

## Balanced Parenthesis in C++

```
#include <iostream>
#include <vector>
using namespace std;

int main() {
    int n = 5;
    vector<int> dp(n + 1, 0);
    dp[0] = 1;
    dp[1] = 1;

    for (int i = 2; i <= n; i++) {
        int inside = i - 1;
        int outside = 0;
        while (inside >= 0) {
            dp[i] += dp[inside] * dp[outside];
            inside--;
            outside++;
        }
    }

    for (int i = 0; i < dp.size(); i++) {
        cout << dp[i] << " ";
    }

    // char c = 'b';
    // cout << (c - '0') << endl;

    return 0;
}
```

### Initial Setup:

- $n = 5$
- $dp$  is a vector of size  $n + 1 = 6$ , initially set to  $\{1, 1, 0, 0, 0, 0\}$ .

### Loop Breakdown:

#### Iteration 1: $i = 2$

1.  $inside = 2 - 1 = 1$
2.  $outside = 0$

For  $inside = 1$  and  $outside = 0$ :

- $dp[2] += dp[1] * dp[0] \rightarrow dp[2] += 1 * 1 \rightarrow dp[2] = 1$ .

Now, decrease  $inside$  to 0 and increase  $outside$  to 1.

For  $inside = 0$  and  $outside = 1$ :

- $dp[2] += dp[0] * dp[1] \rightarrow dp[2] += 1 * 1 \rightarrow dp[2] = 2$ .

So, after this iteration,  $dp[2] = 2$ .

#### Iteration 2: $i = 3$

1.  $inside = 3 - 1 = 2$
2.  $outside = 0$

For  $inside = 2$  and  $outside = 0$ :

- $dp[3] += dp[2] * dp[0] \rightarrow dp[3] += 2 * 1 \rightarrow dp[3] = 2$ .

Now, decrease  $inside$  to 1 and increase  $outside$  to 1.

For  $inside = 1$  and  $outside = 1$ :

- $dp[3] += dp[1] * dp[1] \rightarrow dp[3] += 1 * 1 \rightarrow dp[3] = 3$ .

Now, decrease  $inside$  to 0 and increase  $outside$  to 2.

For  $inside = 0$  and  $outside = 2$ :

- $dp[3] += dp[0] * dp[2] \rightarrow dp[3] += 1 * 2 \rightarrow dp[3] = 5$ .

So, after this iteration,  $dp[3] = 5$ .

**Iteration 3: i = 4**

1.  $\text{inside} = 4 - 1 = 3$
2.  $\text{outside} = 0$

For  $\text{inside} = 3$  and  $\text{outside} = 0$ :

- $\text{dp}[4] += \text{dp}[3] * \text{dp}[0] \rightarrow \text{dp}[4] += 5 * 1 \rightarrow \text{dp}[4] = 5.$

Now, decrease  $\text{inside}$  to 2 and increase  $\text{outside}$  to 1.

For  $\text{inside} = 2$  and  $\text{outside} = 1$ :

- $\text{dp}[4] += \text{dp}[2] * \text{dp}[1] \rightarrow \text{dp}[4] += 2 * 1 \rightarrow \text{dp}[4] = 7.$

Now, decrease  $\text{inside}$  to 1 and increase  $\text{outside}$  to 2.

For  $\text{inside} = 1$  and  $\text{outside} = 2$ :

- $\text{dp}[4] += \text{dp}[1] * \text{dp}[2] \rightarrow \text{dp}[4] += 1 * 2 \rightarrow \text{dp}[4] = 9.$

Now, decrease  $\text{inside}$  to 0 and increase  $\text{outside}$  to 3.

For  $\text{inside} = 0$  and  $\text{outside} = 3$ :

- $\text{dp}[4] += \text{dp}[0] * \text{dp}[3] \rightarrow \text{dp}[4] += 1 * 5 \rightarrow \text{dp}[4] = 14.$

So, after this iteration,  $\text{dp}[4] = 14.$

**Iteration 4: i = 5**

1.  $\text{inside} = 5 - 1 = 4$
2.  $\text{outside} = 0$

For  $\text{inside} = 4$  and  $\text{outside} = 0$ :

- $\text{dp}[5] += \text{dp}[4] * \text{dp}[0] \rightarrow \text{dp}[5] += 14 * 1 \rightarrow \text{dp}[5] = 14.$

Now, decrease  $\text{inside}$  to 3 and increase  $\text{outside}$  to 1.

For  $\text{inside} = 3$  and  $\text{outside} = 1$ :

- $\text{dp}[5] += \text{dp}[3] * \text{dp}[1] \rightarrow \text{dp}[5] += 5 * 1 \rightarrow \text{dp}[5] = 19.$

Now, decrease  $\text{inside}$  to 2 and increase  $\text{outside}$  to 2.

For inside = 2 and outside = 2:

- $dp[5] += dp[2] * dp[2] \rightarrow dp[5] += 2 * 2 \rightarrow dp[5] = 23.$

Now, decrease inside to 1 and increase outside to 3.

For inside = 1 and outside = 3:

- $dp[5] += dp[1] * dp[3] \rightarrow dp[5] += 1 * 5 \rightarrow dp[5] = 28.$

Now, decrease inside to 0 and increase outside to 4.

For inside = 0 and outside = 4:

- $dp[5] += dp[0] * dp[4] \rightarrow dp[5] += 1 * 14 \rightarrow dp[5] = 42.$

So, after this iteration,  $dp[5] = 42.$

### **Final Output:**

The dp array is:

Copy code

1 1 2 5 14 42

Output:-

1 1 2 5 14 42