```
#include <iostream>
#include <algorithm> // For max() function
using namespace std;
struct node {
  int val;
  struct node* left;
  struct node* right;
  int ht;
};
int height(node* n) {
  if (n == NULL)
    return -1;
  return n->ht;
int balanceFactor(node* n) {
  if (n == NULL)
    return 0;
  return height(n->left) - height(n->right);
}
node* rotateRight(node* y) {
  node* x = y->left;
  node* T2 = x->right;
  // Perform rotation
  x - y = y
  y->left = T2;
  // Update heights
  y-ht = max(height(y-left), height(y-right)) +
1;
  x->ht = max(height(x->left), height(x->right)) +
```

1;

1:

1;

// Return new root

node* rotateLeft(node* x) {

node* y = x->right;

node* T2 = y->left;

// Perform rotation

// Update heights

// Return new root

node* newNode(int value) {
 node* n = new node();

return y;

x->ht = max(height(x->left), height(x->right)) +

y->ht = max(height(y->left), height(y->right)) +

y->left = x;x->right = T2;

return x;

AVL Tree in C++

Input Sequence: 10, 20, 30, 40, 50, 25

We'll look at:

- The value being inserted
- Balancing case (if any)
- · Rotation applied
- Root after insertion

7 Step-by-Step Insertion and Rotations

Step	Inserted Value	Balance Factor (BF) at Unbalanced Node	Case	Rotation	New Root
1	10	_		_	10
2	20	_		_	10
3	30	-2 at 10 (BF = -2)	_	Left Rotate(10)	20
4	40	-1 at 20		_	20
5	50	-2 at 20 (BF = -2)	_	Left Rotate(20)	30
6	25	+2 at 40.left (20), then -1 at 40	Right Left	Right(30) then Left(40)	30

♥ Final AVL Tree Structure (via Pre-Order Traversal)

The pre-order traversal (root, left, right) shows the structure:

 $30\;20\;10\;25\;40\;50$

1. In-Order Traversal

This gives sorted order of elements (left-root-right):

10 20 25 30 40 50

Explanation of Rotations

Case 1: $10 \rightarrow 20 \rightarrow 30$

• Inserting 30 caused right-right imbalance at

```
n-val = value;
  n->left = NULL:
  n->right = NULL;
  n->ht = 0; // Height of the node is set to 0
node* insert(node* root, int new_val) {
  // Perform the normal BST insert
  if (root == NULL)
    return newNode(new_val);
  if (new_val < root->val)
    root->left = insert(root->left, new_val);
  else if (new_val > root->val)
     root->right = insert(root->right, new_val);
  else
    return root; // Duplicate values are not
allowed
  // Update the height of the ancestor node
  root->ht = 1 + max(height(root->left),
height(root->right));
  // Get the balance factor
  int bf = balanceFactor(root);
  // If the node becomes unbalanced, there are 4
cases:
  // Case 1 - Left Left
  if (bf > 1 && new val < root->left->val)
    return rotateRight(root);
  // Case 2 - Right Right
  if (bf < -1 \&\& new val > root->right->val)
    return rotateLeft(root);
  // Case 3 - Left Right
  if (bf > 1 \&\& new\_val > root->left->val) {
    root->left = rotateLeft(root->left);
    return rotateRight(root);
  // Case 4 - Right Left
  if (bf < -1 \&\& new val < root->right->val)
    root->right = rotateRight(root->right);
    return rotateLeft(root);
  // Return the (unchanged) root pointer
  return root:
}
// In-order traversal to print the tree in sorted
void inOrderTraversal(node* root) {
  if (root != NULL) {
    inOrderTraversal(root->left);
    cout << root->val << " ";
    inOrderTraversal(root->right);
```

10.

Single left rotation at 10.

Case 2: $20 \rightarrow 30 \rightarrow 40 \rightarrow 50$

- Inserting 50 caused right-right imbalance at 20.
- Single left rotation at 20.

Case 3: $50 \rightarrow 25$

- Inserting 25 caused right-left imbalance at 40.
- First, right rotation at 30 (child), then left rotation at 40.

```
// Pre-order traversal to show the structure of the
AVL tree
void preOrderTraversal(node* root) {
  if (root != NULL) {
    cout << root->val << " ";
    preOrderTraversal(root->left);
    preOrderTraversal(root->right);
  }
}
// Main function to test the AVL tree
implementation
int main() {
  node* root = NULL;
  // Insert values into the AVL tree
  root = insert(root, 10);
  root = insert(root, 20);
  root = insert(root, 30);
  root = insert(root, 40);
  root = insert(root, 50);
  root = insert(root, 25);
  // In-order traversal of the AVL tree (should be
sorted)
  cout << "In-order traversal: ";</pre>
  inOrderTraversal(root);
  cout << endl;
  // Pre-order traversal of the AVL tree (shows
the structure)
  cout << "Pre-order traversal: ";</pre>
  preOrderTraversal(root);
  cout << endl;
  return 0;
In-order traversal: 10 20 25 30 40 50
```

Pre-order traversal: $30\ 20\ 10\ 25\ 40\ 50$