# Egg drop C++ #include <iostream> #include <climits> using namespace std; int eggDrop(int n, int k) { // Initialize a 2D array for DP table int $dp[n + 1][k + 1] = \{0\}$ ; // Array with (n + 1) rows and (k + 1) columns // Fill the DP table for (int i = 1; $i \le n$ ; i++) { for (int j = 1; $j \le k$ ; j++) { if (i == 1) { dp[i][j] = j; // If only one egg is available, weneed j trials $else if (j == 1) {$ dp[i][j] = 1; // If only one floor is there, one trial needed } else { int minDrops = INT\_MAX; // Check all floors from 1 to i to find the minimum drops needed for (int floor = 1; floor $\leq$ j; floor++) { int breaks = dp[i - 1][floor - 1]; // Egg breaks, check below floors int survives = dp[i][j - floor]; // Egg survives, check above floors int maxDrops = 1 + max(breaks,survives); // Maximum drops needed in worst case minDrops = min(minDrops, maxDrops); // Minimum drops to find the critical floor dp[i][j] = minDrops;} } return dp[n][k]; // Return the minimum drops needed } int main() { int n = 4; // Number of eggs int k = 2; // Number of floors cout << eggDrop(n, k) << endl; // Output the minimum drops required

return 0;

}

#### Dry Run of the Program

Let's go through the dry run of the eggDrop function with n = 4 (number of eggs) and k = 2(number of floors).

### Input:

- n = 4 (number of eggs)
- k = 2 (number of floors)

## Step 1: Initialize the DP Table

The DP table is a 2D array of size  $(n+1) \times (k+1)$ :

int  $dp[n+1][k+1] = \{0\}$ ; // Array with 5 rows (0 to 4) eggs) and 3 columns (0 to 2 floors)

So, the DP table initially looks like this:

```
dp[0] = \{0, 0, 0\} // 0 eggs: impossible to drop
dp[1] = \{0, 0, 0\} // 1 egg
dp[2] = \{0, 0, 0\} // 2 \text{ eggs}
dp[3] = \{0, 0, 0\} // 3 \text{ eggs}
dp[4] = \{0, 0, 0\} // 4 \text{ eggs}
```

#### Step 2: Fill the DP Table

Case 1: One egg (i = 1)

If we have only one egg (i = 1), the number of trials needed to check all j floors is equal to j because we must start from the 1st floor and test each floor one by one. This is why dp[1][j] = j.

So, for i = 1:

- dp[1][1] = 1 (1 trial for 1 floor)
- dp[1][2] = 2 (2 trials for 2 floors)

At this point, the table looks like this:

```
dp[0] = \{0, 0, 0\}
dp[1] = \{0, 1, 2\}
dp[2] = \{0, 0, 0\}
dp[3] = \{0, 0, 0\}
dp[4] = \{0, 0, 0\}
```

Case 2: One floor (j = 1)

If we have only one floor (j = 1), then only 1 trial is needed, no matter how many eggs we have. So, for all i (eggs), dp[i][1] = 1.

At this point, the table becomes:

```
dp[0] = \{0, 0, 0\}
dp[1] = \{0, 1, 2\}
```

```
dp[2] = \{0, 1, 0\}

dp[3] = \{0, 1, 0\}

dp[4] = \{0, 1, 0\}
```

 Case 3: More than 1 egg and more than 1 floor (i > 1, j > 1)

Now, we compute the minimum number of trials for each i (eggs) and j (floors) by testing each floor from 1 to j and determining the worst-case number of drops.

For each floor floor:

- If the egg breaks, we look at the number of drops for i 1 eggs and floor 1 floors (dp[i 1][floor 1]).
- If the egg survives, we look at the number of drops for i eggs and j - floor floors (dp[i][j - floor]).
- The worst-case number of drops is 1 + max(breaks, survives).
- We want to minimize this worst-case number of drops.

Let's calculate the values for each combination of i and j.

## For i = 2, j = 2:

- Try floor 1:
  - If the egg breaks, check dp[1][0] (0 floors)  $\rightarrow 0$  drops.
  - o If the egg survives, check dp[2][1] (1 floor)  $\rightarrow$  1 drop.
  - So,  $\max(0, 1) + 1 = 2$  drops.

Therefore, dp[2][2] = 2.

The table becomes:

$$dp[0] = \{0, 0, 0\}$$

$$dp[1] = \{0, 1, 2\}$$

$$dp[2] = \{0, 1, 2\}$$

$$dp[3] = \{0, 1, 0\}$$

$$dp[4] = \{0, 1, 0\}$$

## For i = 3, j = 2:

- Try floor 1:
  - If the egg breaks, check  $dp[2][0] \rightarrow 0$  drops.
  - If the egg survives, check  $dp[3][1] \rightarrow 1 drop$ .
  - o max(0, 1) + 1 = 2 drops.

Therefore, dp[3][2] = 2.

The table becomes:  $dp[0] = \{0, 0, 0\}$  $dp[1] = \{0, 1, 2\}$  $dp[2] = \{0, 1, 2\}$  $dp[3] = \{0, 1, 2\}$  $dp[4] = \{0, 1, 0\}$ For i = 4, j = 2: • Try floor 1: o If the egg breaks, check dp[3][0]  $\rightarrow$ 0 drops. o If the egg survives, check dp[4][1]  $\rightarrow$  1 drop. o max(0, 1) + 1 = 2 drops.Therefore, dp[4][2] = 2. The table becomes:  $dp[0] = \{0, 0, 0\}$  $dp[1] = \{0, 1, 2\}$  $dp[2] = \{0, 1, 2\}$  $dp[3] = \{0, 1, 2\}$  $dp[4] = \{0, 1, 2\}$ Step 3: Output the Result The final value in dp[n][k] (i.e., dp[4][2]) is 2.

Output:-

So, the minimum number of trials needed to find the critical floor with 4 eggs and 2 floors is 2.