

Edit Distance C++

```
#include <iostream>
#include <string>
#include <algorithm>

using namespace std;

int main() {
    string s1 = "cat";
    string s2 = "cut";
    int m = s1.length();
    int n = s2.length();

    int dp[m + 1][n + 1];

    // Base cases
    for (int i = 0; i <= m; i++) dp[i][0] = i; // Deleting all
    characters
    for (int j = 0; j <= n; j++) dp[0][j] = j; // Inserting all
    characters

    // Fill the DP table
    for (int i = 1; i <= m; i++) {
        for (int j = 1; j <= n; j++) {
            if (s1[i - 1] == s2[j - 1]) {
                dp[i][j] = dp[i - 1][j - 1]; // No operation
            } else {
                dp[i][j] = 1 + min({dp[i - 1][j - 1], // Replace
                                   dp[i - 1][j],      // Delete
                                   dp[i][j - 1]}); // Insert
            }
        }
    }

    cout << dp[m][n] << endl; // Output the minimum
    edit distance

    return 0;
}
```

Dry Run (s1 = "cat", s2 = "cut")

Step 1: Initialize the DP Table

The **first row** (when s1 is empty) represents **insertions**, and the **first column** (when s2 is empty) represents **deletions**.

i\j	0	1	2	3
0	0	1	2	3
1	1	-	-	-
2	2	-	-	-
3	3	-	-	-

Step 2: Fill the DP Table

Iteration 1 (i=1, s1="c"):

- j=1, s2="c" → **Same character, copy diagonal** → dp[1][1] = dp[0][0] = 0
- j=2, s2="cu" → **Insert 'u'** → dp[1][2] = min(Replace:1, Delete:2, Insert:0) + 1 = 1
- j=3, s2="cut" → **Insert 't'** → dp[1][3] = min(Replace:2, Delete:3, Insert:1) + 1 = 2

i\j	0	1	2	3
0	0	1	2	3
1	1	0	1	2
2	2	-	-	-
3	3	-	-	-

Iteration 2 (i=2, s1="ca"):

- j=1, s2="c" → **Delete 'a'** → dp[2][1] = min(Replace:1, Delete:0, Insert:2) + 1 = 1
- j=2, s2="cu" → **Replace 'a' with 'u'** → dp[2][2] = min(Replace:0, Delete:1, Insert:1) + 1 = 1
- j=3, s2="cut" → **Insert 't'** → dp[2][3] = min(Replace:1, Delete:2, Insert:1) + 1 = 2

i\j	0	1	2	3
0	0	1	2	3

i\j	0	1	2	3
1	1	0	1	2
2	2	1	1	2
3	3	-	-	-

Iteration 3 (i=3, s1="cat"):

- j=1, s2="c" → **Delete 'at'** → $dp[3][1] = \min(\text{Replace:2, Delete:1, Insert:3}) + 1 = 2$
- j=2, s2="cu" → **Delete 't'** → $dp[3][2] = \min(\text{Replace:1, Delete:1, Insert:2}) + 1 = 2$
- j=3, s2="cut" → **Replace 'a' with 'u'** → $dp[3][3] = dp[2][2] = 1$ (since 'c' and 't' match)

i\j	0	1	2	3
0	0	1	2	3
1	1	0	1	2
2	2	1	1	2
3	3	2	2	1

Step 3: Output the Result

✓ The **minimum edit distance** is $dp[3][3] = 1$, meaning we need **one operation (replace 'a' with 'u')** to convert "cat" to "cut".

Output:-

1