + i_n z_n$$

$$h_1 + h_2 + \dots + h_n$$

$k_2$  = Average permeability perpendicular to the bedding plane

$$V = k_2(i) = k_2\left(\frac{h}{z}\right)$$

(or)  $h = \frac{Vz}{k_2}$

Also,  $i_1 = \frac{V}{k_1}$ ,  $i_2 = \frac{V}{k_2}$

$$i_n = \frac{V}{k_n}$$

$$\frac{Vz}{k_2} = \frac{Vz_1}{k_1} + \frac{Vz_2}{k_2} + \dots + \frac{Vz_n}{k_n}$$

$$k_2 = \left( \frac{z}{\frac{z_1}{k_1} + \frac{z_2}{k_2} + \dots + \frac{z_n}{k_n}} \right)$$

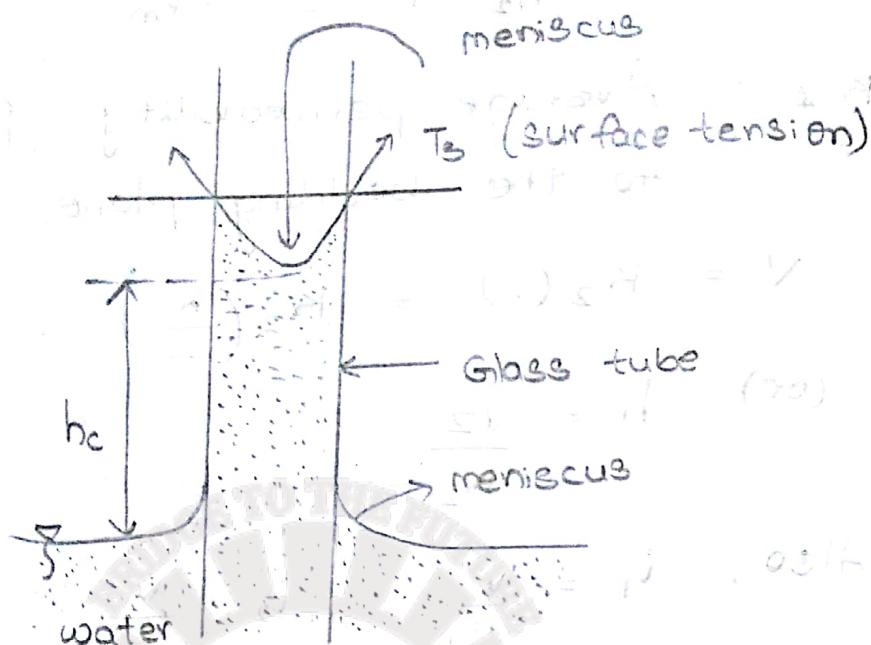
Average permeability parallel to bedding plane

$k_{oc}$  is greater than average permeability perpendicular to the bedding plane.

$$k_{oc} > k_2$$

$$\textcircled{1} > \textcircled{2}$$

## CAPILLARY PHENOMENA:



### Capillary water in Soil

capillary rise results from the combined actions of Surface tension and intermolecular forces between liquid and soil.

The rise of water in soils above the ground water table is comparable to the rise of water in to capillary tubes placed in a source of water but the void spaces in a soil are irregular in size and shape as they inter connect in all directions.

- \* The pressure on the water table level is zero, any water above this level must have a negative pressure.

\* In soils a negative core pressure increases the effective stress and varies with a degree of saturation.

Capillary rise in glass tube :-

For pure water and glass tube of very small diameter capillary rise is given by

$$h_c = \frac{4T_s}{d \gamma_w}$$

$T_s$  = Surface tension

$\gamma_w$  = unit weight of water

$d$  = diameter of capillary tube

$h_c$  = capillary rise in tube

The maximum negative pore pressure is

$$u = h_c \gamma_w = \frac{4T_s}{d}$$

The surface tension  $T_s$  of water at  $20^\circ C$

$$= 75 \times 10^{-3} \text{ KN/cm}$$

\* The pressure is zero when the soil voids are filled with air and is negative when

the voids are partly filled with water and air.

[In which case the surface tension forces operate to achieve a suction effect and the shear strength of the soil is increased]

# SEEPAGE ANALYSIS

## Two-dimensional flow

Flow is two dimensional if it can be assumed that the flow parameters vary in the direction of flow in one direction at right angles to this direction.

Fluid motion is said to be a two-dimensional flow when the flow velocity at every point is parallel to a fixed plane. The velocity on any point on a given normal to the fixed plane should be constant.

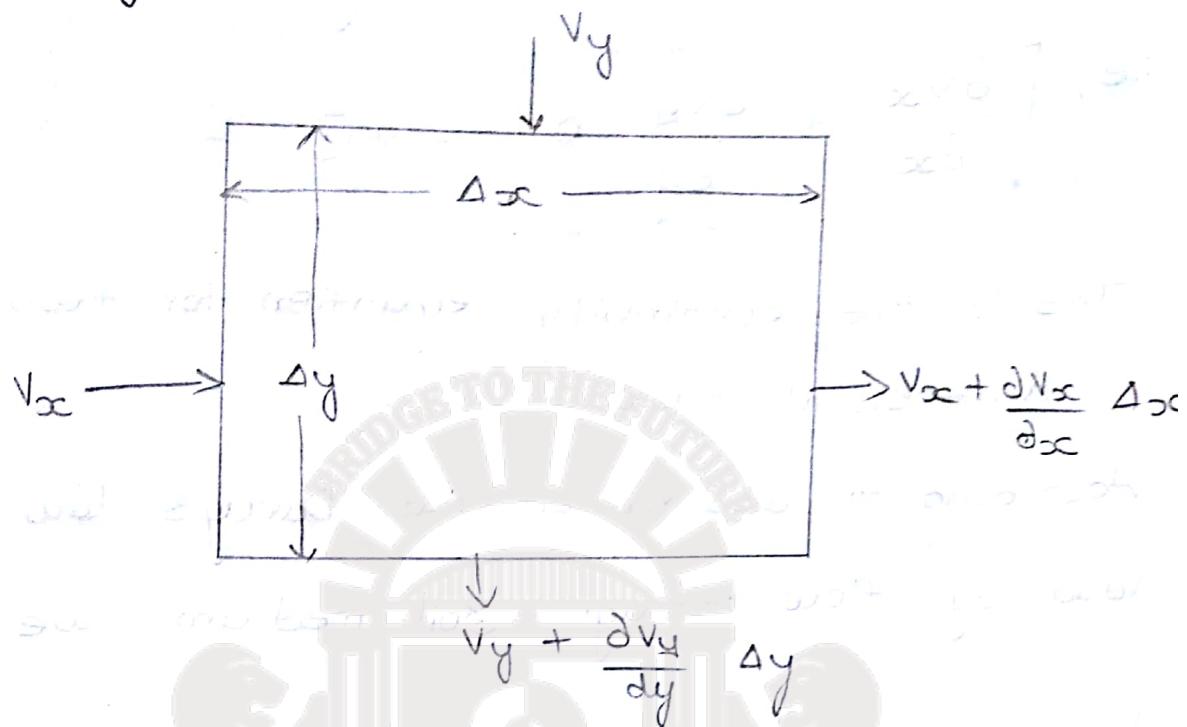
## LAPLACE EQUATION

### Two-dimensional flow

### Assumptions:-

- \* Laplace equation governs the flow of a fluid through a porous material.
- \* Flow is two dimensional.
- \* water and soil are incompressible
- \* Soil is isotropic and homogeneous
- \* The soil is fully saturated

- \* The flow is steady that is flow conditions do not change with time.
- \* Darcy's law is valid.



consider an element of size  $\Delta x$ ,  $\Delta y$  and of unit thickness perpendicular to the plane of figure. Let  $V_x$  and  $V_y$  be the velocity components

at entry in  $x$  and  $y$  directions, then the corresponding velocity components at exit will be

$(V_x + \frac{\partial V_x}{\partial x} \Delta x)$  and  $(V_y + \frac{\partial V_y}{\partial y} \Delta y)$ . According

to the assumption that quantity of water entering an element is equal to the quantity of water leaving the element in any given time.

we have,

$$V_x (\Delta y \cdot 1) + V_y (\Delta x \cdot 1) = \left( V_x + \frac{\partial V_x}{\partial x} \cdot \Delta x \right) (\Delta y \cdot 1) + \left( V_y + \frac{\partial V_y}{\partial y} \cdot \Delta y \right) (\Delta x \cdot 1)$$

i.e.,

$$\frac{\partial V_x}{\partial x} + \frac{\partial V_y}{\partial y} = 0 \quad \rightarrow ①$$

This is the continuity equation for two dimensional flow.

According to assumption that Darcy's law is valid by flow through soil medium, we have

$$V_x = k_{xc} \cdot i_{xc} = k_{xc} \frac{dh}{dx}$$

$$V_y = k_{cy} \cdot i_{cy} = k_{cy} \frac{dh}{dy}$$

$k_{xc}, k_{cy}$  = coefficient of permeability in  $x$  and  $y$  directions

By Substituting in eq<sup>n</sup> ①, we have

$$\left[ k_{xc} + \frac{\partial^2 h}{\partial x^2} \right] + \left[ k_{cy} + \frac{\partial^2 h}{\partial y^2} \right] = 0$$

For isotropic soil medium,

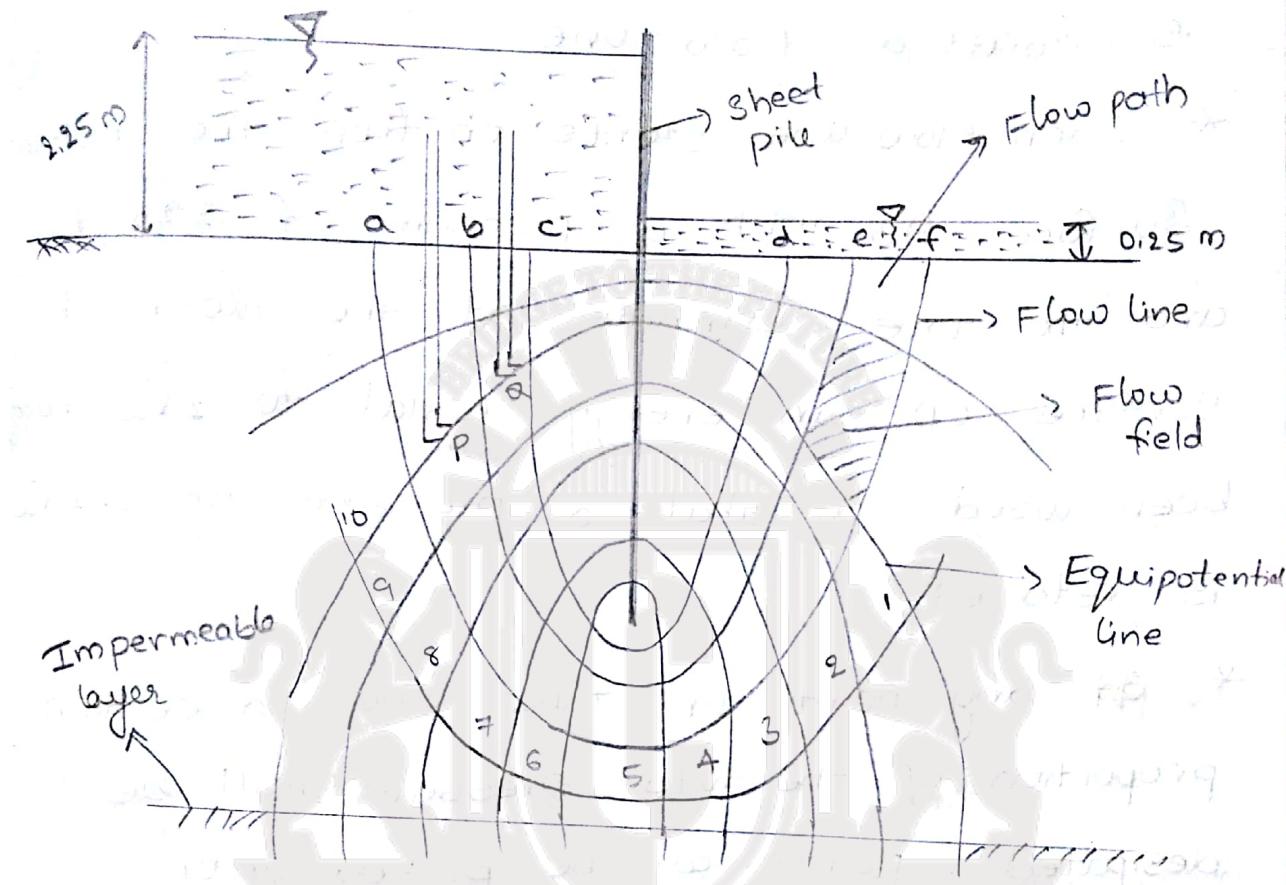
$$k_{xc} = k_{cy} = k$$

so the above equation reduces to form

$$\frac{\partial^2 h}{\partial x^2} + \frac{\partial^2 h}{\partial y^2} = 0$$

Laplace  
this is the equation for two dimensional  
sheet pipe flow.

## FLOW NETS



Above figure shows sheet pipe driven to a depth of 3 m. into pervious sand underlying by impermeable stratum. on one side of sheet pipe the depth of water is 2.25 m and on the other side, the depth of water is 0.25 m. Thus the head loss due to seepage due to soil is 2 m, between the two sides of the sheet pipe wall under this unbalanced head seepage flow takes place.

\* A particle of water enters sand at some

point on upstream, those below the tip of the sheet pipe and ends up at some point on downstream the flow path assumed by the particle of water in previous medium is called a flow line

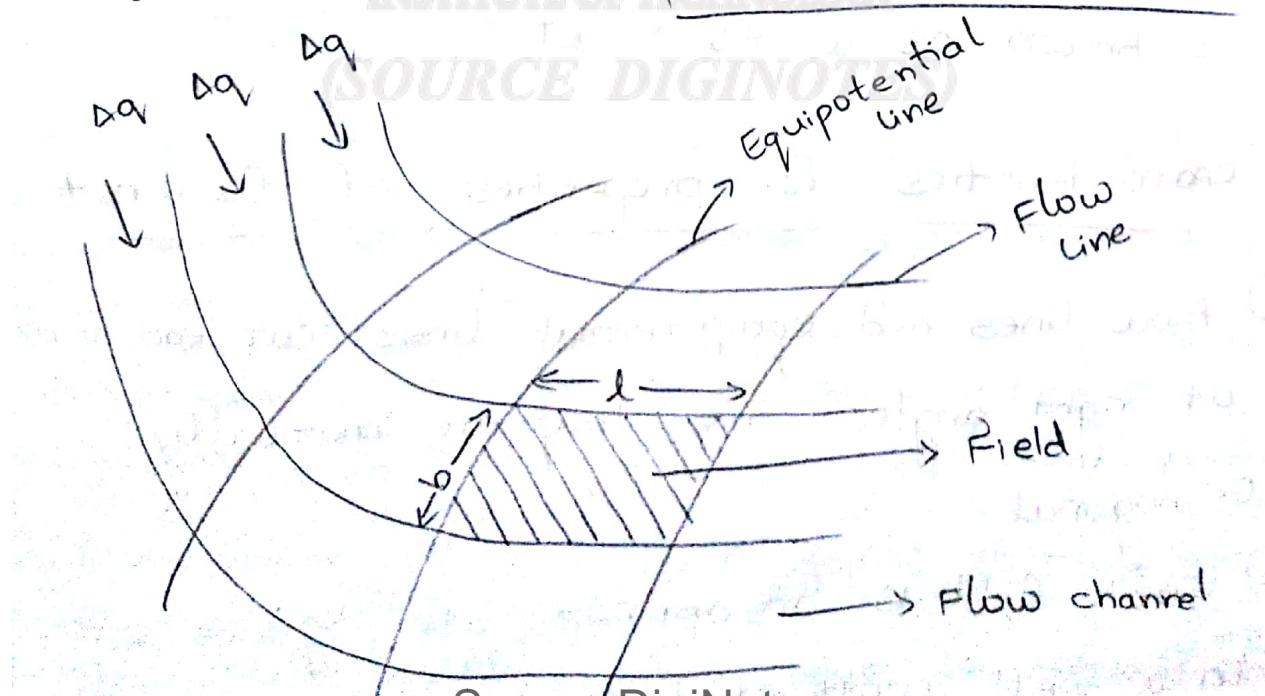
- \* Each flow line starts on from the upstream Surface AB with a pressure of  $2.25 V_w$  and the time terminates at the down side Surface CD, an energy equal to  $2V_w$  have been losted so that a pressure of  $0.25V_w$  is retained
- \* At any point on flow line, a certain proportion of the total pressure will be desipated. points can be picked upon different flow lines such as AB, CD etc where the head desipated during flow upto those point is equal to a given fraction of total head loss of 2m during the entire flow. if such points are joined, the line so obtained is called an equipotential line. on any equipotential line, the head available to cause the flow is same.

- \* If piezometers are inserted into the soil at different points along an equipotential

line, water would rise to the same elevation in all these piezometer at point P and Q on the equipotential line 10. It can be seen that the piezometric heads are different. It is the total head that remains the same.

\* The two sides of curves namely, the flow lines and the equipotential lines form a flow net which is a graphical representation of how the hydraulic energy is dissipated as a water flows through a pervious medium. The hydraulic gradient between two successive equipotential lines such as 10 and q is the head lost between these lines divided by the corresponding length of flow.

portion of a flow net



Flow channel:- The space between any two adjacent flow lines is called flow channel.

Field:- The space enclosed between two adjacent flow lines and two successive equipotential lines is called a field.

Equipotential line :- It is an imaginary line in a field of flow such that the total head is the same for all points on the line and therefore the direction of flow is perpendicular to the line at all points. or

An equipotential line is a contour or line joining points of equal potential or head

Flow net:- A grid obtained by drawing a series of stream lines and equipotential lines is known as a flow net.

characteristics for properties of flow net:-

- ① Flow lines and equipotential lines cut each other at right angles. i.e they are mutually orthogonal.
- ② Each field is an approximate square and in a well constructed flow net one should

be able to draw a circle in a field touching all the four sides.

(\*) In a homogeneous soil, every transition in the shapes of the two types of curves will be smooth being either elliptical or parabolic in shape. (\*) The rate of flow through each channel is same.

(\*) The same potential drop occurs between two successive equipotential lines.

### Uses of flownet :

- ① Estimation of seepage losses from reservoirs
- ② Determination of uplift pressures below dams
- ③ Checking the possibility of piping beneath dams
- ④ Pore-water pressure determination.

#### ① Estimation of seepage losses from reservoirs :

It is possible to use the flow net in the transformed space to calculate the flow underneath the dam.

#### ② Determination of uplift pressures below dams :

From the flow net, the pressure head at any point at the base of the dam can be determined. The uplift pressure distribution along the base can be drawn and then summed up.

#### ③ Checking the possibility of piping beneath dams

At the toe of a dam when the upward exit

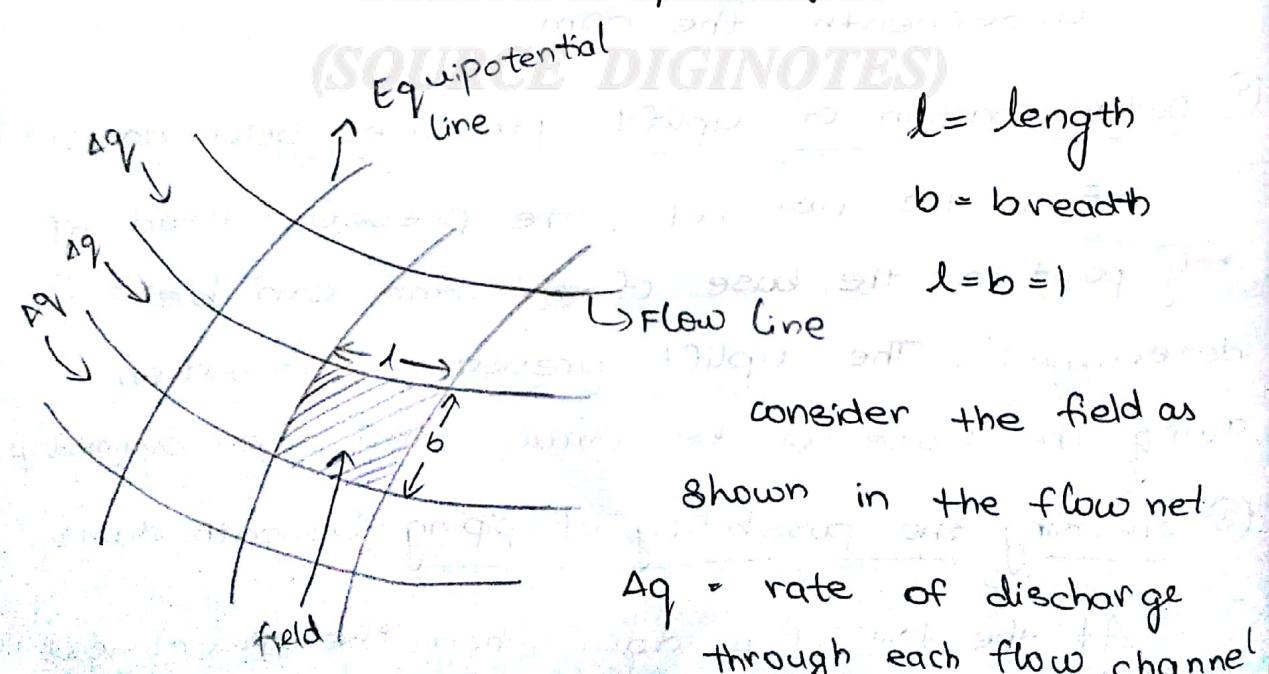
hydraulic gradient approaches unity, boiling conditions can occur leading to erosion in soil and consequent piping.

Many dams on soil foundations have failed because of a sudden formation of a piped shape discharge channel. As the stored water rushes out, the channel widens and catastrophic failure results. This is also referred to as piping failure.

#### (4) Pore - water pressure determination

pore water pressure at a given point due to seepage through an earth dam.

- (i) Quantity of Seepage
- (ii) Seepage pressure at a point
- (iii) Hydrostatic pressure at a point
- (iv) Exit gradient
- (v) Determination of quantity of seepage



$\Delta h$  = head drop per field

$$\Delta h = \frac{H}{N_d}$$

$H$  = Total head causing the flow

$N_d$  = Number of potential drops in the

entire flow net

$N_f$  = Number of flow channels for the complete flownet.

Applying Darcy's law, we have

$$Aq = K \cdot \frac{\Delta h}{l} (b \times 1)$$

$$Aq = K \cdot \frac{H}{N_d} \cdot \frac{b}{l}$$

For flow through entire flow net

$$q = Aq - N_f$$

$$q = K \cdot \frac{H}{N_d} \cdot N_f \cdot \frac{b}{l}$$

$$q = K \cdot H \left( \frac{N_f}{N_d} \right) \quad [\because b=1, l=1]$$

This equation is used for finding the

discharge

(ii) Determination of Seepage pressure at a point :-

Seepage pressure at a point,  $p_s$  is given by

$$P_s = h \gamma_w$$

$h$  = Total head at that point

$$h = (H - n \cdot \Delta h)$$

$H$  = Total head causing flow

$n$  = No. of potential drops upto the point under consideration

$\Delta h$  = potential head drop per field

$$= \frac{H}{Nd}$$

### i) Determination of Hydrostatic pressure at a point

The hydrostatic head at a point is given by,

$$h_w = h - z$$

$z$  = datum head at that point

$h$  = Total head at that point

$$= (H - n \cdot \Delta h)$$

$H$  = Total head causing flow

$n$  = No. of potential drops upto the point under consideration

$\Delta h$  = potential head drop per field =  $\frac{H}{Nd}$

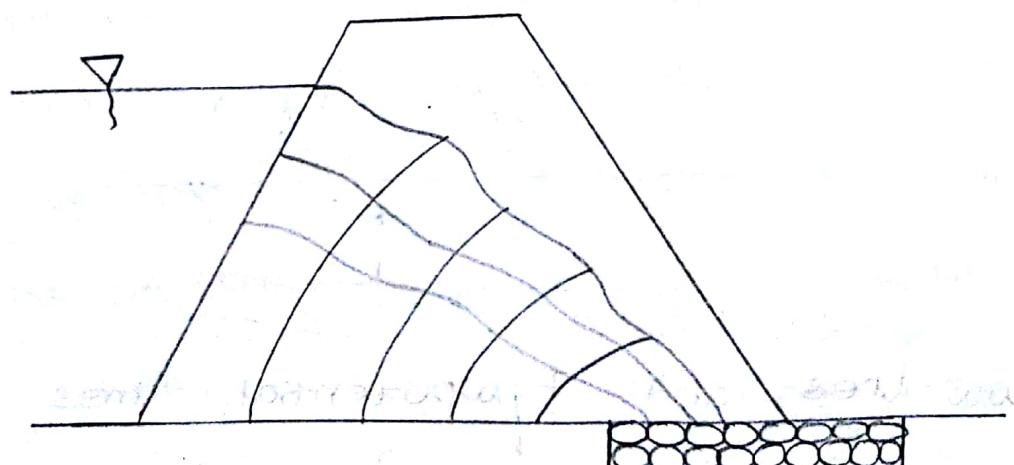
## Seepage through body of homogeneous earth dam

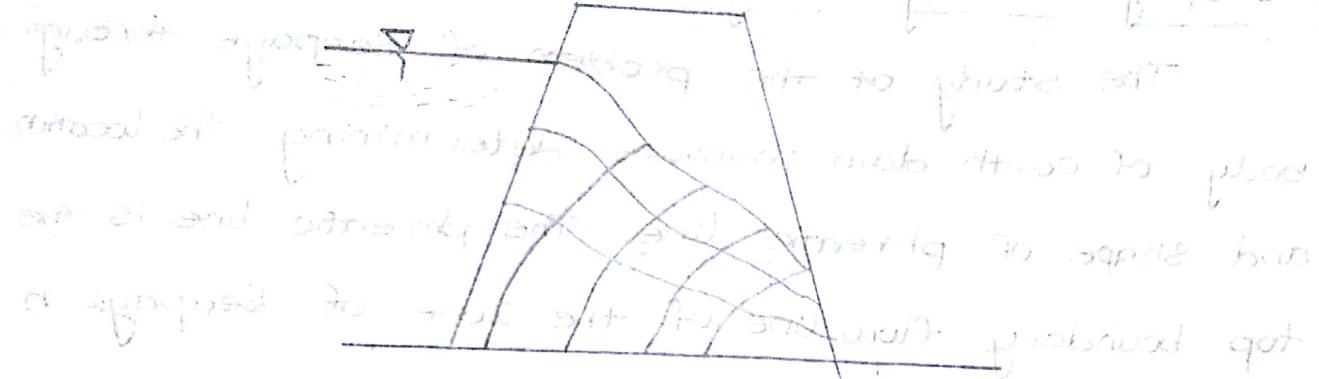
The study of the problem of seepage through body of earth dam involves determining the location and shape of phreatic line. The phreatic line is the top boundary flow line of the zone of seepage in section of earth dam.

Phreatic line can be located by

- ① Graphical method [casagrande's Graphical method]
- ② Analytical method
- ③ Experimental method

It is useful to note that there will be positive hydrostatic pressure whereas on the phreatic line, it is equal to atmospheric pressure. Once the phreatic line is located the flow net can be easily located.



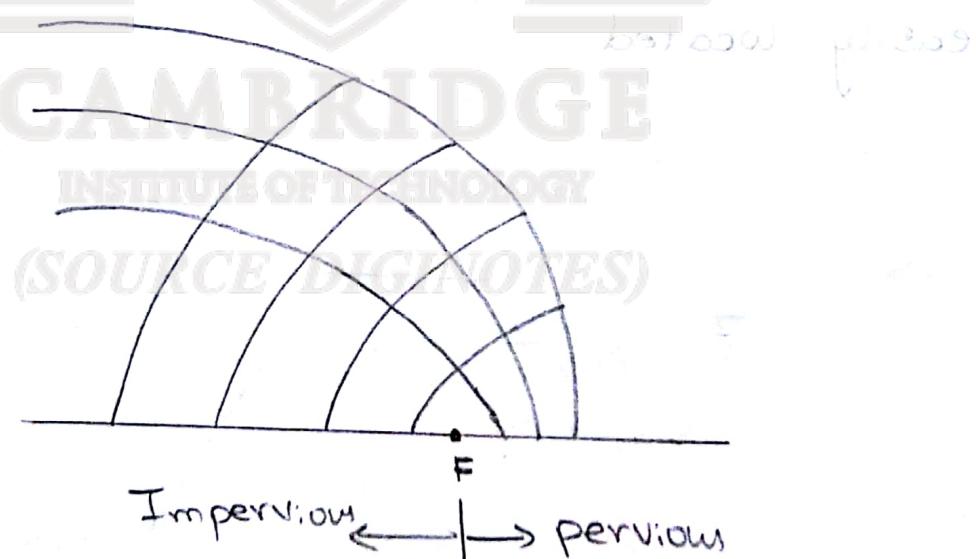


Flow through earth dam without toe filter  
and boundary at base and entry

### Casagrande's Graphical method

In casagrande method, to obtain a phreatic line the base parabola is corrected at entry and exit ends. it suit the boundary conditions

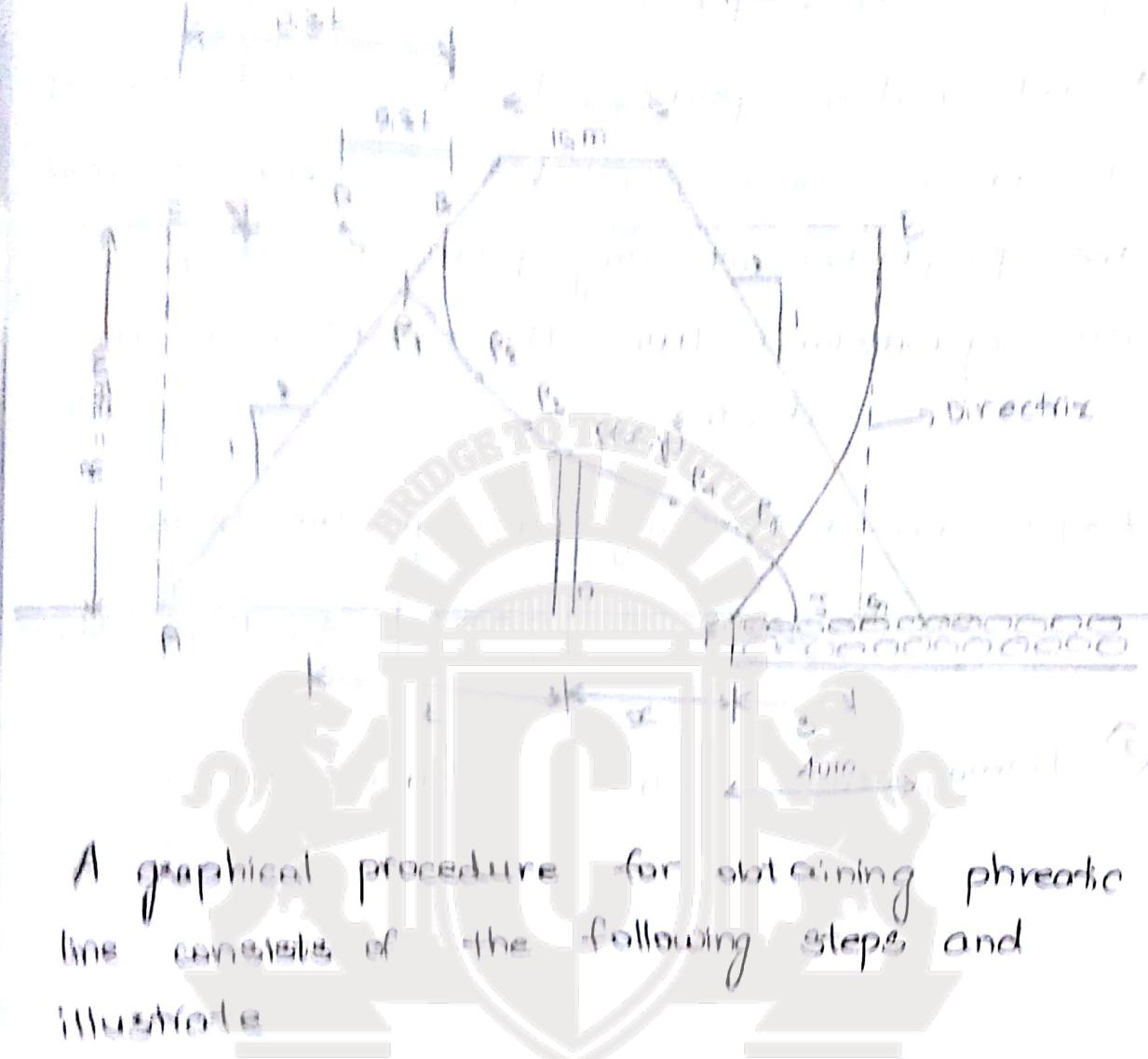
- ① Homogeneous Earth dam with horizontal filter.
- ② Homogeneous earth dam without filter.



Flow lines and Equipotential lines as

Confocal parabolae (F)

- ① Seepage through homogeneous earth dam with horizontal filter



- A graphical procedure for obtaining phreatic line consists of the following steps and illustrate
- Let  $AB$  be the wetted portion of seepage upstream face and  $CB$  be the projection of  $AB$  on the water line. Let  $CB = L$ . A point 'D' is marked on  $CB$  such that  $DB = 0.3L$ . Then 'D' will be the 1<sup>st</sup> point of base parabola.

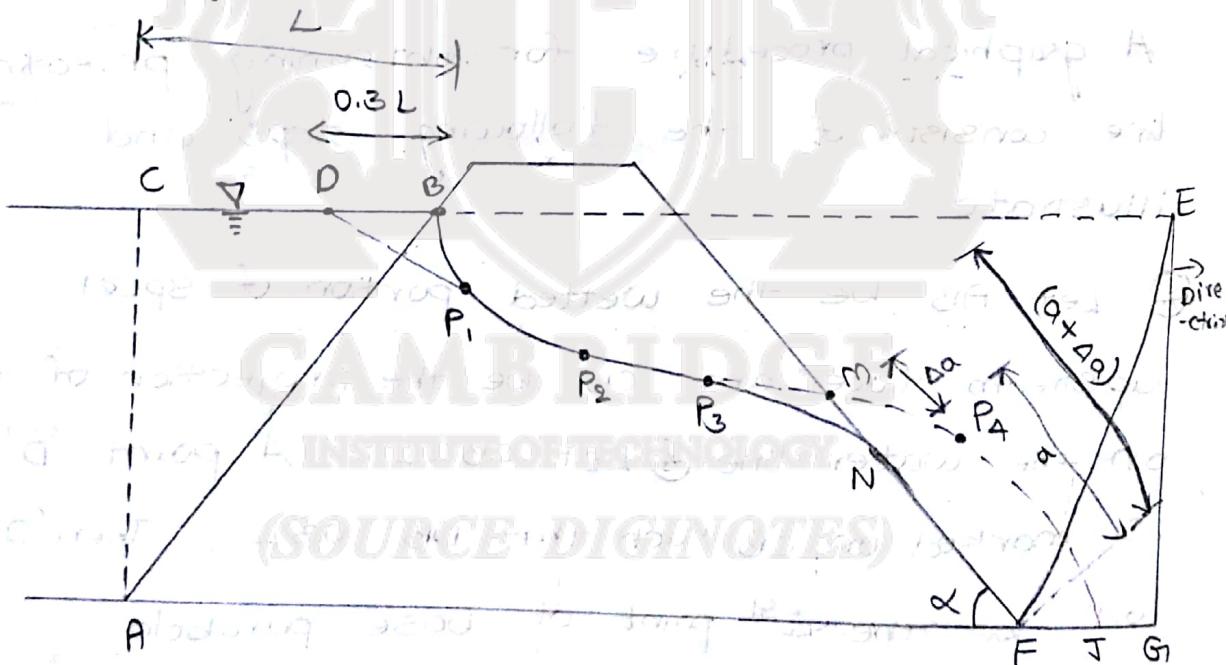
- The begining point 'F' of the filter will be the focus of the base parabola with 'D' as centre and  $DF$  as radius an arc is drawn to cut water line produced at 'B' through 'E'. Vertical line  $EG$  is drawn.  $EG$  will be the 1<sup>st</sup> ordinate of the base parabola.

- \* A midpoint 'J' of FG will be the last point of base parabola in the body of dam.
- \* Intermediate points  $P_1, P_2$  and  $P_3, P_4$  and  $P_5$  on the base parabola are obtained from the properties at any point on the parabola are equidistance from the focus and the directrix.

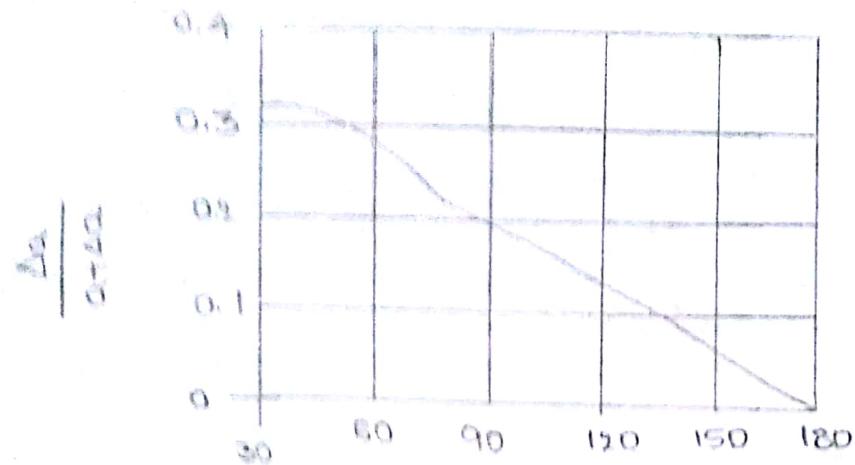
Expression of discharge through the body

of the dam =  $q = k s$   $s$  = focal distance

## ② Homogeneous Earth dam without filter



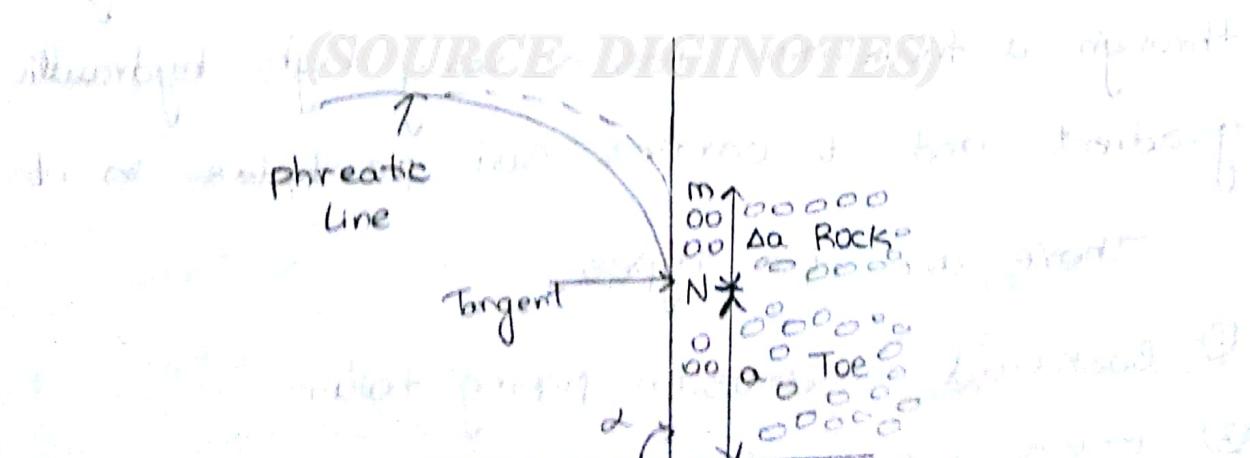
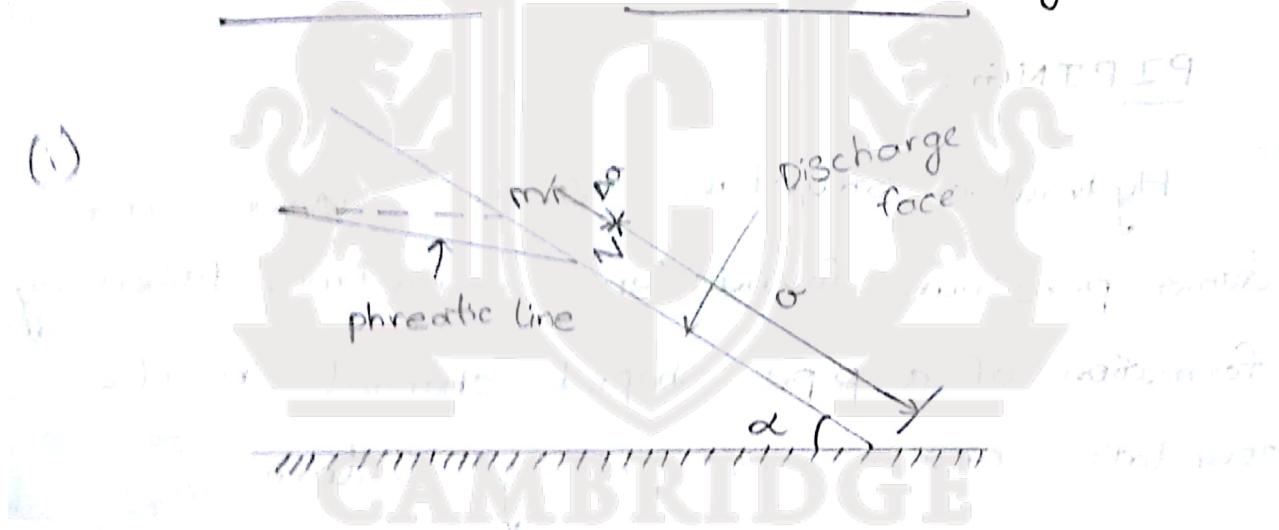
The portion NP is called discharge phase



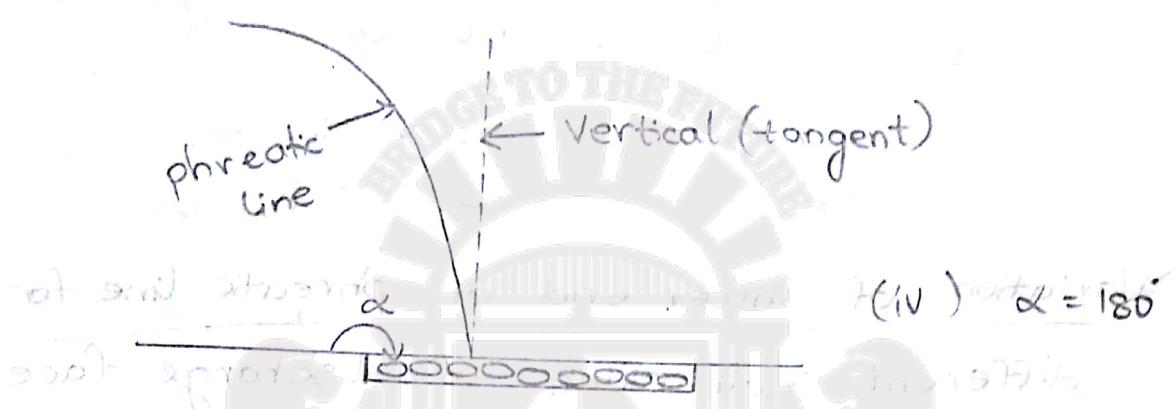
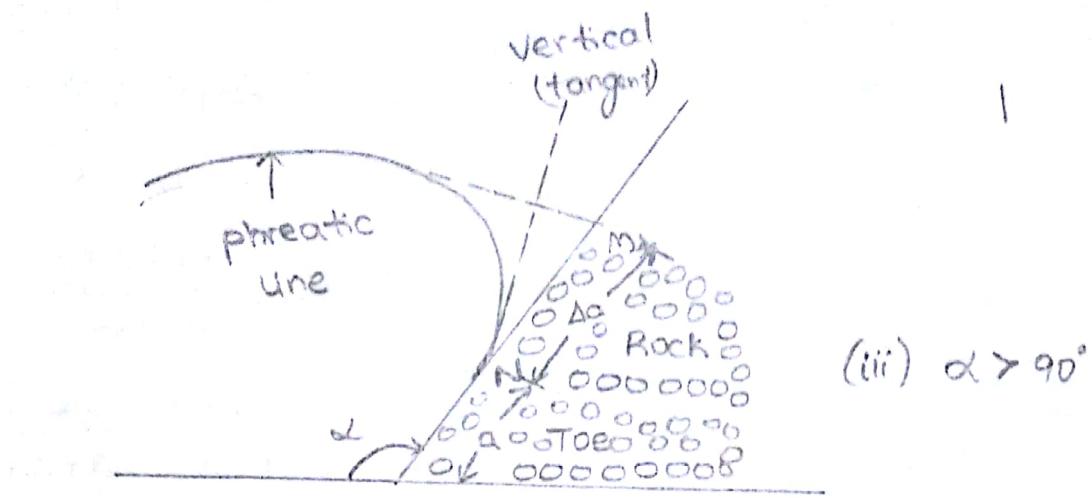
Relation  
between  $\alpha$   
and  $\frac{\Delta a}{\alpha + \Delta a}$

Angle of inclination  $\alpha$  in degrees

Variation of lower end of phreatic line for different inclinations of discharge face



(ii)  $\alpha = 90^\circ$



### PIPING :-

Hydraulic structures such as Weirs and dams on pervious foundations sometimes failed by formation of a pipe shaped channel in its foundation known as piping failure.

The failure occurs when water flowing through a foundation has a very high hydraulic gradient and it carries soil particles in it.

There are two types

- ① Backward - erosion piping failure
- ② Heave piping failure

Geostatic Stress :- Stress caused due to the self weight of soil

Effective Stress :- Stress due to self weight and external loading which leads to compression which again leads to decrease in void ratio and increase in frictional resistance.

Neutral Stress or pore pressure

Stress due to water present in core which tries to expel soil particles with same pressure in all the directions.

Total stress ( $\sigma$ ) = Effective stress + Neutral stress  
 $(\bar{\sigma})$  or pore pressure ( $u$ )

$$\sigma = \bar{\sigma} + u$$

Impact of effective stress in construction of structures

Effective stress plays an important role in

- ① Settlement of soil
- ② Shear strength of soil
- ③ Settlement of soil

The phenomenon of gradual reduction in soil due to expulsion of water from soil force is called consolidation or compression or settlement of soil.

\* As the effective stress strength increases, void ratio decreases. 3

## ② Shear Strength

Many geotechnical problems required an assessment of shear strength (a) structural foundation (b) Earth slope (c) Highway pavement

### (a) Structural Foundation:

Load from structure transferred to ground through foundation, this produces shear stress and compressive stress  
\* If shear stress is produced is more than the shear strength of soil which causes the structure to collapse.

### (b) Earth slope:

on a sloping ground, gravity produces shear stresses in soil of these stresses exceed the shear strength, a land slide occurs.

### (c) High way pavement:

wheel loads from vehicles are transferred to pavement to the ground. These loads produce shear stress which causes shear failure

## Quick Sand phenomenon :- [Quick condition]

In the case of upward flow of water through a soil mass, the seepage pressure acts in the upward direction causing reduction in effective stress. In case of submerged soil mass, the upward seepage pressure may become equal to downward pressure due to submerged weight of soil at a certain level.

When this happens in the case of cohesion less soil, the soil at that level loses all its strength as the effective stress becomes zero.

$$\begin{aligned}C_f &= c + \sigma' \tan \phi \\&= 0 + 0 (\tan \phi) \\&= 0\end{aligned}$$

$C_f$  → shear strength

$c$  → cohesion

$\sigma'$  → Effective stress

$\phi$  → angle of internal friction

Because of this, soil particles have tendency to be carried away by flowing water.

This phenomenon of lifting of soil particles

by flowing water is quick sand phenomenon.