

Prim in C++

```
#include <bits/stdc++.h>
using namespace std;

class Solution
{
public:
    //Function to find sum of weights of edges of the
    Minimum Spanning Tree.
    int spanningTree(int V, vector<vector<int>>
adj[])
    {
        priority_queue<pair<int, int>,
        vector<pair<int, int> >,
greater<pair<int, int>>> pq;

        vector<int> vis(V, 0);
        // {wt, node}
        pq.push({0, 0});
        int sum = 0;
        while (!pq.empty()) {
            auto it = pq.top();
            pq.pop();
            int node = it.second;
            int wt = it.first;

            if (vis[node] == 1) continue;
            // add it to the mst
            vis[node] = 1;
            sum += wt;
            for (auto it : adj[node]) {
                int adjNode = it[0];
                int edW = it[1];
                if (!vis[adjNode]) {
                    pq.push({edW,
adjNode});
                }
            }
        }
        return sum;
    }
};

int main() {
    int V = 5;
    vector<vector<int>> edges = {{0, 1, 2}, {0, 2, 1},
{1, 2, 1}, {2, 3, 2}, {3, 4, 1}, {4, 2, 2}};
    vector<vector<int>> adj[V];
    for (auto it : edges) {
        vector<int> tmp(2);
        tmp[0] = it[1];
        tmp[1] = it[2];
        adj[it[0]].push_back(tmp);

        tmp[0] = it[0];
        tmp[1] = it[2];
        adj[it[1]].push_back(tmp);
    }

    Solution obj;
```

Input Edges

```
edges = {
    {0, 1, 2},
    {0, 2, 1},
    {1, 2, 1},
    {2, 3, 2},
    {3, 4, 1},
    {4, 2, 2}
}
```

Adjacency List

Node	Neighbors
0	[1,2], [2,1]
1	[0,2], [2,1]
2	[0,1], [1,1], [3,2], [4,2]
3	[2,2], [4,1]
4	[3,1], [2,2]

Prim's MST Logic (Min-Heap)

We track:

- pq: min-heap for {weight, node}
- vis[]: visited array
- sum: total MST weight

Dry Run Table

Step	pq (Min-Heap)	node	wt	vis	sum	Action Taken
1	{{0, 0}}	0	0	[1, 0, 0, 0, 0]	0	Add node 0, add neighbors 1 (wt=2), 2 (wt=1) to pq
2	{{(1, 2), (2, 1)}}	2	1	[1, 0, 1, 0, 0]	1	Add node 2, add unvisited neighbors: 1(wt=1), 3(wt=2), 4(wt=2)
3	{{(1, 1), (2, 1), (2, 3), (2, 4)}}	1	1	[1, 1, 1, 0, 0]	2	Add node 1, skip already visited 0 & 2
4	{{(2, 1), (2, 3), (2, 4)}}	1	2	Already visited	-	Skip

<pre>int sum = obj.spanningTree(V, adj); cout << "The sum of all the edge weights: " << sum << endl; return 0; }</pre>	<table><tr><th>Step</th><th>pq (Min-Heap)</th><th>node</th><th>wt</th><th>vis</th><th>sum</th><th>Action Taken</th></tr><tr><td>5</td><td>{{(2, 3), (2, 4)}</td><td>3</td><td>2</td><td>[1, 1, 1, 1, 0]</td><td>4</td><td>Add node 3, add neighbor 4 (wt=1)</td></tr><tr><td>6</td><td>{{(1, 4), (2, 4)}</td><td>4</td><td>1</td><td>[1, 1, 1, 1, 1]</td><td>5</td><td>Add node 4, skip visited 3, 2</td></tr><tr><td>7</td><td>{{(2, 4)}</td><td>4</td><td>2</td><td>Already visited</td><td>-</td><td>Skip</td></tr></table> <p>✔ Final Result:</p> <table><tr><th>Variable</th><th>Value</th></tr><tr><td>sum</td><td>5</td></tr><tr><td>vis</td><td>[1,1,1,1,1] (All visited)</td></tr></table> <p>✔ Output:</p> <p>The sum of all the edge weights: 5</p>	Step	pq (Min-Heap)	node	wt	vis	sum	Action Taken	5	{{(2, 3), (2, 4)}	3	2	[1, 1, 1, 1, 0]	4	Add node 3, add neighbor 4 (wt=1)	6	{{(1, 4), (2, 4)}	4	1	[1, 1, 1, 1, 1]	5	Add node 4, skip visited 3, 2	7	{{(2, 4)}	4	2	Already visited	-	Skip	Variable	Value	sum	5	vis	[1,1,1,1,1] (All visited)
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