LCA in C++ #include <iostream> using namespace std; // Definition of a binary tree node struct Node { int data; Node *left, *right; Node(int item) { data = item; left = nullptr: right = nullptr; **}**; // Function to find the Lowest Common Ancestor (LCA) of two nodes Node* getLCA(Node* root, int a, int b) { if (root == nullptr) { return nullptr; if $(root->data == a \mid \mid root->data == b)$ { return root; Node* lca1 = getLCA(root->left, a, b);Node* lca2 = getLCA(root->right, a, b); if (lca1!= nullptr && lca2!= nullptr) { return root; if (lca1 != nullptr) { return lca1; } else { return lca2; } // Function to create a binary tree and find LCA int main() { // Hardcoded tree construction Node* root = new Node(6); root->left = new Node(3);root->right = new Node(8); root->right->left = new Node(7);root->right->right = new Node(9); // Find LCA of nodes 3 and 7 Node* lcaNode = getLCA(root, 3, 7); cout << "Lowest Common Ancestor of 3 and 7 is: " << lcaNode->data << endl; // Clean up dynamically allocated memory delete root->right->right; delete root->right->left; delete root->left; delete root; return 0; }

Lowest Common Ancestor of 3 and 7 is: 6

Tree Structure:

You're finding the LCA of 3 and 7.

Q Dry Run of getLCA(root, 3, 7):

Function Call	Returns	Reason
getLCA(6, 3, 7)	→ 6	Found 3 in left subtree, 7 in right subtree → current is LCA
	→ 3	root->data == a (found node 3)
getLCA(8, 3, 7)	→ 7	found 7 in left subtree, right subtree (9) doesn't contain target
	→ 7	root->data == b (found node 7)
getLCA(9, 3, 7)	ightarrow nullptr	no match

Output:

Lowest Common Ancestor of 3 and 7 is: 6

Node at distance K in C++

```
#include <iostream>
#include <queue>
using namespace std;
// Definition of a binary
tree node
struct Node {
  int data;
  Node* left;
  Node* right;
  Node(int item) {
    data = item;
    left = nullptr;
    right = nullptr;
};
// Function declaration
printNodesDown(Node*
root, int k);
// Function to print nodes
at distance k from the
given node
int
nodes At Distance KWith Ro\\
otDistance(Node* root, int
node, int k) {
  if (root == nullptr) {
    return -1;
  // If the current node is
the target node, print
nodes at distance k from it
  if (root->data == node) {
printNodesDown(root, k);
    return 0;
  // Recursively search in
left subtree
  int leftHeight =
nodes At Distance KW ith Ro\\
otDistance(root->left,
node, k);
  if (leftHeight != -1) {
    // If the target node is
found in the left subtree
    if (leftHeight + 1 ==
k) {
       cout << root->data
<< endl;
    } else {
       // Print nodes at
distance k from the right
subtree
```

Binary Tree Structure:



Objective:

Print all nodes that are **exactly k=2 distance** away from node with value 3.

" Dry Run Table:

Ste p	Function Call	Curr ent Nod e	Action	Out	Retu rn Valu e
1	<pre>nodesAtDistanceK(root=2, node=3, k=2)</pre>	2	Call nodesAtDistanceKWith RootDistance		
2	<pre>nodesAtDistanceKWithRoot Distance(root=2, node=3, k=2)</pre>	2	Not target → search left and right		
3	<pre>nodesAtDistanceKWithRoot Distance(root=3, node=3, k=2)</pre>	3	© Target found! Call printNodesDown(3, 2)		0
4	<pre>printNodesDown(root=3, k=2)</pre>	3	Go down to distance 2		
5	<pre>printNodesDown(root=4, k=1)</pre>	4	Recurse to left → node 4		
6	<pre>printNodesDown(root=4, k=0)</pre>	4 (leaf)	Ø Distance 0 → print 4	4	
7	<pre>printNodesDown(root=8, k=1)</pre>	8	No children		
8	Back to step 2, leftHeight = 0		Check if root (2) is at k=2? No → Call printNodesDown(right , k-2)		
9	<pre>printNodesDown(root=9, k=0)</pre>	9	Ø Distance 0 → print 9	9	
10	All done		Final output = 4, 9		

```
printNodesDown(root-
>right, k - leftHeight - 2);
    return leftHeight + 1;
  }
  // Recursively search in
right subtree
  int rightHeight =
nodes At Distance KWith Ro\\
otDistance(root->right,
node, k);
  if (rightHeight != -1) {
    // If the target node is
found in the right subtree
    if (rightHeight + 1 ==
k) {
       cout << root->data
<< endl;
    } else {
       // Print nodes at
distance k from the left
subtree
printNodesDown(root-
>left, k - rightHeight - 2);
    return rightHeight +
1;
  }
  // If the target node is
not found in either subtree
  return -1;
}
// Function to print nodes
at distance k from a given
node downwards
void
printNodesDown(Node*
root, int k) {
  if (root == nullptr | | k
< 0) {
    return;
  }
  // If reached the
required distance, print
the node
  if (k == 0) {
    cout << root->data <<
endl;
    return;
  // Recursively print
nodes at distance k in both
subtrees
  printNodesDown(root-
>left, k - 1);
```

```
∜ Final Output:
```

9

```
printNodesDown(root-
>right, k - 1);
// Function to initiate
printing nodes at distance
k from a given node value
nodesAtDistanceK(Node*
root, int node, int k) {
nodesAtDistanceKWithRo
otDistance(root, node, k);
int main() {
  // Hardcoded tree
construction
  Node* root = new
Node(2);
  root->left = new
Node(3);
  root->left->left = new
Node(4);
  root->left->right = new
Node(8);
  {\tt root\text{-}}{\tt left\text{-}}{\tt left\text{-}}{\tt left} =
new Node(4);
  root->right = new
Node(9);
  root->right->right =
new Node(2);
  root->right->right->left
= new Node(6);
  // Call function to print
nodes at distance k from
node with value 3
  nodesAtDistanceK(root,
3, 2);
  // Clean up dynamically
allocated memory
  delete root->right-
>right->left;
  delete root->right-
>right;
  delete root->right;
  delete root->left->left-
>left;
  delete root->left->left;
  delete root->left->right;
  delete root->left:
  delete root;
  return 0;
```

9

Size,Sum,Max,Min,Height in C++

```
#include <iostream>
#include <algorithm>
#include <climits>// for std::max
using namespace std;
// Definition of a binary tree node
struct Node {
  int data;
  Node* left;
  Node* right;
  Node(int data, Node* left = nullptr, Node* right =
nullptr) {
    this->data = data;
    this > left = left;
    this->right = right;
  }
};
// Function to calculate the size (number of nodes) of
the binary tree
int size(Node* node) {
  if (node == nullptr) {
    return 0;
  } else {
    return 1 + size(node->left) + size(node->right);
}
// Function to calculate the sum of all nodes in the
binary tree
int sum(Node* node) {
  if (node == nullptr) {
    return 0;
  } else {
    int lsum = sum(node-> left);
    int rsum = sum(node->right);
    return node->data + lsum + rsum;
}
// Function to find the maximum value in the binary
tree
int max(Node* node) {
  if (node == nullptr) {
     return INT_MIN; // from <climits> for INT_MIN
  } else {
    int lmax = max(node-> left);
    int rmax = max(node->right);
    return std::max(node->data, std::max(lmax,
rmax));
}
// Function to calculate the height of the binary tree
int height(Node* node) {
  if (node == nullptr) {
    return -1;
  } else {
    int lh = height(node->left);
```

Binary Tree Structure:

```
50

/ \

25 75

/ \ / \

12 37 62 87

/ \

30 70
```

♥ Expected Outputs:

Function	Description	Output
size	Number of nodes	9
sum	Sum of all node values	448
max	Maximum value in the tree	87
height	Height of the tree (edges, not nodes)	3
display	Inorder traversal (left \rightarrow root \rightarrow right)	12 25 30 37 50 62 70 75 87

Let's go through function results step-bystep:

1. size(root):

Total nodes = 9

2. sum(root):

```
= 50 + \text{sum}(25 \text{ subtree}) + \text{sum}(75 \text{ subtree})

= 50 + (25 + 12 + 37 + 30) + (75 + 62 + 70 + 87)

= 50 + 104 + 294

= 448
```

3. max(root):

- Max in left subtree = max(25, 12, 37, 30) = 37
- Max in right subtree = max(75, 62, 70, 87)
- Final max = max(50, 37, 87) = 87

4. height(root):

• Longest path (e.g., $50 \rightarrow 75 \rightarrow 62 \rightarrow 70$) has $3 \text{ edges} \rightarrow \text{height} = 3$

5. display(root) (Inorder):

Left subtree (25): 12 25 30 37

Root: 50

Right subtree (75): 62 70 75 87 => Full: 12 25 30 37 50 62 70 75 87

```
int rh = height(node->right);
    return 1 + std::max(lh, rh);
  }
}
// Function to display the binary tree (inorder
traversal)
void display(Node* node) {
  if (node == nullptr) {
    return;
  }
  display(node->left);
  cout << node->data << " ";
  display(node->right);
}
int main() {
  // Hardcoded tree construction
  Node* root = new Node(50);
  root->left = new Node(25);
  root->left->left = new Node(12);
  root->left->right = new Node(37);
  root->left->right->left = new Node(30);
  root->right = new Node(75);
  root->right->left = new Node(62);
  root->right->left->right = new Node(70);
  root->right->right = new Node(87);
  // Calculating size, sum, max value, and height
  int treeSize = size(root);
  int treeSum = sum(root);
  int treeMax = max(root):
  int treeHeight = height(root);
  // Displaying results
  cout << "Size of the binary tree: " << treeSize <<
endl;
  cout << "Sum of all nodes in the binary tree: " <<
treeSum << endl:
  cout << "Maximum value in the binary tree: " <<
treeMax << endl;
  cout << "Height of the binary tree: " << treeHeight
<< endl:
  // Displaying the binary tree (inorder traversal)
  cout << "Inorder traversal of the binary tree:" <<
endl:
  display(root);
  cout << endl;
  // Clean up dynamically allocated memory
  delete root->right->left->right;
  delete root->right->left;
  delete root->right;
  delete root->left->right->left;
  delete root->left->right;
  delete root->left->left;
  delete root->left;
  delete root;
  return 0;
```

➡ Final Output (Console):

Size of the binary tree: 9

Sum of all nodes in the binary tree: 448 Maximum value in the binary tree: 87

Height of the binary tree: 3

Inorder traversal of the binary tree:

12 25 30 37 50 62 70 75 87

}	
size of the binary tree: 9	
Sum of all nodes in the binary tree: 448	
Maximum value in the binary tree: 87	
Height of the binary tree: 3	
Inorder traversal of the binary tree:	
12 25 30 37 50 62 70 75 87	

Tilt in C++

```
#include <iostream>
#include <cstdlib> // for abs function
using namespace std;
// Definition of a binary tree node
struct Node {
  int data:
  Node* left;
  Node* right;
  Node(int item) {
    data = item;
    left = nullptr;
    right = nullptr;
};
// Function to display the binary tree (for debugging
purposes)
void display(Node* node) {
  if (node == nullptr) {
    return;
  }
  string str = "";
  str += (node->left == nullptr) ? "." : to_string(node-
>left->data);
  str += " <- " + to_string(node->data) + " -> ";
  str += (node->right == nullptr)? ".":
to string(node->right->data):
  cout << str << endl:
  display(node->left);
  display(node->right);
// Function to calculate the height of the binary tree
int height(Node* node) {
  if (node == nullptr) {
     return -1;
  int lh = height(node->left);
  int rh = height(node->right);
  return max(lh, rh) + 1;
}
// Global variable to store the tilt of the entire tree
int tilt = 0;
// Function to calculate the tilt of the binary tree
int calculateTilt(Node* node) {
  if (node == nullptr) {
    return 0;
  }
  int ls = calculateTilt(node->left);
  int rs = calculateTilt(node->right);
```

Tree Structure:

Dry Run with Tilt Values

Let's go **bottom-up** and calculate each node's tilt with its left and right subtree sums:

Node	Left Sum	Right Sum	Node Tilt = abs(L - R)
12	0	0	0
30	0	0	0
37	30	0	30
25	12	67 (37+30)	55
70	0	0	0
62	0	70	70
87	0	0	0
75	132	87	45
50	104	294	190

Total Tilt:

```
0 (12)
+ 0 (30)
+ 30 (37)
+ 55 (25)
+ 0 (70)
+ 70 (62)
+ 0 (87)
+ 45 (75)
+ 190 (50)
= **390**
```

Output:

Tilt of the binary tree: 390

```
int ltilt = abs(ls - rs);
  tilt += ltilt;
  int sum = ls + rs + node -> data;
  return sum;
int main() {
  // Hardcoded tree construction
  Node* root = new Node(50);
  root->left = new Node(25);
  root->left->left = new Node(12);
  root->left->right = new Node(37);
  root->left->right->left = new Node(30);
  root->right = new Node(75);
  root->right->left = new Node(62);
  root->right->left->right = new Node(70);
  root->right->right = new Node(87);
  // Calculate the tilt of the tree
  calculateTilt(root);
  // Output the tilt value
  cout << "Tilt of the binary tree: " << tilt << endl;</pre>
  // Clean up dynamically allocated memory
  delete root->left->left;
  delete root->left->right->left;
  delete root->left->right;
  delete root->left;
  delete root->right->left->right;
  delete root->right->left;
  delete root->right->right;
  delete root->right;
  delete root;
  return 0;
}
```

Tilt of the binary tree: 390

All single child parent in C++ #include <iostream> #include <vector> using namespace std; // Definition of a Node in the Binary Tree struct Node { int val; Node* left; Node* right; Node(int item) { val = item; left = nullptr; right = nullptr; **}**; // Function to find all nodes with exactly one child void exactlyOneChild(Node* root, vector<int>& ans) { if (root == nullptr | | (root->left == nullptr && root->right == nullptr)) { return; } if (root->left == nullptr | | root->right == nullptr) { ans.push_back(root->val); exactlyOneChild(root->left, ans); exactlyOneChild(root->right, ans); // Wrapper function for exactlyOneChild vector<int> exactlyOneChild(Node* root) { vector<int> res; exactlyOneChild(root, res); return res; int main() { // Constructing the example binary tree Node* root = new Node(1);root->left = new Node(2);root->right = new Node(3); root->left->left = new Node(4);root->left->left->left = new Node(5);// Finding nodes with exactly one child vector<int> ans = exactlyOneChild(root); // Printing the result cout << "Nodes with exactly one child: ";</pre> for (int num: ans) {

cout << num << " ";

Nodes with exactly one child: 2 4

cout << endl;

return 0;

Tree Structure:

```
1
   / \
  2 3
 4
5
```

Q Nodes with Exactly One Child

We traverse and look for nodes that have **only one** non-null child:

Node	Left Child	Right Child	Exactly One Child?	Added to ans?
1	2	3	X (has both)	×
2	4	nullptr	≪	$\varnothing \to 2$
4	5	nullptr	≪	
5	nullptr	nullptr	X (no children)	×
3	nullptr	nullptr	X (no children)	×

♥ Final Output:

Nodes with exactly one child: 2 4

BottomView in C++

```
#include <iostream>
#include <map>
#include <queue>
#include <vector>
using namespace std;
// Definition for a binary tree node.
struct TreeNode {
  int val:
  TreeNode *left:
  TreeNode *right;
  TreeNode(int x) {
    val = x;
    left = nullptr;
    right = nullptr;
  }
};
vector<int> bottomView(TreeNode* root) {
  vector<int> bottomViewNodes;
  if (!root) {
    return bottomViewNodes;
  // TreeMap equivalent in C++ is std::map
  map<int, int> map;
  queue<pair<TreeNode*, int>> q;
  q.push({root, 0});
  while (!q.empty()) {
    auto front = q.front();
    q.pop();
    TreeNode* node = front.first;
    int hd = front.second;
    // Update the map with current node's value at
its horizontal distance
    map[hd] = node > val;
    // Enqueue left child with horizontal distance hd -
1
    if (node->left) {
       q.push({node->left, hd - 1});
    // Enqueue right child with horizontal distance
hd + 1
    if (node->right) {
       q.push({node->right, hd + 1});
  }
  // Populate bottomViewNodes with values from map
  for (const auto& pair : map) {
    bottomViewNodes.push_back(pair.second);
  return bottomViewNodes;
```

Binary Tree Structure:

■ Step-by-Step Dry Run Table

We'll simulate the level order traversal using a queue storing (node, horizontal_distance) and map $hd \rightarrow node-val$.

Step	Queue Content	Popped Node	HD	Map After Step
1	(1, 0)	1	0	$\{0 \rightarrow 1\}$
2	(2, -1), (3, 1)	2	-1	$\{-1 \to 2, \ 0 \to 1\}$
3	(3, 1), (4, -2), (5, 0)	3	1	$\{-1 \to 2, 0 \to 1, 1 \to 3\}$
4	(4, -2), (5, 0), (6, 0), (7, 2)	4		$\{-2 \to 4, -1 \to 2, 0 \to 1, 1 \to 3\}$
5	(5, 0), (6, 0), (7, 2)	5		$ \begin{cases} -2 \rightarrow 4, -1 \rightarrow \\ 2, 0 \rightarrow 5, 1 \rightarrow \\ 3 \end{cases} $
6	(6, 0), (7, 2)	6		$\{-2 \to 4, -1 \to 2, 0 \to 6, 1 \to 3\}$
7	(7, 2)	7		$\{-2 \to 4, -1 \to 2, 0 \to 6, 1 \to 3, 2 \to 7\}$

Final Bottom View:

Take values from the map in order of keys (i.e., horizontal distance):

 $\begin{array}{c}
-2 \rightarrow 4 \\
-1 \rightarrow 2 \\
0 \rightarrow 6 \\
1 \rightarrow 3
\end{array}$

 $2 \rightarrow 7$

▼ Output:

42637

```
// Utility function to create a new node
TreeNode* newNode(int \ key) \ \{
  TreeNode* node = new TreeNode(key);
  return node;
int main() {
  TreeNode* root = newNode(1);
  root->left = newNode(2);
  root->right = newNode(3);
  root->left->left = newNode(4);
  root->left->right = newNode(5);
  root->right->left = newNode(6);
  root->right->right = newNode(7);
  vector<int> result = bottomView(root);
  // Print the result
  for (int value : result) {
    cout << value << " ";
  cout << endl;
  // Memory cleanup (optional in this example)
  // You may need to delete nodes if not using smart
pointers
  return 0;
```

 $4\ 2\ 6\ 3\ 7$

Diagonal Order in C++

```
#include <iostream>
#include <vector>
#include <queue>
using namespace std;
// TreeNode structure definition
struct TreeNode {
  int val;
  TreeNode* left;
  TreeNode* right;
  TreeNode(int x) {
    val = x;
    left = nullptr;
    right = nullptr;
};
// Function to perform diagonal order traversal of
a binary tree
vector<vector<int>> diagonalOrder(TreeNode*
root) {
  vector<vector<int>> ans;
  if (root == nullptr) return ans;
  queue<TreeNode*> que;
  que.push(root);
  while (!que.empty()) {
    int size = que.size();
    std::vector<int> smallAns;
    while (size--) {
       TreeNode* node = que.front();
       que.pop();
       while (node != nullptr) {
         smallAns.push_back(node->val);
         if (node->left) que.push(node->left);
         node = node->right;
    ans.push_back(smallAns);
  return ans;
}
int main() {
  // Constructing the binary tree
  TreeNode* root = new TreeNode(1);
  root->left = new TreeNode(2);
  root->right = new TreeNode(3);
  root->left->left = new TreeNode(4);
  root->left->right = new TreeNode(5);
  root->right->left = new TreeNode(6);
  root->right->right = new TreeNode(7);
  // Calling diagonalOrder function and printing
```

Tree Structure:

```
1
/\
2 3
/\ /\
4 5 6 7
```

◆ Diagonal View Intuition:

- Diagonal lines go **from top-right to bottom- left**, i.e., every time you go to .right, you stay on the same diagonal.
- Every time you go to .left, you move to the next diagonal.

⊘ Dry Run Table:

We'll simulate the queue and how the diagonal groups are formed.

Iteration	Queue (Before)	Extracted	Collected (Diagonal)	Queue (After pushing lefts)
1	[1]	$1 \rightarrow 3 \rightarrow 7$	[1, 3, 7]	[2, 6]
2	[2, 6]	$2 \rightarrow 5$	[2, 5]	[4]
3	[4]	4	[4]	

♦ Final Output:

Diagonal Order Traversal: 1 3 7 2 5 4

Preakdown:

- Diagonal $0 \rightarrow 1 \rightarrow 3 \rightarrow 7$
- Diagonal $1 \rightarrow 2 \rightarrow 5$
- Diagonal $2 \rightarrow 4$

```
the result
  vector<vector<int>> ans =
diagonalOrder(root);
  cout << "Diagonal Order Traversal:\n";</pre>
  for (const auto level: ans) {
     for (int num : level) {
       cout << num << " ";
     cout << " \backslash n";
  }
  // Deallocating memory to avoid memory leaks
  delete root->right->right;
  delete root->right->left;
  delete root->left->right;
  delete root->left->left;
  delete root->right;
  delete root->left;
  delete root;
  return 0;
```

Diagonal Order Traversal:

137

256

4

```
#include <iostream>
#include <queue>
#include <climits> // for INT_MIN and INT_MAX
using namespace std;
// Definition of a Node in the Binary Tree
struct Node {
  int val;
  Node* left;
  Node* right;
  Node(int x) {
    val = x;
    left = nullptr;
    right = nullptr;
};
// Function to calculate the height of the tree using
BFS (level-order traversal)
int getHeight(Node* root) {
  if (root == nullptr) return 0;
  queue<Node*> q;
  q.push(root);
  int height = 0;
  while (!q.empty()) {
    int levelSize = q.size();
    height++:
    for (int i = 0; i < levelSize; i++) {
       Node* node = q.front();
       q.pop();
       if (node->left != nullptr) q.push(node->left);
       if (node->right != nullptr) q.push(node->right);
  }
  return height;
// Function to count the number of nodes in the tree
using BFS (level-order traversal)
int getNodeCount(Node* root) {
  if (root == nullptr) return 0;
  queue<Node*> q;
  q.push(root);
  int count = 0;
  while (!q.empty()) {
    Node* node = q.front();
    q.pop();
    count++:
    if (node->left != nullptr) q.push(node->left);
    if (node->right != nullptr) q.push(node->right);
  return count;
```

Tree Structure:

```
1
/\
2 3
/\
4 5
```

Iterative tree operations in C++

♦ Function: getHeight(root)

This uses level-order traversal (BFS).

Level	Nodes at Level	Height So Far
1	1	1
2	2, 3	2
3	4, 5	3

[⊘] Result: 3

♦ Function: getNodeCount(root)

Counts nodes using BFS:

Step	Node Processed	Count	Queue
1	1	1	2, 3
2	2	2	3, 4, 5
3	3	3	4, 5
4	4	4	5
5	5	5	

[⊘] Result: 5

◆ Function: getMax(root)

Finds maximum using BFS:

Step	Node Processed	Max So Far
1	1	1
2	2	2
3	3	3
4	4	4
5	5	5 ∜

[⊘] Result: 5

◆ Function: getMin(root)

Finds minimum using BFS:

```
// Function to find the maximum value in the tree
using BFS (level-order traversal)
int getMax(Node* root) {
  if (root == nullptr) throw invalid argument("Tree is
empty");
  queue<Node*> q;
  q.push(root);
  int maxValue = INT_MIN;
  while (!q.empty()) {
    Node* node = q.front();
    q.pop();
    maxValue = max(maxValue, node->val);
    if (node->left != nullptr) q.push(node->left);
    if (node->right != nullptr) q.push(node->right);
  return maxValue;
// Function to find the minimum value in the tree
using BFS (level-order traversal)
int getMin(Node* root) {
  if (root == nullptr) throw invalid_argument("Tree is
empty");
  queue<Node*> q;
  q.push(root);
  int minValue = INT MAX;
  while (!q.empty()) {
    Node* node = q.front();
    q.pop();
    minValue = min(minValue, node->val);
    if (node->left != nullptr) q.push(node->left);
    if (node->right != nullptr) q.push(node->right);
  return minValue;
}
int main() {
  // Constructing the example binary tree
  Node* root = new Node(1);
  root->left = new Node(2);
  root->right = new Node(3);
  root->left->left = new Node(4);
  root->left->right = new Node(5);
  // Using the functions to demonstrate the
functionality
  cout << "Height of the tree: " << getHeight(root) <<</pre>
endl:
  cout << "Number of nodes in the tree: " <<
getNodeCount(root) << endl;</pre>
    cout << "Maximum value in the tree: " <<
getMax(root) << endl:
    cout << "Minimum value in the tree: " <<
```

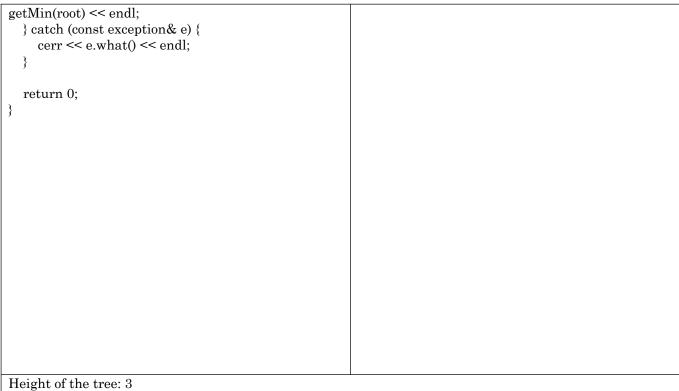
Step	Node Processed	Min So Far
1	1	1 ∜
2	2	1
3	3	1
4	4	1
5	5	1

⊘ Result: 1

∜ Final Output:

Height of the tree: 3

Number of nodes in the tree: 5 Maximum value in the tree: 5 Minimum value in the tree: 1



Number of nodes in the tree: 5 Maximum value in the tree: 5 Minimum value in the tree: 1

```
Top View in C++
#include <iostream>
#include <vector>
#include <queue>
#include <map>
using namespace std;
// Definition for a binary tree node.
struct TreeNode {
  int val;
  TreeNode* left:
  TreeNode* right;
  TreeNode(int x) {
    val = x;
    left = nullptr;
    right = nullptr;
};
// Function to compute the top view of a binary tree
vector<int> topView(TreeNode* root) {
  vector<int> topViewNodes;
  if (!root) {
    return topViewNodes;
  map<int, int> hdMap; // Horizontal Distance Map
(hd -> node value)
  queue<pair<TreeNode*, int>> q; // Queue to store
nodes and their horizontal distance
  q.push({root, 0}); // Start with the root node at
horizontal distance 0
  while (!q.empty()) {
    TreeNode* node = q.front().first;
    int hd = q.front().second;
    q.pop();
    // If this horizontal distance is not already in the
map, add the node value
    if (hdMap.find(hd) == hdMap.end()) {
       hdMap[hd] = node->val;
    // Enqueue left and right children with updated
horizontal distances
    if (node->left) {
       q.push({node->left, hd - 1});
    if (node->right) {
       q.push({node->right, hd + 1});
  // Extract values from the map in order of
horizontal distance
  for (const auto& pair : hdMap) {
```

topViewNodes.push_back(pair.second);

Constructed Binary Tree:

1 / \

Step-by-Step Traversal Table (Level Order with HD)

We'll perform a BFS traversal and track each node with its Horizontal Distance (HD) from root.

Step	Queue Content	Popped Node	HD	hdMap Before	hdMap After
1	(1, 0)	1	0	8	{0: 1}
2	(2, -1), (3, 1)	2	-1	{0: 1}	{-1: 2, 0: 1}
3	(3, 1), (4, 0)	3	1	{-1: 2, 0: 1}	{-1: 2, 0: 1, 1: 3}
4	(4, 0), (5, 1)	4	0	already filled	(no change)
5	(5, 1), (6, 2)	5	1	already filled	(no change)
6	(6, 2)	6	2	{-1: 2, 0: 1, 1: 3}	{, 2: 6}

Final Map (hdMap) Sorted by HD:

 $-1 \rightarrow 2$ $0 \rightarrow 1$ $1 \rightarrow 3$ $2 \rightarrow 6$

⊘ Output (Top View):

2136

```
return topViewNodes;
// Utility function to create a new node
TreeNode* newNode(int key) {
  TreeNode* node = new TreeNode(key);
  return node;
int main() {
  // Constructing the binary tree
  TreeNode* root = newNode(1);
  root->left = newNode(2);
  root->right = newNode(3);
  root->left->right = newNode(4);
  root->left->right->right = newNode(5);
  root->left->right->right = newNode(6);
  // Get the top view of the binary tree
  vector<int> result = topView(root);
  // Print the top view of the binary tree
  cout << "Top view of the binary tree:" << endl;</pre>
  for (int nodeValue : result) {
    \operatorname{cout} << \operatorname{nodeValue} << "";
  cout << endl;</pre>
  // Clean up memory (optional in this example)
  // You may need to delete nodes if not using smart
pointers
  return 0;
```

Top view of the binary tree: 2 1 3 6

```
#include <iostream>
#include <algorithm>
using namespace std;
// Node structure for the binary tree
struct Node {
  int key;
  Node* left;
  Node* right;
  Node(int item) {
    key = item;
    left = right = nullptr;
};
// Function to calculate the height of
the tree and check balance
pair<br/>bool, int>
isBalancedHelper(Node* root) {
  if (root == nullptr)
    return {true, 0};
  // Recursively get heights of left
and right subtrees
  auto left = isBalancedHelper(root-
>left);
  auto right =
isBalancedHelper(root->right);
  // If either subtree is unbalanced,
the whole tree is unbalanced
  if (!left.first | | !right.first)
    return {false, -1};
  // Check if the current subtree is
balanced
  if (abs(left.second - right.second) >
1)
    return {false, -1};
  // Return balanced status and
height of the current subtree
  return {true, max(left.second,
right.second) + 1;
// Function to check if the binary tree
is balanced
bool isBalanced(Node* root) {
  return
isBalancedHelper(root).first;
}
int main() {
  Node* root = new Node(1);
  root->left = new Node(2);
  root->right = new Node(3);
  root->left->left = new Node(4);
  root->left->right = new Node(5);
```

root->left->left->left = new

Balanced in C++

Binary Tree Structure

```
1
/\
2 3
/\
4 5
/
```

IIII Dry Run Table: isBalancedHelper

We'll do a **postorder traversal** (left \to right \to root) and track the balance and height of each subtree.

Node	Left Subtree (Balanced, Height)	Right Subtree (Balanced, Height)		Is Current Balanced?	
6	(true, 0)	(true, 0)	0	∜ Yes	1
4	(true, 1)	(true, 0)	1	∜ Yes	2
5	(true, 0)	(true, 0)	0	∜ Yes	1
2	(true, 2)	(true, 1)	1	∜ Yes	3
3	(true, 0)	(true, 0)	0	∜ Yes	1
1	(true, 3)	(true, 1)	2	X No	

X Final Result:

- Node 1 is **not balanced** because its left and right subtrees have a height difference of **2**, which is more than 1.
- Hence, isBalanced(root) returns false.

Output:

Is the tree balanced? No

```
Node(6);

bool balanced = isBalanced(root);
cout << "Is the tree balanced? " <<
(balanced? "Yes": "No") << endl;
return 0;
}

Is the tree balanced? No
```

Binary Tree 2 LL in C++

```
#include <iostream>
using namespace std;
class Node {
public:
  int key;
  Node* left;
  Node* right;
  Node(int value) {
    key = value;
    left = nullptr;
    right = nullptr;
};
class BinTree2LL {
private:
  static Node* prev;
public:
  static void flatten(Node* root) {
    if (root == nullptr) return;
    flatten(root->right);
    flatten(root->left);
    root->right = prev;
    root->left = nullptr;
    prev = root;
  static void printList(Node* root) {
    while (root->right != nullptr) {
       cout << root->key << "->";
       root = root->right;
    cout << root->key;
};
Node* BinTree2LL::prev = nullptr;
int main() {
  Node* root = new Node(1):
  root->left = new Node(2);
  root->left->left = new Node(3);
  root->left->right = new Node(4);
  root->right = new Node(5);
  root->right->right = new Node(6);
  root->right->right->left = new Node(7);
  BinTree2LL::flatten(root);
  BinTree2LL::printList(root);
  // Clean up allocated memory (not present in Java
version)
  while (root != nullptr) {
    Node* temp = root;
    root = root->right;
     delete temp;
```

Original Binary Tree Structure

```
1
/\
2 5
/\ \
3 4 6
/
7
```

% Flattening Logic: Reverse Postorder (Right \rightarrow Left \rightarrow Node)

The algorithm works like this:

- Traverse the tree in **reverse postorder**.
- Use a static prev pointer to keep track of the previously processed node.
- Set the current node's right to prev, and its left to nullptr.

Step-by-Step Tabular Dry Run

We will track:

- The current node being visited
- The state of prev
- · Links updated

Step	Node Visited	Previous (prev)	Action	Updated Links
1	7	nullptr	Set 7.right = nullptr, 7.left = nullptr, prev = 7	7 ightarrownullptr
2	6	7	Set 6.right = 7, 6.left = nullptr, prev = 6	$6 \rightarrow 7$
3	5	6	Set 5.right = 6, 5.left = nullptr, prev = 5	$5 \to 6 \to 7$
4	4	5	Set 4.right = 5, 4.left = nullptr, prev = 4	$\begin{array}{c} 4 \rightarrow 5 \rightarrow 6 \\ \rightarrow 7 \end{array}$
5	3	4	Set 3.right = 4, 3.left = nullptr, prev = 3	$3 \rightarrow 4 \rightarrow \dots$
6	2	3	Set 2.right = 3, 2.left = nullptr,	$2 \rightarrow 3 \rightarrow \dots$

return 0; }	7	1	2	$\begin{array}{c c} \text{prev} = 2 \\ \text{Set 1.right} \\ = 2, 1.\text{left} = 1 \rightarrow 2 \rightarrow 3 \\ \text{nullptr,} \\ \text{prev} = 1 \end{array}$
	Poir	nters)		inked List (Right
	1 -> 2 -> 3 -> 4 -> 5 -> 6 -> 7 All left pointers are nullptr, forming a single right-skewed list.			
		utput		
	1->2	->3->4->	>5->6->7	

1->2->3->4->5->6->7

Boundary traversal in C++

```
#include <iostream>
#include <vector>
using namespace std;
// Definition of the Node class
class Node {
public:
  int key;
  Node* left:
  Node* right;
  Node(int item) {
    key = item;
    left = right = nullptr;
};
// Utility function to check if a node is a leaf node
bool isLeaf(Node* root) {
  return (root->left == nullptr && root->right ==
nullptr);
}
// Function to add nodes of the left boundary
(excluding the leaf node itself)
void addLeftBoundary(Node* root, vector<int>&
res) {
  Node* cur = root -> left;
  while (cur != nullptr) {
    if (!isLeaf(cur))
       res.push_back(cur->key);
    if (cur->left != nullptr)
       cur = cur->left;
    else
       cur = cur->right;
}
// Function to add nodes of the right boundary
(excluding the leaf node itself)
void addRightBoundary(Node* root, vector<int>&
res) {
  Node* cur = root->right;
  vector<int> tmp;
  while (cur != nullptr) {
    if (!isLeaf(cur))
       tmp.push_back(cur->key);
    if (cur->right != nullptr)
       cur = cur->right;
    else
       cur = cur - left;
  for (int i = tmp.size() - 1; i \ge 0; --i) {
    res.push_back(tmp[i]);
// Function to add all leaf nodes in left-to-right
order
```

Binary Tree Structure

Here's the tree again for reference:

```
1
/ \
2 7
/ \
3 8
\ / /
4 9
/\ /\
5 6 10 11
```

1. Root Node

Step	Node Visited	Is Leaf?	Action	Vector State
1	1		Add to result	[1]

2. Left Boundary (excluding leaves)

Traversal path: $2 \rightarrow 3 \rightarrow 4$ (stop before leaf nodes 5, 6)

Step	Node Visited	Is Leaf?	Action	Vector State
2	2	No	Add to result	[1, 2]
3	3	No	Add to result	[1, 2, 3]
4	4	No	Add to result	[1, 2, 3, 4]

3. Leaf Nodes (from left to right)

Leaf nodes: 5, 6, 10, 11

Step	Node Visited	Is Leaf?	Action	Vector State
5	5	Yes	Add to result	[1, 2, 3, 4, 5]
6	6	Yes	Add to result	[1, 2, 3, 4, 5, 6]
7	10	Yes	Add to	[1, 2, 3, 4, 5, 6,

```
void addLeaves(Node* root, vector<int>& res) {
  if (isLeaf(root)) {
    res.push_back(root->key);
    return;
  if (root->left != nullptr)
    addLeaves(root->left, res);
  if (root->right != nullptr)
    addLeaves(root->right, res);
}
// Function to perform boundary traversal and
return the result as vector
vector<int> printBoundary(Node* node) {
  vector<int> ans;
  if (!isLeaf(node))
    ans.push_back(node->key);
  addLeftBoundary(node, ans);
  addLeaves(node, ans);
  addRightBoundary(node, ans);
  return ans;
int main() {
  // Constructing the binary tree
  Node* root = new Node(1);
  root->left = new Node(2);
  root->left->left = new Node(3);
  root->left->right = new Node(4);
  root->left->right->left = new Node(5);
  root->left->right->right = new Node(6);
  root->right = new Node(7);
  root->right->right = new Node(8);
  root->right->left = new Node(9);
  root->right->right->left->left = new Node(10);
  root->right->right->left->right = new Node(11);
  // Performing boundary traversal
  vector<int> boundaryTraversal =
printBoundary(root);
  // Printing the result
  cout << "The Boundary Traversal is : ";</pre>
  for (int i = 0; i < boundaryTraversal.size(); i++)</pre>
    cout << boundaryTraversal[i] << " ";</pre>
  }
  cout << endl;
  return 0;
}
```

Step	Node Visited	Is Leaf?	Action	Vector State
			result	10]
8	11	Yes	Add to result	[1, 2, 3, 4, 5, 6, 10, 11]

4. Right Boundary (excluding leaves) — reversed

Traversal path: $7 \rightarrow 8 \rightarrow 9$ (reverse order, ignore 10 and 11)

Step	Node Visited	Is Leaf?	Action (store in temp, then reverse)	Temporary Stack	Vector State (after reverse append)
9	7	No	Push to temp	[7]	
10	8	No	Push to temp	[7, 8]	
11	9	No	Push to temp	[7, 8, 9]	
12			Reverse and append to result		[1, 2, 3, 4, 5, 6, 10, 11, 9, 8, 7]

& Final Result

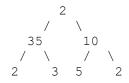
Boundary Traversal: [1, 2, 3, 4, 5, 6, 10, 11, 9, 8, 7]

 $Boundary\ Traversal: [1,\,2,\,3,\,4,\,5,\,6,\,10,\,11,\,9,\,8,\,7]$

Children Sum in C++

```
#include <iostream>
using namespace std;
// Definition of the Node class
class Node {
public:
  int key;
  Node* left;
  Node* right;
  Node(int item) {
    key = item;
    left = right = nullptr;
};
// Function to reorder the binary tree based on
Children Sum Property
void reorder(Node* root) {
  if (root == nullptr) return;
  int child = 0;
  if (root->left != nullptr) {
    child += root->left->key;
  if (root->right != nullptr) {
    child += root->right->key;
  if (child < root->key) {
    if (root->left != nullptr) root->left->key = root-
>key;
    else if (root->right != nullptr) root->right->key =
root->key;
  }
  reorder(root->left);
  reorder(root->right);
  int tot = 0;
  if (root->left != nullptr) tot += root->left->key;
  if (root->right != nullptr) tot += root->right->key;
  if (root->left != nullptr | | root->right != nullptr)
root->key = tot;
// Function to change the tree based on Children Sum
Property
void changeTree(Node* root) {
  reorder(root);
}
int main() {
  Node* root = new Node(2);
  root->left = new Node(35);
  root->left->left = new Node(2);
  root->left->right = new Node(3);
  root->right = new Node(10);
  root->right->left = new Node(5);
  root->right->right = new Node(2);
```

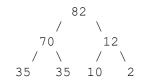
Initial Tree Structure



\$ Dry Run: Step-by-Step Execution

Node Visited	Children Before	Action Taken	Node Key After
2 (root)	35 + 10 = 45	Children > root → No update to children	
35	2 + 3 = 5	Children < 35 → Set both children to 35	
2 (left)	null	Leaf node	35
3 (right)	null	Leaf node	35
Back to 35	35 + 35 = 70	Set node key = sum of children	70
10	5 + 2 = 7	Children < 10 → Set left to 10 (since left exists)	
5 (left)	null	Leaf node	10
2 (right)	null	Leaf node	2
Back to 10	10 + 2 = 12	Set node key = sum of children	12
Back to root	70 + 12 = 82	Set root = sum of its updated children	82

♣ Final Tree Structure



Output

```
Modified Tree:
Root: 82
Left: 70, Left Left: 35, Left Right: 35
Right: 12, Right Left: 10, Right Right: 2
```

```
changeTree(root);

// Display the modified tree
cout << "Modified Tree:" << endl;
cout << "Root: " << root->key << endl;
cout << "Left: " << root->left->key << ", Left Left: "
<< root->left->left->key << ", Left Right: " << root->left->right->key << endl;
cout << "Right: " << root->right->key << ", Right
Left: " << root->right->left->key << ", Right Right: "
<< root->right->left->key << endl;
return 0;
}</pre>
```

Summary of Key Logic in reorder():

1. Preorder Phase:

 Push parent's value down to children if sum of children < parent.

2. Postorder Phase:

 After children updated, update parent's value as sum of updated children.

Modified Tree: Root: 50

Left: 38, Left Left: 35, Left Right: 3 Right: 12, Right Left: 10, Right Right: 2

#include <iostream> #include <algorithm> // For std::max using namespace std; // Definition of the Node class class Node { public: int key; Node* left; Node* right; Node(int item) { key = item;left = right = nullptr; **}**; // Function prototype for height int height(Node* node, int* diameter); // Function to calculate diameter of binary tree int diameterOfBinaryTree(Node* root) { int diameter = 0; height(root, &diameter); return diameter; } // Helper function to calculate height and update diameter int height(Node* node, int* diameter) { if (node == nullptr) { return 0; int leftHeight = height(node->left, diameter); int rightHeight = height(node->right, diameter); *diameter = max(*diameter, leftHeight + rightHeight); return 1 + max(leftHeight, rightHeight); } int main() { Node* root = new Node(1); root->left = new Node(2);root->right = new Node(3); root->left->left = new Node(4);root->left->right = new Node(5); root->left->left->left = new Node(6); int dia = diameterOfBinaryTree(root); cout << "Diameter of the binary tree: " << dia << endl; return 0;

}

Diameter of the binary tree: 4

Diameter in C++

Tree Structure

Based on your construction, the tree looks like this:

```
1
/\
2 3
/\
4 5
/
```

Q What Is *Diameter*?

The **diameter** is the **length of the longest path** between any two nodes in the tree (measured by number of edges, not nodes).

This path does not necessarily pass through the root.

Core Logic Summary

- For each node:
 - o Compute leftHeight and rightHeight.
 - Update diameter = max(diameter, leftHeight + rightHeight).
- Height is returned as 1 + max(leftHeight, rightHeight).

Dry Run Table

Node	Left Height	Right Height	Local Diameter (L + R)	Max Diameter So Far	Returned Height
6	0	0	0	0	1
4	1	0	1	1	2
5	0	0	0	1	1
2	2	1	3	⊘ 3	3
3	0	0	0	3	1
1	3	1	4	∜ 4	4

∜ Final Output

Diameter of the binary tree: 4

```
#include <iostream>
using namespace std;
// Definition for a binary
tree node.
struct TreeNode {
  int val;
  TreeNode* left;
  TreeNode* right;
  TreeNode(int x) {
    val = x;
    left = nullptr;
    right = nullptr;
};
class Identical {
public:
  static bool
isIdentical(TreeNode*
node1, TreeNode* node2) {
    if (node1 == nullptr
&& node2 == nullptr)
       return true;
    else if (node1 ==
nullptr | | node2 ==
nullptr)
       return false;
    return (node1->val ==
node2->val) &&
        isIdentical(node1-
>left, node2->left) &&
        isIdentical(node1-
>right, node2->right);
};
int main() {
  TreeNode* root1 = new
TreeNode(1);
  root1->left = new
TreeNode(2);
  root1->right = new
TreeNode(3);
  root1->right->left = new
TreeNode(4);
  root1->right->right =
new TreeNode(5);
  TreeNode* root2 = new
TreeNode(1);
  root2->left = new
TreeNode(2);
  root2->right = new
TreeNode(3);
  root2->right->left = new
TreeNode(4);
```

Identical in C++

Tree Structures:

Tree 1:

1 / \ 2 3 / \ 4 5

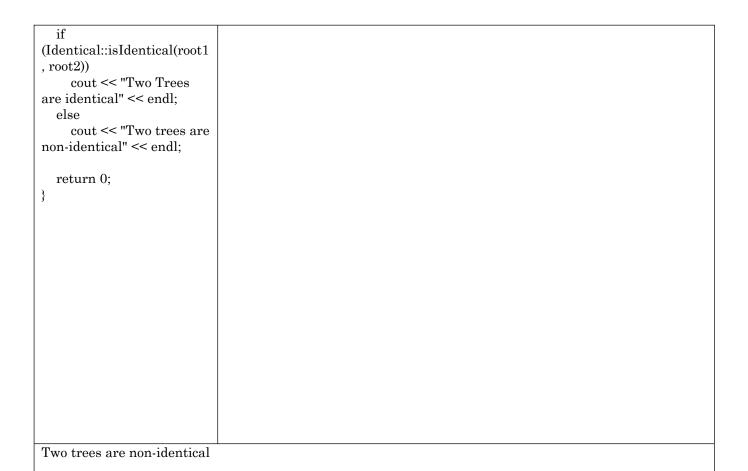
Tree 2:

1 2 3

Dry Run Table: isIdentical(root1, root2)						
Call	node1 Val	node2 Val	Equal?	Recursive Calls	Final Result	
isIdentical(1, 1)	1	1	≪	isIdentical(2, 2) && isIdentical(3, 3)	depends	
isIdentical(2, 2)	2	2	≪	isIdentical(nullptr, nullptr)	≪	
isIdentical(NULL, NULL)	NULL	NULL	≪		≪	
isIdentical(NULL, NULL)	NULL	NULL	≪		≪	
isIdentical(3, 3)	3	3	≪	isIdentical(4, 4) && isIdentical(5, NULL)	×	
isIdentical(4, 4)	4	4	≪	isIdentical(NULL, NULL)	<	
isIdentical(NULL,NULL)	NULL	NULL	✓		≪	
isIdentical(NULL,NULL)	NULL	NULL	✓		≪	
isIdentical(5, NULL)	5	NULL	×		×	

X Final Output:

Two trees are non-identical



Iterative Inorder in C++ #include <iostream> #include <vector> #include <stack> using namespace std; // TreeNode structure definition struct TreeNode { int key; TreeNode* left; TreeNode* right; TreeNode(int x) { key = x; left = nullptr; right = nullptr; **}**; // Function to perform iterative inorder traversal vector<int> inOrderTrav(TreeNode* root) { vector<int> inOrder: stack<TreeNode*> s: TreeNode* curr = root; while (true) { if (curr != nullptr) { s.push(curr); curr = curr->left; } else { if (s.empty()) break; curr = s.top();inOrder.push_back(curr->key); s.pop(); curr = curr->right; return inOrder; int main() { // Constructing the binary tree TreeNode* root = new TreeNode(1); root->left = new TreeNode(2); root->right = new TreeNode(3); root->left->left = new TreeNode(4); root->left->right = new TreeNode(5); root->left->right->left = new TreeNode(8); root->right->left = new TreeNode(6); root->right->right = new TreeNode(7); root->right->right->left = new TreeNode(9); root->right->right->right = new TreeNode(10); // Perform iterative inorder traversal vector<int> inOrder = inOrderTrav(root); // Print the result cout << "The inorder traversal is : ";</pre> for (int i = 0; i < inOrder.size(); i++) { cout << inOrder[i] << " ";

cout << endl;

Tree Structure:

```
1
4 5 6 7
 /
     /\
     9 10
```

III Dry Run Table

Step	Current Node (curr)	$\begin{array}{c} \textbf{Stack} \\ \textbf{(top} \rightarrow \\ \textbf{bottom)} \end{array}$	Action	Output (inOrder)
1	1		Push 1, move to left	
2	2	1	Push 2, move to left	
3	4	$2 \rightarrow 1$	Push 4, move to left	
4	nullptr	$4 \to 2 \to 1$	Pop 4, visit	4
5	nullptr (right of 4)	$2 \rightarrow 1$	Pop 2, visit	4 2
6	5	1	Push 5, move to left	4 2
7	8	$5 \rightarrow 1$	Push 8, move to left	4 2
8	nullptr	$8 \to 5 \to 1$	Pop 8, visit	4 2 8
9	nullptr (right of 8)	$5 \rightarrow 1$	Pop 5, visit	4 2 8 5
10	nullptr (right of 5)	1	Pop 1, visit	4 2 8 5 1
11	3		Push 3, move to left	4 2 8 5 1
12	6	3	Push 6, move to left	4 2 8 5 1

return 0; }	13	nullptr	$6 \rightarrow 3$	Pop 6, visit	4 2 8 5 1 6
	14	nullptr (right of 6)	3	Pop 3, visit	4 2 8 5 1 6 3
	15	7		Push 7, move to left	4 2 8 5 1 6 3
	16	9	7	Push 9, move to left	4 2 8 5 1 6 3
	17	nullptr	$9 \rightarrow 7$	Pop 9, visit	4 2 8 5 1 6 3 9
	18	nullptr (right of 9)	7	Pop 7, visit	4 2 8 5 1 6 3 9 7
	19	10		Push 10, move to left	4 2 8 5 1 6 3 9 7
	20	nullptr	10	Pop 10, visit	4 2 8 5 1 6 3 9 7 10

∜ Final Output:

The inorder traversal is : $4\ 2\ 8\ 5\ 1\ 6\ 3\ 9\ 7\ 10$

The inorder traversal is : 4 2 8 5 1 6 3 9 7 10

#include <iostream> #include <climits> // For INT_MIN #include <algorithm> // For std::max using namespace std; // TreeNode structure definition struct TreeNode { int key; TreeNode* left; TreeNode* right; TreeNode(int x) { key = x; left = nullptr; right = nullptr; **}**; // Helper function to calculate the maximum path sum going down from a node int maxPathDown(TreeNode* node, int& maxValue) { if (node == nullptr) return 0; // Calculate maximum path sums from left and right subtrees int left = std::max(0, maxPathDown(node->left, maxValue)); // Ignore negative sums int right = std::max(0,maxPathDown(node->right, maxValue)); // Ignore negative sums // Update maxValue with the maximum path sum found so far maxValue = std::max(maxValue, left + right + node->key); // Return the maximum path sum going down from the current node return std::max(left, right) + node->key; } // Function to find the maximum path sum in a binary tree int maxPathSum(TreeNode* root) { int maxValue = INT MIN; // Initialize with minimum possible integer value maxPathDown(root, maxValue); return maxValue; } int main() { // Constructing the binary tree TreeNode* root = new TreeNode(-10); root->left = new TreeNode(9);

root->right = new TreeNode(20);
root->right->left = new TreeNode(15);
root->right->right = new TreeNode(7);

int answer = maxPathSum(root);

binary tree

// Finding the maximum path sum in the

Max path sum in C++

Tree Structure

You built this binary tree:

```
-10
/ \
9 20
/ \
15 7
```

Core Logic (Recap)

- 1. maxPathDown(node):
 - o Gets **max sum** for any path **starting** from the current node and going **downward**.
 - Ignores negative subtrees (max(0, left/right)).
 - Updates the global maxValue if a new candidate sum left + right + node->key is higher.

Dry Run Table

Node	Left Subtree	Right Subtree	Local Max (left + right + node)	Return	maxValue Updated
15	0	0	15	15	⊘ 15
7	0	0	7	7	×
20	15	7	42 (=15+7+20)	35	√ 42
9	0	0	9	9	×
-10	9	35	34 (=9+35- 10)	25	×

 \bigcirc So the final max path goes through $15 \rightarrow 20 \rightarrow 7 = 42$

Output:

The Max Path Sum for this tree is 42

```
std::cout << "The Max Path Sum for this tree is " << answer << std::endl;

// Deallocating memory delete root->right->right; delete root->right; delete root->right; delete root->left; delete root;

return 0;
}

The Max Path Sum for this tree is 42
```

Morris traversal in C++

```
#include <iostream>
#include <vector>
using namespace std;
// TreeNode structure definition
struct TreeNode {
  int key;
  TreeNode* left;
  TreeNode* right;
  TreeNode(int x) {
    key = x;
    left = nullptr;
    right = nullptr;
};
// Function to perform Morris preorder traversal
vector<int> preorderTraversal(TreeNode* root) {
  vector<int> preorder;
  TreeNode* cur = root;
  while (cur != nullptr) {
    if (cur->left == nullptr) {
       preorder.push back(cur->key);
       cur = cur->right;
    } else {
       TreeNode* prev = cur->left;
       while (prev->right != nullptr && prev->right !
= cur) {
         prev = prev->right;
       if (prev->right == nullptr) {
         prev->right = cur;
         preorder.push_back(cur->key);
         cur = cur->left;
       } else {
         prev->right = nullptr;
         cur = cur->right;
  return preorder;
int main() {
  // Constructing the binary tree
  TreeNode* root = new TreeNode(1);
  root->left = new TreeNode(2);
  root->right = new TreeNode(3);
  root->left->left = new TreeNode(4):
  root->left->right = new TreeNode(5);
  root->left->right->right = new TreeNode(6);
  // Performing Morris preorder traversal
  vector<int> preorder = preorderTraversal(root);
  // Printing the result
  cout << "The Preorder Traversal is: ";</pre>
  for (int i = 0; i < preorder.size(); i++) {
```

Tree Structure

```
1
/\
2 3
/\
4 5
\
6
```

Morris Preorder Key Idea

- Use the **rightmost node** in the left subtree to **thread** back to the current node.
- When revisiting via the thread, remove the link and move right.

☐ Dry Run Table

We'll walk through the preorderTraversal function.

Step	cur	Action	preorder	Thread Created?
1	1	Left exists → find predecessor (5)	[1]	<pre></pre>
2	2	Left exists → find predecessor (4)	[1, 2]	<pre> prev- right = 2</pre>
3	4	No left child → visit, move right (nullptr)	[1, 2, 4]	×
4	2	Thread exists → remove, move right to 5		ಭ
5	5	No left child → visit, move right to 6	[1, 2, 4, 5]	×
6	6	No left child → visit, move right (nullptr)	[1, 2, 4, 5, 6]	×
7	1	Thread exists → remove, move right to 3		ø
8	3	No left child → visit, move right (nullptr)	[1, 2, 4, 5, 6, 3]	×

♥ Final Output:

The Preorder Traversal is: 1 2 4 5 6 3

```
cout << pre>cout << endl;

// Deallocating memory
delete root->left->right->right;
delete root->left;
delete root->right;
delete root->right;
delete root;
return 0;
}
```

The Preorder Traversal is: 1 2 4 5 6 3

Root 2 Node path in C++ #include <iostream> #include <vector> using namespace std; // TreeNode structure definition struct TreeNode { int key; TreeNode* left; TreeNode* right; TreeNode(int x) { key = x; left = nullptr; right = nullptr; **}**; // Function to get the path from root to a node with bool getPath(TreeNode* root, vector<int>& arr, int x) // If root is NULL, there is no path if (root == nullptr) return false; // Push the node's value into 'arr' arr.push_back(root->key); // If it is the required node, return true if (root->key == x)return true; // Check in the left subtree and right subtree if (getPath(root->left, arr, x) | | getPath(root->right, arr, x)) return true; // If the required node does not lie in either subtree, // remove current node's value from 'arr' and return false arr.pop back(); return false; } int main() { // Constructing the binary tree TreeNode* root = new TreeNode(1); root->left = new TreeNode(2); root->left->left = new TreeNode(4); root->left->right = new TreeNode(5); root->left->right->left = new TreeNode(6); root->left->right->right = new TreeNode(7); root->right = new TreeNode(3); vector<int> arr; bool res = getPath(root, arr, 7); if (res) { cout << "The path is: ";</pre> for (int it : arr) {

cout << it << " ":

Tree Structure

Narget: 7

We'll step through getPath(root, arr, 7).

Step	Current Node	arr Content	Found?
1	1	[1]	×
2	2	[1, 2]	×
3	4	[1, 2, 4]	$X \rightarrow \text{backtrack}$
4	Backtrack	[1, 2]	
5	5	[1, 2, 5]	×
6	6	[1, 2, 5, 6]	$\mathbf{X} \rightarrow \mathrm{backtrack}$
7	Backtrack	[1, 2, 5]	
8	7	[1, 2, 5, 7]	∜ Found!

♥ Final Output:

The path is: 1 2 5 7

```
cout << endl;
} else {
   cout << "Node not found in the tree." << endl;
}

// Deallocating memory
delete root->left->right->right;
delete root->left->right;
delete root->left->right;
delete root->left->left;
delete root->left;
delete root->right;
delete root->right;
delete root;

return 0;
}
```

The path is: 1 2 5 7