

BellmanFord in C++

```
#include <bits/stdc++.h>
using namespace std;

class Solution {
public:
    /* Function to implement Bellman Ford
    * edges: vector of vectors which represents the
    graph
    * S: source vertex to start traversing graph with
    * V: number of vertices
    */
    vector<int> bellman_ford(int V,
vector<vector<int>>& edges, int S) {
        vector<int> dist(V, 1e8);
        dist[S] = 0;
        for (int i = 0; i < V - 1; i++) {
            for (auto it : edges) {
                int u = it[0];
                int v = it[1];
                int wt = it[2];
                if (dist[u] != 1e8 &&
dist[u] + wt < dist[v]) {
                    dist[v] = dist[u] +
wt;
                }
            }
        }
        // Nth relaxation to check negative cycle
        for (auto it : edges) {
            int u = it[0];
            int v = it[1];
            int wt = it[2];
            if (dist[u] != 1e8 && dist[u] + wt
< dist[v]) {
                return { -1};
            }
        }

        return dist;
    }
};

int main() {

    int V = 6;
    vector<vector<int>> edges(7, vector<int>(3));
    edges[0] = {3, 2, 6};
    edges[1] = {5, 3, 1};
    edges[2] = {0, 1, 5};
    edges[3] = {1, 5, -3};
    edges[4] = {1, 2, -2};
    edges[5] = {3, 4, -2};
    edges[6] = {2, 4, 3};

    int S = 0;
    Solution obj;
    vector<int> dist = obj.bellman_ford(V, edges, S);
    for (auto d : dist) {
        cout << d << " ";
    }
}
```

Dry Run:

Let's dry run the given code with the input:

```
int V = 6;
vector<vector<int>> edges(7,
vector<int>(3));
edges[0] = {3, 2, 6};
edges[1] = {5, 3, 1};
edges[2] = {0, 1, 5};
edges[3] = {1, 5, -3};
edges[4] = {1, 2, -2};
edges[5] = {3, 4, -2};
edges[6] = {2, 4, 3};
int S = 0;
```

Step 1: Initialize Variables

- `dist[]`: Distance array initialized to {1e8, 1e8, 1e8, 1e8, 1e8, 1e8}.
- Set `dist[0] = 0` (since `S = 0`).

Step 2: Relaxation (V-1) Times

- **First iteration (i = 0):** Relax all edges.
 - Relax edge (3, 2, 6): No change.
 - Relax edge (5, 3, 1): No change.
 - Relax edge (0, 1, 5):
`dist[1] = min(1e8, dist[0] + 5) = 5.`
 - Relax edge (1, 5, -3):
`dist[5] = min(1e8, dist[1] - 3) = 2.`
 - Relax edge (1, 2, -2):
`dist[2] = min(1e8, dist[1] - 2) = 3.`
 - Relax edge (3, 4, -2):
`dist[4] = min(1e8, dist[3] - 2) = 3.`
 - Relax edge (2, 4, 3): No change.
- **Second iteration (i = 1):** Relax all edges again.
 - Relax edge (3, 2, 6): No change.
 - Relax edge (5, 3, 1): No change.
 - Relax edge (0, 1, 5): No change.
 - Relax edge (1, 5, -3): No change.
 - Relax edge (1, 2, -2): No

<pre> } cout << endl; return 0; } </pre>	<p>change.</p> <ul style="list-style-type: none"> ○ Relax edge (3, 4, -2): No change. ○ Relax edge (2, 4, 3): No change. <p>(No updates during the second iteration.)</p> <ul style="list-style-type: none"> • Third to Fifth iterations (i = 2, 3, 4): Relax all edges again. <ul style="list-style-type: none"> ○ No further changes, as all shortest paths are already updated. <p>Step 3: Negative Cycle Detection</p> <ul style="list-style-type: none"> • Nth iteration (i = 5): Perform one more relaxation round. <ul style="list-style-type: none"> ○ All distances are unchanged, meaning no negative cycle exists. <p>Step 4: Return the Result</p> <ul style="list-style-type: none"> • Final dist[] array: {0, 5, 3, 3, 1, 2}. <p>Thus, the shortest distances from source 0 to all other nodes are:</p> <p>0 5 3 3 1 2</p>
<p>Output:- 0 5 3 3 1 2</p>	