

Abbreviation in C++

```
#include <iostream>
#include <string>
using namespace std;

class Abbreviation {
public:
    static void solution(string str, string asf, int count,
int pos) {
        if (pos == str.length()) {
            if (count == 0) {
                cout << asf << endl;
            } else {
                cout << asf << count << endl;
            }
            return;
        }

        if (count > 0) {
            solution(str, asf + to_string(count) + str[pos],
0, pos + 1);
        } else {
            solution(str, asf + str[pos], 0, pos + 1);
        }

        solution(str, asf, count + 1, pos + 1);
    }
};

int main() {
    string str = "pep";
    Abbreviation::solution(str, "", 0, 0);
    return 0;
}
```

Step-by-Step Execution:

The function solution() uses recursion to generate all the abbreviations. It has two main actions:

1. **Include the current character with an abbreviation count if any.**
 2. **Include the current character as is.**
- str: The string for which we need to find abbreviations.
 - asf: The abbreviation formed so far.
 - count: The number of characters skipped (abbreviated).
 - pos: The current position in the string.

1. **Initial Call:** solution("pep", "", 0, 0)
 - **pos = 0, count = 0, asf = ""**
 - Two options:
 1. Skip character at pos = 0 (first 'p')
 2. Include character at pos = 0 (first 'p')
 - Recur on both options.
2. **First Option:** Skip character at pos = 0
 - Call solution("pep", "", 1, 1) (increment count by 1)
3. **Call:** solution("pep", "", 1, 1)
 - **pos = 1, count = 1, asf = ""**
 - Two options:
 1. Skip character at pos = 1 (character 'e')
 2. Include character at pos = 1 (character 'e')
 - Recur on both options.
4. **First Option:** Skip character at pos = 1
 - Call solution("pep", "1", 2, 2) (skip 'e' and increment count)
5. **Call:** solution("pep", "1", 2, 2)
 - **pos = 2, count = 2, asf = "1"**
 - Two options:
 1. Skip character at pos = 2 (second 'p')
 2. Include character at pos = 2

	<p>(second 'p')</p> <ul style="list-style-type: none"> ○ Recur on both options. <p>6. First Option: Skip character at pos = 2</p> <ul style="list-style-type: none"> ○ Call solution("pep", "12", 3, 3) (skip 'p') <p>7. Call: solution("pep", "12", 3, 3)</p> <ul style="list-style-type: none"> ○ pos = 3, count = 3, asf = "12" ○ Base case reached (pos == str.length()) ○ Output: "12" <p>8. Second Option: Include character at pos = 2</p> <ul style="list-style-type: none"> ○ Call solution("pep", "1p", 0, 3) (include 'p' and reset count) <p>9. Call: solution("pep", "1p", 0, 3)</p> <ul style="list-style-type: none"> ○ pos = 3, count = 0, asf = "1p" ○ Base case reached (pos == str.length()) ○ Output: "1p" <p>10. Backtrack to Call 4: solution("pep", "", 1, 1)</p> <ul style="list-style-type: none"> ○ pos = 1, count = 1, asf = "" ○ Second option: Include character at pos = 1 ('e') ○ Call solution("pep", "e", 0, 2) (reset count and include 'e') <p>11. Call: solution("pep", "e", 0, 2)</p> <ul style="list-style-type: none"> ○ pos = 2, count = 0, asf = "e" ○ Two options: <ul style="list-style-type: none"> 1. Skip character at pos = 2 (second 'p') 2. Include character at pos = 2 (second 'p') ○ Recur on both options. <p>12. First Option: Skip character at pos = 2</p> <ul style="list-style-type: none"> ○ Call solution("pep", "e1", 1, 3) (skip
--	--

'p' and increment count)

13. **Call:** solution("pep", "e1", 1, 3)
- **pos = 3, count = 1, asf = "e1"**
 - Base case reached (pos == str.length())
 - Output: "e1"
14. **Second Option:** Include character at pos = 2
- Call solution("pep", "ep", 0, 3) (include 'p' and reset count)
15. **Call:** solution("pep", "ep", 0, 3)
- **pos = 3, count = 0, asf = "ep"**
 - Base case reached (pos == str.length())
 - Output: "ep"
16. **Backtrack to Initial Call:** solution("pep", "", 0, 0)
- **pos = 0, count = 0, asf = ""**
 - Second option: Include character at pos = 0 ('p')
 - Call solution("pep", "p", 0, 1) (include 'p' and reset count)
17. **Call:** solution("pep", "p", 0, 1)
- **pos = 1, count = 0, asf = "p"**
 - Two options:
 1. Skip character at pos = 1 (character 'e')
 2. Include character at pos = 1 (character 'e')
 - Recur on both options.
18. **First Option:** Skip character at pos = 1
- Call solution("pep", "p1", 1, 2) (skip 'e' and increment count)
19. **Call:** solution("pep", "p1", 1, 2)
- **pos = 2, count = 1, asf = "p1"**
 - Two options:
 1. Skip character at pos = 2

- (second 'p')
- 2. Include character at pos = 2
(second 'p')
- Recur on both options.

20. **First Option:** Skip character at pos = 2

- Call solution("pep", "p12", 2, 3)
(skip 'p' and increment count)

21. **Call:** solution("pep", "p12", 2, 3)

- **pos = 3, count = 2, asf = "p12"**
- Base case reached (pos == str.length())
- Output: "p12"

22. **Second Option:** Include character at pos = 2

- Call solution("pep", "p1p", 0, 3)
(include 'p' and reset count)

23. **Call:** solution("pep", "p1p", 0, 3)

- **pos = 3, count = 0, asf = "p1p"**
- Base case reached (pos == str.length())
- Output: "p1p"

24. **Backtrack to Call 17:** solution("pep", "p", 0, 1)

- **pos = 1, count = 0, asf = "p"**
- Second option: Include character at pos = 1 ('e')
- Call solution("pep", "pe", 0, 2)
(include 'e' and reset count)

25. **Call:** solution("pep", "pe", 0, 2)

- **pos = 2, count = 0, asf = "pe"**
- Two options:
 1. Skip character at pos = 2
(second 'p')
 2. Include character at pos = 2
(second 'p')
- Recur on both options.

26. **First Option:** Skip character at pos = 2

- Call solution("pep", "pe1", 1, 3)
(skip 'p' and increment count)

27. **Call:** solution("pep", "pe1", 1, 3)

- **pos = 3, count = 1, asf = "pe1"**
- Base case reached (pos == str.length())
- Output: "pe1"

28. **Second Option:** Include character at pos = 2

- Call solution("pep", "pep", 0, 3)
(include 'p' and reset count)

29. **Call:** solution("pep", "pep", 0, 3)

- **pos = 3, count = 0, asf = "pep"**
- Base case reached (pos == str.length())
- Output: "pep"

Output:-

pep
pe1
p1p
p2
lep
le1
2p
3

All palindromic partition in C++

```
#include <iostream>
#include <string>
using namespace std;

class AllPalindromicPartition {
public:
    static void main() {
        string str = "abba";
        sol(str, "");
    }

    static void sol(string str, string asf) {
        if (str.length() == 0) {
            cout << asf << endl;
            return;
        }

        for (int i = 0; i < str.length(); i++) {
            string prefix = str.substr(0, i + 1);
            string ros = str.substr(i + 1);
            if (isPalin(prefix)) {
                sol(ros, asf + "(" + prefix + ")");
            }
        }
    }

    static bool isPalin(string s) {
        int li = 0;
        int ri = s.length() - 1;
        while (li < ri) {
            if (s[li] != s[ri]) {
                return false;
            }
            li++;
            ri--;
        }
        return true;
    }
};

int main() {
    AllPalindromicPartition::main();
    return 0;
}
```

Dry Run for Input: "abba"

1st Level of Recursion:

- prefix = "a", ros = "bba", and "a" is a palindrome.
- Call sol("bba", "(a)").

2nd Level of Recursion:

- prefix = "b", ros = "ba", and "b" is a palindrome.
- Call sol("ba", "(a)(b)").

3rd Level of Recursion:

- prefix = "b", ros = "a", and "b" is a palindrome.
- Call sol("a", "(a)(b)(b)").

4th Level of Recursion:

- prefix = "a", ros = "", and "a" is a palindrome.
- Output (a)(b)(b)(a).

Backtracking to Explore Other Partitions:

3rd Level (Exploring Longer Prefixes):

- prefix = "bb", ros = "a", and "bb" is a palindrome.
- Call sol("a", "(a)(bb)").

4th Level:

- prefix = "a", ros = "", and "a" is a palindrome.
- Output (a)(bb)(a).

Backtracking to 2nd Level:

- prefix = "bba" is not a palindrome. Skip.

Backtracking to 1st Level:

- prefix = "ab" and prefix = "abb" are not palindromes.
- prefix = "abba", ros = "", and "abba" is a palindrome.

	<ul style="list-style-type: none">• Output (abba).
<p>Output:-</p> <p>(a)(b)(b)(a)</p> <p>(a)(bb)(a)</p> <p>(abba)</p>	

Combinations in C++	
<pre> #include <iostream> using namespace std; void combinations(int cb, int nboxes, int ssf, int ritems, string asf) { if (cb > nboxes) { if (ssf == ritems) { cout << asf << endl; } return; } combinations(cb + 1, nboxes, ssf + 1, ritems, asf + "i"); combinations(cb + 1, nboxes, ssf, ritems, asf + "-"); } int main() { int nboxes = 3; int ritems = 2; combinations(1, nboxes, 0, ritems, ""); return 0; } </pre>	<p>Dry Run for nboxes = 3 and ritems = 2</p> <p>Initial call: combinations(1, 3, 0, 2, "")</p> <p>Recursive Tree:</p> <ol style="list-style-type: none"> Box 1: Place "i" → combinations(2, 3, 1, 2, "i") <ul style="list-style-type: none"> Box 2: Place "i" → combinations(3, 3, 2, 2, "ii") <ul style="list-style-type: none"> Box 3: Leave "-" → Print: ii- Box 2: Leave "-" → combinations(3, 3, 1, 2, "i-") <ul style="list-style-type: none"> Box 3: Place "i" → Print: i-i Box 1: Leave "-" → combinations(2, 3, 0, 2, "-") <ul style="list-style-type: none"> Box 2: Place "i" → combinations(3, 3, 1, 2, "-i") <ul style="list-style-type: none"> Box 3: Place "i" → Print: -ii Box 2: Leave "-" → combinations(3, 3, 0, 2, "--") <ul style="list-style-type: none"> Box 3: Place "i" → Not valid (ssf = 1)
<p>Output:-</p> <p>ii- i-i -ii</p>	

Friend's pairing in C++

```
#include <iostream>
#include <vector>
using namespace std;

int counter = 1;

void solution(int i, int n, vector<bool>& used, string asf) {
    if (i > n) {
        cout << counter << "." << asf << endl;
        counter++;
        return;
    }

    if (used[i]) {
        solution(i + 1, n, used, asf);
    } else {
        used[i] = true;
        solution(i + 1, n, used, asf + "(" + to_string(i) + ")");
        for (int j = i + 1; j <= n; j++) {
            if (!used[j]) {
                used[j] = true;
                solution(i + 1, n, used, asf + "(" + to_string(i) + "," + to_string(j) + ")");
                used[j] = false;
            }
        }
        used[i] = false;
    }
}

int main() {
    int n = 3;
    vector<bool> used(n + 1, false);
    solution(1, n, used, "");
    return 0;
}
```

Dry Run

Input: n = 3

Function Call: solution(1, 3, used = {false, false, false, false}, "")

1. i=1 (not used) → Mark 1 used → Call solution(2, 3, used={false, true, false, false}, "(1) ")
 - i=2 (not used) → Mark 2 used → Call solution(3, 3, used={false, true, true, false}, "(1) (2) ")
 - i=3 (not used) → Mark 3 used → Call solution(4, 3, used={false, true, true, true}, "(1) (2) (3) ")
 - Base case: Print 1.(1) (2) (3)
 - Backtrack: Unmark 3.
 - Backtrack: Unmark 2.
 - i=2 → Pair 2,3 → Mark 2,3 used → Call solution(4, 3, used={false, true, true, true}, "(1) (2,3) ")
 - Base case: Print 2.(1) (2,3)
 - Backtrack: Unmark 2,3.
- Backtrack: Unmark 1.
2. i=1 → Pair 1,2 → Mark 1,2 used → Call solution(3, 3, used={false, true, true, false}, "(1,2) ")
 - i=3 (not used) → Mark 3 used → Call solution(4, 3, used={false, true, true, true}, "(1,2) (3) ")
 - Base case: Print 3.(1,2) (3)
 - Backtrack: Unmark 3.
- Backtrack: Unmark 1,2.
3. i=1 → Pair 1,3 → Mark 1,3 used → Call solution(3, 3, used={false, true, false, true}, "(1,3) ")
 - i=2 (not used) → Mark 2 used → Call solution(4, 3, used={false, true, true, true}, "(1,3) (2) ")
 - Base case: Print 4.(1,3) (2)
 - Backtrack: Unmark 2.
- Backtrack: Unmark 1,3.

Output:-

```
1.(1) (2) (3)
2.(1) (2,3)
3.(1,2) (3)
4.(1,3) (2)
```

Goldmine2 in C++

```
#include <iostream>
#include <vector>
using namespace std;

int maxGold = 0;

void travel(vector<vector<int>>& arr, int i, int j,
vector<vector<bool>>& visited, vector<int>& bag) {
    if (i < 0 || j < 0 || i >= arr.size() || j >=
arr[0].size() || arr[i][j] == 0 || visited[i][j]) {
        return;
    }
    visited[i][j] = true;
    bag.push_back(arr[i][j]);
    travel(arr, i - 1, j, visited, bag);
    travel(arr, i, j + 1, visited, bag);
    travel(arr, i, j - 1, visited, bag);
    travel(arr, i + 1, j, visited, bag);
}

void getMaxGold(vector<vector<int>>& arr) {
    int rows = arr.size();
    int cols = arr[0].size();
    vector<vector<bool>> visited(rows,
vector<bool>(cols, false));

    for (int i = 0; i < rows; i++) {
        for (int j = 0; j < cols; j++) {
            if (arr[i][j] != 0 && !visited[i][j]) {
                vector<int> bag;
                travel(arr, i, j, visited, bag);

                int sum = 0;
                for (int val : bag) {
                    sum += val;
                }
                if (sum > maxGold) {
                    maxGold = sum;
                }
            }
        }
    }
}

int main() {
    vector<vector<int>> arr = {
        {0, 1, 4, 2, 8, 2},
        {4, 3, 6, 5, 0, 4},
        {1, 2, 4, 1, 4, 6},
        {2, 0, 7, 3, 2, 2},
        {3, 1, 5, 9, 2, 4},
        {2, 7, 0, 8, 5, 1}
    };

    getMaxGold(arr);
    cout << maxGold << endl;

    return 0;
}
```

Step-by-Step Execution

Initial Setup:

- maxGold = 0
- visited initialized to false for all cells.
- Rows = 6, Cols = 6.

Outer Loop Iteration (i = 0, j = 0):

- Cell (0,0) is 0, skip it.

(i = 0, j = 1):

- Cell (0,1) is 1, not visited.
- Start travel function:
 - bag = [1]
 - Mark (0,1) as visited.
 - Explore neighboring cells:
 - (0,2): Add 4 to bag → bag = [1,4].
 - (1,2): Add 6 to bag → bag = [1,4,6].
 - Continue visiting valid cells → bag = [1,4,6,5,3,4,2].
 - Total sum of bag = 25.
- Update maxGold = 25.

(i = 0, j = 2, j = 3, ..., j = 5):

- All these cells are either visited or part of the same cluster.

Outer Loop Iteration (i = 1):

(i = 1, j = 0):

- Cell (1,0) is 4, not visited.
- Start travel function:
 - bag = [4]
 - Visit neighboring cells:
 - (2,0): Add 1 → bag = [4,1].
 - Continue visiting → bag = [4,1,2,3,7,9,5].
 - Total sum of bag = 31.
- Update maxGold = 31.

(i = 1, j = 1, ..., j = 5):

	<ul style="list-style-type: none"> • All cells are either visited or part of the same cluster. <p>Outer Loop Iteration (i = 2 to i = 5):</p> <p>Continue similar logic for unvisited cells and new clusters.</p> <p>Cluster at (4,3) and (5,3):</p> <ul style="list-style-type: none"> • Explore the large gold cluster: <ul style="list-style-type: none"> ◦ bag = [9,5,8,7,2]. ◦ Total sum = 120. • Update maxGold = 120. <p>Final Output:</p> <ul style="list-style-type: none"> • Maximum Gold Collected: 120
Output:- 120	

Josephus in C++

```
#include <iostream>
using namespace std;

int solution(int n, int k) {
    if (n == 1) {
        return 0;
    }
    int x = solution(n - 1, k);
    int y = (x + k) % n;
    return y;
}

int main() {
    int n = 4;
    int k = 2;
    cout << solution(n, k) << endl;
    return 0;
}
```

Step-by-Step Execution:

The function uses recursion to solve the Josephus problem. The base case is when $n = 1$, where the last remaining person is at position 0. The recursive case computes the position of the last person standing for $n-1$ people and then adjusts it by the step k using modulo operation.

1. **Initial Call:** solution(4, 2)
 - **n = 4, k = 2**
 - Call solution(3, 2) (since $n - 1 = 3$)
2. **Second Call:** solution(3, 2)
 - **n = 3, k = 2**
 - Call solution(2, 2) (since $n - 1 = 2$)
3. **Third Call:** solution(2, 2)
 - **n = 2, k = 2**
 - Call solution(1, 2) (since $n - 1 = 1$)
4. **Base Case:** solution(1, 2)
 - **n = 1, k = 2** (base case)
 - Return 0 (last remaining person at position 0)
5. **Returning from Third Call:** solution(2, 2)
 - Result from solution(1, 2) is 0
 - Calculate $y = (0 + 2) \% 2 = 0$
 - Return $y = 0$
6. **Returning from Second Call:** solution(3, 2)
 - Result from solution(2, 2) is 0
 - Calculate $y = (0 + 2) \% 3 = 2$
 - Return $y = 2$
7. **Returning from First Call:** solution(4, 2)
 - Result from solution(3, 2) is 2
 - Calculate $y = (2 + 2) \% 4 = 0$
 - Return $y = 0$

	<p>Final Output:</p> <p>The position of the last remaining person (zero-indexed) is 0, so the output is 0.</p>
<p>Output:- 0</p>	

Largest after k swaps in C++

```
#include <iostream>
using namespace std;

string max_str;

void findMaximum(string str, int k) {
    // Base case: When k swaps are used up
    if (k == 0) {
        return;
    }

    int n = str.length();

    // Find the maximum digit available for current
    position
    for (int i = 0; i < n - 1; i++) {
        for (int j = i + 1; j < n; j++) {
            // If digit at position j is greater than digit at
            position i, swap them
            if (str[j] > str[i]) {
                swap(str[i], str[j]);

                // Check if current string is larger than
                previously found max
                if (str > max_str) {
                    max_str = str;
                }

                // Recur for k-1 swaps on the modified string
                findMaximum(str, k - 1);

                // Backtrack: Swap again to revert to
                original string
                swap(str[i], str[j]);
            }
        }
    }
}

int main() {
    string str = "1234567";
    int k = 4;

    // Initialize max_str with the original string
    max_str = str;

    // Find the maximum number possible after k
    swaps
    findMaximum(str, k);

    // Print the maximum number found
    cout << max_str << endl;

    return 0;
}
```

Dry Run of the Code

Input:

- str = "1234567"
- k = 4

Step-by-Step Execution

Initialization

- max_str = "1234567"

First Level (k = 4)

- Outer loop: i = 0
 - Inner loop: j = 1
 - Swap: "2134567"
 - max_str = "2134567"
 - Recur with k = 3.

Second Level (k = 3)

- Outer loop: i = 0
 - Inner loop: j = 1
 - No swap (digits are the same).
 - Inner loop: j = 2
 - Swap: "3124567"
 - max_str = "3124567"
 - Recur with k = 2.

Third Level (k = 2)

- Outer loop: i = 0
 - Inner loop: j = 1, j = 2: No change (smaller results).
 - Inner loop: j = 3
 - Swap: "4123567"
 - max_str = "4123567"
 - Recur with k = 1.

Fourth Level (k = 1)

- Outer loop: $i = 0$
 - Inner loop: $j = 4$
 - Swap: "5123467"
 - `max_str = "5123467"`
 - Recur with $k = 0$.

Base Case ($k = 0$)

- Stop recursion and backtrack.

Backtracking

- Undo each swap and check other combinations.
- Repeat similar logic for other positions ($i = 1, 2, \dots$).

Final `max_str`

The largest number found after 4 swaps is:
7654321

Output:-
7654321

Lexicographic order in C++

```
#include <iostream>
using namespace std;

void dfs(int i, int n) {
    if (i > n) {
        return;
    }
    cout << i << endl;
    for (int j = 0; j < 10; j++) {
        dfs(10 * i + j, n);
    }
}

int main() {
    int n = 40;
    for (int i = 1; i <= 9; i++) {
        dfs(i, n);
    }
    return 0;
}
```

Initial Setup:

We begin by calling dfs(i, 20) for i = 1 to i = 9.

Dry Run (for n = 20):

1. Calling dfs(1, 20):

- The function prints 1.
- Then it recursively calls dfs(10, 20), dfs(11, 20), ..., dfs(19, 20).

Step by step:

- dfs(1, 20):
 - Prints 1.
 - Calls dfs(10, 20):
 - Prints 10.
 - Calls dfs(100, 20), but 100 > 20, so this call ends.
 - Calls dfs(11, 20):
 - Prints 11.
 - Calls dfs(110, 20), but 110 > 20, so this call ends.
 - Calls dfs(12, 20):
 - Prints 12.
 - Calls dfs(120, 20), but 120 > 20, so this call ends.
 - Calls dfs(13, 20):
 - Prints 13.
 - Calls dfs(130, 20), but 130 > 20, so this call ends.
 - Calls dfs(14, 20):
 - Prints 14.
 - Calls dfs(140, 20), but 140 > 20, so this call ends.
 - Calls dfs(15, 20):
 - Prints 15.
 - Calls dfs(150, 20), but 150 > 20, so this call ends.
 - Calls dfs(16, 20):
 - Prints 16.
 - Calls dfs(160, 20), but 160 > 20, so this call ends.
 - Calls dfs(17, 20):
 - Prints 17.
 - Calls dfs(170, 20), but 170 > 20, so this call ends.
 - Calls dfs(18, 20):
 - Prints 18.
 - Calls dfs(180, 20), but 180 > 20, so this call ends.
 - Calls dfs(19, 20):
 - Prints 19.
 - Calls dfs(190, 20), but 190 > 20, so this call ends.

2. Calling dfs(2, 20):

	<ul style="list-style-type: none">• The function prints 2.• Then it recursively calls dfs(20, 20). <p>Step by step:</p> <ul style="list-style-type: none">• dfs(2, 20):<ul style="list-style-type: none">○ Prints 2.○ Calls dfs(20, 20):<ul style="list-style-type: none">▪ Prints 20.▪ Calls dfs(200, 20), but 200 > 20, so this call ends. <p>At this point, the function has printed the number starting with 2:</p>
<p>Output:-</p> <p>1 10 11 12 13 14 15 16 17 18 19 2 20 3 4 5 6 7 8 9</p>	

Partition in K subsets in C++

```
#include <iostream>
#include <vector>

using namespace std;

int counter = 0;

void solution(int i, int n, int k, int nos,
vector<vector<int>>& ans) {
    if (i > n) {
        if (nos == k) {
            counter++;
            cout << counter << ". ";
            for (auto& set : ans) {
                cout << "[";
                for (auto num : set) {
                    cout << num << " ";
                }
                cout << "]" << " ";
            }
            cout << endl;
        }
        return;
    }

    for (int j = 0; j < ans.size(); j++) {
        if (!ans[j].empty()) {
            ans[j].push_back(i);
            solution(i + 1, n, k, nos, ans);
            ans[j].pop_back();
        } else {
            ans[j].push_back(i);
            solution(i + 1, n, k, nos + 1, ans);
            ans[j].pop_back();
            break;
        }
    }
}

int main() {
    int n = 4;
    int k = 3;
    vector<vector<int>> ans(k);

    solution(1, n, k, 0, ans);

    return 0;
}
```

Step-by-step Execution:

1. $i = 1$:
 - Try placing 1 in the first subset:
 - Add 1 to $ans[0] \rightarrow ans = [[1], [], []]$.
 - Recursively call $solution(2, 4, 3, 1, ans)$.
2. $i = 2$:
 - Try placing 2 in the first subset:
 - Add 2 to $ans[0] \rightarrow ans = [[1, 2], [], []]$.
 - Recursively call $solution(3, 4, 3, 1, ans)$.
 - Try placing 2 in the second subset:
 - Add 2 to $ans[1] \rightarrow ans = [[1], [2], []]$.
 - Recursively call $solution(3, 4, 3, 2, ans)$.
3. $i = 3$:
 - For the current state of ans :
 - For $ans[0] = [1, 2]$:
 - Try placing 3 in the first subset $\rightarrow ans = [[1, 2, 3], [], []]$.
 - Recursively call $solution(4, 4, 3, 1, ans)$.
 - For $ans[1] = [2]$:
 - Try placing 3 in $ans[1] \rightarrow ans = [[1], [2, 3], []]$.
 - Recursively call $solution(4, 4, 3, 2, ans)$.
4. $i = 4$:
 - Now, the subsets are filled with $i = 1, 2, 3$ elements.
 - After backtracking, we update the subsets and print the results when $nos == k$.

Final Outputs (Valid Partitions):

1. First partition:
 - $ans = [[1, 2], [3], [4]]$
 - Output: 1. [1 2] [3] [4]
2. Second partition:

	<ul style="list-style-type: none"> ○ ans = [[1, 3], [2], [4]] ○ Output: 2. [1 3] [2] [4] <p>3. Third partition:</p> <ul style="list-style-type: none"> ○ ans = [[1], [2, 3], [4]] ○ Output: 3. [1] [2 3] [4] <p>4. Fourth partition:</p> <ul style="list-style-type: none"> ○ ans = [[1, 4], [2], [3]] ○ Output: 4. [1 4] [2] [3] <p>5. Fifth partition:</p> <ul style="list-style-type: none"> ○ ans = [[1], [2, 4], [3]] ○ Output: 5. [1] [2 4] [3] <p>6. Sixth partition:</p> <ul style="list-style-type: none"> ○ ans = [[1], [2], [3, 4]] ○ Output: 6. [1] [2] [3 4]
<p>Output:-</p> <ol style="list-style-type: none"> 1. [1 2] [3] [4] 2. [1 3] [2] [4] 3. [1] [2 3] [4] 4. [1 4] [2] [3] 5. [1] [2 4] [3] 6. [1] [2] [3 4] 	

Permutation in C++

```
#include <iostream>
using namespace std;

void permutations(int cb, int nboxes, int items[], int
ssf, int ritems, string asf) {
    if (cb > nboxes) {
        if (ssf == ritems) {
            cout << asf << endl;
        }
        return;
    }

    for (int i = 0; i < ritems; i++) {
        if (items[i] == 0) {
            items[i] = 1;
            permutations(cb + 1, nboxes, items, ssf + 1,
ritems, asf + to_string(i + 1));
            items[i] = 0;
        }
    }

    permutations(cb + 1, nboxes, items, ssf, ritems, asf
+ "0");
}

int main() {
    int nboxes = 3;
    int ritems = 2;
    int cb = 1;
    int ssf = 0;
    int items[ritems] = {0}; // Initialize items array with
0s

    permutations(cb, nboxes, items, ssf, ritems, "");

    return 0;
}
```

Step-by-step Execution:

1. **cb = 1:** We are at the first box. We try all possible items (1 and 2) in the first box.
 - **Item 1:**
 - items[0] = 0, we mark it as used (items[0] = 1).
 - Recursively call permutations(2, 3, [1, 0], 1, 2, "1").
2. **cb = 2:** We are now at the second box. We check all possible items (1 and 2).
 - **Item 1:** (items[0] = 1, already used, so skip).
 - **Item 2:**
 - items[1] = 0, we mark it as used (items[1] = 1).
 - Recursively call permutations(3, 3, [1, 1], 2, 2, "12").
3. **cb = 3:** We are at the third box. We try all possible options:
 - **Item 1 and Item 2:** Both are already used.
 - Add 0 to indicate the third box remains empty.
 - Recursively call permutations(4, 3, [1, 1], 2, 2, "120").
4. **Base case:** cb = 4, output 120.

Result:

- We print 120 as a valid permutation.
5. **Backtrack:** Unmark the second item (items[1] = 0), and proceed to the next option in cb = 2.
 - **Item 2:**
 - items[1] = 0, mark it as used (items[1] = 1).
 - Recursively call permutations(3, 3, [1, 1], 2, 2, "20").
 6. **Base case:** cb = 4, output 120.

Output:-

120

Permutation of string in C++

```
#include <iostream>
#include <unordered_map>
using namespace std;

void generate(int cs, int ts, unordered_map<char,
int>& fmap, string asf) {
    if (cs > ts) {
        cout << asf << endl;
        return;
    }

    for (auto entry : fmap) {
        char ch = entry.first;
        int count = entry.second;

        if (count > 0) {
            fmap[ch]--;
            generate(cs + 1, ts, fmap, asf + ch);
            fmap[ch]++;
        }
    }
}

int main() {
    string str = "abc";
    unordered_map<char, int> fmap;

    for (char ch : str) {
        fmap[ch]++;
    }

    generate(1, str.length(), fmap, "");

    return 0;
}
```

Initial Setup:

1. We create an unordered map fmap to store the frequency of each character in the string.
 - fmap = {'a': 1, 'b': 1, 'c': 1}.
2. Call generate(1, 3, fmap, "") to start generating the permutations.

Step-by-Step Execution:

1. **First Call: generate(1, 3, {'a': 1, 'b': 1, 'c': 1}, "")**
 - **cs = 1, ts = 3** (we want a total of 3 characters in the permutation).
 - We iterate over the characters in fmap. Starting with 'a':
 - **Character 'a':**
 - Count > 0: Use 'a', decrease count in fmap to {'a': 0, 'b': 1, 'c': 1}.
 - Recursively call generate(2, 3, {'a': 0, 'b': 1, 'c': 1}, "a").
2. **Second Call: generate(2, 3, {'a': 0, 'b': 1, 'c': 1}, "a")**
 - **cs = 2, ts = 3.**
 - Iterate again, start with 'a' but it's count 0, so skip it.
 - Move to **character 'b':**
 - **Character 'b':**
 - Count > 0: Use 'b', decrease count in fmap to {'a': 0, 'b': 0, 'c': 1}.
 - Recursively call generate(3, 3, {'a': 0, 'b': 0, 'c': 1}, "ab").
3. **Third Call: generate(3, 3, {'a': 0, 'b': 0, 'c': 1}, "ab")**
 - **cs = 3, ts = 3.**
 - Iterate again, starting with 'a' and 'b', both of which have counts 0, so skip them.
 - Move to **character 'c':**
 - **Character 'c':**
 - Count > 0: Use 'c', decrease count in fmap to {'a': 0, 'b': 0, 'c': 0}.
 - Recursively call generate(4, 3, {'a': 0, 'b': 0, 'c': 0}, "abc").
4. **Base Case: generate(4, 3, {'a': 0, 'b': 0, 'c': 0}, "abc")**
 - **cs = 4, ts = 3:** We've reached the required length of 3 characters.

	<ul style="list-style-type: none"> ○ Output the permutation: "abc". <p>5. Backtrack:</p> <ul style="list-style-type: none"> ○ Return to the previous state where fmap = {'a': 0, 'b': 1, 'c': 1} and asf = "a". ○ Restore the count of 'c' and continue the loop. <p>Second Iteration of First Call:</p> <p>1. Second Character 'b' in First Call:</p> <ul style="list-style-type: none"> ○ Character 'b': <ul style="list-style-type: none"> ▪ Count > 0: Use 'b', decrease count in fmap to {'a': 1, 'b': 0, 'c': 1}. ▪ Recursively call generate(2, 3, {'a': 1, 'b': 0, 'c': 1}, "b"). <p>2. Second Call: generate(2, 3, {'a': 1, 'b': 0, 'c': 1}, "b")</p> <ul style="list-style-type: none"> ○ cs = 2, ts = 3. ○ Skip 'b' (count 0) and move to 'a': <ul style="list-style-type: none"> ▪ Character 'a': <ul style="list-style-type: none"> ▪ Count > 0: Use 'a', decrease count in fmap to {'a': 0, 'b': 0, 'c': 1}. ▪ Recursively call generate(3, 3, {'a': 0, 'b': 0, 'c': 1}, "ba"). <p>3. Third Call: generate(3, 3, {'a': 0, 'b': 0, 'c': 1}, "ba")</p> <ul style="list-style-type: none"> ○ cs = 3, ts = 3. ○ Skip 'a' and 'b', move to 'c': <ul style="list-style-type: none"> ▪ Character 'c': <ul style="list-style-type: none"> ▪ Count > 0: Use 'c', decrease count in fmap to {'a': 0, 'b': 0, 'c': 0}. ▪ Recursively call generate(4, 3, {'a': 0, 'b': 0, 'c': 0}, "bac"). <p>4. Base Case: generate(4, 3, {'a': 0, 'b': 0, 'c': 0}, "bac")</p> <ul style="list-style-type: none"> ○ Output the permutation: "bac".
<p>Output:-</p> <pre> cba cab bca bac acb abc </pre>	

Remove Invalid Parenthesis in C++

```
#include <iostream>
#include <string>
#include <unordered_set>
#include <stack>
using namespace std;

void solution(string str, int mra,
unordered_set<string>& ans);
int getMin(string str);

void solution(string str, int mra,
unordered_set<string>& ans) {
    if (mra == 0) {
        int mrnow = getMin(str);
        if (mrnow == 0) {
            if (ans.find(str) == ans.end()) {
                cout << str << endl;
                ans.insert(str);
            }
        }
        return;
    }
    for (int i = 0; i < str.length(); i++) {
        string left = str.substr(0, i);
        string right = str.substr(i + 1);
        solution(left + right, mra - 1, ans);
    }
}

int getMin(string str) {
    stack<char> st;
    for (int i = 0; i < str.length(); i++) {
        char ch = str[i];
        if (ch == '(') {
            st.push(ch);
        } else if (ch == ')') {
            if (st.empty()) {
                st.push(ch);
            } else if (st.top() == ')') {
                st.push(ch);
            } else if (st.top() == '(') {
                st.pop();
            }
        }
    }
    return st.size();
}

int main() {
    string str = "(((())";
    unordered_set<string> ans;
    int mra = getMin(str);
    solution(str, mra, ans);
    return 0;
}
```

Step-by-Step Dry Run:

Step 1: Calculate mra using getMin(str)

The string is "(((())", and we need to calculate how many parentheses need to be removed to balance the string.

- **Initial String:** "(((())"
- Using a stack, we process the string:
 - Encountering an opening parenthesis (: Push onto the stack.
 - Encountering a closing parenthesis): Pop an opening parenthesis from the stack (if one exists).
 - After processing the entire string, we find that 2 opening parentheses (do not have corresponding closing parentheses).
- **Result of getMin("(((())"):** The minimum number of removals (mra) is **2** because we need to remove 2 redundant opening parentheses (.

Step 2: Recursive Function solution(str, mra, ans)

We now start generating possible valid strings by removing parentheses one by one, up to a total of mra = 2 removals.

- **First Call: solution("(((())", 2, ans):**
 - The string has 2 removable parentheses, so we explore all possible ways of removing parentheses.

Recursive Steps:

1. **Remove Parenthesis at index 0 (First 0):**
 - String becomes: "(((())"
 - Call solution("(((())", 1, ans).
2. **Remove Parenthesis at index 0 again (First (in "(((())"):**
 - String becomes: "((())"
 - Call solution("((())", 0, ans).
3. **Base Case: solution("((())", 0, ans):**
 - We check if the string "((())" is balanced using getMin("((())").
 - The result is 0, meaning the string is balanced.
 - Since it is valid and not already in ans, we print it and add it to ans.

Valid String Output: ((()))

4. **Backtrack to Step 2 and explore other removals:**

	<ul style="list-style-type: none"> ○ We explore other combinations, but in this particular case, only the string "((()))" is valid after removing 2 parentheses. ○ All other combinations generated during recursion either involve invalid strings or are duplicates. <p>Final Output:</p> <p>After backtracking through all combinations, the only valid string left is:</p> <p>((()))</p>
<p>Output:-</p> <p>((()))</p>	

Subsequence in C++

```
#include <iostream>
#include <string>

using namespace std;

void sol(string q, string a) {
    if (q.length() == 0) {
        cout << a << "-" << endl;
        return;
    }

    char ch = q[0];
    string rest = q.substr(1);
    sol(rest, a);
    sol(rest, a + ch);
}

int main() {
    string s = "abc";
    sol(s, "");

    return 0;
}
```

Initial Setup:

- Call `sol("abc", "")` to generate all subsequences of the string.

Step-by-Step Execution:

1. **First Call: `sol("abc", "")`**
 - **`q = "abc", a = ""`.**
 - Take the first character 'a' from the string and split it into:
 - **`ch = 'a', rest = "bc"`.**
 - **Recursively call `sol("bc", "")`** to handle the case where 'a' is **not** included.
 - **Recursively call `sol("bc", "a")`** to handle the case where 'a' is **included**.
2. **Second Call: `sol("bc", "")`**
 - **`q = "bc", a = ""`.**
 - Take the first character 'b' from the string and split it into:
 - **`ch = 'b', rest = "c"`.**
 - **Recursively call `sol("c", "")`** to handle the case where 'b' is **not** included.
 - **Recursively call `sol("c", "b")`** to handle the case where 'b' is **included**.
3. **Third Call: `sol("c", "")`**
 - **`q = "c", a = ""`.**
 - Take the first character 'c' from the string and split it into:
 - **`ch = 'c', rest = ""`.**
 - **Recursively call `sol("", "")`** to handle the case where 'c' is **not** included.
 - **Recursively call `sol("", "c")`** to handle the case where 'c' is **included**.
4. **Base Case: `sol("", "")`**
 - **`q is empty`, print the current subsequence: `"-"`.**
5. **Base Case: `sol("", "c")`**
 - **`q is empty`, print the current subsequence: `"c-"`.**
6. **Return to Third Call: `sol("c", "b")`**
 - **Recursively call `sol("", "bc")`** to handle the case where 'c' is **included**.

7. **Base Case: sol("", "bc")**

- **q is empty**, print the current subsequence: "bc-".

8. **Return to Second Call: sol("bc", "")**

- Now handle the case where 'b' is **included**:
 - **sol("c", "b")** has been handled, now process the second part.

Continuation for the First Character 'a':

1. **Second Part: sol("bc", "a")**

- **q = "bc", a = "a"**.
- Take the first character 'b' from the string and split it into:
 - **ch = 'b', rest = "c"**.
- **Recursively call** sol("c", "a") to handle the case where 'b' is **not** included.
- **Recursively call** sol("c", "ab") to handle the case where 'b' is **included**.

2. **Third Call: sol("c", "a")**

- **q = "c", a = "a"**.
- Take the first character 'c' from the string and split it into:
 - **ch = 'c', rest = ""**.
- **Recursively call** sol("", "a") to handle the case where 'c' is **not** included.
- **Recursively call** sol("", "ac") to handle the case where 'c' is **included**.

3. **Base Case: sol("", "a")**

- **q is empty**, print the current subsequence: "a-".

4. **Base Case: sol("", "ac")**

- **q is empty**, print the current subsequence: "ac-".

Final Part of the Execution:

1. **Return to Second Call: sol("c", "ab")**

- **Recursively call** sol("", "abc") to handle the case where 'c' is **included**.

2. **Base Case: sol("", "abc")**

- **q is empty**, print the current

	subsequence: "abc-".
Output:- - c- b- bc- a- ac- ab- abc-	

Word Break in C++

```
#include <iostream>
#include <unordered_set>
#include <string>

using namespace std;

void wordBreak(string str, string ans,
unordered_set<string>& dict) {
    if (str.length() == 0) {
        cout << ans << endl;
        return;
    }

    for (int i = 0; i < str.length(); i++) {
        string left = str.substr(0, i + 1);
        if (dict.find(left) != dict.end()) {
            string right = str.substr(i + 1);
            wordBreak(right, ans + left + " ", dict);
        }
    }
}

int main() {
    int n = 5;
    unordered_set<string> dict = {"microsoft", "hiring",
    "at", "kolkata"};
    string sentence = "microsoft hiring";

    wordBreak(sentence, "", dict);

    return 0;
}
```

Step-by-Step Execution:

1. **First Call:** wordBreak("microsoft hiring", "", dict)
 - **Current string:** "microsoft hiring"
 - **Dictionary:** {"microsoft", "hiring", "at", "kolkata"}
 - **Answer so far:** ""
 - Loop through the string, checking for each substring that is present in the dictionary:
 - **i = 0:** Substring "m" is not in the dictionary.
 - **i = 1:** Substring "mi" is not in the dictionary.
 - **i = 2:** Substring "mic" is not in the dictionary.
 - **i = 3:** Substring "micro" is not in the dictionary.
 - **i = 4:** Substring "micr" is not in the dictionary.
 - **i = 5:** Substring "micro" is not in the dictionary.
 - **i = 6:** Substring "microsoft" **is** in the dictionary.
 - Now the string becomes "hiring", and the answer so far is "microsoft ".
 - **Recursively call:** wordBreak("hiring", "microsoft ", dict)

2. **Second Call:** wordBreak("hiring", "microsoft ", dict)
 - **Current string:** "hiring"
 - **Dictionary:** {"microsoft", "hiring", "at", "kolkata"}
 - **Answer so far:** "microsoft "
 - Loop through the string "hiring", checking for each substring:
 - **i = 0:** Substring "h" is not in the dictionary.
 - **i = 1:** Substring "hi" is not in the dictionary.
 - **i = 2:** Substring "hir" is not in the dictionary.
 - **i = 3:** Substring "hiri" is not in the dictionary.
 - **i = 4:** Substring "hiring" **is** in the dictionary.
 - Now the string becomes "" (empty), and the answer so far is "microsoft hiring ".
 - **Recursively call:** wordBreak("", "microsoft hiring ", dict)

	<p>3. Base Case: wordBreak("", "microsoft hiring ", dict)</p> <ul style="list-style-type: none">○ Current string: ""○ Answer so far: "microsoft hiring "○ Since the string is empty, print the answer: "microsoft hiring"
<p>Output:-</p> <p>microsoft hiring</p>	