

## Fast and Last Index in C++

```
#include <iostream>
using namespace std;

void findFirstAndLastIndex(int arr[], int n,
int d) {
    int low = 0;
    int high = n - 1;
    int firstIndex = -1;
    int lastIndex = -1;

    // Finding the first occurrence
    while (low <= high) {
        int mid = low + (high - low) / 2;
        if (d > arr[mid]) {
            low = mid + 1;
        } else if (d < arr[mid]) {
            high = mid - 1;
        } else {
            firstIndex = mid;
            high = mid - 1;
        }
    }

    // Finding the last occurrence
    low = 0;
    high = n - 1;
    while (low <= high) {
        int mid = low + (high - low) / 2;
        if (d > arr[mid]) {
            low = mid + 1;
        } else if (d < arr[mid]) {
            high = mid - 1;
        } else {
            lastIndex = mid;
            low = mid + 1;
        }
    }

    cout << "First Index: " << firstIndex <<
endl;
    cout << "Last Index: " << lastIndex <<
endl;
}

int main() {
    int arr[] = {1, 5, 10, 15, 22, 33, 33, 33, 33,
33, 40, 42, 55, 66, 77, 33};
    int n = sizeof(arr) / sizeof(arr[0]);
    int d = 33;

    findFirstAndLastIndex(arr, n, d);

    return 0;
}
```

### Dry Run Example (on sorted array):

Sorted version of the array:

{1, 5, 10, 15, 22, 33, 33, 33, 33, 33, 40, 42, 55, 66, 77}

We want to find **first and last index of 33**.

#### First Occurrence:

Iteration	low	high	mid	arr[mid]	firstIndex	high (updated)
1	0	15	7	33	7	6
2	0	6	3	15		
3	4	6	5	33	5	4
4	4	4	4	22		

→ First index = **5**

#### Last Occurrence:

Iteration	low	high	mid	arr[mid]	lastIndex	low (updated)
1	0	15	7	33	7	8
2	8	15	11	40		
3	8	10	9	33	9	10
4	10	10	10	33	10	11

→ Last index = **10**

#### 📦 Final Output:

First Index: 5  
Last Index: 10

First Index: 5 Last Index: 10	

IsSorted in C++																																					
<pre>#include &lt;iostream&gt; using namespace std;  bool isSortedEff(int arr[], int n) {     for (int i = 1; i &lt; n; i++) {         if (arr[i] &lt; arr[i - 1]) {             return false;         }     }     return true; }  bool isSorted(int arr[], int n) {     for (int i = 0; i &lt; n; i++) {         for (int j = i + 1; j &lt; n; j++) {             if (arr[j] &lt; arr[i]) {                 return false;             }         }     }     return true; }  int main() {     int arr1[] = {1, 2, 3, 4, 5, 6};     int arr2[] = {11, 2, 3, 4, 5, 6};     int n1 = sizeof(arr1) / sizeof(arr1[0]);     int n2 = sizeof(arr2) / sizeof(arr2[0]);      cout &lt;&lt; boolalpha; // Print boolean values as true/false     cout &lt;&lt; isSortedEff(arr1, n1) &lt;&lt; endl;     cout &lt;&lt; isSortedEff(arr2, n2) &lt;&lt; endl;      cout &lt;&lt; isSorted(arr1, n1) &lt;&lt; endl;     cout &lt;&lt; isSorted(arr2, n2) &lt;&lt; endl;      return 0; }</pre>		Check if an array is <b>sorted in non-decreasing order</b> (each element is $\leq$ the next).																																			
		🔍 Difference between isSortedEff and isSorted:																																			
		<table><tr><th>Function</th><th>Approach</th><th>Time Complexity</th></tr><tr><td>isSortedEff</td><td>Linear scan (compare adjacent)</td><td><b>O(n)</b></td></tr><tr><td>isSorted</td><td>Brute force (nested loops)</td><td><b>O(n²)</b></td></tr></table>			Function	Approach	Time Complexity	isSortedEff	Linear scan (compare adjacent)	<b>O(n)</b>	isSorted	Brute force (nested loops)	<b>O(n²)</b>																								
		Function	Approach	Time Complexity																																	
		isSortedEff	Linear scan (compare adjacent)	<b>O(n)</b>																																	
		isSorted	Brute force (nested loops)	<b>O(n²)</b>																																	
		✔ Dry Run with Sample Arrays																																			
		Array 1: {1, 2, 3, 4, 5, 6} (Sorted)																																			
		isSortedEff(arr1, n1):																																			
		<table><tr><th>i</th><th>arr[i-1]</th><th>arr[i]</th><th>Comparison</th><th>Result</th></tr><tr><td>1</td><td>1</td><td>2</td><td>2 ≥ 1</td><td>✔</td></tr><tr><td>2</td><td>2</td><td>3</td><td>3 ≥ 2</td><td>✔</td></tr><tr><td>3</td><td>3</td><td>4</td><td>4 ≥ 3</td><td>✔</td></tr><tr><td>4</td><td>4</td><td>5</td><td>5 ≥ 4</td><td>✔</td></tr><tr><td>5</td><td>5</td><td>6</td><td>6 ≥ 5</td><td>✔</td></tr><tr><td colspan="5">→ All passed → <b>Returns: true</b></td></tr></table>			i	arr[i-1]	arr[i]	Comparison	Result	1	1	2	2 ≥ 1	✔	2	2	3	3 ≥ 2	✔	3	3	4	4 ≥ 3	✔	4	4	5	5 ≥ 4	✔	5	5	6	6 ≥ 5	✔	→ All passed → <b>Returns: true</b>		
i	arr[i-1]	arr[i]	Comparison	Result																																	
1	1	2	2 ≥ 1	✔																																	
2	2	3	3 ≥ 2	✔																																	
3	3	4	4 ≥ 3	✔																																	
4	4	5	5 ≥ 4	✔																																	
5	5	6	6 ≥ 5	✔																																	
→ All passed → <b>Returns: true</b>																																					
isSorted(arr1, n1): Checks every pair (i, j) where j > i:																																					
<ul style="list-style-type: none"><li>For every arr[i] ≤ arr[j] → all OK → <b>Returns: true</b></li></ul>																																					
Array 2: {11, 2, 3, 4, 5, 6} (Not sorted)																																					
isSortedEff(arr2, n2):																																					
<table><tr><th>i</th><th>arr[i-1]</th><th>arr[i]</th><th>Comparison</th><th>Result</th></tr><tr><td>1</td><td>11</td><td>2</td><td>2 &lt; 11 ✖</td><td>●</td></tr><tr><td colspan="5">→ Early exit → <b>Returns:</b></td></tr></table>			i	arr[i-1]	arr[i]	Comparison	Result	1	11	2	2 < 11 ✖	●	→ Early exit → <b>Returns:</b>																								
i	arr[i-1]	arr[i]	Comparison	Result																																	
1	11	2	2 < 11 ✖	●																																	
→ Early exit → <b>Returns:</b>																																					

	<table><tr><th>i</th><th>arr[i-1]</th><th>arr[i]</th><th>Comparison</th><th>Result</th></tr><tr><td>false</td><td></td><td></td><td></td><td></td></tr></table>	i	arr[i-1]	arr[i]	Comparison	Result	false				
i	arr[i-1]	arr[i]	Comparison	Result							
false											
	<p>isSorted(arr2, n2):</p> <ul style="list-style-type: none"><li>(0,1) → 2 &lt; 11 → ✖ → Returns: false</li></ul> <p>🖨 Output:</p> <p>true false true false</p>										
true false true false											

Leaders Array in C++

```
#include <iostream>
using namespace std;

void leaders(int arr[], int n) {
    int curr = arr[n - 1];
    cout << curr << " ";

    for (int i = n - 2; i >= 0; i--) {
        if (arr[i] > curr) {
            curr = arr[i];
            cout << curr << " ";
        }
    }
}

int main() {
    int arr[] = {7, 10, 4, 10, 6, 5, 2};
    int n = sizeof(arr) / sizeof(arr[0]);

    leaders(arr, n);
    cout << endl;

    return 0;
}
```

Dry Run Table

Input array: {7, 10, 4, 10, 6, 5, 2}

We process from **right to left**:

Index	arr[i]	Current Leader (curr)	Is arr[i] > curr?	Print Leader?	Updated curr
6	2	2	-	✓	2
5	5	2	✓	✓	5
4	6	5	✓	✓	6
3	10	6	✓	✓	10
2	4	10	✗	✗	10
1	10	10	✗	✗	10
0	7	10	✗	✗	10

✓ **Output (Printed from right to left):**

2 5 6 10

2 5 6 10

## Majority element in C++

```
#include <iostream>
using namespace std;

int majority(int arr[], int n) {
    int res = 0, count = 1;
    for (int i = 1; i < n; i++) {
        if (arr[res] == arr[i]) {
            count++;
        } else {
            count--;
        }
        if (count == 0) {
            res = i;
            count = 1;
        }
    }

    count = 0;
    for (int i = 0; i < n; i++) {
        if (arr[res] == arr[i]) {
            count++;
        }
    }

    if (count <= n / 2) {
        res = -1;
    }
    return res;
}

int main() {
    int arr[] = {6, 8, 4, 8, 8};
    int n = sizeof(arr) / sizeof(arr[0]);

    cout << majority(arr, n) << endl;

    return 0;
}
```

### Array Given:

```
arr[] = {6, 8, 4, 8, 8}
n = 5
```

We need to find the element (if any) that appears **more than  $5 / 2 = 2$**  times.

### 🔄 Moore's Voting Algorithm Dry Run

We'll go step-by-step through the first for loop which finds a *candidate*.

i	arr[i]	arr[res]	count	Explanation
0	6	6	1	Initial candidate at index 0
1	8	6	0	$8 \neq 6 \rightarrow \text{count--}$
		8	1	$\text{count} = 0 \rightarrow$ new candidate at index 1
2	4	8	0	$4 \neq 8 \rightarrow \text{count--}$
		4	1	$\text{count} = 0 \rightarrow$ new candidate at index 2
3	8	4	0	$8 \neq 4 \rightarrow \text{count--}$
		8	1	$\text{count} = 0 \rightarrow$ new candidate at index 3
4	8	8	2	$8 == 8 \rightarrow \text{count++}$

**Candidate Index:** res = 3, arr[3] = 8

### ✔ Second loop: Confirm the candidate

We check how many times 8 appears in the array.

```
count = 0;
for (int i = 0; i < n; i++) {
    if (arr[i] == 8) count++;
}
```

8 appears **3 times** (at indices 1, 3, and 4).

Since  $3 > 2$ , it **is** the majority element.

### ✔ Final Output

3

	That's the index of the majority element 8.
3	

## Max Subarray sum in C++

```
#include <iostream>
using namespace std;

int maxsub(int arr[], int n) {
    int res = arr[0];
    int maxEnding = arr[0];
    for (int i = 1; i < n; i++) {
        maxEnding = max(maxEnding + arr[i], arr[i]);
        res = max(res, maxEnding);
    }
    return res;
}

int main() {
    int arr[] = {-3, 8, -2, 4, -5, 6};
    int n = sizeof(arr) / sizeof(arr[0]);
    cout << maxsub(arr, n) << endl;
    return 0;
}
```

### Input:

arr[] = {-3, 8, -2, 4, -5, 6}  
n = 6

### Variables:

- res: Stores the **maximum subarray sum found so far**
- maxEnding: Stores the **maximum subarray sum ending at the current index**

### 🔄 Dry Run Table:

i	arr[i]	maxEnding = max(maxEnding + arr[i], arr[i])	res = max(res, maxEnding)
0	-3	maxEnding = -3	res = -3
1	8	max(-3 + 8, 8) = 8	res = 8
2	-2	max(8 - 2, -2) = 6	res = 8
3	4	max(6 + 4, 4) = 10	res = 10
4	-5	max(10 - 5, -5) = 5	res = 10
5	6	max(5 + 6, 6) = 11	res = 11

### ✔ Final Output:

11



## Tapping Rain Water in C++

```
#include <iostream>
#include <algorithm>
using namespace std;

int getWater(int arr[], int n) {
    int res = 0;
    for (int i = 0; i < n; i++) {
        int lmax = arr[i];
        for (int j = 0; j < i; j++) {
            lmax = max(arr[j], lmax);
        }
        int rmax = arr[i];
        for (int j = i + 1; j < n; j++) {
            rmax = max(arr[j], rmax);
        }

        res += min(lmax, rmax) - arr[i];
    }
    return res;
}

int main() {
    int arr[] = {3, 0, 1, 2, 5};
    int n = sizeof(arr) / sizeof(arr[0]);
    cout << getWater(arr, n) << endl;
    return 0;
}
```

### Problem Explanation: Trapping Rain Water

At each index i, the amount of water it can hold is:

$$\text{water\_at\_i} = \min(\text{lmax}, \text{rmax}) - \text{arr}[i]$$

Where:

- lmax: Max height to the left of i (including i)
- rmax: Max height to the right of i (including i)
- If  $\min(\text{lmax}, \text{rmax}) - \text{arr}[i] > 0$ , it adds to total water trapped.

### ▣ Dry Run Table

Array: {3, 0, 1, 2, 5}

i	arr[i]	lmax (max left)	rmax (max right)	min(lmax, rmax)	Water at i = min(lmax, rmax) - arr[i]	res
0	3	3	5	3	0	0
1	0	3	5	3	3	3
2	1	3	5	3	2	5
3	2	3	5	3	1	6
4	5	5	5	5	0	6

### ✔ Final Output:

6

Output:

6

## Remove Duplicates in C++

```
#include <iostream>
using namespace std;

int removeDup(int arr[], int n) {
    int res = 1;
    for (int i = 1; i < n; i++) {
        if (arr[i] != arr[res - 1]) {
            arr[res] = arr[i];
            res++;
        }
    }
    return res;
}

int main() {
    int arr[] = {2, 2, 3, 4, 5, 6};
    int n = sizeof(arr) / sizeof(arr[0]);
    int p = removeDup(arr, n);

    cout << "After Removal" << endl;

    for (int i = 0; i < p; i++) {
        cout << arr[i] << " ";
    }
    cout << endl;

    return 0;
}
```

## Dry Run Table

i	arr[i]	arr[res - 1]	Condition Met (!=)	Action	arr[res]	res
1	2	2	✗ No	Skip	-	1
2	3	2	✓ Yes	arr[1] = 3	3	2
3	4	3	✓ Yes	arr[2] = 4	4	3
4	5	4	✓ Yes	arr[3] = 5	5	4
5	6	5	✓ Yes	arr[4] = 6	6	5

✓ **Final Values:**

- `res = 5` → means 5 unique elements.
- Modified array (first `res` elements):

$$\text{arr}[] = \{2, 3, 4, 5, 6\}$$

After Removal
2 3 4 5 6

Rotate Array in C++

```
#include <iostream>
using namespace std;

void rotate(int arr[], int d, int n) {
    int temp[d];
    for (int i = 0; i < d; i++) {
        temp[i] = arr[i];
    }

    for (int i = d; i < n; i++) {
        arr[i - d] = arr[i];
    }

    for (int i = 0; i < d; i++) {
        arr[n - d + i] = temp[i];
    }

    for (int i = 0; i < n; i++) {
        cout << " " << arr[i];
    }
    cout << endl;
}

int main() {
    int arr[] = {1, 3, 6, 2, 5, 4, 3, 2, 4};
    int n = sizeof(arr) / sizeof(arr[0]);
    rotate(arr, 5, n);
    return 0;
}
```

Input:

```
arr[] = {1, 3, 6, 2, 5, 4, 3, 2, 4}
d = 5
n = 9
```

🔄 Step-by-step Breakdown:

1. Store first d elements in temp

temp = {1, 3, 6, 2, 5}

i	temp[i]
0	1
1	3
2	6
3	2
4	5

2. Shift remaining n - d elements to the left

```
arr[0] = arr[5] → 4
arr[1] = arr[6] → 3
arr[2] = arr[7] → 2
arr[3] = arr[8] → 4
```

i	arr[i] (after shift)
0	4
1	3
2	2
3	4

3. Copy temp back to the end

```
arr[4] = temp[0] = 1
arr[5] = temp[1] = 3
arr[6] = temp[2] = 6
arr[7] = temp[3] = 2
arr[8] = temp[4] = 5
```

i	arr[i] (final state)
4	1

	i	arr[i] (final state)
	5	3
	6	6
	7	2
	8	5
	<div>📄 <b>Final Output:</b></div> <div>4 3 2 4 1 3 6 2 5</div>	
4 3 2 4 1 3 6 2 5		