Abbreviation in C++

```
#include <iostream>
#include <string>
using namespace std;
class Abbreviation {
public:
  static void solution(string str, string asf, int count,
int pos) {
     if (pos == str.length()) {
       if (count == 0) {
          cout << asf << endl;
       } else {
          cout << asf << count << endl;
       return;
     if (count > 0) {
       solution(str, asf + to_string(count) + str[pos],
0, pos + 1);
     } else {
       solution(str, asf + str[pos], 0, pos + 1);
     solution(str, asf, count + 1, pos + 1);
};
int main() {
  string str = "pep";
  Abbreviation::solution(str, "", 0, 0);
  return 0;
```

Dry Run Table (Step-by-Step)

We'll list:

- pos: current position in the string
- count: how many characters we've skipped (abbreviated)
- asf: abbreviation-so-far

pos	char	count	asf	Recursive Call		
0	р	0	"""	choose 'p' \rightarrow asf = "p"		
1	e	0	"p"	choose 'e' → asf = "pe"		
2	р	0	"pe"	choose 'p' → asf = "pep"		
3		0	"pep"	output: pep		
2	р	1	"pe"	skip 'p' (count = 1)		
3		1	"pe"	output: pe1		
1	e	1	"p"	skip 'e' (count = 1)		
2	р	0	"p1p"	count $> 0 \rightarrow add 1$ then 'p'		
3		0	"p1p"	output: p1p		
2	р	2	"p"	skip 'p' (count = 2)		
3		2	"p"	output: p2		
0	р	1	"""	skip 'p' (count = 1)		
1	e	0	"1e"	count $> 0 \rightarrow add 1$, then 'e'		
2	р	0	"1ep"	choose 'p'		
3	_	0	"1ep"	output: 1ep		
2	p	1	"1e"	skip 'p' (count = 1)		
3	_	1	"1e"	output: 1e1		
1	e	1	""	skip 'e'		
2	p	0	"2p"	$count = 2 \rightarrow asf = "2p"$		
3		0	"2p"	output: 2p		
2	p	2	"""	skip 'p'		
3		3	"""	output: 3		

\checkmark Final Output:

pep pe1 p1p

	p2 1ep 1e1 2p 3	
Output:-	<u> </u>	
pep		
pe1		
p1p		
p2		
pe1 p1p p2 lep		
1e1		
2p 3		
3		

All palindromic partition in C++

```
#include <iostream>
#include <string>
using namespace std;
class AllPalindromicPartition {
public:
  static void main() {
     string str = "abba";
     sol(str, "");
  }
  static void sol(string str, string asf) {
     if (str.length() == 0) {
        cout << asf << endl;
        return;
     for (int i = 0; i < str.length(); i++) {
        string prefix = str.substr(0, i + 1);
        string ros = str.substr(i + 1);
        if (isPalin(prefix)) {
          sol(ros, asf + "(" + prefix + ")");
  }
  static bool isPalin(string s) {
     int li = 0;
     int ri = s.length() - 1;
     while (li < ri) {
        if (s[li] != s[ri]) {
          return false;
        li++;
        ri--;
     return true;
};
int main() {
  AllPalindromicPartition::main();
  return 0;
```

Dry Run for Input "abba"

We will track the recursive calls with:

- str: Remaining string to process
- prefix: Currently selected prefix
- ros: Remaining string after prefix
- asf: Accumulated string so far
- Action: What's happening

Step	str	prefix	ros	asf	Action / Reason
1	abba	а	bba	(a)	'a' is palindrome → recurse
2	bba	b	ba	(a)(b)	'b' is palindrome → recurse
3	ba	b	a	(a)(b)(b)	'b' is palindrome → recurse
4	a	a	*****	(a)(b)(b)(a)	∜ 'a' is palindrome → print
5	ba	ba			not palindrome
6	bba	bb	a	(a)(bb)	∜ 'bb' is palindrome → recurse
7	a	a	"""	(a)(bb)(a)	∜ 'a' is palindrome → print
8	bba	bba			not palindrome
9	abba	ab			not palindrome
10	abba	abb			not palindrome
11	abba	abba	****	(abba)	⊗ 'abba' is palindrome → print

♥ Final Output

(a)(b)(b)(a) (a)(bb)(a)

	(abba)
Output:-	
(a)(b)(b)(a)	
(a)(b)(a) (a)(bb)(a) (abba)	
(abba)	

Combinations in C++

```
#include <iostream>
using namespace std;
void combinations(int cb, int nboxes, int ssf, int
ritems, string asf) {
  if (cb > nboxes) {
    if (ssf == ritems) {
       cout << asf << endl;
    return;
  }
  combinations(cb + 1, nboxes, ssf + 1, ritems, asf +
  combinations(cb + 1, nboxes, ssf, ritems, asf + "-");
int main() {
  int nboxes = 3;
  int ritems = 2;
  combinations(1, nboxes, 0, ritems, "");
  return 0;
```

Dry Run with Table for Input:

- nboxes = 3
- ritems = 2

We're tracing the recursive calls:

- cb: current box index
- ssf: selected so far
- asf: answer so far

Step	cb	ssf	asf	Action
1	1	0	****	\rightarrow i at box 1 \rightarrow recurse
2	2	1	"i"	\rightarrow i at box 2 \rightarrow recurse
3	3	2	"ii"	\rightarrow i at box 3 \rightarrow recurse
4	4	3	"iii"	X too many items (ssf > ritems)
5	3	2	"ii"	\rightarrow - at box 3 \rightarrow \otimes print: ii-
6	2	1	"i"	\rightarrow - at box 2 \rightarrow recurse
7	3	1	"i-"	\rightarrow i at box 3 \rightarrow recurse
8	4	2	"i-i"	∨ valid → print: i-i
9	3	1	"i-"	\rightarrow - at box 3 \rightarrow recurse
10	4	1	"i"	X too few items
11	1	0	""	\rightarrow - at box 1 \rightarrow recurse
12	2	0	"-"	\rightarrow i at box 2 \rightarrow recurse
13	3	1	''-i''	\rightarrow i at box 3 \rightarrow recurse
14	4	2	"-ii"	√ valid → print: -ii
15	3	1	''-i''	\rightarrow - at box 3 \rightarrow recurse
16	4	1	"-i-"	X too few items
17	2	0	''-''	\rightarrow - at box 2 \rightarrow recurse
18	3	0	""	\rightarrow i at box 3 \rightarrow recurse
19	4	1		X too few items
20	3	0	""	\rightarrow - at box 3 \rightarrow recurse
21	4	0	""	X too few items

Final Output

```
ii-
i-i
```

-ii

Output:-

```
ii-
```

i-i

-ii

Friend's pairing in C++

```
#include <iostream>
#include <vector>
using namespace std;
int counter = 1;
void solution(int i, int n, vector<br/>
bool>& used, string
asf) {
  if (i > n) {
     cout << counter << "." << asf << endl;
     counter++;
     return;
  if (used[i]) {
     solution(i + 1, n, used, asf);
  } else {
     used[i] = true;
     solution(i + 1, n, used, asf + "(" + to_string(i) + ")
");
     for (int j = i + 1; j \le n; j++) {
       if (!used[j]) {
          used[j] = true;
          solution(i + 1, n, used, asf + "(" + to_string(i)
+ "," + to_string(j) + ") ");
          used[j] = false;
     used[i] = false;
int main() {
  int n = 3;
  vector < bool > used(n + 1, false);
  solution(1, n, used, "");
  return 0;
}
```

Function Logic Recap

\square Dry Run for n = 3

Step	i	used	Action	Output (if any)
1	1	[F, F, F, F]	1 unused \rightarrow go	
		r, r]	alone: (1)	
2	2	[F, T, F, F]	2 unused \rightarrow go	
			alone: (2)	
3	3	[F, T,	3 unused → go	1.(1) (2)
]	5	T, F]	alone: (3)	(3)
4			backtrack to pair	
4			2 and 3	(2,3)
5			backtrack to try 1	
3			with 2	
6	2	[F, T, T, F]	3 unused →	3.(1,2)
6	2	T, F]	alone: (3)	(3)
7			backtrack	
8			try 1 with 3	
9	2	[F, T,	2 unused →	4.(1,3)
9	2	F, T]	alone: (2)	(2)

∜ Final Output

```
1.(1) (2) (3)
2.(1) (2,3)
3.(1,2) (3)
4.(1,3) (2)
```

```
1.(1) (2) (3)
2.(1) (2,3)
3.(1,2) (3)
4.(1,3) (2)
```

```
Goldmine2 in C++
#include <iostream>
#include <vector>
using namespace std;
int maxGold = 0;
void travel(vector<vector<int>>& arr, int i, int j,
vector<vector<bool>>& visited, vector<int>& bag) {
  if (i < 0 | | j < 0 | | i >= arr.size() | | j >=
arr[0].size() \mid | arr[i][j] == 0 \mid | visited[i][j]) 
     return:
  }
  visited[i][j] = true;
  bag.push_back(arr[i][j]);
  travel(arr, i - 1, j, visited, bag);
  travel(arr, i, j + 1, visited, bag);
  travel(arr, i, j - 1, visited, bag);
  travel(arr, i + 1, j, visited, bag);
void getMaxGold(vector<vector<int>>& arr) {
  int rows = arr.size();
  int cols = arr[0].size();
  vector<vector<br/>bool>> visited(rows,
vector<bool>(cols, false));
  for (int i = 0; i < rows; i++) {
     for (int j = 0; j < cols; j++) {
        if (arr[i][j] != 0 && !visited[i][j]) {
           vector<int> bag;
           travel(arr, i, j, visited, bag);
          int sum = 0;
          for (int val : bag) {
             sum += val;
          if (sum > maxGold) {
             maxGold = sum;
  }
}
int main() {
  vector<vector<int>> arr = {
     \{0, 1, 4, 2, 8, 2\},\
     \{4, 3, 6, 5, 0, 4\},\
     \{1, 2, 4, 1, 4, 6\},\
     \{2, 0, 7, 3, 2, 2\},\
     \{3, 1, 5, 9, 2, 4\},\
     \{2,\,7,\,0,\,8,\,5,\,1\}
  };
  getMaxGold(arr);
  cout << maxGold << endl;</pre>
  return 0;
}
```

Sample Grid (Visual):

```
Ο,
                2,
                     8,
                         2 },
{
      1,
      3,
                5,
                         4 },
  4,
                    Ο,
                         6 },
  1,
       2,
           4,
                1,
                     4,
  2,
           7,
                    2,
                         2 },
               3,
{ 3,
                    2,
           5,
               9,
                         4 },
  2,
```

We'll start traversal from (1,2) where value = 6

Dry Run Table (DFS Traversal Steps):

Step	Cell Visited	Gold at Cell	Cumulative Sum	Stack (DFS Recursion Path)
1	(1,2)	6	6	(1,2)
2	(0,2)	4	10	$(1,2) \rightarrow (0,2)$
3	(0,3)	2	12	$(1,2) \rightarrow (0,2)$ $\rightarrow (0,3)$
4	(0,4)	8	20	
5	(0,5)	2	22	
6	(1,5)	4	26	
7	(2,5)	6	32	
8	(2,4)	4	36	
9	(3,4)	2	38	
10	(3,5)	2	40	
11	(4,5)	4	44	
12	(4,4)	2	46	
13	(4,3)	9	55	
14	(5,3)	8	63	
15	(5,4)	5	68	
16	(5,5)	1	69	
17	(3,3)	3	72	
18	(2,3)	1	73	
19	(2,2)	4	77	
20	(1,3)	5	82	
21	(1,1)	3	85	
22	(2,1)	2	87	
23	(2,0)	1	88	
24	(3,0)	2	90	
25	(4,0)	3	93	
26	(4,1)	1	94	
27	(5,1)	7	101	
28	(5,0)	2	103	

	Resu				
32	(4,2	2)	5	120	
31	(3,2)	2)	7	115	•••
30	(0,1)	1)	1	108	
29	(1,0	0)	4	107	•••

At the end of this traversal:

- All connected gold cells are visited
- Sum = 120
- This is the **maximum** among all components

♣ Final Output:

Output: 120

Output:-

Josephus in C++

```
#include <iostream>
using namespace std;

int solution(int n, int k) {
   if (n == 1) {
      return 0;
   }
   int x = solution(n - 1, k);
   int y = (x + k) % n;
   return y;
}

int main() {
   int n = 4;
   int k = 2;
   cout << solution(n, k) << endl;
   return 0;
}</pre>
```

Dry Run Table for solution(4, 2)

We'll compute this step-by-step recursively:

Function Call	Value Returned	Explanation
solution(1, 2)		Base case: Only one person, return 0
	0	
		Last survivor in 3 people = 2
solution(4, 2)	(2 + 2) % 4 = 0	Last survivor in 4 people = 0

∜ Final Output:

0

Output:-

Largest after k swaps in C++

```
#include <iostream>
using namespace std;
string max_str;
void findMaximum(string str, int k) {
  // Base case: When k swaps are used up
  if (k == 0) {
    return;
  }
  int n = str.length();
  // Find the maximum digit available for
current position
  for (int i = 0; i < n - 1; i++) {
    for (int j = i + 1; j < n; j++) {
       // If digit at position j is greater than
digit at position i, swap them
       if (str[j] > str[i]) 
          swap(str[i], str[j]);
          // Check if current string is larger
than previously found max
          if (str > max_str) {
            max_str = str;
          // Recur for k-1 swaps on the
modified string
          findMaximum(str, k - 1);
          // Backtrack: Swap again to revert
to original string
          swap(str[i], str[j]);
       }
  }
}
int main() {
  string str = "1234567";
  int k = 4;
  // Initialize max_str with the original
string
  max_str = str;
  // Find the maximum number possible after
k swaps
  findMaximum(str, k);
  // Print the maximum number found
  cout << max_str << endl;</pre>
  return 0;
}
```

Explanation of the Algorithm:

- For every pair (i, j) where i < j, if str[j] > str[i], swap i and j.
- After each swap, check if the new number is greater than the current max_str.
- Recurse with k 1.
- Backtrack (swap back) to explore other options.

Call#	k	Swap Made (i↔j)	str After Swap	max_str Before	max_str After	Remarks
1	4	0↔6	7234561	1234567	∜ 7234561	New max
2	3	1↔5	7634521	7234561	∜ 7634521	New max
3	2	2↔4	7654321	7634521	∜ 7654321	Final max
4	1	No beneficial swap	-	7654321	7654321	Stop recursion
5	3	1↔4	7534261	7654321	×	Not greater
6	3	1↔3	7435261	7654321	×	Not greater
7	2	2↔3 (from 7435261)	7453261	7654321	×	Still not better
	-					Many paths explored

We only continue recursion when beneficial. As you can see, once 7654321 is reached, **no further recursion produces a better result**, so that becomes the final output.

Final Output:

7654321

Lexicographic order in C++

```
#include <iostream>
using namespace std;
void dfs(int i, int n) {
  if (i > n) {
     return;
  cout \le i \le endl;
  for (int j = 0; j < 10; j++) {
     dfs(10 * i + j, n);
  }
}
int main() {
  int n = 40;
  for (int i = 1; i \le 9; i++) {
     dfs(i, n);
  }
  return 0;
```

Lexicographical Order Output:

This simulates how numbers are sorted like dictionary words:

```
1, 10, 100, ..., 11, 12, ..., 2, 20, 21, ..., 3, 30, ..., 4, 40, ..., 5, ..., 9
```

But only numbers ≤ 40 are printed.

I Dry Run Table (Partial for Clarity)

Here's a step-by-step snapshot of what's happening:

Function Call	i	Output	Explanation
dfs(1, 40)	1	⊘ 1	Valid, print
dfs(10, 40)	10	∜ 10	Valid, print
dfs(100, 40)	>40	×	Stop recursion
dfs(11, 40)	11	√ 11	Continue same way
dfs(12, 40)	12	∜ 12	
dfs(19, 40)	19	∜ 19	
dfs(2, 40)	2	⊘ 2	Start from next i
dfs(20, 40)	20	⊘ 20	
dfs(21, 40)	21	⊘ 21	
dfs(40, 40)	40	∜ 40	Final valid number
dfs(41, 40)	>40	×	Stop here

```
Output:-

1
10
11
12
13
14
15
16
17
18
```

19		
2		
20		
3		
4		
5		
6		
7		
8		
9		

Partition in K subsets in C++

```
#include <iostream>
#include <vector>
using namespace std;
int counter = 0;
void solution(int i, int n, int k, int nos,
vector<vector<int>>& ans) {
  if (i > n) {
     if (nos == k) {
       counter++;
       cout << counter << ". ";
       for (auto& set: ans) {
          cout << "[";
          for (auto num : set) {
            cout << num << " ";
          cout << "] ";
       cout << endl;
     return;
  for (int j = 0; j < ans.size(); j++) {
     if (!ans[j].empty()) {
       ans[j].push_back(i);
       solution(i + 1, n, k, nos, ans);
       ans[j].pop_back();
     } else {
       ans[j].push_back(i);
       solution(i + 1, n, k, nos + 1, ans);
       ans[j].pop_back();
       break;
  }
}
int main() {
  int n = 3;
  int k = 2;
  vector<vector<int>> ans(k);
  solution(1, n, k, 0, ans);
  return 0;
}
```

Dry Run Table:

Step	i	nos	ans (state)	Action Taken
1	1	0	[[], []]	Put 1 in first empty subset
2	2	1	[[1], []]	Put 2 in subset 0
3	3	1	[[1, 2], []]	Put 3 in subset 0
4	4	1		nos != k, discard
5	3	2	[[1, 2], [3]]	
6	2	2	[[1], [2]]	Output path starts
7	3	2	[[1, 3], [2]]	
8	3	2	[[1], [2, 3]]	

Final Output:

```
1. [1 2] [3]
2. [1 3] [2]
3. [1] [2 3]
```

Output:-

1. [1 2] [3]

2. [1 3] [2]

3. [1] [23]

Permutation in C++

```
#include <iostream>
using namespace std;
void permutations(int cb, int nboxes, int items[], int
ssf, int ritems, string asf) {
  if (cb > nboxes) {
     if (ssf == ritems) {
       cout << asf << endl;
     return;
  }
  for (int i = 0; i < ritems; i++) {
     if (items[i] == 0) {
       items[i] = 1;
       permutations(cb + 1, nboxes, items, ssf + 1,
ritems, asf + to_string(i + 1));
       items[i] = 0;
     }
  }
  permutations(cb + 1, nboxes, items, ssf, ritems, asf
+ "0");
}
int main() {
  int nboxes = 3;
  int ritems = 2;
  int cb = 1;
  int ssf = 0;
  int items[ritems] = {0}; // Initialize items array with
0s
  permutations(cb, nboxes, items, ssf, ritems, "");
  return 0;
```

Key Variables:

Var	Meaning
cb	current box index
ssf	selected so far – number of items placed
items[]	array of 0/1, indicating whether each item (1 to ritems) is used
asf	answer so far – the configuration of items across boxes

Dry Run Table:

cb	items	ssf	asf	Description
1	[0,0]	0	""	Start, box 1
2	[1,0]	1	"1"	Place item 1 in box 1
3	[1,1]	2	"12"	Place item 2 in box 2
4	[1,1]	2	"120"	
3	[1,1]	2	"102"	item2 in box3
3	[1,0]	1	"10"	skip box 2
4	[1,1]	2	"102"	
2	[0,1]	1	"2"	item2 in box 1
3	[1,1]	2	"21"	item1 in box2
4	[1,1]	2	"210"	Output
3	[0,1]	1	"20"	box2 empty
4	[1,1]	2	"201"	Output
2	[0,0]	0	"0"	box1 empty
3	[1,0]	1	"01"	item1 in box2
4	[1,1]	2	"012"	
3	[0,1]	1	"02"	item2 in box2
4	[1,1]	2	"021"	Output
3	[0,0]	0	"00"	box2 empty
4	-	0	"000"	X Not valid − ssf < ritems

Output:-

102		
210		
201		
012		
102 210 201 012 021		

Permutation of string in C++

```
#include <iostream>
#include <unordered_map>
using namespace std;
void generate(int cs, int ts, unordered_map<char,
int>& fmap, string asf) {
  if (cs > ts) {
    cout << asf << endl;
    return;
  }
  for (auto entry : fmap) {
    char ch = entry.first;
    int count = entry.second;
    if (count > 0) {
       fmap[ch]--;
       generate(cs + 1, ts, fmap, asf + ch);
       fmap[ch]++;
  }
}
int main() {
  string str = "abc";
  unordered_map<char, int> fmap;
  for (char ch: str) {
    fmap[ch]++;
  generate(1, str.length(), fmap, "");
  return 0;
```

Goal:

Generate all permutations of "abc" using recursion and a frequency map.

ℰ Setup:

- fmap: { a:1, b:1, c:1 }
- ts = total size = 3
- cs = current size (starts from 1)
- asf = answer so far

Dry Run Table

Call Stack	fmap (a,b,c)	asf	$\mathbf{c}\mathbf{s}$	Output?
generate(1, 3, {1,1,1}, """)				
L a \rightarrow generate(2, 3, {0,1,1}, "a")		"a"	2	
$L b \rightarrow generate(3, 3, \{0,0,1\}, "ab")$		"ab"	3	
$L c \rightarrow generate(4, 3, \{0,0,0\}, "abc")$		"abc"	4	∀ Print
$^{L}\mathrm{c} o \mathrm{backtrack}$ to "ab"				
$L c \rightarrow generate(3, 3, \{0,1,0\}, "ac")$		"ac"	3	
$L b \rightarrow generate(4, 3, \{0,0,0\}, "acb")$		"acb"	4	∀ Print
$^{L}\mathrm{b} \to \mathrm{backtrack}\;\mathrm{to}$ "a"				
$L b \rightarrow generate(2, 3, \{1,0,1\}, "b")$		"b"	2	
L a \rightarrow generate(3, 3, $\{0,0,1\}$, "ba")		"ba"	3	
$L c \rightarrow generate(4, 3, \{0,0,0\}, "bac")$		"bac"	4	∀ Print
$L c \rightarrow generate(3, 3, \{1,0,0\}, "bc")$		"bc"	3	
L a \rightarrow generate(4, 3, $\{0,0,0\}$, "bca")		"bca"	4	∀ Print
$\ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ $		"c"	2	
L a \rightarrow generate(3, 3, $\{0,1,0\}$, "ca")		"ca"	3	
$\begin{array}{c} \label{eq:Lb} \begin{picture}(1,2) \put(0,0,0){\line(0,0){\line(0,0){\lin$		"cab"	4	∀ Print
$L b \rightarrow generate(3, 3, \{1,0,0\}, "cb")$		"cb"	3	
$\begin{array}{c} L \; a \to generate(4,3,\\ \{0,0,0\},"cba") \end{array}$		"cba"	4	∀ Print

Output:- cba cab bca bac acb abc			
cba			
cab			
bca			
bac			
acb			
abc			

Remove Invalid Parenthesis in C++

```
#include <iostream>
#include <string>
#include <unordered set>
#include <stack>
using namespace std;
void solution(string str, int mra,
unordered_set<string>& ans);
int getMin(string str);
void solution(string str, int mra,
unordered set<string>& ans) {
  if (mra == 0) {
     int mrnow = getMin(str);
     if (mrnow == 0) {
       if (ans.find(str) == ans.end()) {
          cout \ll str \ll endl;
          ans.insert(str);
     return;
  for (int i = 0; i < str.length(); i++) {
     string left = str.substr(0, i);
     string right = str.substr(i + 1);
     solution(left + right, mra - 1, ans);
}
int getMin(string str) {
  stack<char> st:
  for (int i = 0; i < str.length(); i++) {
     char ch = str[i];
     if (ch == '(')  {
       st.push(ch);
     } else if (ch == ')') {
       if (st.empty()) {
          st.push(ch);
       else if (st.top() == ')') {
          st.push(ch);
       else if (st.top() == '(') {
          st.pop();
  }
  return st.size();
int main() {
  string str = "((((())))";
  unordered set<string> ans;
  int mra = getMin(str);
  solution(str, mra, ans);
  return 0;
```

Goal:

Remove the **minimum number** of parentheses to make the string valid.

★ Step 1: getMin("((((()))")

Step Char Stack Action

```
1
             (
                    push
             ((
                    push
3
             (((
                    push
4
             ((((
                    push
5
      (
             (((((
                    push
      )
             ((((
                    pop (match)
      )
             (((
                    pop (match)
      )
             ((
                    pop (match)
```

□ Final stack size = ((\rightarrow 2 unmatched \checkmark So mra = 2 (Minimum Removals Allowed)

Step 2: Recursive Dry Run Table

We'll track:

Call #	Current String (str)	Removals Left (mra)		Is Valid (getMin=0)?	Output
1	((((()))	2	Start	X (getMin=2)	
2	(((()))	1	Removed char at index 0	X (getMin=1)	
3	((()))	0	Removed char at index 0	∜ (getMin=0)	<> ((()))
4	(same string)	0	Duplicate path	✓	(skipped by set)
	many more paths tried	≤ 0	But not valid	Х	

Only ((())) satisfies getMin == 0 with exactly 2 removals

Final Output:
((()))

Subsequence in C++

```
#include <iostream>
#include <string>
using namespace std;
void sol(string q, string a) {
  if (q.length() == 0) {
    cout << a << "-" << endl;
    return;
  }
  char ch = q[0];
  string rest = q.substr(1);
  sol(rest, a);
  sol(rest, a + ch);
int main() {
  string s = "abc";
  sol(s, "");
  return 0;
```

Execution Tree:

We'll denote:

- q = remaining string
- a = answer so far

Call#	q	a	Output if base case
1	abc	"""	
2	bc	""	
3	с	"""	
4	""	""	-
5	""	"c"	c-
6	bc	"b"	
7	c	"b"	
8	""	"b"	b-
9	""	"bc"	bc-
10	abc	"a"	
11	bc	"a"	
12	c	"a"	
13	""	"a"	a-
14	""	"ac"	ac-
15	bc	"ab"	
16	c	"ab"	
17	""	"ab"	ab-
18	""	"abc"	abc-

\checkmark Final Output (Subsequences with -):

cbbcaacababc-

Output:-

cb-

bc-

a-

ac-

ab-

abc-

#include <iostream> #include <unordered_set> #include <string> using namespace std; void wordBreak(string str, string ans, unordered_set<string>& dict) { $if (str.length() == 0) {$ cout << ans << endl; return: } for (int i = 0; i < str.length(); i++) { string left = str.substr(0, i + 1);if (dict.find(left) != dict.end()) { string right = str.substr(i + 1); $wordBreak(right,\,ans+left+"",$ dict); } int main() { int n = 5; unordered_set<string> dict = {"microsoft", "hiring", "at", "kolkata"}; string sentence = "microsofthiring"; wordBreak(sentence, "", dict); return 0;

Word Break in C++

Dry Run Table:

Call	str	ans	Lo op i	left = str.substr(0 , i+1)	left in dict ?	Action Taken
1	microsofthir ing	""	0	m	×	skip
1	microsofthir ing	""	1	mi	×	skip
1	microsofthir ing	""	2	mic	×	skip
1	microsofthir ing	""	3	micr	×	skip
1	microsofthir ing	""	4	micro	×	skip
1	microsofthir ing	""	5	micros	×	skip
1	microsofthir ing	""	6	microso	×	skip
1	microsofthir ing	""	7	microsof	×	skip
1	microsofthir ing	""	8	microsoft	✓	Recurse with str=hiring, ans=microso ft
2	hiring	microsoft	0	h	×	skip
2	hiring	microsoft	1	hi	×	skip
2	hiring	microsoft	2	hir	×	skip
2	hiring	microsoft	3	hiri	×	skip
2	hiring	microsoft	4	hirin	×	skip
2	hiring	microsoft	5	hiring	≪	Recurse with str="", ans=microso ft hiring
3	""	microsoft hiring	-	_		Print: microsoft hiring

ℰ Final Output:

microsoft hiring

Output:-	
microsoft hiring	

Check number exists in array in C++

```
#include <iostream>
using namespace std;
int array11(int nums[], int index, int length) {
  if (index \ge length) {
     return 0;
  int small = array11(nums, index + 1, length);
  if (nums[index] == 11) {
     return 1 + small;
  } else {
     return small;
int main() {
  int arr[] = \{1, 11, 3, 11, 11, 11\};
  int length = sizeof(arr) / sizeof(arr[0]);
  cout << array11(arr, 0, length) << endl;</pre>
  return 0;
}
```

Input

```
arr = \{1, 11, 3, 11, 11, 11\}
```

Q Function Call Tree

```
array11(arr, 0, 6)

→ nums[0] == 1 → skip

→ array11(arr, 1, 6)

→ nums[1] == 11 → count +1

→ array11(arr, 2, 6)

→ nums[2] == 3 → skip

→ array11(arr, 3, 6)

→ nums[3] == 11 → count +1

→ array11(arr, 4, 6)

→ nums[4] == 11 → count +1

→ array11(arr, 5, 6)

→ nums[5] == 11 → count +1

→ array11(arr, 6, 6)

→ index >= length → return 0
```

Dry Run Table

Call	index	nums[index]	Matches 11?	Return Value
array11(arr, 0, 6)	0	1	×	0 + 4 = 4
array11(arr, 1, 6)	1	11		1 + 3 = 4
array11(arr, 2, 6)	2	3	×	0 + 3 = 3
array11(arr, 3, 6)	3	11		1 + 2 = 3
array11(arr, 4, 6)	4	11		1 + 1 = 2
array11(arr, 5, 6)	5	11	≪	1 + 0 = 1
array11(arr, 6, 6)	6	N/A	N/A	0

Output

4

Output:-

#include <iostream> #include <string> using namespace std; bool is String Palindrome (const string & input, int s, int e) { // Base case: if start index equals end index, the string is a palindrome if (s == e) { return true; // If the characters at the start and end do not match, it's not a palindrome if (input[s] != input[e]) { return false; // If there are more characters to compare, call the function recursively if (s < e + 1) { return isStringPalindrome(input, s + 1, e - 1);} return true; } bool isStringPalindrome(const string& input) { int s = 0; int e = input.length() - 1; return isStringPalindrome(input, s, e); } int main() { cout << (isStringPalindrome("abba")? "true": "false") << endl; return 0:

Check Palindrome in C++

Input

string = "abba"

Q Function Call Tree

```
isStringPalindrome("abba", 0, 3)

→ 'a' == 'a' 

→ isStringPalindrome("abba", 1, 2)

→ 'b' == 'b' 

→ isStringPalindrome("abba", 2, 1)

→ s > e → return true
```

Dry Run Table

Call	s	е	input[s]	input[e]	Match?	Return
isStringPalindrome	0	3	'a'	'a'	\sim	√/
("abba", 0, 3)					\	V
isStringPalindrome			., .	., .		^
("abba", 1, 2)	1	2	'b'	'b'	≪	≪
isStringPalindrome						^
("abba", 2, 1)	2	1	N/A	N/A	Base	\≪

Output

true

Your program will print:

true

Output:true

Check sorted in C++

```
#include <iostream>
using namespace std;

bool sorted(int arr[], int n) {
   if (n == 1 | | n == 0) {
      return true;
   } else if (arr[n - 1] < arr[n - 2]) {
      return false;
   } else {
      return sorted(arr, n - 1);
   }
}

int main() {
   int arr[] = {1, 2, 3, 4, 5};
   int n = sizeof(arr) / sizeof(arr[0]);
   cout << boolalpha << sorted(arr, n) << endl;
   return 0;
}</pre>
```

Input

```
arr[] = \{1, 2, 3, 4, 5\}

n = 5
```

A Recursive Calls

We check if the last two elements are in correct order $(arr[n-2] \le arr[n-1])$, and recursively reduce the array size.

Dry Run Table

Call	n	arr[n- 2]	arr[n- 1]	Comparison	Result
sorted(arr, 5)	5	4	5	4 ≤ 5	≪
sorted(arr, 4)	4	3	4	3 ≤ 4	8
sorted(arr, 3)	3	2	3	2 ≤ 3	⊗
sorted(arr, 2)	2	1	2	1 ≤ 2	≪
sorted(arr, 1)	1	_	_	Base case	<

Output

true

Your program will print:

true

Output:true

Count zeroes in C++

```
#include <iostream>
using namespace std;
int cnt = 0;
int countZerosRec(int input) {
  // Base case for initial input of \mathbf{0}
  if (input == 0 \&\& cnt == 0) {
     return 1;
  }
  // Base case for recursion
  if (input == 0) {
     return cnt;
  }
  // Check if the current last digit is zero
  if (input \% 10 == 0) {
     cnt++;
  /\!/ Recursive call to process the next digit
  return countZerosRec(input / 10);
}
int main() {
  cout \le countZerosRec(10034) \le endl;
  return 0;
}
```

Dry Run for countZerosRec(10034)

Call	input	input % 10	is zero?	sum
countZerosRec(10034)	10034	4	×	0 + next
countZerosRec(1003)	1003	3	×	0 + next
countZerosRec(100)	100	0	≪	1 + next
countZerosRec(10)	10	0	≪	1 + next
countZerosRec(1)	1	-	×	0

 \rightarrow Total = 1 + 1 = 2

Output:-

Factorial in C++

```
#include <iostream>
using namespace std;
int fact(int n) {
   if (n == 0) {
      return 1;
   } else {
      int prev = fact(n - 1);
      return n * prev;
   }
}
int main() {
   cout << fact(6) << endl;
   return 0;
}</pre>
```

Dry Run Table for fact(6):

Call Level	n	Recursive Call	Returned Value	Computation
1	6	6 * fact(5)	720	6 * 120
2	5	5 * fact(4)	120	5 * 24
3	4	4 * fact(3)	24	4 * 6
4	3	3 * fact(2)	6	3 * 2
5	2	2 * fact(1)	2	2 * 1
6	1	1 * fact(0)	1	1 * 1
7 (Base)	0	return 1	1	Base case hit

⚠ Final Output:

720

Min-Max in C++

```
#include <iostream>
#include <climits> // for INT_MAX and INT_MIN
using namespace std;
int\ getMin(int\ arr[],\ int\ i,\ int\ n)\ \{
  if (n == 1) {
     return arr[i];
  } else {
     return min(arr[i], getMin(arr, i + 1, n - 1));
}
int getMax(int arr[], int i, int n) {
  if (n == 1) {
     return arr[i];
  } else {
     return max(arr[i], getMax(arr, i + 1, n - 1));
}
int main() {
  int arr[] = \{12, 8, 45, 67, 9\};
  int n = sizeof(arr) / sizeof(arr[0]);
  cout << "Minimum element of array: " <<
getMin(arr, 0, n) << endl;
  cout << "Maximum element of array: " <<
getMax(arr, 0, n) \leq endl;
  return 0;
```

Dry Run Table for getMin(arr, 0, 5)

Call Level	i	arr[i]	Recursive Call	Returned Value	Computation
1	0	12	min(12, getMin(1, 4))	8	min(12, 8)
2	1	8	min(8, getMin(2, 3))	8	min(8, 9)
3	2	45	min(45, getMin(3, 2))	9	min(45, 9)
4	3	67	min(67, getMin(4, 1))	9	min(67, 9)
5 (base)	4	9	return arr[4]	9	Base case

Dry Run Table for getMax(arr, 0, 5)

Call Level	i	arr[i]	Recursive Call	Returned Value	Computation
1	0	12	max(12, getMax(1, 4))	67	max(12, 67)
2	1	8	max(8, getMax(2, 3))	67	max(8, 67)
3	2	45	max(45, getMax(3, 2))	67	max(45, 67)
4	3	67	max(67, getMax(4, 1))	67	max(67, 9)
5 (base)	4	9	return arr[4]	9	Base case

∜ Final Output:

Minimum element of array: 8 Maximum element of array: 67

Minimum element of array: 8 Maximum element of array: 67

Stair Case in C++

```
#include <iostream>
using namespace std;
// Function to calculate number of ways to reach nth
int staircase(int n) {
  // Base cases
  if (n == 0 \mid | n == 1) {
     return 1;
  if (n == 2) {
     return 2;
  // Recursive case
  return staircase(n-1) + staircase(n-2) +
staircase(n-3);
int main() {
  // Test case
  int n = 7;
  cout << staircase(n) << endl;</pre>
  return 0;
```

Dry Run Table for staircase (7)

Track the **calls** and their **return values** from the bottom up (memoized-style for understanding):

n	staircase(n) Calculation	Result
0	1 (base case)	1
1	1 (base case)	1
2	2 (base case)	2
3	staircase(2) + staircase(1) + staircase(0)	2 + 1 + 1 = 4
4	staircase(3) + staircase(2) + staircase(1)	4 + 2 + 1 = 7
5	staircase(4) + staircase(3) + staircase(2)	7 + 4 + 2 = 13
6	staircase(5) + staircase(4) + staircase(3)	13 + 7 + 4 = 24
7	staircase(6) + staircase(5) + staircase(4)	24 + 13 + 7 = 44

∜ Final Output:

44

Subset Sum in C++

```
#include <iostream>
using namespace std;
// Function to calculate subset sums recursively
void subsetSums(int arr[], int l, int r, int sum) {
  // Base case: if l exceeds r, print the current sum
  if (l > r) {
    cout << sum << " ";
    return;
  }
  // Recursive case: include current element arr[l] in
the subset sum
  subsetSums(arr, l + 1, r, sum + arr[l]);
int main() {
  // Initialize the array and its length
  int arr[] = \{5, 4, 3, 5, 4\};
  int n = sizeof(arr) / sizeof(arr[0]);
  // Call the function to calculate subset sums,
starting with l=0, r=n-1, and initial sum=0
  subsetSums(arr, 0, n - 1, 0);
  return 0;
```

Input:

int arr[] = $\{5, 4, 3, 5, 4\};$

This adds:

$$5 + 4 + 3 + 5 + 4 = 21$$

And when 1 > r, it prints sum, which is 21.

Dry Run Table (for your input):

Step	1	r	sum	Action
1	0	4	0	sum = 0 + arr[0] = 5
2	1	4	5	sum = 5 + arr[1] = 9
3	2	4	9	sum = 9 + arr[2] = 12
4	3	4	12	sum = 12 + arr[3] = 17
5	4	4	17	sum = 17 + arr[4] = 21
6	5	4	21	1 > r, print 21 and return

∜ Final Output:

21

Output:-

```
Tiling in C++
#include <iostream>
                                                            Function
                                                                         Returns
                                                                                            Reason
using namespace std;
                                                              Call
                                                                                    tilingways(3) +
                                                         tilingways(4)
int tilingways(int n) {
                                                                                    tilingways(2)
  if (n == 0) {
                                                                                    tilingways(2) +
                                                         tilingways(3)
    return 0;
                                                                                    tilingways(1)
                                                                                    tilingways(1) +
  if (n == 1) {
                                                         tilingways(2)
                                                                                    tilingways(0)
    return 1;
                                                                        1
                                                                                    Base case
                                                         tilingways(1)
  }
                                                                                    Wrong base case — it
  return tilingways(n - 1) + tilingways(n - 2);
                                                         tilingways(0)
                                                                        0 X
                                                                                    should be 1
}
                                                         tilingways(2)
                                                                        1 + 0 = 1
int main() {
                                                                                    Base case
                                                         tilingways(1)
                                                                        1
  cout << tilingways(4) << endl;</pre>
                                                                         1 + 1 = 2
                                                         tilingways(3)
  return 0;
                                                         tilingways(2)
                                                                                    Already computed
                                                                        1
                                                                        2 + 1 = 3
                                                         tilingways(4)
```