

Seive in C++

```
#include <iostream>
#include <cmath>
#include <vector>
using namespace std;

class SeiveofErastostenins {
public:
    static void main() {
        vector<bool> myseive = seive(20);
        for (int i = 0; i < myseive.size(); i++) {
            cout << i << " " << (myseive[i] ? "true" : "false")
        }
    }

    static vector<bool> seive(int n) {
        vector<bool> arr(n + 1, true);
        arr[0] = false;
        arr[1] = false;
        for (int i = 2; i <= sqrt(n); i++) {
            if (arr[i]) {
                for (int j = i * i; j <= n; j += i) {
                    arr[j] = false;
                }
            }
        }
        return arr;
    }
};

int main() {
    SeiveofErastostenins::main();
    return 0;
}
```

Sieve of Eratosthenes Dry Run for n = 20

🔢 Step 1: Initialize Boolean Vector

vector<bool> arr(n + 1, true); // arr[0..20] all set to true
arr[0] = false;
arr[1] = false;

📋 Initial Table:

| i | isPrime |
|----|---------|
| 0 | false |
| 1 | false |
| 2 | true |
| 3 | true |
| 4 | true |
| 5 | true |
| 6 | true |
| 7 | true |
| 8 | true |
| 9 | true |
| 10 | true |
| 11 | true |
| 12 | true |
| 13 | true |
| 14 | true |
| 15 | true |
| 16 | true |
| 17 | true |
| 18 | true |
| 19 | true |
| 20 | true |

🔄 Step 2: Outer loop — for (int i = 2; i <= sqrt(n); i++)

- sqrt(20) is ~4.47 → so i goes from 2 to 4

➤ i = 2:

arr[2] == true → mark all multiples of 2 from 4 onward as false

Inner loop (j = i*i; j <= n; j += i) → j = 4, 6, 8, 10, 12, 14, 16, 18, 20

✖ Marked False:

4, 6, 8, 10, 12, 14, 16, 18, 20

► **i = 3:**

arr[3] == true → mark all multiples of 3 from 9 onward as false

j = 9, 12, 15, 18

✕ **Marked False:**

9, 15

(12 and 18 already marked by i = 2)

► **i = 4:**

arr[4] == false → skip

✓ **Final Table After Sieve:**

| i | isPrime |
|----|---------|
| 0 | false |
| 1 | false |
| 2 | true |
| 3 | true |
| 4 | false |
| 5 | true |
| 6 | false |
| 7 | true |
| 8 | false |
| 9 | false |
| 10 | false |
| 11 | true |
| 12 | false |
| 13 | true |
| 14 | false |
| 15 | false |
| 16 | false |
| 17 | true |
| 18 | false |
| 19 | true |
| 20 | false |

📄 **Output Printed by the Code:**

0 false

| | |
|--|---|
| | 1 false 2 true 3 true 4 false 5 true 6 false 7 true 8 false 9 false 10 false 11 true 12 false 13 true 14 false 15 false 16 false 17 true 18 false 19 true 20 false ✔ Prime Numbers ≤ 20 : 2, 3, 5, 7, 11, 13, 17, 19 |
| 0 false 1 false 2 true 3 true 4 false 5 true 6 false 7 true 8 false 9 false 10 false 11 true 12 false 13 true 14 false 15 false 16 false 17 true 18 false 19 true 20 false | |