

Gradient Domain Manipulation Techniques in Vision and Graphics

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Course WebPage :
<http://www.cfar.umd.edu/~aagrwal/ICCV2007Course/>



Course: Gradient Domain Techniques

Course Web Page

Google “ICCV 2007 gradient course”

Welcome

- Understanding Gradient Fields
 - Integrability, Curl, Divergence
- Manipulating Gradient Fields
 - Image editing, Stitching, HDR compression, Mosaics, Shadow Removal, Intrinsic Images
- Reconstruction Tools
 - Direct Solvers, Multigrid, Preconditioning, Hierarchical Basis
 - Feature Preserving Reconstructions
- Advanced Topics
 - Gradient camera, Video editing, Mesh editing, Large neighborhood differences

Goals

- Review of 20+ recent/classical papers
- Understanding gradient domain processing
 - Estimation & Manipulation of gradients
 - Reconstruction from gradients
 - Algorithmic & Numerical aspects
 - Learn vision and graphics techniques for image/video editing, computational photography
- What we will not cover
 - Traditional image processing/editing
 - Non-gradient domain methods for applications such as Shape from Shading/Photometric Stereo

Speaker: Amit Agrawal

Amit Agrawal is a Visiting Research Scientist at MERL.

His research interests include computational photography, novel sensing and computer vision. During his doctoral studies at Univ. of Maryland, he investigated gradient domain methods for scene analysis. He has published several articles on imaging and photography including coded exposure & coded aperture photography and gradient-domain imaging. His papers have appeared in several vision and graphics conferences including SIGGRAPH, CVPR, ICCV and ECCV. He is a member of IEEE and ACM.



<http://www.merl.com/people/agrawal/index.html>

Speaker: Ramesh Raskar

Ramesh Raskar is a Senior Research Scientist at MERL.

His research interests include projector-based graphics, computational photography and non-photorealistic rendering. He has published several articles on imaging and photography including multi-flash photography for depth edge detection, image fusion, gradient-domain imaging and projector-camera systems. His papers have appeared in SIGGRAPH, EuroGraphics, IEEE Visualization, CVPR and many other graphics and vision conferences. He was a course organizer at Siggraph 2002, 2003 and 2004. He is a panel organizer at the Symposium on Computational Photography and Video in Cambridge, MA in May 2005. He is a member of the ACM and IEEE.



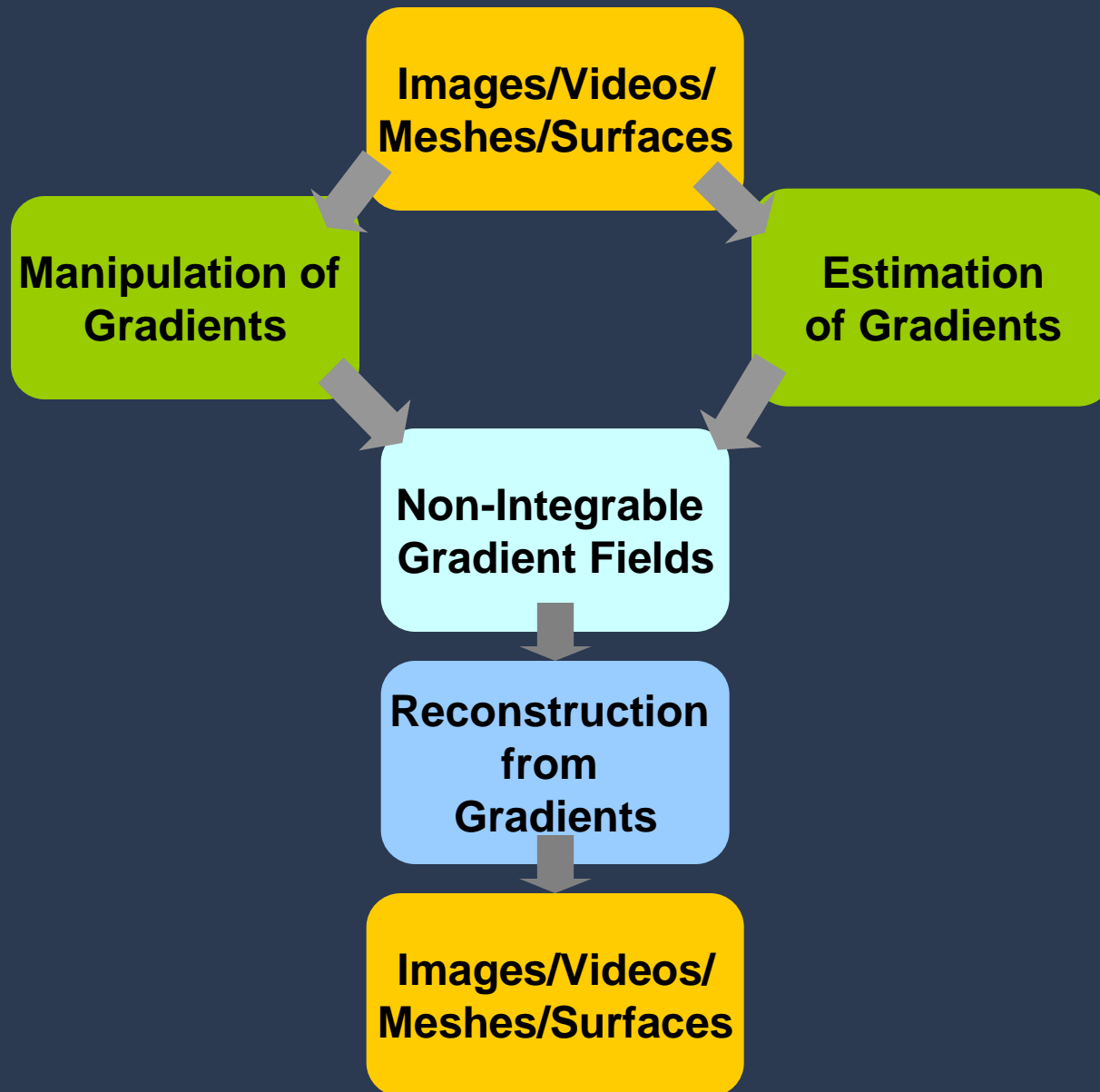
<http://www.merl.com/people/raskar/raskar.html>

Schedule

Introduction	(30 min, Agrawal)
Gradient Domain Manipulations	(1 hr, Raskar)
Break	(15 min)
Reconstruction Techniques	(1 hr, Agrawal)
Advanced Topics	(30 min, Raskar)
Discussion	

Course WebPage : [Google "ICCV 2007 gradient course"](#)

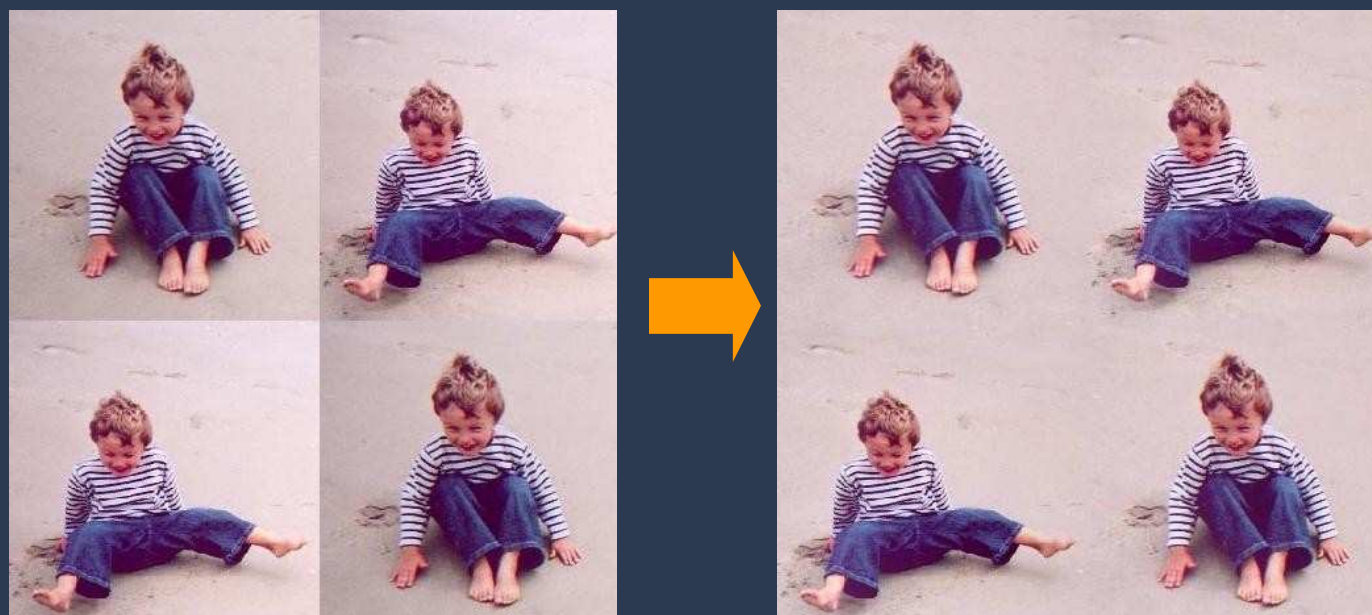
Gradient Domain Manipulations



Example Applications Discussed



Removing Glass Reflections



Seamless Image Stitching



Image Editing



Changing Local Illumination

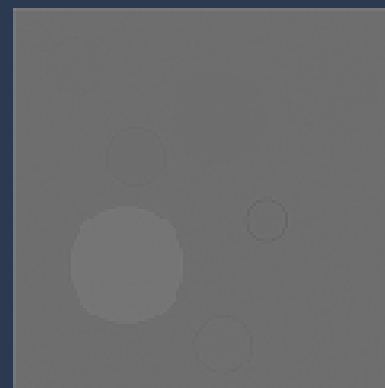




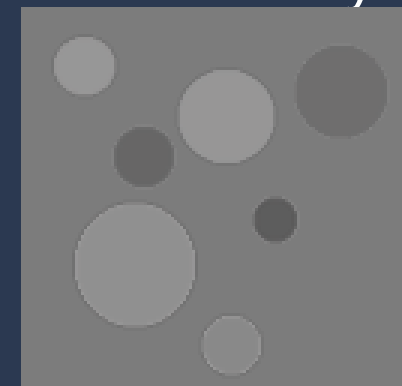
Original



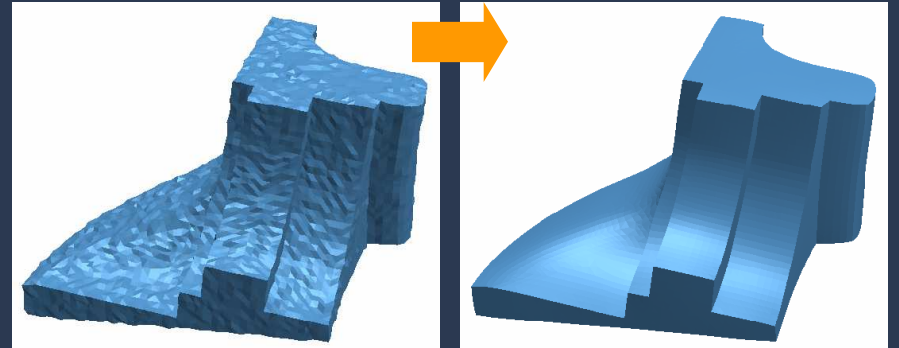
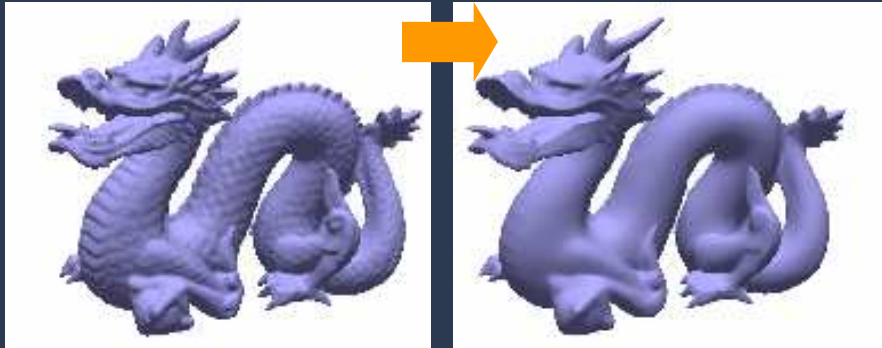
PhotoshopGrey



Color2Gray



Color to Gray Conversion



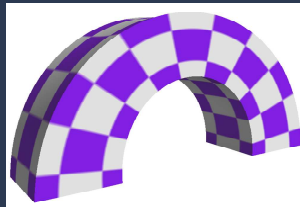
Mesh Smoothing



(a)



(b)



(c)

Mesh deformations



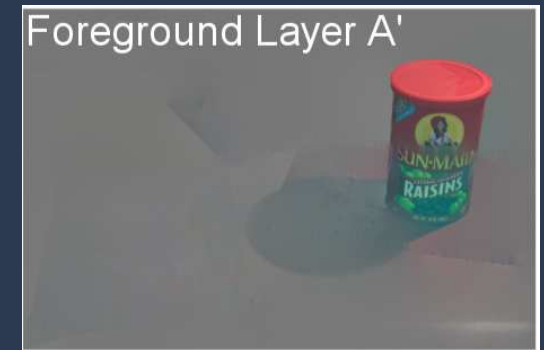
+



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High Dynamic Range Compression



Edge Suppression under Significant Illumination Variations



+



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Fusion of day and night images

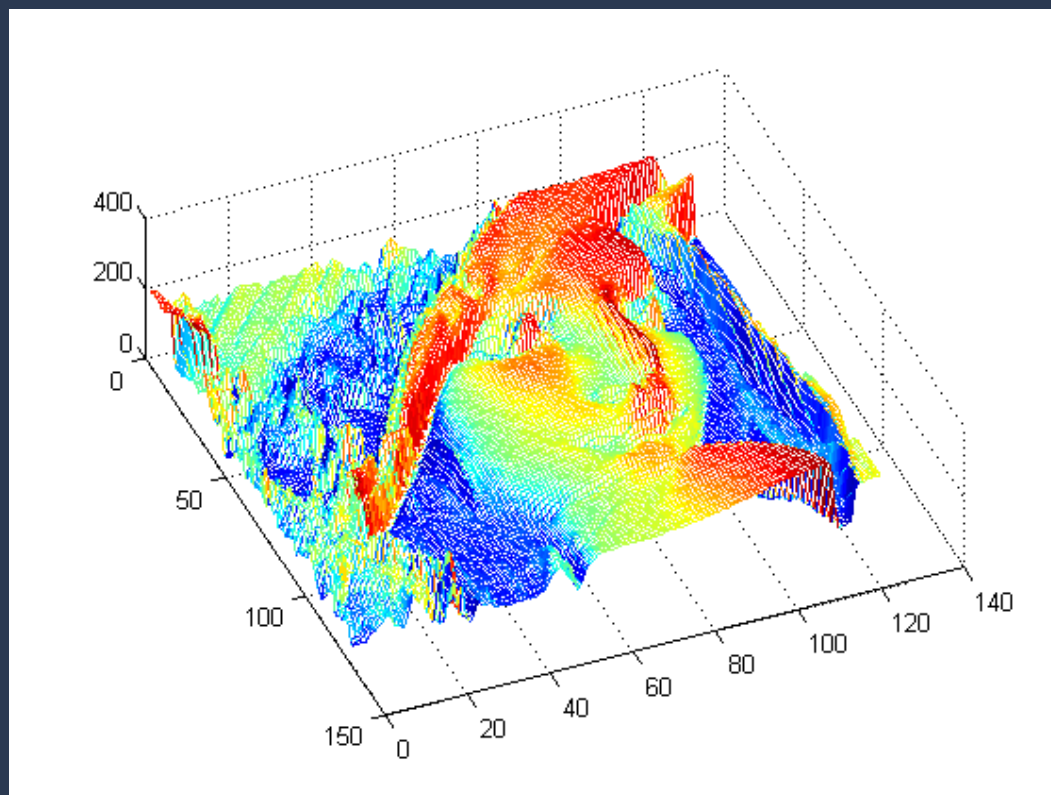
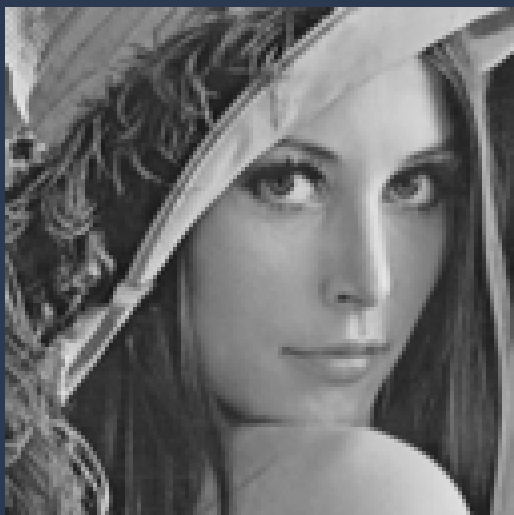
Overview

- Curl, Divergence
- Non-integrable gradient fields
- Reconstruction problem
- Motivating Applications

Basics

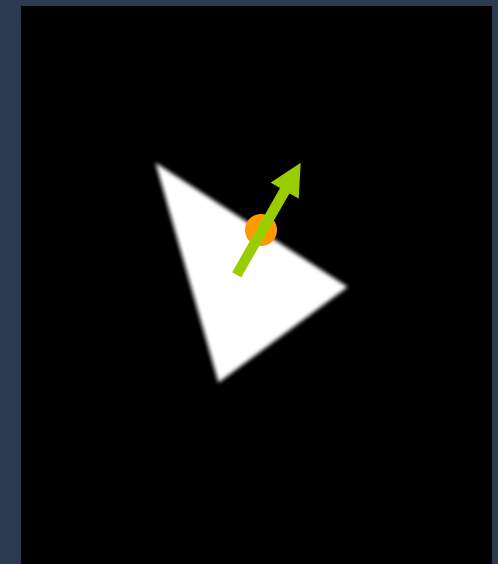
- Images as scalar fields

- $\mathbb{R}^2 \rightarrow \mathbb{R}$



Gradients

- Vector field (gradient field)
 - Derivative of a scalar field
- Direction
 - Maximum rate of change of scalar field
- Magnitude
 - Rate of change



Gradient Field

- Components of gradient
 - Partial derivatives of scalar field

$$I(x, y)$$

$$\nabla I = \left\{ \frac{\partial I}{\partial x}, \frac{\partial I}{\partial y} \right\}$$

$$I(x, y, t)$$

$$\nabla I = \left\{ \frac{\partial I}{\partial x}, \frac{\partial I}{\partial y}, \frac{\partial I}{\partial t} \right\}$$

Example



Image
 $I(x,y)$



I_x

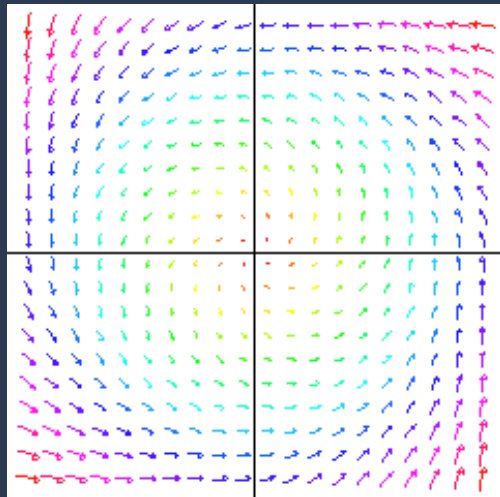


I_y

Finite Differences

Curl

- Vector operator
- Shows rate of **rotation** of a vector field
 - Circulation density
 - Direction of axis of rotation and magnitude of rotation



$$\text{Curl}(\nabla I) = \nabla \times \nabla I$$

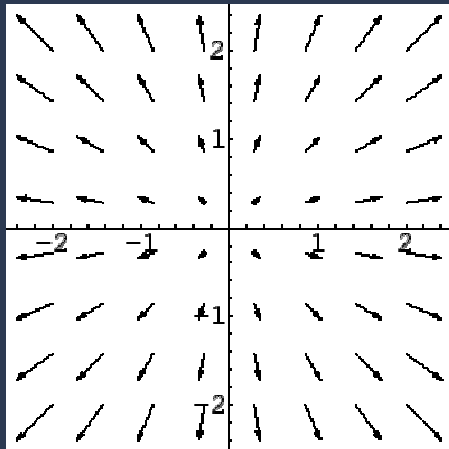
Curl

$$\text{Curl}(\nabla I) = \nabla \times \nabla I$$

$$\det \begin{vmatrix} \frac{\partial}{\partial x} & \frac{\partial}{\partial y} \\ I_x & I_y \end{vmatrix} = \frac{\partial I_y}{\partial x} - \frac{\partial I_x}{\partial y} = I_{yx} - I_{xy}$$

Divergence

- Vector Operator
- Shows magnitude of **source** and **sink**
- e.g. Translation Optical flow in Z direction



Divergence

$$\textit{Div}(\nabla I) = \nabla \bullet \nabla I$$

$$\textit{div}(I_x, I_y) = \frac{\partial I_x}{\partial x} + \frac{\partial I_y}{\partial y} = I_{xx} + I_{yy}$$

Example



Image



I_x



I_y

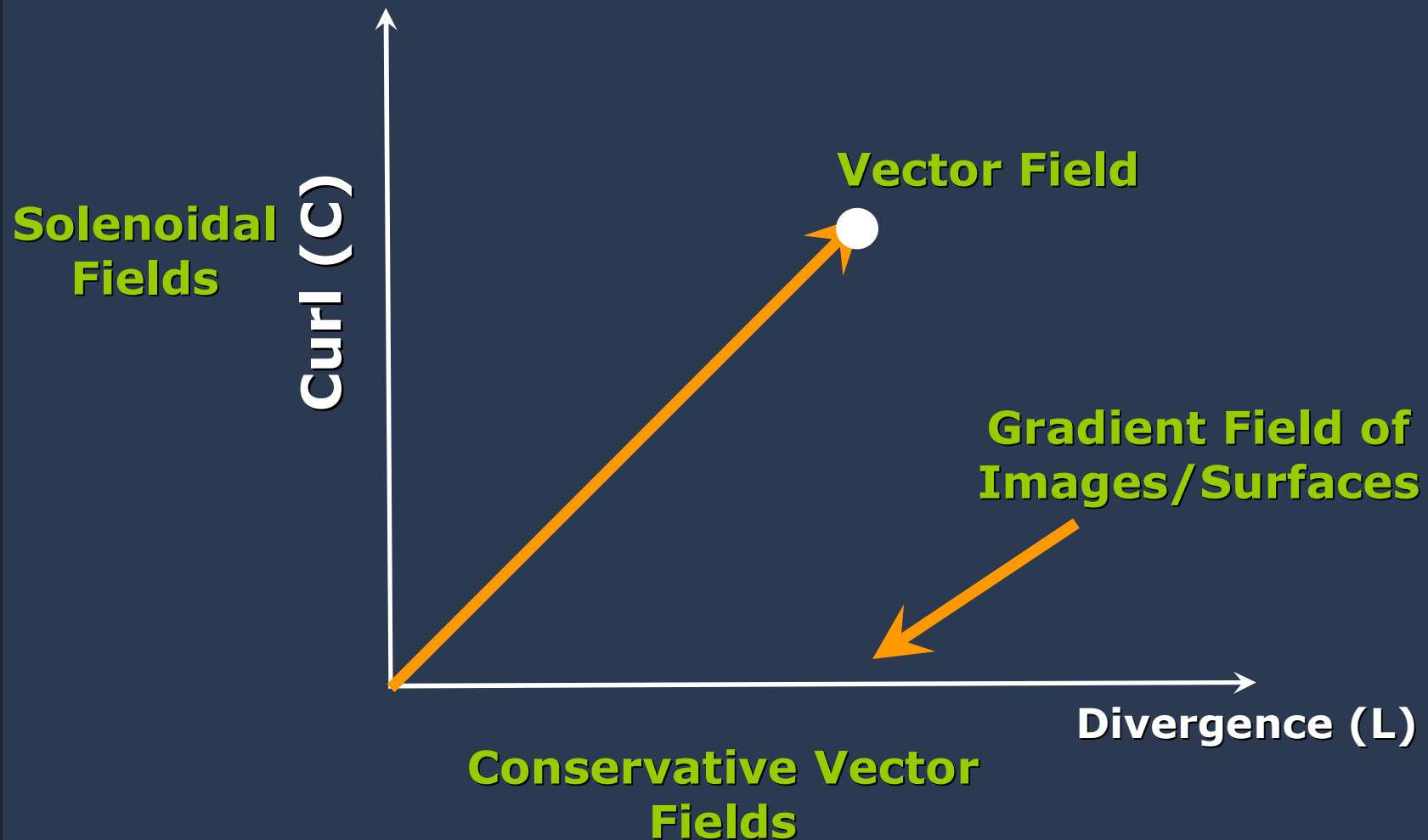


$\text{Div}(I_x, I_y)$



$\text{Curl}(I_x, I_y)$

Understanding Curl-Divergence



Integrability: Conservative vector field

- For a scalar field $I(x,y)$ $\nabla \times \nabla I = 0$
 - Curl of the gradient field should be zero

$$\text{Curl}(\nabla I) = I_{yx} - I_{xy} = 0$$

$$I_{yx} = I_{xy}$$

- Same result independent of differentiation order

Example



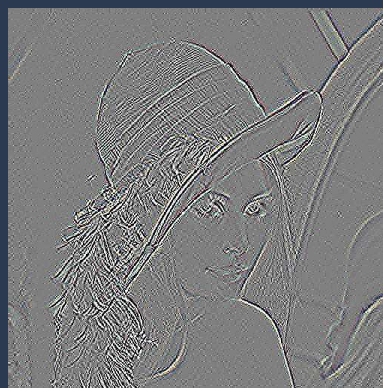
Image



I_x

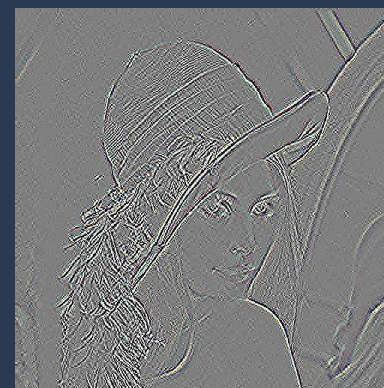


I_y



I_{xy}

=



I_{yx}

Integrability



Image

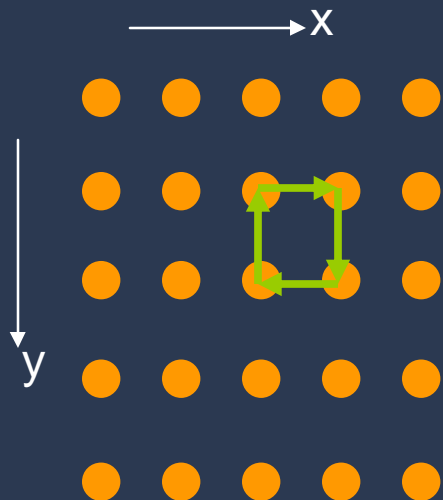


I_x



I_y

$$\text{Curl}(x,y) = I_x(x,y) + I_y(x+1,y) - I_x(x,y+1) - I_y(x,y) = 0$$



$\text{Div}(I_x, I_y)$



$\text{Curl}(I_x, I_y)$

Non-integrable gradient fields

- Several vision/graphics applications
- Two main causes
 - Estimation of gradients
 - E.g. Shape from Shading, Photometric Stereo
 - Surface gradients
 - Noise, outliers in estimation



Input Images



Surface
Normals/Gradients

Not Integrable!!

Non-integrable gradient fields

Manipulation of integrable gradients

- Synthesis of new gradient field



Image



I_x



I_y



Gradient
Manipulations



New
Gradients



New
Image???

Not Integrable!!!!

Example Gradient Manipulation

- Rotate gradient at every pixel by same angle
- How does Curl and Divergence change?



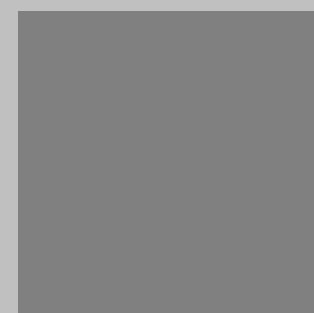
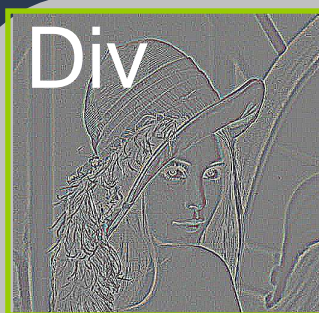
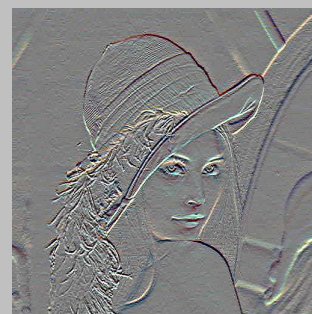
Gradient Rotation

$$I_{x'} = I_x \cos(\theta) - I_y \sin(\theta)$$

$$I_{y'} = I_x \sin(\theta) + I_y \cos(\theta)$$

$$\text{Div}(I_{x'}, I_{y'}) = \text{Div}(I_x, I_y) * \cos(\theta)$$

$$\text{Curl}(I_{x'}, I_{y'}) = -\text{Div}(I_x, I_y) * \sin(\theta)$$



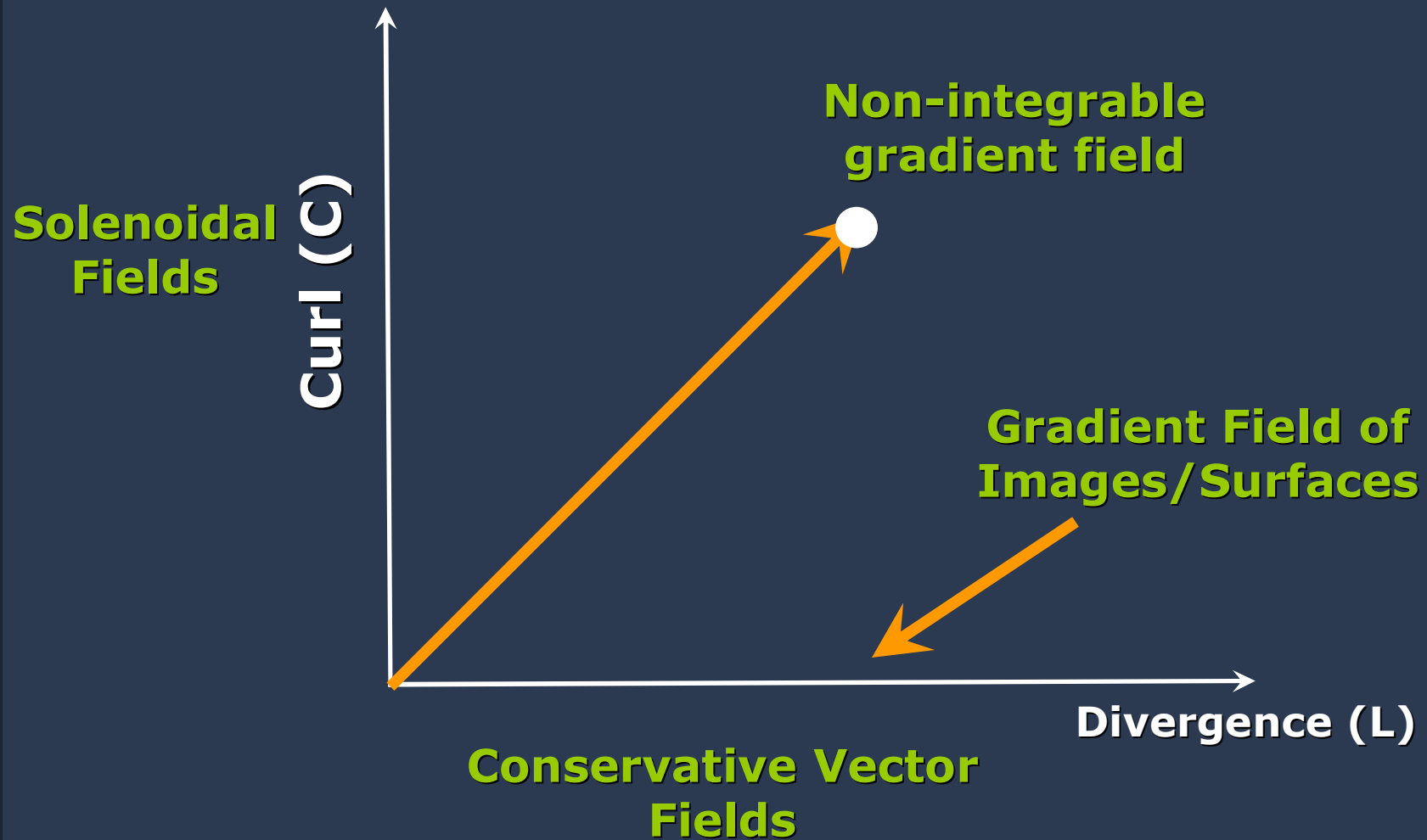
0

45

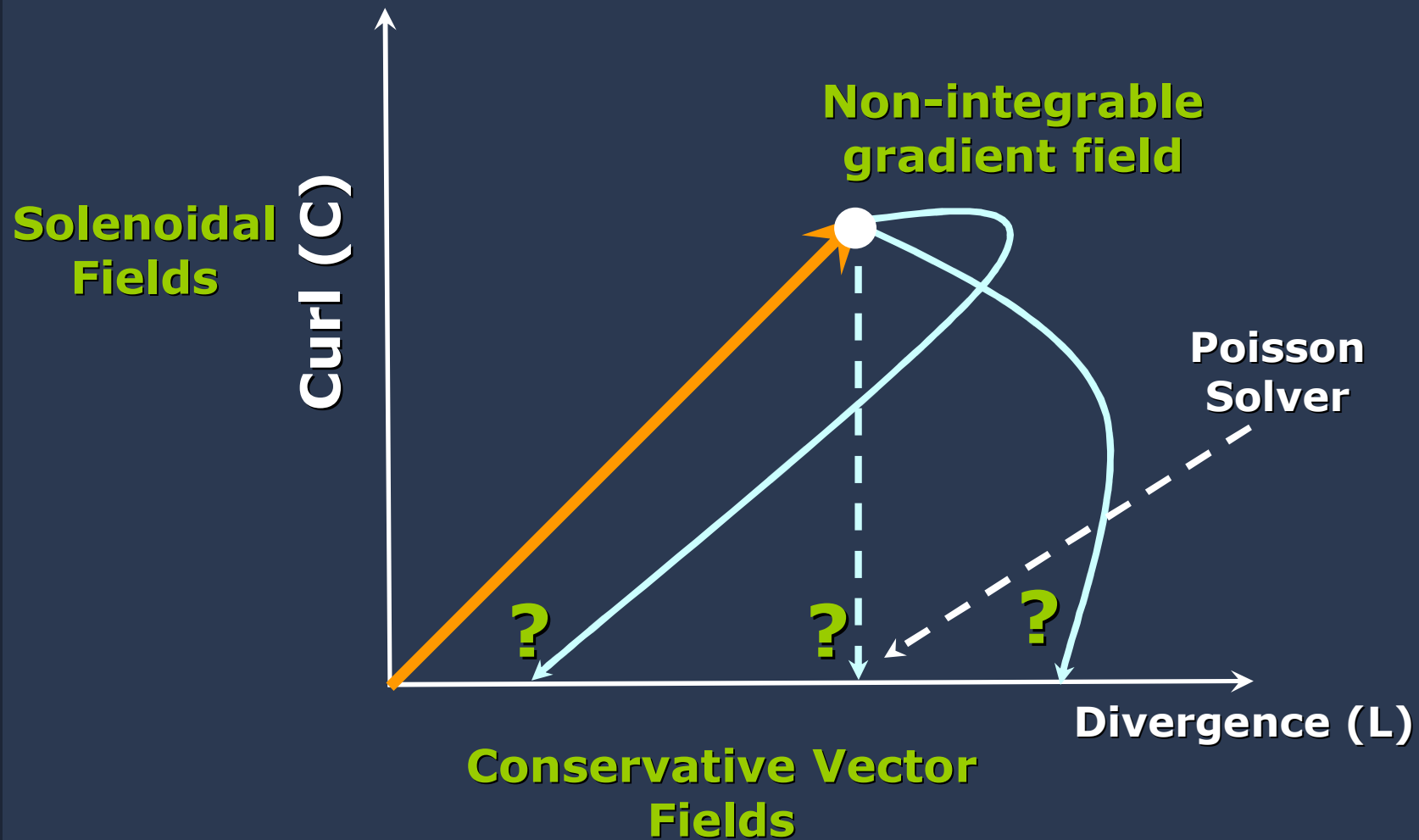
90

180

Understanding Curl-Divergence



The Reconstruction Problem



Overview

- Curl, Divergence
- Non-integrable gradient fields
- Reconstruction problem
- Motivating Applications

Problems involving Integrability

- Reconstructing height field from gradients (**Next**)
 - Applications: Shape from Shading, Photometric Stereo
- Manipulating image gradients (**Section 2**)
 - Applications: HDR compression, Image editing, matting, Fusion, Mosaics
- Manipulation of 3D gradients (**Section 4**)
 - Applications: Mesh editing, Video operations

Reconstruction from non-integrable fields

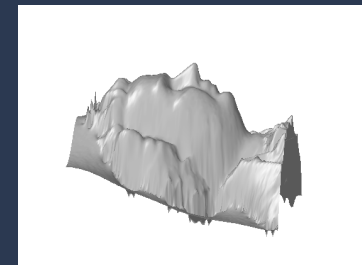


- Algorithms
 - Poisson solver. Based on least squares fitting
 - Other approaches?
 - Projection on basis, Robust reconstruction, gradient transformations
- Numerical Methods
 - Direct solutions, Multigrid, Preconditioned conjugate gradients, Hierarchical basis
 - Tradeoffs
- More in Section 3

Example Applications

- Analysis

- Shape from Shading, Photometric Stereo



Height Field

- Synthesis

- High Dynamic Range (HDR) Compression



Photometric Stereo (**Gradient Estimation**)

- Shape from multiple images
 - Fixed viewpoint, varying illumination
- Common Assumptions
 - Lambertian surfaces, Point light source
- We focus on recovering height fields by **first** estimating gradients

Photometric Stereo

- Lambertian reflectance model
 - Relates image intensities to surface normals $\mathbf{n} = [n_x, n_y, n_z]$

$$I(x, y) = \rho(x, y) \mathbf{n}(x, y) \cdot \mathbf{s}$$

albedo

Light source
direction

- Multiple images


$$I_i(x, y) = \rho(x, y) \mathbf{n}(x, y) \cdot \mathbf{s}_i \quad i = 1 \dots n.$$

Estimating Gradient Field

$$I_i(x, y) = \rho(x, y) \mathbf{n}(x, y) \cdot \mathbf{s}_i \quad i = 1 \dots n.$$

$$\mathbf{a}(x, y) = \rho(x, y) \mathbf{n}(x, y)$$

Scaled normal



$$\begin{bmatrix} \mathbf{s}_1^T \\ \mathbf{s}_2^T \\ \vdots \\ \mathbf{s}_n^T \end{bmatrix} \mathbf{a}(x, y) = \begin{bmatrix} I_1(x, y) \\ I_2(x, y) \\ \vdots \\ I_n(x, y) \end{bmatrix}$$

$p = -n_x/n_z, q = -n_y/n_z$ Estimated surface gradients

Photometric Stereo

- Multiple images, varying illumination
- Obtain surface gradient field from images
 - Lambertian reflectance model



Images



X Gradient



Y Gradient



Images



X Gradient



Y Gradient



X Gradient



Y Gradient



Height Field

Isotropic



Poisson
Solver

Anisotropic



Alpha-Surface
Binary weights



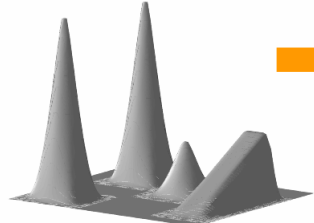
M-estimator, Regularization
Continuous weights

Scaling

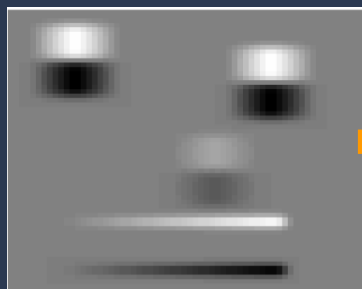


Diffusion
Affine
Transformation

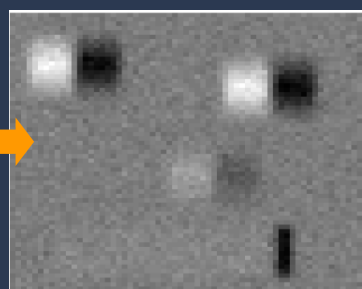
Ground Truth



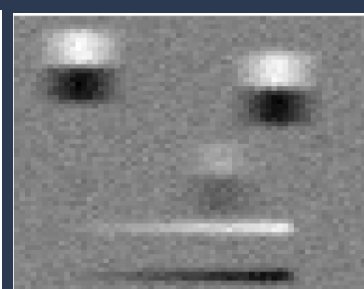
g_x



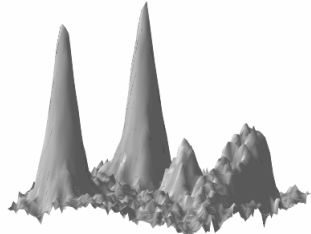
g_y



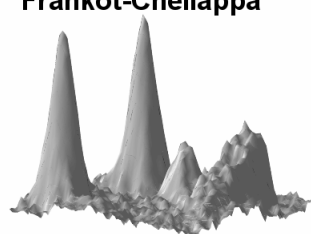
Add noise and outliers



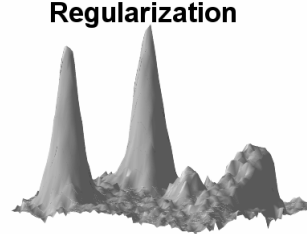
Poisson Solver



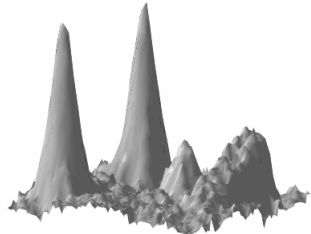
Frankot-Chellappa



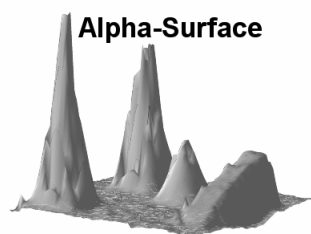
Regularization



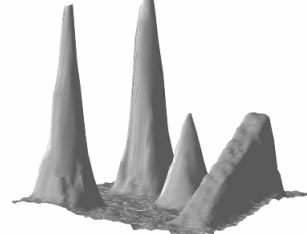
M-estimator



Alpha-Surface



Diffusion



High Dynamic Range Imaging

- Cameras have limited dynamic range



Small Exposure image, dark inside
1/500 sec



Large exposure image, saturated outside
1/4 sec

High Dynamic Range Imaging

- Combine images at different exposures
- [Mann and Picard 95, Debevec et al 96]

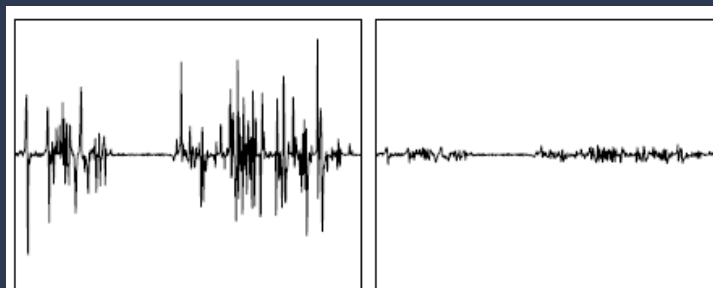




High Dynamic Range Compression (Gradient Manipulation)

- Synthesize new gradient field
- Key Idea: Suppress large gradients, keep small gradients
- Integrate to obtain Low Dynamic Range (LDR) Image

High Dynamic
Range Image



Gradients

Modified



Low Dynamic
Range Image

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Mesh Editing & Texture

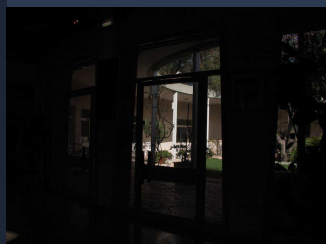
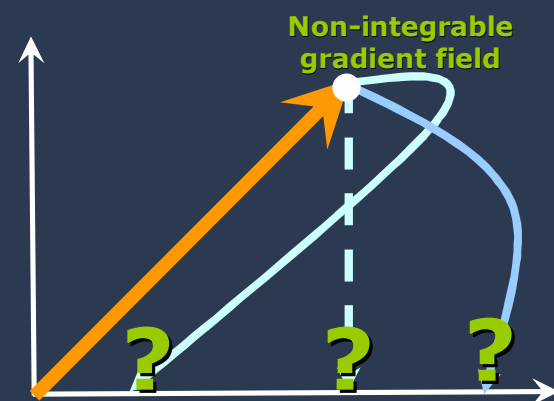
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Photometric Stereo, Shape from Shading

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Summary

- Basics
 - Curl, Divergence, Integrability
- Non-integrable gradient fields in vision/graphics
 - Estimation & Manipulation of gradients
- Reconstruction from gradients
- Motivating applications
 - HDR compression, Photometric Stereo



Next Section

- Gradient Domain Manipulation of images



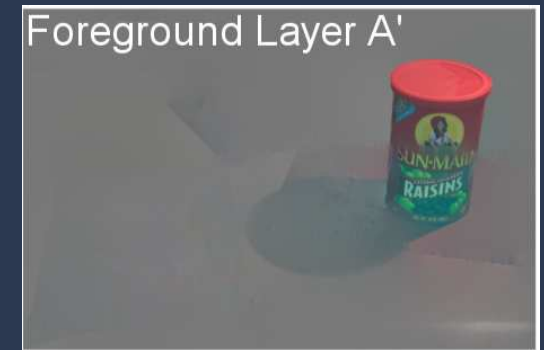


Image Editing



Changing Local Illumination





Edge Suppression under Significant Illumination Variations



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Fusion of day and night images

Schedule

Introduction	(30 min, Agrawal)
Gradient Domain Manipulations	(1 hr, Raskar)
Break	(15 min)
Reconstruction Techniques	(1 hr, Agrawal)
Advanced Topics	(30 min, Raskar)
Discussion	

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