

Egg drop C++

```
#include <iostream>
#include <climits>
using namespace std;

int eggDrop(int n, int k) {
    // Initialize a 2D array for DP table
    int dp[n + 1][k + 1]; // Array with (n + 1) rows and
    (k + 1) columns
    for (int i = 0; i <= n; i++) {
        for (int j = 0; j <= k; j++) {
            dp[i][j] = 0;
        }
    }

    // Fill the DP table
    for (int i = 1; i <= n; i++) {
        for (int j = 1; j <= k; j++) {
            if (i == 1) {
                dp[i][j] = j; // If only one egg is available, we
                need j trials
            } else if (j == 1) {
                dp[i][j] = 1; // If only one floor is there, one
                trial needed
            } else {
                int minDrops = INT_MAX;
                // Check all floors from 1 to j to find the
                minimum drops needed
                for (int floor = 1; floor <= j; floor++) {
                    int breaks = dp[i - 1][floor - 1]; // Egg
                    breaks, check below floors
                    int survives = dp[i][j - floor]; // Egg
                    survives, check above floors
                    int maxDrops = 1 + max(breaks,
                    survives); // Maximum drops needed in worst case
                    minDrops = min(minDrops, maxDrops); //
                    Minimum drops to find the critical floor
                }
                dp[i][j] = minDrops;
            }
        }
    }

    return dp[n][k]; // Return the minimum drops
    needed
}

int main() {
    int n = 4; // Number of eggs
    int k = 2; // Number of floors

    cout << eggDrop(n, k) << endl; // Output the
    minimum drops required
    return 0;
}
```

Step 1: Understanding the DP State

- $dp[i][j]$ = **Minimum number of trials** needed to find the critical floor with i eggs and j floors.
- If we have **1 egg**, we must check **each floor one by one** $\rightarrow dp[1][j] = j$
- If we have **1 floor**, only **1 trial** is needed $\rightarrow dp[i][1] = 1$

Step 2: Dry Run for $n = 4$ (eggs), $k = 2$ (floors)

We build the **DP table** from $dp[1][1]$ up to $dp[4][2]$.

Step 2.1: Initialize Base Cases

| $dp[i][j]$ | 0 Floors | 1 Floor | 2 Floors |
|------------|----------|---------|----------|
| 0 Eggs | 0 | 0 | 0 |
| 1 Egg | 0 | 1 | 2 |
| 2 Eggs | 0 | 1 | ? |
| 3 Eggs | 0 | 1 | ? |
| 4 Eggs | 0 | 1 | ? |

Step 2.2: Fill DP Table Using Recurrence

For $dp[i][j]$, we check all floors f from 1 to j , and take the worst-case minimum:

$$dp[i][j] = 1 + \min_{\forall f} (\max(dp[i-1][f-1], dp[i][j-f]))$$

Filling for $dp[2][2]$

- Try dropping from **floor 1**:
 - If **breaks**, check below: $dp[1][0] = 0$
 - If **survives**, check above: $dp[2][1] = 1$
 - **Max** $\rightarrow \max(0, 1) + 1 = 2$
- Try dropping from **floor 2**:
 - If **breaks**, check below: $dp[1][1] = 1$
 - If **survives**, check above: $dp[2][0] = 0$
 - **Max** $\rightarrow \max(1, 0) + 1 = 2$
- **Final Result:** $dp[2][2] = \min(2, 2) = 2$

Filling for $dp[3][2]$

- Try dropping from **floor 1**:
 - If **breaks**, check below: $dp[2][0] = 0$
 - If **survives**, check above: $dp[3][1] = 1$

- **Max** $\rightarrow \max(0,1) + 1 = 2$
- Try dropping from **floor 2**:
 - If **breaks**, check below: $dp[2][1] = 1$
 - If **survives**, check above: $dp[3][0] = 0$
 - **Max** $\rightarrow \max(1,0) + 1 = 2$
- **Final Result:** $dp[3][2] = \min(2,2) = 2$

Filling for $dp[4][2]$

- Try dropping from **floor 1**:
 - If **breaks**, check below: $dp[3][0] = 0$
 - If **survives**, check above: $dp[4][1] = 1$
 - **Max** $\rightarrow \max(0,1) + 1 = 2$
- Try dropping from **floor 2**:
 - If **breaks**, check below: $dp[3][1] = 1$
 - If **survives**, check above: $dp[4][0] = 0$
 - **Max** $\rightarrow \max(1,0) + 1 = 2$
- **Final Result:** $dp[4][2] = \min(2,2) = 2$

Final DP Table

| $dp[i][j]$ | 0 Floors | 1 Floor | 2 Floors |
|---------------|----------|---------|----------|
| 0 Eggs | 0 | 0 | 0 |
| 1 Egg | 0 | 1 | 2 |
| 2 Eggs | 0 | 1 | 2 |
| 3 Eggs | 0 | 1 | 2 |
| 4 Eggs | 0 | 1 | 2 |

Step 3: Final Answer

$dp[4][2] = 2$

Thus, the **minimum trials needed** to determine the critical floor with **4 eggs** and **2 floors** is **2**.

Output:-
2