Coin Change Combination in C++

```
#include <iostream>
#include <vector>
using namespace std;
int main() {
  vector<int> arr = \{2, 3, 5\};
  int amt = 7;
  vector<int> dp(amt + 1, 0);
  dp[0] = 1; // Base case: 1 way to make amount 0
(using no coins)
  for (int i = 0; i < arr.size(); i++) {
    for (int j = arr[i]; j \le amt; j++) {
       dp[j] += dp[j - arr[i]];
  }
  cout << dp[amt] << endl; // Output the number of
combinations for amount 'amt'
  return 0;
}
```

Input:

- $arr = \{2, 3, 5\}$
- amt = 7

Initialization:

• $dp = \{1, 0, 0, 0, 0, 0, 0, 0\}$ (size = amt + 1, initialized to 0 except dp[0] = 1).

Iterations:

Step 1: Using Coin 2 (arr[0]):

- For each j from 2 to 7:
 o dp[j] += dp[j 2]
- Updates:

$$dp[2] = dp[2] + dp[0] = 0 + 1 = 1$$

$$dp[3] = dp[3] + dp[1] = 0 + 0 = 0$$

$$dp[4] = dp[4] + dp[2] = 0 + 1 = 1$$

$$dp[5] = dp[5] + dp[3] = 0 + 0 = 0$$

$$dp[6] = dp[6] + dp[4] = 0 + 1 = 1$$

$$dp[7] = dp[7] + dp[5] = 0 + 0 = 0$$

• $dp = \{1, 0, 1, 0, 1, 0, 1, 0\}$

Step 2: Using Coin 3 (arr[1]):

- For each j from 3 to 7:
 o dp[j] += dp[j 3]
- Updates:

$$dp[3] = dp[3] + dp[0] = 0 + 1 = 1$$

$$dp[4] = dp[4] + dp[1] = 1 + 0 = 1$$

$$dp[5] = dp[5] + dp[2] = 0 + 1 = 1$$

$$dp[6] = dp[6] + dp[3] = 1 + 1 = 2$$

$$dp[7] = dp[7] + dp[4] = 0 + 1 = 1$$

• $dp = \{1, 0, 1, 1, 1, 1, 2, 1\}$

Step 3: Using Coin 5 (arr[2]):

- For each j from 5 to 7:
 o dp[j] += dp[j 5]
- Updates:

$$dp[5] = dp[5] + dp[0] = 1 + 1 = 2$$

 $dp[6] = dp[6] + dp[1] = 2 + 0 = 2$
 $dp[7] = dp[7] + dp[2] = 1 + 1 = 2$

• $dp = \{1, 0, 1, 1, 1, 2, 2, 2\}$ Final DP Array: $dp = \{1, 0, 1, 1, 1, 2, 2, 2\}$ Output: dp[amt] = dp[7] = 2There are 2 ways to form amount 7 using coins $\{2, 3, 5\}$.

Output:-

2