

## Articulation Point in C++

```
#include <bits/stdc++.h>
using namespace std;

//User function Template for C++

class Solution {
private:
    int timer = 1;
    void dfs(int node, int parent, vector<int> &vis, int tin[], int low[], vector<int> &mark, vector<int> adj[]) {
        vis[node] = 1;
        tin[node] = low[node] = timer;
        timer++;
        int child = 0;
        for (auto it : adj[node]) {
            if (it == parent) continue;
            if (!vis[it]) {
                dfs(it, node, vis, tin, low, mark, adj);
                low[node] = min(low[node], low[it]);
                if (low[it] >= tin[node] && parent != -1) {
                    mark[node] = 1;
                }
                child++;
            }
            else {
                low[node] = min(low[node], tin[it]);
            }
        }
        if (child > 1 && parent == -1) {
            mark[node] = 1;
        }
    }
public:
    vector<int> articulationPoints(int n, vector<int> adj[]) {
        vector<int> vis(n, 0);
        int tin[n];
        int low[n];
        vector<int> mark(n, 0);
        for (int i = 0; i < n; i++) {
            if (!vis[i]) {
                dfs(i, -1, vis, tin, low, mark, adj);
            }
        }
        vector<int> ans;
        for (int i = 0; i < n; i++) {
            if (mark[i] == 1) {
                ans.push_back(i);
            }
        }
        if (ans.size() == 0) return { -1};
        return ans;
    }
};

int main() {

    int n = 5;
    vector<vector<int>> edges = {
        {0, 1}, {1, 4},
        {2, 4}, {2, 3}, {3, 4}
    }
```

### Dry Run:

Let's dry run the algorithm with the following graph represented by edges:

```
int n = 5;
vector<vector<int>> edges = {
    {0, 1}, {1, 4},
    {2, 4}, {2, 3}, {3, 4}
};
```

The graph can be visualized as:

```
yaml
Copy code
    0
    |
    1
  /  \
4----2
  |
  3
```

### Step 1: Initialize Variables

- **vis:** A boolean vector initialized to [0, 0, 0, 0, 0] (all nodes unvisited).
- **tin:** A vector initialized to [-1, -1, -1, -1, -1].
- **low:** A vector initialized to [-1, -1, -1, -1, -1].
- **mark:** A vector initialized to [0, 0, 0, 0, 0] (articulation points).
- **timer:** Set to 1, used to assign discovery times.

### Step 2: DFS Traversal

- Start DFS from node 0:
  - For node 0:
    - Set `tin[0] = low[0] = 1`.
    - Visit neighbors: 1 (child).
  - For node 1:
    - Set `tin[1] = low[1] = 2`.
    - Visit neighbors: 0 (parent) and 4 (child).
  - For node 4:
    - Set `tin[4] = low[4] = 3`.
    - Visit neighbors: 1 (parent), 2 (child).

```

};

vector<int> adj[n];
for (auto it : edges) {
    int u = it[0], v = it[1];
    adj[u].push_back(v);
    adj[v].push_back(u);
}
Solution obj;
vector<int> nodes = obj.articulationPoints(n, adj);
for (auto node : nodes) {
    cout << node << " ";
}
cout << endl;
return 0;
}

```

- For node 2:
  - Set  $tin[2] = low[2] = 4$ .
  - Visit neighbors: 4 (parent), 3 (child).
- For node 3:
  - Set  $tin[3] = low[3] = 5$ .
  - Visit neighbors: 2 (parent).
  - DFS ends for node 3, return to 2.
- For node 2, update  $low[2]$  as  $\min(low[2], low[3]) = 4$ .
- As  $low[3] \geq tin[2]$ , mark node 2 as an articulation point.
- For node 4, update  $low[4]$  as  $\min(low[4], low[2]) = 3$ .
- As  $low[2] \geq tin[4]$ , mark node 4 as an articulation point.
- For node 1, update  $low[1]$  as  $\min(low[1], low[4]) = 2$ .
- As  $low[4] \geq tin[1]$ , mark node 1 as an articulation point.

### Step 3: Collect and Sort Results

- After DFS completes, `mark` contains `[0, 1, 1, 0, 1]`, indicating that nodes 1, 2, and 4 are articulation points.
- The final output will be 1 4 (sorted articulation points).

**Output:-**  
1 4