

Optimize water distribution in C++

```
#include <iostream>
#include <vector>
#include <queue>
#include <utility>

using namespace std;

class Pair {
public:
    int vtx;
    int wt;
    Pair(int vtx, int wt) {
        this->vtx = vtx;
        this->wt = wt;
    }
    bool operator>(const Pair& other) const {
        return this->wt > other.wt;
    }
};

int minCostToSupplyWater(int n, vector<int>& wells, vector<vector<int>>& pipes) {
    vector<vector<Pair>> graph(n + 1);
    for (const auto& pipe : pipes) {
        int u = pipe[0];
        int v = pipe[1];
        int wt = pipe[2];
        graph[u].emplace_back(v, wt);
        graph[v].emplace_back(u, wt);
    }
    for (int i = 1; i <= n; ++i) {
        graph[i].emplace_back(0, wells[i - 1]);
        graph[0].emplace_back(i, wells[i - 1]);
    }

    int ans = 0;
    priority_queue<Pair, vector<Pair>, greater<Pair>> pq;
    pq.emplace(0, 0);
    vector<bool> vis(n + 1, false);

    while (!pq.empty()) {
        Pair rem = pq.top();
        pq.pop();
        if (vis[rem.vtx]) continue;
        ans += rem.wt;
        vis[rem.vtx] = true;
        for (const Pair& nbr : graph[rem.vtx]) {
            if (!vis[nbr.vtx]) {
                pq.push(nbr);
            }
        }
    }
    return ans;
}

int main() {
    int v = 3, e = 2;
    vector<int> wells = {1, 2, 2};
    vector<vector<int>> pipes = {{1, 2, 1}, {2, 3, 1}};
```

Input:

- **Number of houses (n)** = 3
- **Wells:** [1, 2, 2] → Cost to build wells at house 1, 2, 3
- **Pipes:**

```
[1, 2, 1]
[2, 3, 1]
```

Graph Construction (Adjacency List):

Node Connections

```
0      (1,1), (2,2), (3,2)
1      (2,1), (0,1)
2      (1,1), (3,1), (0,2)
3      (2,1), (0,2)
```

Dry Run of Prim's Algorithm:

Step	Min Edge Picked (u→v, wt)	Added to MST	MST Cost	Visited Nodes	Heap Contents After Push
1	(0→0, 0)	0	0	{0}	(1,1), (2,2), (3,2)
2	(0→1, 1)	1	1	{0,1}	(2,2), (3,2), (2,1)
3	(1→2, 1)	2	2	{0,1,2}	(3,2), (2,2), (3,1)
4	(2→3, 1)	3	3	{0,1,2,3}	Remaining edges ignored (already visited nodes)

✓ All nodes visited.

✓ Final Output:

3

Explanation:

- Use well at house 1: cost 1

```
cout << minCostToSupplyWater(v, wells, pipes) <<
endl;

return 0;
}
```

- Use **pipe 1–2**: cost 1
 - Use **pipe 2–3**: cost 1
- **Total = 3**

🧠 This is cheaper than building all wells
(1+2+2=5)

Output:-
3