

Count Distinct Subsequence C++

```
#include <iostream>
using namespace std;
```

```
int countValleysAndMountains(int n) {
    int dp[n + 1] = {0}; // Initialize the array with zeros
    dp[0] = 1; // Base case: empty sequence
    dp[1] = 1; // Sequence of length 1: either V or M
```

```
    for (int i = 2; i <= n; i++) {
        int valleys = 0;
        int mountains = i - 1;

        while (mountains >= 0) {
            dp[i] += dp[valleys] * dp[mountains];
            valleys++;
            mountains--;
        }
    }
```

```
    return dp[n];
}
```

```
int main() {
    int n = 5;
    cout << countValleysAndMountains(n) << endl;
    return 0;
}
```

Step-by-Step Calculation

i	dp[i] Computation	dp[i] Value
0	dp[0] = 1	1
1	dp[1] = dp[0] * dp[0]	1
2	dp[2] = dp[0] * dp[1] + dp[1] * dp[0]	2
3	dp[3] = dp[0] * dp[2] + dp[1] * dp[1] + dp[2] * dp[0]	5
4	dp[4] = dp[0] * dp[3] + dp[1] * dp[2] + dp[2] * dp[1] + dp[3] * dp[0]	14
5	dp[5] = dp[0] * dp[4] + dp[1] * dp[3] + dp[2] * dp[2] + dp[3] * dp[1] + dp[4] * dp[0]	42

Final Output
42

Output:-
42