

## Dijkstra in C++

```
#include <bits/stdc++.h>
using namespace std;

class Solution
{
public:
    // Function to find the shortest distance of all
    the vertices
    // from the source vertex S.
    vector<int> dijkstra(int V,
    vector<vector<int>> adj[], int S)
    {

        // Create a priority queue for storing the
        nodes as a pair {dist,node}
        // where dist is the distance from source to
        the node.
        priority_queue<pair<int, int>,
        vector<pair<int, int>>, greater<pair<int, int>>>
        pq;

        // Initialising distTo list with a large
        number to
        // indicate the nodes are unvisited initially.
        // This list contains distance from source to
        the nodes.
        vector<int> distTo(V, INT_MAX);

        // Source initialised with dist=0.
        distTo[S] = 0;
        pq.push({0, S});

        // Now, pop the minimum distance node
        first from the min-heap
        // and traverse for all its adjacent nodes.
        while (!pq.empty())
        {
            int node = pq.top().second;
            int dis = pq.top().first;
            pq.pop();

            // Check for all adjacent nodes of the
            popped out
            // element whether the prev dist is larger
            than current or not.
            for (auto it : adj[node])
            {
                int v = it[0];
                int w = it[1];
                if (dis + w < distTo[v])
                {
                    distTo[v] = dis + w;

                    // If current distance is smaller,
                    // push it into the queue.
                    pq.push({dis + w, v});
                }
            }
        }

        // Return the list containing shortest
        distances
```

### Graph Setup

Given:

- **Vertices (V):** 3
- **Source (S):** 2
- **Adjacency list (adj):**

```
adj[0] = {{1, 1}, {2, 6}};
adj[1] = {{2, 3}, {0, 1}};
adj[2] = {{1, 3}, {0, 6}};
```

This translates to:

| From | To | Weight |
|------|----|--------|
| 0    | 1  | 1      |
| 0    | 2  | 6      |
| 1    | 2  | 3      |
| 1    | 0  | 1      |
| 2    | 1  | 3      |
| 2    | 0  | 6      |

### 🔄 Dijkstra's Algorithm

**Start from source 2**, initialize:

```
distTo = [∞, ∞, 0]
pq = [(0, 2)]
```

Now iterate:


| Step | Node | Pop (dist,node) | Neighbors    | Update Distances             | pq After     |
|------|------|-----------------|--------------|------------------------------|--------------|
| 1    | 2    | (0, 2)          | (1,3), (0,6) | dist[1] = 3, dist[0] = 6     | (3,1), (6,0) |
| 2    | 1    | (3, 1)          | (2,3), (0,1) | dist[0] = min(6, 4) = 4      | (4,0), (6,0) |
| 3    | 0    | (4, 0)          | (1,1), (2,6) | dist[1] already 3 < 5 → skip | (6,0)        |
| 4    | 0    | (6, 0)          | -            | Already visited with smaller | —            |

### 📖 Final Distance Array:

```
res = [4, 3, 0]
```

Means:

| Vertex | Shortest Distance from Source (2) |
|--------|-----------------------------------|
| 0      | 4                                 |

| <pre> // from source to all the nodes. return distTo; } };  int main() {     // Driver code.     int V = 3, E = 3, S = 2;     vector&lt;vector&lt;int&gt;&gt;&gt; adj[V];     vector&lt;vector&lt;int&gt;&gt;&gt; edges;     vector&lt;int&gt; v1{1, 1}, v2{2, 6}, v3{2, 3}, v4{0, 1}, v5{1, 3}, v6{0, 6};     int i = 0;     adj[0].push_back(v1);     adj[0].push_back(v2);     adj[1].push_back(v3);     adj[1].push_back(v4);     adj[2].push_back(v5);     adj[2].push_back(v6);      Solution obj;     vector&lt;int&gt; res = obj.dijkstra(V, adj, S);      for (int i = 0; i &lt; V; i++)     {         cout &lt;&lt; res[i] &lt;&lt; " ";     }     cout &lt;&lt; endl;     return 0; } </pre> | <table border="1" data-bbox="762 118 1353 230"> <thead> <tr> <th>Vertex</th><th>Shortest Distance from Source (2)</th></tr> </thead> <tbody> <tr> <td>1</td><td>3</td></tr> <tr> <td>2</td><td>0 (source itself)</td></tr> </tbody> </table> <p data-bbox="762 309 904 338">  <b>Output:</b> </p> <p data-bbox="762 376 823 405">4 3 0</p> | Vertex | Shortest Distance from Source (2) | 1 | 3 | 2 | 0 (source itself) |
|---|---|--------|-----------------------------------|---|---|---|-------------------|
| Vertex  | Shortest Distance from Source (2)   |        |                                   |   |   |   |                   |
| 1   | 3   |        |                                   |   |   |   |                   |
| 2   | 0 (source itself)   |        |                                   |   |   |   |                   |
| <p data-bbox="124 1144 245 1173"><b>Output:-</b></p> <p data-bbox="124 1176 191 1205">4 3 0</p>   |   |        |                                   |   |   |   |                   |