Optimize water distribution in C++ #include <iostream> #include <vector> #include <queue> #include <utility> using namespace std; class Pair { public: int vtx; int wt: Pair(int vtx, int wt) { this->vtx = vtx; this->wt=wt;bool operator>(const Pair& other) const { return this->wt > other.wt; } **}**; int minCostToSupplyWater(int n, vector<int>& wells, vector<vector<int>>& pipes) { vector < Pair >> graph(n + 1);for (const auto& pipe : pipes) { int u = pipe[0]; int v = pipe[1]; int wt = pipe[2]; graph[u].emplace_back(v, wt); graph[v].emplace_back(u, wt); for (int i = 1; $i \le n$; ++i) { graph[i].emplace_back(0, wells[i - 1]); graph[0].emplace_back(i, wells[i - 1]); int ans = 0; priority_queue<Pair, vector<Pair>, greater<Pair>> pq; pq.emplace(0, 0);vector < bool > vis(n + 1, false);while (!pq.empty()) { Pair rem = pq.top(); pq.pop(); if (vis[rem.vtx]) continue; ans += rem.wt; vis[rem.vtx] = true; for (const Pair& nbr : graph[rem.vtx]) { if (!vis[nbr.vtx]) { pq.push(nbr); } return ans; int main() { int v = 3, e = 2; vector \leq int \geq wells = $\{1, 2, 2\}$; vector<vector<int>> pipes = {{1, 2, 1}, {2, 3, 1}};

cout << minCostToSupplyWater(v, wells, pipes) <<</pre>

```
int v = 3, e = 2;
vector<int> wells = {1, 2, 2};
vector<vector<int>> pipes = {{1, 2, 1}, {2, 3, 1}};
```

- v = 3: Number of houses (vertices).
- wells = $\{1, 2, 2\}$: The cost to build a well at house 1, 2, and 3.
- pipes = {{1, 2, 1}, {2, 3, 1}}: The pipes connecting houses, with respective costs.

Step 1: Construct the Graph

We begin by creating an adjacency list that represents the graph, including both the pipes and wells.

• Graph Construction:

- Create an adjacency list graph with v + 1 = 4 nodes (including the virtual node 0).
- Add edges for the pipes between houses:
 - Pipe from 1 to 2 with cost 1.
 - Pipe from 2 to 3 with cost 1.
- Add edges for the wells:
 - Well for house 1 (cost 1), connect node 0 to node 1.
 - Well for house 2 (cost 2), connect node 0 to node 2.
 - Well for house 3 (cost 2), connect node 0 to node 3.

• Graph Representation:

```
Node 0 (virtual node) \rightarrow {(1, 1), (2, 2), (3, 2)}
Node 1 \rightarrow {(2, 1), (0, 1)}
Node 2 \rightarrow {(1, 1), (3, 1), (0, 2)}
Node 3 \rightarrow {(2, 1), (0, 2)}
```

Step 2: Prim's Algorithm with Min-Heap

We will use **Prim's Algorithm** to find the Minimum Spanning Tree (MST) with a priority queue (min-heap).

• **Priority Queue Initialization**: Start with node 0 (virtual node), which has no cost yet, so we push (0, 0) into the priority queue.

```
endl;
                                                                       Priority Queue: [(0, 0)]
  return 0;
                                                                       Step 3: First Iteration (start with
                                                                       node 0)
                                                                              Pop from the priority queue:
                                                                           0
                                                                               (0, 0) is popped, meaning we're
                                                                               at the virtual node 0 with a cost
                                                                               Visit Node 0 and explore its
                                                                               neighbors (nodes 1, 2, 3):
                                                                                       Add the edges to the
                                                                                       priority queue:
                                                                                                Edge (0 \rightarrow 1,
                                                                                                cost 1)
                                                                                                Edge (0 \rightarrow 2,
                                                                                                cost 2)
                                                                                                Edge (0 \rightarrow 3,
                                                                                                cost 2)
                                                                       After this step:
                                                                       Priority Queue: [(1, 1), (2, 2), (2, 3)]
                                                                       Visited nodes: [0]
                                                                       Total Cost: 0
                                                                       Step 4: Second Iteration (pop node
                                                                              Pop from the priority queue:
                                                                               (1, 1) is popped, meaning we're
                                                                               now at node 1 with a cost of 1.
                                                                               Visit Node 1 and explore its
                                                                               neighbors:
                                                                                       Node 0 has already been
                                                                                       visited, so ignore.
                                                                                       Add edge (1 \rightarrow 2, \cos t 1)
                                                                                       to the priority queue.
                                                                       After this step:
                                                                       Priority Queue: [(1, 2), (2, 3), (1, 2)]
                                                                       Visited nodes: [0, 1]
                                                                       Total Cost: 1
                                                                       Step 5: Third Iteration (pop node 2)
                                                                               Pop from the priority queue:
                                                                               (1, 2) is popped, meaning we're
                                                                               now at node 2 with a cost of 1.
                                                                               Visit Node 2 and explore its
                                                                               neighbors:
                                                                                       Node 1 has already been
                                                                                       visited, so ignore.
                                                                                       Node 3 is unvisited, so
                                                                                       add edge (2 \rightarrow 3, \cos t 1)
                                                                                       to the priority queue.
                                                                                       Node 0 has already been
                                                                                       visited, so ignore.
                                                                       After this step:
```

Priority Queue: [(1, 3), (2, 3), (1, 2)]

Visited nodes: [0, 1, 2] Total Cost: 2 Step 6: Fourth Iteration (pop node Pop from the priority queue: (1, 3) is popped, meaning we're now at node 3 with a cost of 1. Visit Node 3 and explore its neighbors: Node 2 has already been visited, so ignore. Node 0 has already been visited, so ignore. After this step: Priority Queue: [(2, 3)] Visited nodes: [0, 1, 2, 3] Total Cost: 3 **Step 7: Termination** The priority queue is empty, and all nodes are visited. Final Total Cost: 3. **Final Output** The minimum cost to supply water is: 3Output:-