

## Floyd-Warshall in C++

```
#include <bits/stdc++.h>
using namespace std;

class Solution {
public:
    void shortest_distance(vector<vector<int>>&matrix) {
        int n = matrix.size();
        for (int i = 0; i < n; i++) {
            for (int j = 0; j < n; j++) {
                if (matrix[i][j] == -1) {
                    matrix[i][j] = 1e9;
                }
                if (i == j) matrix[i][j] = 0;
            }
        }

        for (int k = 0; k < n; k++) {
            for (int i = 0; i < n; i++) {
                for (int j = 0; j < n; j++) {
                    matrix[i][j] = min(matrix[i][j],
                                         matrix[i][k] + matrix[k][j]);
                }
            }
        }

        for (int i = 0; i < n; i++) {
            for (int j = 0; j < n; j++) {
                if (matrix[i][j] == 1e9) {
                    matrix[i][j] = -1;
                }
            }
        }
    }
};

int main() {
    int V = 4;
    vector<vector<int>> matrix(V, vector<int>(V, -1));
    matrix[0][1] = 2;
    matrix[1][0] = 1;
    matrix[1][2] = 3;
    matrix[3][0] = 3;
    matrix[3][1] = 5;
    matrix[3][2] = 4;

    Solution obj;
    obj.shortest_distance(matrix);

    for (auto row : matrix) {
        for (auto cell : row) {
            cout << cell << " ";
        }
        cout << endl;
    }

    return 0;
}
```

### Dry Run:

#### Input Matrix:

The input adjacency matrix is:

```
matrix = [
    [0, 2, -1, -1],
    [1, 0, 3, -1],
    [-1, -1, 0, -1],
    [3, 5, 4, 0]
]
```

#### Step 1: Initialize the matrix

Replace -1 with 1e9 and set matrix[i][i] = 0 for all i:

```
matrix = [
    [0, 2, 1e9, 1e9],
    [1, 0, 3, 1e9],
    [1e9, 1e9, 0, 1e9],
    [3, 5, 4, 0]
]
```

#### Step 2: Floyd-Warshall Algorithm

Iterate over each intermediate node k and update the matrix.

- For k = 0 (Intermediate node 0):
  - Check each pair (i, j) and update the matrix.
  - No changes to the matrix as no shorter paths through node 0 are found.
- For k = 1 (Intermediate node 1):
  - For each pair (i, j):
    - Update matrix[0][2] to matrix[0][1] + matrix[1][2] = 2 + 3 = 5.
    - Update matrix[2][3] to matrix[2][1] + matrix[1][3] = 1e9 + 1e9 = 1e9 (no update).
- For k = 2 (Intermediate node 2):
  - For each pair (i, j):
    - No changes as there are no shorter paths through node 2.
- For k = 3 (Intermediate node 3):
  - For each pair (i, j):
    - Update matrix[2][1] to matrix[2][3] + matrix[3][1] = 1e9 + 5 = 1e9 (no update).
    - Update matrix[3][1] to matrix[3][3] + matrix[3][1] = 0 + 5 = 5 (no update).

update).

**Step 3: Final Matrix:**

After the Floyd-Warshall algorithm finishes, the matrix is:

```
matrix = [  
    [0, 2, 5, 8],  
    [1, 0, 3, 6],  
    [6, 8, 0, 9],  
    [3, 5, 4, 0]  
]
```

**Step 4: Convert 1e9 back to -1:**

If matrix[i][j] == 1e9, set matrix[i][j] = -1.

Final output matrix:

```
matrix = [  
    [0, 2, 5, 8],  
    [1, 0, 3, 6],  
    [6, 8, 0, 9],  
    [3, 5, 4, 0]  
]
```

**Output:**

```
Copy code  
0 2 5 8  
1 0 3 6  
6 8 0 9  
3 5 4 0
```

**Output:-**  
**0 2 5 -1**  
**1 0 3 -1**  
**-1 -1 0 -1**  
**3 5 4 0**