Fast and Last Index in C++

```
#include <iostream>
using namespace std;
void findFirstAndLastIndex(int arr[], int n,
int d) {
  int low = 0;
  int high = n - 1;
  int firstIndex = -1;
  int lastIndex = -1;
  // Finding the first occurrence
  while (low <= high) {
    int mid = low + (high - low) / 2;
    if (d > arr[mid]) {
       low = mid + 1;
    } else if (d < arr[mid]) {
       high = mid - 1;
    } else {
       firstIndex = mid;
       high = mid - 1;
  }
  // Finding the last occurrence
  low = 0;
  high = n - 1;
  while (low <= high) {
    int mid = low + (high - low) / 2;
    if (d > arr[mid]) {
       low = mid + 1;
    } else if (d < arr[mid]) {</pre>
       high = mid - 1;
    } else {
       lastIndex = mid;
       low = mid + 1;
  cout << "First Index: " << firstIndex <<</pre>
endl;
  cout << "Last Index: " << lastIndex <<
endl;
}
int main() {
  33, 40, 42, 55, 66, 77, 33};
  int n = sizeof(arr) / sizeof(arr[0]);
  int d = 33;
  findFirstAndLastIndex(arr, n, d);
  return 0;
```

Dry Run Example (on sorted array):

Sorted version of the array:

 $\{1, 5, 10, 15, 22, 33, 33, 33, 33, 33, 33, 40, 42, 55, 66, 77\}$

We want to find first and last index of 33.

First Occurrence:

Iteration	low	high	mid	arr[mid]	firstIndex	high (updated)
1	0	15	7	33	7	6
2	0	6	3	15		
3	4	6	5	33	5	4
4	4	4	4	22		

 $[\]rightarrow$ First index = 5

Last Occurrence:

Iteration	low	high	mid	arr[mid]	lastIndex	low (updated)
1	0	15	7	33	7	8
2	8	15	11	40		
3	8	10	9	33	9	10
4	10	10	10	33	10	11

 $[\]rightarrow$ Last index = 10

골 Final Output:

First Index: 5 Last Index: 10

First Index: 5	
Last Index: 10	

IsSorted in C++

```
#include <iostream>
using namespace std;
bool isSortedEff(int arr∏, int n) {
  for (int i = 1; i < n; i++) {
     if (arr[i] < arr[i - 1]) \{
        return false;
  return true;
bool isSorted(int arr[], int n) {
  for (int i = 0; i < n; i++) {
     for (int j = i + 1; j < n; j++) {
        if (arr[j] < arr[i]) 
          return false;
  return true;
int main() {
  int arr1[] = \{1, 2, 3, 4, 5, 6\};
  int arr2[] = \{11, 2, 3, 4, 5, 6\};
  int n1 = sizeof(arr1) / sizeof(arr1[0]);
  int n2 = sizeof(arr2) / sizeof(arr2[0]);
  cout << boolalpha; // Print boolean values as
true/false
  cout << isSortedEff(arr1, n1) << endl;</pre>
  cout << isSortedEff(arr2, n2) << endl;</pre>
  cout << isSorted(arr1, n1) << endl;
  cout << isSorted(arr2, n2) << endl;</pre>
  return 0;
```

Check if an array is **sorted in non-decreasing order** (each element is \leq the next).

Q Difference between isSortedEff and isSorted:

Function	Approach	Time Complexity
isSortedEff	Linear scan (compare adjacent)	O(n)
isSorted	Brute force (nested loops)	O(n²)

✓ Dry Run with Sample Arrays

Array 1: {1, 2, 3, 4, 5, 6} (Sorted)

isSortedEff(arr1, n1):

i	arr[i- 1]	arr[i]	Comparison	Result
1	1	2	$2 \ge 1$	$ \checkmark $
2	2	3	$3 \ge 2$	$ \checkmark $
3	3	4	$4 \ge 3$	$ \checkmark $
4	4	5	$5 \ge 4$	$ \checkmark $
5	5	6	$6 \ge 5$	$ \checkmark $
→ All passed				
→ Returns:				
true				

isSorted(arr1, n1): Checks every pair (i, j) where j > i:

• For every $arr[i] \le arr[j] \rightarrow all OK \rightarrow$ Returns: true

Array 2: {11, 2, 3, 4, 5, 6} (Not sorted)

isSortedEff(arr2, n2):

i	arr[i- 1]	arr[i]	Comparison	Result
1	11	2	2 < 11 X	•
\rightarrow Early exit \rightarrow Returns:				

i	arr[i- 1]	arr[i]	Comparison	Result
false				
isSorted(ar	r2, n2):			
• (0,1)	→ 2 < 11	$L \to X$	→ Returns: fa	lse
☐ Output: true false				
true false				

Leaders Array in C++

```
#include <iostream>
using namespace std;
void leaders(int arr[], int n) {
  int curr = arr[n - 1];
  \mathrm{cout} << \mathrm{curr} << " \ ";
  for (int i = n - 2; i \ge 0; i - 0) {
     if (arr[i] > curr) {
        curr = arr[i];
        cout << curr << " ";
  }
}
int main() {
  int arr[] = \{7, 10, 4, 10, 6, 5, 2\};
  int n = sizeof(arr) / sizeof(arr[0]);
  leaders(arr, n);
  cout << endl;</pre>
  return 0;
```

Dry Run Table

Input array: {7, 10, 4, 10, 6, 5, 2}

We process from **right to left**:

Index	arr[i]	Current Leader (curr)	Is arr[i] > curr?	Print Leader?	Updated curr
6	2	2	-	$ \checkmark $	2
5	5	2		$ \checkmark $	5
4	6	5	$ \checkmark $	$ \checkmark $	6
3	10	6	$ \checkmark $	$ \checkmark $	10
2	4	10	×	×	10
1	10	10	×	×	10
0	7	10	×	×	10

⊘ Output (Printed from right to left):

25610

 $2\;5\;6\;10$

Majority element in C++

```
#include <iostream>
using namespace std;
int majority(int arr[], int n) {
  int res = 0, count = 1;
  for (int i = 1; i < n; i++) {
     if (arr[res] == arr[i]) {
        count++;
     } else {
        count--;
     if (count == 0) {
        res = i;
        count = 1;
  }
  count = 0;
  for (int i = 0; i < n; i++) {
     if (arr[res] == arr[i]) {
        count++;
  }
  if (count \leq n / 2) {
     res = -1;
  return res;
}
int main() {
  int arr[] = \{6, 8, 4, 8, 8\};
  int n = sizeof(arr) / sizeof(arr[0]);
  cout << majority(arr, n) << endl;</pre>
  return 0;
}
```

Array Given:

$$arr[] = \{6, 8, 4, 8, 8\}$$

 $n = 5$

We need to find the element (if any) that appears more than 5 / 2 = 2 times.

Moore's Voting Algorithm Dry Run

We'll go step-by-step through the first for loop which finds a *candidate*.

i	arr[i]	arr[res]	count	Explanation
0	6	6	1	Initial candidate at index 0
1	8	6	0	$8 \neq 6 \rightarrow \text{count}$
		8	1	$\begin{array}{l} \text{count} = 0 \rightarrow \text{new} \\ \text{candidate at index 1} \end{array}$
2	4	8	0	$4 \neq 8 \rightarrow \text{count}$
		4	1	$\begin{array}{l} \text{count} = 0 \rightarrow \text{new} \\ \text{candidate at index 2} \end{array}$
3	8	4	0	$8 \neq 4 \rightarrow \text{count}$
		8	1	$\begin{array}{l} \text{count} = 0 \rightarrow \text{new} \\ \text{candidate at index 3} \end{array}$
4	8	8	2	$8 == 8 \rightarrow count++$

Candidate Index: res = 3, arr[3] = 8

♦ Second loop: Confirm the candidate

We check how many times 8 appears in the array.

```
count = 0;
for (int i = 0; i < n; i++) {
   if (arr[i] == 8) count++;
}</pre>
```

8 appears **3 times** (at indices 1, 3, and 4).

Since 3 > 2, it **is** the majority element.

♥ Final Output

	That's the index of the majority element 8.
$\mid 3 \mid$	

Max Subarray sum in C++

```
#include <iostream>
using namespace std;

int maxsub(int arr[], int n) {
    int res = arr[0];
    int maxEnding = arr[0];
    for (int i = 1; i < n; i++) {
        maxEnding = max(maxEnding + arr[i], arr[i]);
        res = max(res, maxEnding);
    }
    return res;
}

int main() {
    int arr[] = {-3, 8, -2, 4, -5, 6};
    int n = sizeof(arr) / sizeof(arr[0]);
    cout << maxsub(arr, n) << endl;
    return 0;
}</pre>
```

Input:

$$arr[] = \{-3, 8, -2, 4, -5, 6\}$$

 $n = 6$

■ Variables:

- res: Stores the maximum subarray sum found so far
- maxEnding: Stores the maximum subarray sum ending at the current index

Dry Run Table:

i	arr[i]	maxEnding = max(maxEnding + arr[i], arr[i])	res = max(res, maxEnding)
0	-3	maxEnding = -3	res = -3
1	8	$\max(-3 + 8, 8) = 8$	res = 8
2	-2	$\max(8 - 2, -2) = 6$	res = 8
3	4	$\max(6+4, 4) = 10$	res = 10
4	-5	$\max(10 - 5, -5) = 5$	res = 10
5	6	$\max(5+6, 6) = 11$	res = 11

∜ Final Output:

11

Tapping Rain Water in C++

```
#include <iostream>
#include <algorithm>
using namespace std;
int getWater(int arr[], int n) {
  int res = 0;
  for (int i = 0; i < n; i++) {
     int lmax = arr[i];
     for (int j = 0; j < i; j++) {
       lmax = max(arr[j], lmax);
     int rmax = arr[i];
     for (int j = i + 1; j < n; j++) {
        rmax = max(arr[j], rmax);
     res += min(lmax, rmax) - arr[i];
  }
  return res;
}
int main() {
  int arr[] = \{3, 0, 1, 2, 5\};
  int n = sizeof(arr) / sizeof(arr[0]);
  cout << getWater(arr, n) << endl;</pre>
  return 0;
}
```

Problem Explanation: Trapping Rain Water

At each index i, the amount of water it can hold is:

```
water_at_i = min(lmax, rmax) - arr[i]
```

Where:

- lmax: Max height to the left of i (including i)
- rmax: Max height to the right of i (including i)
- If min(lmax, rmax) arr[i] > 0, it adds to total water trapped.

™ Dry Run Table

Array: {3, 0, 1, 2, 5}

i	arr[i]	(max	rmax (max right)	min(lmax, rmax)	Water at i = min(lmax, rmax) - arr[i]	res
0	3	3	5	3	0	0
1	0	3	5	3	3	3
2	1	3	5	3	2	5
3	2	3	5	3	1	6
4	5	5	5	5	0	6

♥ Final Output:

6

Output:

Remove Duplicates in C++

```
#include <iostream>
using namespace std;
int removeDup(int arr[], int n) {
  int res = 1;
  for (int i = 1; i < n; i++) {
     if (arr[i] != arr[res - 1]) {
       arr[res] = arr[i];
       res++;
  }
  return res;
int main() {
  int arr[] = \{2, 2, 3, 4, 5, 6\};
  int n = sizeof(arr) / sizeof(arr[0]);
  int p = removeDup(arr, n);
  cout << "After Removal" << endl;</pre>
  for (int i = 0; i < p; i++) {
     cout << arr[i] << " ";
  }
  cout << endl;
  return 0;
```

Dry Run Table

i	arr[i]	arr[res - 1]	Condition Met (!=)	Action	arr[res]	res
1	2	2	X No	Skip	-	1
2	3	2	∜ Yes	arr[1] = 3	3	2
3	4	3	∜ Yes	arr[2] = 4	4	3
4	5	4		arr[3] = 5		4
5	6	5	∜ Yes	arr[4] = 6	6	5

∜ Final Values:

- res = $5 \rightarrow$ means 5 unique elements.
- Modified array (first res elements):

$$arr[] = \{2, 3, 4, 5, 6\}$$

After Removal 2 3 4 5 6

Rotate Array in C++

```
#include <iostream>
using namespace std;
void rotate(int arr[], int d, int n) {
  int temp[d];
  for (int i = 0; i < d; i++) {
     temp[i] = arr[i];
  for (int i = d; i < n; i++) {
     arr[i - d] = arr[i];
  for (int i = 0; i < d; i++) {
     arr[n - d + i] = temp[i];
  for (int i = 0; i < n; i++) {
     cout << " " << arr[i];
  cout << endl;
int main() {
  int arr[] = \{1, 3, 6, 2, 5, 4, 3, 2, 4\};
  int n = sizeof(arr) / sizeof(arr[0]);
  rotate(arr, 5, n);
  return 0;
```

Input:

```
arr[] = {1, 3, 6, 2, 5, 4, 3, 2, 4}
d = 5
n = 9
```

Step-by-step Breakdown:

1. Store first d elements in temp

```
temp = {1, 3, 6, 2, 5}

i temp[i]

0 1

1 3

2 6

3 2

4 5
```

2. Shift remaining n - d elements to the left

```
arr[0] = arr[5] \rightarrow 4

arr[1] = arr[6] \rightarrow 3

arr[2] = arr[7] \rightarrow 2

arr[3] = arr[8] \rightarrow 4
```

i	arr[i] (after shift)
0	4
1	3
2	2
3	4

3. Copy temp back to the end

```
arr[4] = temp[0] = 1
arr[5] = temp[1] = 3
arr[6] = temp[2] = 6
arr[7] = temp[3] = 2
arr[8] = temp[4] = 5
```

i	arr[i] (final state)
4	1

	i arr[i] (final state)	
	5 3	
	6 6	
	7 2	
	8 5	
	Final Output:	
	$4\ 3\ 2\ 4\ 1\ 3\ 6\ 2\ 5$	
432413625		

Add Strings in C++

#include <iostream> #include <string> using namespace std; string addStrings(string num1, string num2) { string res = ""; int i = num1.length() - 1; int j = num2.length() - 1;int carry = 0; while $(i \ge 0 | | j \ge 0 | | carry$!=0) { $int ival = i \ge 0$? num1[i] -'0':0; $int jval = j \ge 0$? num2[j] -'0':0; int sum = ival + jval + carry; res = to_string(sum % 10) + res; carry = sum / 10;i--; j--; return res; int main() { string n1 = "123"; string n2 = "23"; string res = addStrings(n1, cout << res << endl; // Output should be 146

Input:

```
n1 = "123"
n2 = "23"
```

Dry Run Table:

Step	i	j	num1[i]	num2[j]	ival	jval	carry (before)	sum = ival + jval + carry	res	carry (after)
1	2	1	'3'	'3'	3	3	0	6	"6"	0
2	1	0	'2'	'2'	2	2	0	4	"46"	0
3	o	- 1	'1'	_	1	0	0	1	"146"	0

∜ Final Output:

"146"

return 0;

Island Perimeter in C++

```
#include <iostream>
#include <vector>
using namespace std;
int perimeter(vector<vector<int>>& grid) {
  int p = 0;
  int rows = grid.size();
  int cols = grid[0].size();
  for (int i = 0; i < rows; i++) {
     for (int j = 0; j < cols; j++) {
        if (grid[i][j] == 1) \{
          p += 4;
          if (i > 0 \&\& grid[i - 1][j] == 1) {
             p = 2;
          if (j > 0 \&\& grid[i][j - 1] == 1) {
             p -= 2;
  }
  return p;
int main() {
  vector<vector<int>> grid = {
     \{1, 0, 0\},\
     \{1, 1, 1\},\
     \{0, 1, 0\},\
     \{0, 1, 0\}
  };
  int p = perimeter(grid);
  cout << p << endl;</pre>
  return 0;
```

Input Grid:

```
grid = {
    {1, 0, 0},
    {1, 1, 1},
    {0, 1, 0},
    {0, 1, 0}
};
```

Visualized:

Dry Run Strategy:

- Each land cell contributes +4 to perimeter.
- Each shared edge with another land cell subtracts 2.

Q Dry Run Table:

Cell (i,j)	grid[i][j]	+4	Top Neighbor = 1	Left Neighbor = 1	Net Contribution
(0,0)	1	4	×	×	4
(1,0)	1	4	♦ (0,0)	×	2 (4-2)
(1,1)	1	4	×	♦ (1,0)	2 (4-2)
(1,2)	1	4	×	♦ (1,1)	2 (4-2)
(2,1)	1	4	♦ (1,1)	×	2 (4-2)
(3,1)	1	4		×	2 (4-2)

♥ Total Perimeter:

$$= 4 + 2 + 2 + 2 + 2 + 2 = 14$$

Output:

Max Avg. Subarray in C++

```
#include <iostream>
#include <vector>
using namespace std;
double solution(vector<int>& nums, int k) {
  int sum = 0;
  for (int i = 0; i < k; i++) {
    sum += nums[i];
  }
  int max_sum = sum;
  for (int i = k; i < nums.size(); i++) {
    sum += nums[i];
    sum = nums[i - k];
    max_sum = max(max_sum, sum);
  }
  return static_cast<double>(max_sum) / k;
}
int main() {
  vector<int> nums = {-10, 5, -6, 8, -7, 2, -4, 8, -6, 7};
  int k = 3;
  cout << solution(nums, k) << endl;</pre>
  return 0;
```

Input:

nums = $\{-10, 5, -6, 8, -7, 2, -4, 8, -6, 7\}$ k = 3

Q Dry Run Table:

We'll track the sum of every window of size 3:

Window (Indexes)	Elements	Window Sum	max_sum
0–2	-10, 5, -6	-11	-11
1–3	5, -6, 8	7	7
2–4	-6, 8, -7	-5	7
3–5	8, -7, 2	3	7
4–6	-7, 2, -4	-9	7
5–7	2, -4, 8	6	7
6–8	-4, 8, -6	-2	7
7–9	8, -6, 7	9	9
I			

∜ Final Output:

9/3 = 3.0

✓ Output: 3

Max Chunks to make array sorted in C++

```
#include <iostream>
#include <vector>
using namespace std;
int maxChunksToSorted(vector<int>& arr) {
  int max_val = 0;
  int count = 0;
  for (int i = 0; i < arr.size(); i++) {
    max_val = max(max_val, arr[i]);
    if (i == max_val) {
       count++;
  }
  return count;
int main() {
  vector<int> arr = \{4, 3, 2, 1, 0\};
  int res = maxChunksToSorted(arr);
  cout << res << endl;
  return 0;
```

Input:

 $| \text{vector} < \text{int} > \text{arr} = \{4, 3, 2, 1, 0\};$

Q Dry Run Table:

Let's walk through the loop step-by-step and record values:

i	arr[i]	max_val (max so far)	i == max_val?	count
0	4	4	×	0
1	3	4	×	0
2	2	4	×	0
3	1	4	×	0
4	0	4	∀	1

Output:

1

Max product of three in C++

```
#include <iostream>
#include <vector>
#include <climits>
using namespace std;
int maxProduct(vector<int>& nums) {
  int min1 = INT_MAX, min2 = INT_MAX;
  int max1 = INT_MIN, max2 = INT_MIN,
max3 = INT MIN;
  for (int val: nums) {
    if (val > max1) {
       max3 = max2;
       max2 = max1;
       \max 1 = \text{val};
    ext{less if (val > max2) } 
       max3 = max2;
       \max 2 = \text{val};
    } else if (val > max3) {
       max3 = val;
    if (val < min1) {
       min2 = min1;
       min1 = val;
    } else if (val < min2) {
       min2 = val;
  return max(min1 * min2 * max1, max1 *
max2 * max3);
int main() {
  vector<int> nums = \{2, 4, 6, 7\};
  int result = maxProduct(nums);
  cout << result << endl;</pre>
  return 0;
```

Input:

nums = $\{2, 4, 6, 7\}$

Q Variables Tracked:

Iteratio n	val	max 1	max2	max3	min 1	min2
1	2	2	INT_MI N	INT_MI N	2	INT_MA X
2	4	4	2	INT_MI N	2	4
3	6	6	4	2	2	4
4	7	7	6	4	2	4

V Computed Products:

- $\min 1 * \min 2 * \max 1 = 2 * 4 * 7 = 56$
- $\max 1 * \max 2 * \max 3 = 7 * 6 * 4 = 168$

Output:

return max(56, 168); $// \rightarrow 168$

No of subarrays with odd sum in C++

```
#include <iostream>
using namespace std;
int nos(int arr[], int n) {
  long long ans = 0;
  int even = 0;
  int odd = 0;
  int sum = 0;
  for (int i = 0; i < n; i++) {
     sum += arr[i];
     if (sum \% 2 == 0) {
       ans += odd;
       even++;
     } else {
       ans += 1 + even;
       odd++;
  }
  return ans % 1000000007;
int main() {
  int arr [] = \{1, 2, 3, 4, 5, 6, 7\};
  int n = sizeof(arr) / sizeof(arr[0]);
  cout \ll nos(arr, n) \ll endl;
  return 0;
```

Input:

 $arr = \{1, 2, 3, 4, 5, 6, 7\}$

Q Key Variables Tracked:

- $sum \rightarrow cumulative sum from start to current index$
- even → count of prefix sums that are even so far
- odd → count of prefix sums that are odd so far
- ans \rightarrow count of subarrays with odd sum

Ⅲ Dry Run Table:

i	arr[i]	sum	sum%2	Action	ans	even	odd
0	1	1	1 (odd)	Add 1 + even $(0) \rightarrow$ ans += 1	1	0	1
1	2	3	, ,	Add 1 + even $(0) \rightarrow$ ans += 1		0	2
2	3	6	0 (even)	Add odd (2) → ans += 2	4	1	2
3	4	10	0 (even)	Add odd (2) \rightarrow ans += 2	6	2	2
4	5	15	1 (odd)	Add 1 + even (2) \rightarrow ans += 3	9	2	3
5	6	21		Add 1 + even $(2) \rightarrow$ ans += 3		2	4
6	7	28	0 (even)	Add odd (4) → ans += 4	16	3	4

♥ Final Output:

16

Reverse Vowel of String in C++

```
#include <iostream>
#include <string>
#include <algorithm>
using namespace std;
bool isVowel(char ch) {
  return (ch == 'A' | | ch == 'E' | | ch == 'I' | | ch ==
'O' \mid \mid ch == 'U' \mid \mid
       ch == 'a' | | ch == 'e' | | ch == 'i' | | ch == 'o'
| | ch == 'u');
string reverseVowel(string s) {
  int left = 0;
  int right = s.length() - 1;
  while (left < right) {
     while (left < right && !isVowel(s[left])) {
       left++;
     while (left < right && !isVowel(s[right])) {</pre>
       right--;
     if (left < right) {
        swap(s[left], s[right]);
        left++;
       right--;
  return s;
int main() {
  string s = "hello";
  string result = reverseVowel(s);
  cout << result << endl; // Output should be "holle"</pre>
  return 0;
```

Input:

string s = "hello"; Vowels: e, o

Dry Run Table:

Step	left	right	s[left]	s[right]	Action	String After Change
1	0	4	h	0	h is not a vowel → left+ +	"hello"
2	1	4	e	0	Both are vowels → swap e and o	
3	2	3	1	1	No further vowel swap needed	"holle"

∜ Final Output:

holle

holle

```
#include <iostream>
#include <vector>
#include <algorithm>
using namespace std;
vector<vector<int>> twoSum(vector<int>
nums, int target) {
  vector<vector<int>> res;
  int n = nums.size();
  sort(nums.begin(), nums.end()); // Sorting
the array
  int left = 0, right = n - 1;
  while (left < right) {
    if (left > 0 \&\& nums[left] == nums[left -
1]) { // Skip duplicates for left pointer
       left++:
       continue;
    int sum = nums[left] + nums[right];
    if (sum == target) {
       res.push_back({nums[left],
nums[right]});
       left++;
       right--;
       // Skip duplicates for both left and
right pointers
       while (left < right && nums[left] ==
nums[left - 1]) left++;
       while (left < right && nums[right] ==
nums[right + 1]) right--;
    } else if (sum > target) {
       right--;
    } else {
       left++;
  return res;
int main() {
  vector\leqint\geq nums = \{2, 2, 4, 3, 1, 6, 6, 7, 5, ...
9, 1, 8, 9};
  int target = 10;
  vector<vector<int>> res = twoSum(nums,
target);
  // Sorting each pair and then sorting all
pairs lexicographically
  sort(res.begin(), res.end(), [](const
vector<int>& a, const vector<int>& b) {
    return a[0] == b[0] ? a[1] < b[1] : a[0] <
b[0];
  });
```

Two Sum in C++

Input:

nums = $\{2, 2, 4, 3, 1, 6, 6, 7, 5, 9, 1, 8, 9\}$ target = 10

After sorting:

 $nums = \{1, 1, 2, 2, 3, 4, 5, 6, 6, 7, 8, 9, 9\}$

Q Step-by-step Table Dry Run:

Ste p	lef t	right	num s[lef t]		su m	Actio n	Result
1	0	12	1	9	10	Found a pair, store it	{1, 9}
	1	11	1	9	10	Skip duplic ate left	
	2	11	2	9	11	Sum > target , move right	
2	2	10	2	8	10	Found	{1, 9}, {2, 8}
	3	9	2	7	9	Skip duplic ate left, move left++	
3	4	9	3	7	10	Found a pair, store it	{1,9},{2,8}, {3,7}
4	5	8	4	6	10	Found a pair, store it	{1,9},{2,8}, {3,7},{4,6}
5	6	7	5	6	11	Sum > target , move right	
6	6	6	5	5	10	Stop (left >= right)	

♥ Final Result:

 $\{\{1, 9\}, \{2, 8\}, \{3, 7\}, \{4, 6\}\}$

```
// Printing the result
for (auto& pair : res) {
    for (int val : pair) {
        cout << val << " ";
    }
    cout << endl;
}

return 0;

1 9
2 8
3 7
```

All Subarray in C++

```
#include <iostream>
using namespace std;

int main() {
    int arr[] = {1, 2, 3, 4};
    int n = sizeof(arr) / sizeof(arr[0]);

for (int sp = 0; sp < n; sp++) {
    for (int ep = sp; ep < n; ep++) {
        cout << arr[i] << " ";
      }
      cout << endl;
    }
}

return 0;
}</pre>
```

Input:

```
arr[] = \{1, 2, 3, 4\};
```

■ Loop Structure:

- sp: Start point of subarray
- ep: End point of subarray
- i: Index for printing elements from sp to ep

Dry Run Table:

\mathbf{sp}	ер	Subarray Printed
0	0	1
0	1	1 2
0	2	1 2 3
0	3	1 2 3 4
1	1	2
1	2	2 3
1	3	2 3 4
2	2	3
2	3	3 4
3	3	4

⚠ Output:

```
1
1 2
1 2 3
1 2 3 4
2
2 3
2 3 4
3
3 4
4
```

```
\begin{array}{c} 1 \\ 1\ 2 \\ 1\ 2\ 3 \\ 1\ 2\ 3\ 4 \\ 2 \\ 2\ 3 \\ 4\ 3 \\ 3\ 4 \\ 4 \end{array}
```

Print Boundary in C++ #include <iostream> #include <vector> using namespace std; void printBoundary(vector<vector<int>>& mat) { int n = mat.size();int m = mat[0].size();// Print top row for (int j = 0; j < m; j++) { cout << mat[0][j] << " "; // Print right column (excluding the top and bottom elements already printed) for (int i = 1; i < n; i++) { cout << mat[i][m - 1] << " ";// Print bottom row (excluding the bottom-right corner already printed) if (n > 1) { for (int j = m - 2; $j \ge 0$; j - 0) { cout << mat[n - 1][j] << "";} // Print left column (excluding the top-left and bottom-left corners already printed) if (m > 1) { for (int i = n - 2; i > 0; i - 1) { cout << mat[i][0] << " "; } } int main() { vector<vector<int>> mat = { $\{1, 2, 3, 4, 5\},\$ $\{6, 7, 8, 9, 10\},\$ {11, 12, 13, 14, 15}, $\{16, 17, 18, 19, 20\},\$ {21, 22, 23, 24, 25} **}**; printBoundary(mat); cout << endl;

```
Input Matrix (5x5):
```

```
[1, 2, 3, 4, 5],
[6, 7, 8, 9, 10],
[11, 12, 13, 14, 15],
[16, 17, 18, 19, 20],
[21, 22, 23, 24, 25]
1
```

▼ Step-by-step Dry Run Table:

Step	Indices	Printed Values
Top row	mat[0][0 to 4]	1 2 3 4 5
Right column	mat[1 to 4][4]	10 15 20 25
Bottom row	mat[4][3 to 0]	24 23 22 21
Left column	mat[3 to 1][0]	16 11 6

Dry Run Table

Phase	Loop Variable(s)	Value Printed
Top Row	j = 0 to 4	1 2 3 4 5
Right Col	i = 1 to 4	10 15 20 25
Bottom Row	j = 3 to 0 (reverse)	24 23 22 21
Left Col	i = 3 to 1 (reverse)	16 11 6

 $1\; 2\; 3\; 4\; 5\; 10\; 15\; 20\; 25\; 24\; 23\; 22\; 21\; 16\; 11\; 6$

return 0;

}

First Missing Positive in C++

```
#include <iostream>
#include <vector>
using namespace std;
int firstMissingPositive(vector<int>& nums) {
  int n = nums.size();
  int i = 0;
  while (i < n) {
     if (nums[i] == i + 1) {
       i++;
       continue;
     if (nums[i] \le 0 \mid | nums[i] > n) {
       i++;
       continue;
     int idx1 = i;
     int idx2 = nums[i] - 1;
     if (nums[idx1] == nums[idx2]) {
       i++;
       continue;
     int temp = nums[idx1];
     nums[idx1] = nums[idx2];
     nums[idx2] = temp;
  }
  for (int j = 0; j < n; j++) {
     if (nums[j] != j + 1) {
       return j + 1;
  }
  return n + 1;
int main() {
  vector<int> nums = \{3, 4, -1, 1\};
  int result = firstMissingPositive(nums);
  cout << "First missing positive: " << result << endl;</pre>
  return 0;
}
```

Input:

vector<int> nums = $\{3, 4, -1, 1\}$;

¶ Goal:

Find the **smallest positive integer** that is **missing** from the array.

𝔰 Algorithm Insight:

You're trying to place each positive integer x (1 \leq x \leq n) at index x - 1 using cyclic swaps.

Q Dry Run Table:

♦ While loop swaps

Step	i	nums[i]	Action	nums after
1	0	3	swap nums[0] with nums[2] (index 2 = 3 - 1)	{-1, 4, 3, 1}
2	0	-1	invalid (\leq 0), move to $i = 1$	{-1, 4, 3, 1}
3	1	4	swap nums[1] with nums[3] (index 3 = 4 - 1)	{-1, 1, 3, 4}
4	1	1	swap nums[1] with nums[0] (index 0 = 1 - 1)	{1, -1, 3, 4}
5	1	-1	invalid, move to i = 2	{1, -1, 3, 4}
6	2	3	already at correct index (2 = 3 - 1)	no change
7	3	4	already at correct index (3 = 4 - 1)	no change

★ Final nums array after placements:

 $\{1, -1, 3, 4\}$

♥ Final Check:

Go through the array to find first j where nums[j] ! = j + 1:

j nums[j] j + 1 Match? $0.1 1 \checkmark$

1 -1 2 $\times \rightarrow$ return 2

	① Output: First missing positive: 2
First missing positive: 2	

Range Sum in C++

```
#include <iostream>
#include <vector>
using namespace std;
vector<int> prefixSum;
void NumArray(vector<int>& nums) {
  prefixSum.resize(nums.size());
  prefixSum[0] = nums[0];
  for (int i = 1; i < nums.size(); i++) {
    prefixSum[i] = prefixSum[i - 1] + nums[i];
int sumRange(int i, int j) {
  if (i == 0) {
    return prefixSum[j];
  return prefixSum[j] - prefixSum[i - 1];
int main() {
  vector<int> arr = \{1, 2, 3, 4\};
  NumArray(arr);
  int res = sumRange(1, 2);
  cout << res << endl; // Output should be 5
  return 0;
```

Prefix Sum Table Construction in NumArray(arr)

Let's build prefixSum[] based on the input arr = $\{1, 2, 3, 4\}$.

Index i	nums[i]	prefixSum[i] = prefixSum[i - 1] + nums[i]	prefixSum array
0	1	1	[1]
1	2	1 + 2 = 3	[1, 3]
2	3	3 + 3 = 6	[1, 3, 6]
3	4	6 + 4 = 10	[1, 3, 6, 10]

Final prefixSum = [1, 3, 6, 10]

sumRange(1, 2) Execution

We want to find sum from index 1 to 2 in original array (2 + 3 = 5).

Since i = 0, it uses:

prefixSum[2] - prefixSum[0] = 6 - 1 = 5

Expression	Value
prefixSum[2]	6
prefixSum[0]	1
Result	5

✓ Output printed: 5

Rotate Image in C++

```
#include <iostream>
#include <vector>
using namespace std;
void rotate(vector<vector<int>>& matrix) {
  int n = matrix.size();
  int m = matrix[0].size();
  // Transpose the matrix
  for (int i = 0; i < n; i++) {
     for (int j = i; j < m; j++) {
       swap(matrix[i][j], matrix[j][i]);
  // Reverse each row
  for (int i = 0; i < n; i++) {
     int sp = 0;
     int ep = m - 1;
     while (sp < ep) {
       swap(matrix[i][sp], matrix[i][ep]);
       sp++;
       ep--;
  }
void print2DArray(const vector<vector<int>>& array)
  for (size_t i = 0; i < array.size(); i++) {
     for (size_t j = 0; j < array[i].size(); j++) {
       cout << array[i][j] << " ";
     cout << endl;
int main() {
  vector<vector<int>> matrix = {
     \{1, 2, 3\},\
     \{4, 5, 6\},\
     \{7, 8, 9\}
  cout << "Original matrix:" << endl;</pre>
  print2DArray(matrix);
  rotate(matrix);
  cout << "Rotated matrix:" << endl;</pre>
  print2DArray(matrix);
  return 0;
}
```

Input Matrix:

Original matrix:

123

456

789

Step 1: Transpose the matrix

Transposing means swapping matrix[i][j] with matrix[j][i] for j > i.

i	j	matrix[i][j]	matrix[j][i]	Action
0	1	2	4	$Swap \rightarrow 2 \leftrightarrow 4$
0	2	3	7	$Swap \rightarrow 3 \leftrightarrow 7$
1	2	6	8	$Swap \rightarrow 6 \leftrightarrow 8$

After transpose:

147

258

369

Step 2: Reverse each row

Reverse each row of the transposed matrix:

Row Before	Row After
1 4 7	7 4 1
2 5 8	8 5 2
3 6 9	963

♥ Final Output:

Rotated matrix:

741

852

963

Original matrix:

123

456

789

Rotated matrix:

741

852

Running Sum in C++

```
#include <iostream>
#include <vector>
using namespace std;
vector<int> runningSum(vector<int>& nums) {
  int n = nums.size();
  vector<int> pre(n);
  pre[0] = nums[0];
  for (int i = 1; i < n; i++) {
    pre[i] = pre[i - 1] + nums[i];
  return pre;
int main() {
  vector<int> arr = \{1, 2, 3, 4\};
  vector<int> res = runningSum(arr);
  for (int i = 0; i < res.size(); i++) {
    cout << res[i] << endl;</pre>
  }
  return 0;
```

Input:

vector<int> arr = $\{1, 2, 3, 4\}$;

Dry Run Table:

i	nums[i]	pre[i - 1]	pre[i] = pre[i - 1] + nums[i]	pre vector after iteration
0	1	-		[1, _, _, _]
1	2	1	pre[1] = 1 + 2 = 3	[1, 3, _, _]
2	3		pre[2] = 3 + 3 = 6	
3	4	6	pre[3] = 6 + 4 = 10	[1, 3, 6, 10]

∀ Final Output (printed one per line):

1 3

6