

# Advanced Datastructures: Project 3

## Functional Queues

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# Contents

<b>1</b>	<b>Intro</b>	<b>3</b>
<b>2</b>	<b>The Haskell Data Structures</b>	<b>3</b>
<b>3</b>	<b>Haskell Performance Concerns</b>	<b>5</b>
3.1	The GHC Compiler . . . . .	5
3.2	Haskell and Lazy Thunks . . . . .	6
3.3	Using <code>case</code> to Force Strictness . . . . .	6
3.4	Strict Data Types . . . . .	6
3.5	Using Non-Generic Types . . . . .	7
3.6	Using Strict Parameters . . . . .	7
3.7	Numeric Types in Haskell . . . . .	7
<b>4</b>	<b>Test Framework - Criterion</b>	<b>7</b>
<b>5</b>	<b>Experiments</b>	<b>8</b>
5.1	Expectations . . . . .	8
5.2	Computer Specs: . . . . .	9
5.3	Result . . . . .	9
5.4	Conclusions . . . . .	13

# 1 Intro

Queues are an important type of structures, and we often see them used as the basic tools for different algorithms. In imperative languages, it is easy to implement queues with  $O(1)$  worst-case guarantees for `pop` and `inject`, with common implementations being a Linked List or a Circular Buffer. When using a functional language, such as Haskell, we do not have access to side-effects, and as such, implementing a queue with the nice  $O(1)$  guarantees becomes much harder, and we need to make certain trade-offs, such as relying on amortization or global rebuilding. In this project we look at several different queue implementations in the lazy functional language of Haskell, and try to show their different properties through experiments.

## 2 The Haskell Data Structures

As specified in the problem description, 4 different queues were implemented in Haskell. They have various properties, described as follows:

1. **Haskell List** A queue can be implemented using a single built-in list from Haskell. Performing a `pop` is simple, just remove the head of the list into the head and tail part. `Inject` on the other hand is slow, since we need to insert at the tail of the list. We do this, by reversing the list, adding the new final element as a head, and reversing again. Note that this could probably be sped up by performing only a single run through the list, but it is, under any circumstance, an  $O(n)$  operation. Depending on how Haskell's strictness analysis performs, we might actually see that the heavy work of the `inject` function gets thunked, and evaluated at the next `pop` operation.

**Alternative Single-List Options** There are alternative ways to implement a queue in Haskell using only one list. We chose ours as being the conceptually simplest.

Another way to keep store the queue, would be to keep it in a single list, in reverse order. This would give  $O(1)$  `injects`, but  $O(n)$  `pop`.

A quite interesting approach is to switch between reversed and normal ordering of the queue as needed, making operations  $O(n)$  only when switching between `inject` and `pop`.

2. **Paired  $O(1)$  Non-Reusable Queue** This queue implementation is based on maintaining a pair of queues, with one being the front of the queue,

and one being the end of the queue, in reverse order. When we **pop**, we simply return the head of the front list, or, if it is empty, reverse the en list into the front list, and perform the **pop**. **Inject** is done by adding the injected element as the head of the end list. If we assume that any operation is only done on the currently newest version of the list, we can have the **inject** pay an amortized  $O(1)$ , to **pop** be an  $O(1)$  cost operation amortized in a strict execution context.

Note that even with lazy evaluation, we will most likely perform the entire reverse operation each time we need to reverse, since we need to remove the head.

**3. Real-Time Strict Queues** For the  $O(1)$  worst case queues we use the queues of (TODO:Ref Melville Real-time queues in pure lisp). Instead of using the implementation example from the slides of (TODO: Ref Gerth slides), we adapted the implementation presented in (TODO: ref Oskaki purely functional data structures (bogen, ikke thesis)). This queue maintains a front and a reversed end list, much like amortized  $O(1)$  strict queue, but uses global rebuilding to ensure that we can always pop in  $O(1)$  worst case time. The implementation we are working with explicitly keeps track of state it is in when doing global rebuilding. At any point in time, the global rebuilding of the queue may be in one of the following states:

**Reversing** The queue is in the process of reversing the front and end list, in preparation of concatenating them. This phase uses 4 lists.

**Appending** After having reversed the lists, the queue will append the front list to the end list one element at a time. This phase uses 2 lists.

**Done** The queue is done reversing and appending, and the new front list is ready. This phase uses 1 list.

**Idle** The queue needs not do any more work right now.

Since we use at most 4 lists in any phase, and 2 list in the queue itself, we use at most 6 lists in total.

After doing a **inject** or **pop**, we perform 2 steps of work on the current state, which ensures that we will always be ready to perform **pop**.

Note that we also keep 3 counters in the queue; the front list length, the end list length and the amount of valid elements in the state. This ensures that we can easily determine whether or not to initiate a global rebuild, and which elements we can discard from the global rebuild.

In terms of strictness, we use a `case` statement to ensure strict work step is strictly executed, but we fear that Haskell may still lazily thunk either some of the inner contents of the work operation, or during some of the functions leading to the work statement.

- 4. Lazy Amortized  $O(1)$  Queues** The lazy queue keeps track of 2 lists, a front and a reversed end list, and their lengths. Whenever the reverse end list grows longer than the front list, we replace the front list by the concatenation of the front list and the end list reversed. Note that by requiring the end list to have grown significantly since each concat-reverse, we ensure that we have done enough `pop` or `inject` operations to have a  $O(1)$  amortized cost.

Since these queues all follow the same interface, we also included wrapper functions that map generic `pop`, `inject` and `make` operations to the corresponding implementation-specific operation.

## 3 Haskell Performance Concerns

This is our first encounter with the development of performance-critical components in Haskell, and therefore we took our time looking into the different ways of making Haskell fast. Though we are sure that we have not done every trick in the book, and expect to have missed quite a few tricks that a Haskell veteran would have never let go, we were able to improve the performance of our initial data structures significantly through certain optimization patterns.

### 3.1 The GHC Compiler

The GHC compiler, short for *Glasgow Haskell Compiler* (TODO:link til <http://www.haskell.org/ghc/>), was the compiler used in this project. GHC was chosen, since it is the most widely used compiler supporting the entire feature set of Haskell, and has a wide array of optimization options.

The programs were compiled using the following set of command line parameters `ghc -O2 -funbox-strict-fields -XBangPatterns -optc-O3`. Each parameter has the following function:

- O2** Perform heavy compile-time optimizations. This option should make the programs run a tiny bit faster than using `[-O]`.
- funbox-strict-fields** Automatically unbox strict fields. This is mostly a cosmetic parameter allowing us to omit UNPAK tags from our code.

**-XBangPatterns** Allow the use of the bang patterns extension, which is used for strict parameters.

**-optc-O3** If using the C back-end, make GHC use the `-O3` option for GCC.

Used together, these flags allowed us to fine-tune the compilation of our Haskell code.

## 3.2 Haskell and Lazy Thunks

Haskell programs are lazily evaluated, using so-called *thunks*. This means that the execution of any expression gets replaced by a *thunk*, which acts as a placeholder for the value until it is actually needed. As soon as it becomes necessary to know the value of the expression, we evaluate the *thunk*, and store the associated value.

Note that a *thunked* expression is only evaluated once, a key feature of the Lazy Queue, and any expression that is never used will not be evaluated.

Lazy *thunks* do however have some performance concerns. Delayed execution may lead to a very heavy workload being assigned to a single operation, since long chains of unevaluated thunks might have developed. Also, the memory usage of storing these *thunks*, if they are not forced in time.

Since lazy evaluation is such a big part of Haskell performance, many of the optimization techniques used are based on forcing evaluation of thunks at certain critical points, and the GHC itself will try analyse when a value is immediately needed, and evaluate it strictly.

## 3.3 Using case to Force Strictness

In the Real-Time Strict Queues, we wish to enforce strictness on the evaluation of the global rebuilding. We do this using the `case` statement, which performs pattern matching on the result of a given expression. Since we need to know the structure of the result, we force the execution of the thunk representing the global rebuilding state, and maintain the  $O(1)$  worst-case guarantee for all operations.

## 3.4 Strict Data Types

Strictness can be enforced for type members, and unpacked into function parameters using the `-funbox-strict-fields` compiler flag. In certain parts of the program data structure, this can save us the overhead of thunking, and lead to a significant speedup.

Simply marking the general structure of the Lazy Queue as strict (note that inner values are still lazy, we do not force strict execution of the lists making up the queue), and unpacking it, lead to a speedup of  $\sim 5\% - 30\%$ , depending on the test suite.

Using strictness in the Real-Time Strict Queue structure was also used, but it did not in itself provide any speed-up.

### 3.5 Using Non-Generic Types

Haskell is statically typed, but uses type inference for most functions. If we however guarantee that we only use certain types, we allow the compiler to perform more in-depth optimization.

This is done by explicitly specifying the type of functions, and fully specifying what types will be used, which should provide a small performance gain.

### 3.6 Using Strict Parameters

Using the bangpatterns extension, we can mark certain parameters in pattern matching for strict execution. This can remove some of the overhead from thunking, and help the compiler perform strictness analysis.

When used in conjunction with strict typing, we achieved a  $\sim 5\%$  performance gain on the Real-Time Strict Queues.

### 3.7 Numeric Types in Haskell

Haskell has a quite good arbitrary-precision integer type. However, for optimum performance, we switched to using machine-word integers, which gave us a  $\sim 10\% - 30\%$  performance gain across the different tests.

## 4 Test Framework - Criterion

Criterion (TODO: Criterion github ref) is a benchmarking framework for Haskell developed by Bryan O’Sullivan (TODO:ref Bryan’s webpage) that gives accurate statistical information about the code segment that one is testing. This includes the mean and standard deviation of the running time for each sample. Timing values are useful, but having an indication of which times occurred most often is a lot more useful, because it can hint at outliers offsetting the mean running time. Criterion can output histograms in html showing this information.

When we test using Criterion the first thing it does is measure how long it takes for the system clock to tick and then run the code several times to ensure that the resolution of the clock does not introduce any significant errors. If the code takes  $5\mu s$  to evaluate but the clock only ticks every  $9\mu s$ , we cannot just run the code once and subtract start time from end time because then it would look like the code evaluated instantly sometimes and sometimes not. By running the code thousands of times the error is reduced to only a few instances out of the whole.

Criterion automatically calculates how many times it needs to evaluate the code and also reports an estimate of how long it will take. It uses a boxplot technique to get a quick sense of the quality of the data by calculating outliers, which are values that lies far from the mean of the sample. Once the system clock period has been found criterion figures out how expensive it is to use the clock and adjusts the time measurements to take the clock into account.

In the end criterion performs some statistical analysis on the results using a technique called bootstrapping to see if other processes on the computer might have influenced the results by looking at the number of outliers. If there are many outliers the results are essentially junk because the computer then would have varied compute capability during testing, which corrupts the results.

The graphs showing our test results was computed using the mean as execution time as it was close to the time that occurred most often in all test cases.

Due to all of these excellent features of Criterion, and its ease of use, we chose it as our the basis for all of our tests.

## 5 Experiments

### 5.1 Expectations

When comparing the 4 different queue implementations, we expect them to perform as follow:

- 1. Haskell List** The Haskell List queue implementation performs **inject** in  $O(n)$  time, and as such, we expect it to perform horribly on any test case that requires pushes. On pure **pop** operations however, it will be  $O(1)$ , with a very low overhead, and as such it will most likely be among the fastest queues at performing **pops**-
- 2. Paired  $O(1)$  Non-Reusable Queue** The Paired Queue implementa-



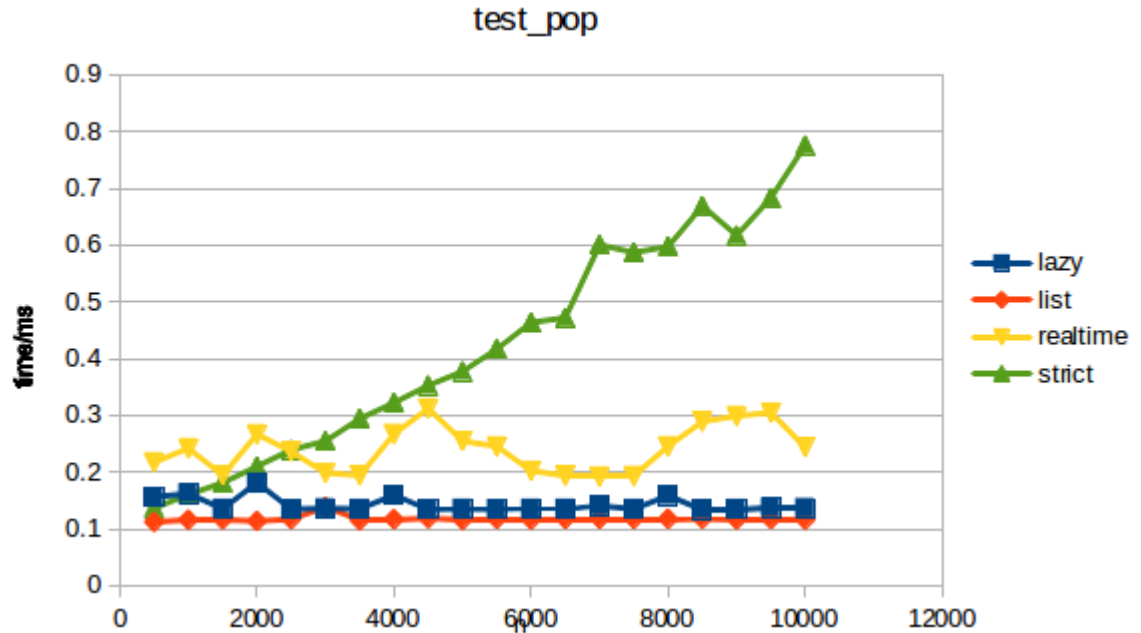
tion should be fairly low-overhead, and as such perform quite well, except on the special test case, where we reuse queues.

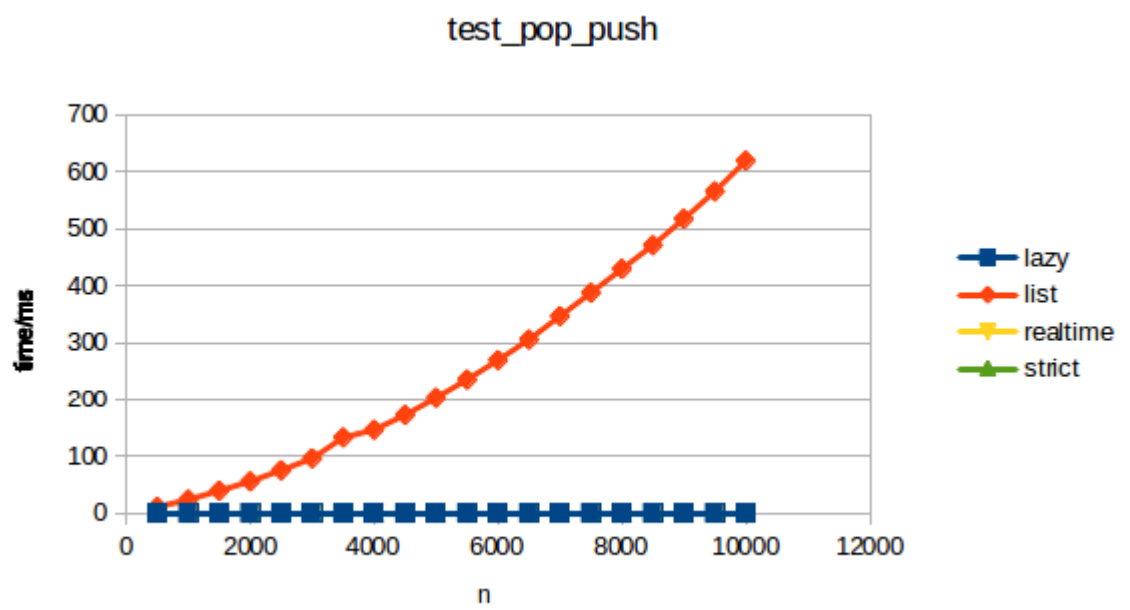
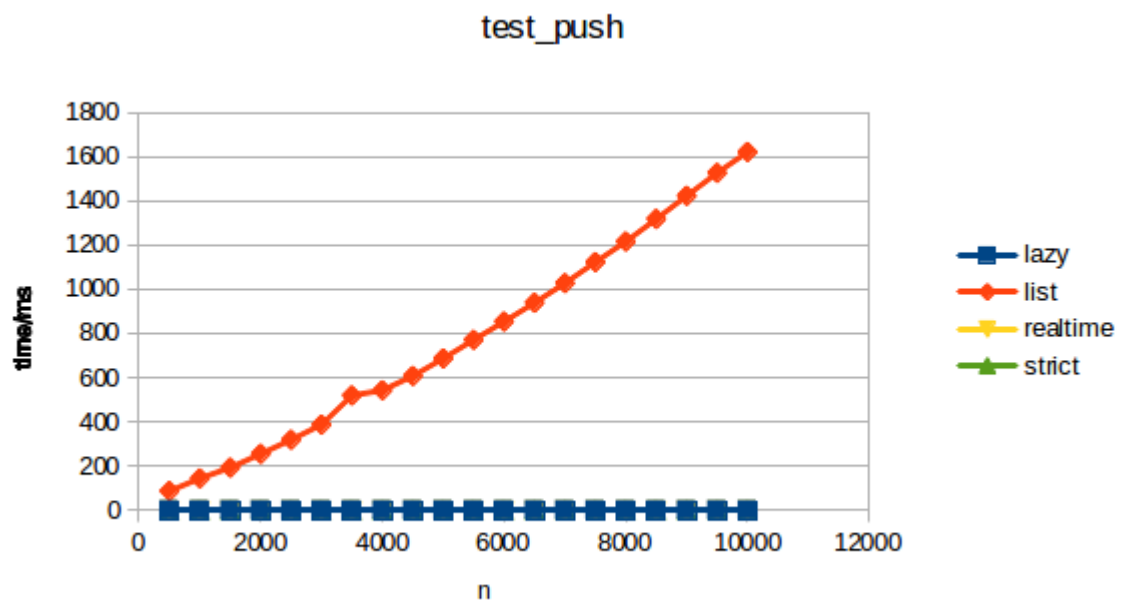
3. **Real-Time Strict Queues** The Real-Time Strict Queue should generally perform well on all test cases, since we have a nice  $O(1)$  worst-case guarantee for all operations. This queue however, has quite a large overhead, and will therefore most likely be outperformed by most other queues in tests cases where they exhibit  $O(1)$  performance.
4. **Lazy Amortized  $O(1)$  Queues** The Lazy Queue should perform very well on all test cases. Not only does it have  $O(1)$  amortized cost for all operation, it also has quite a low overhead.

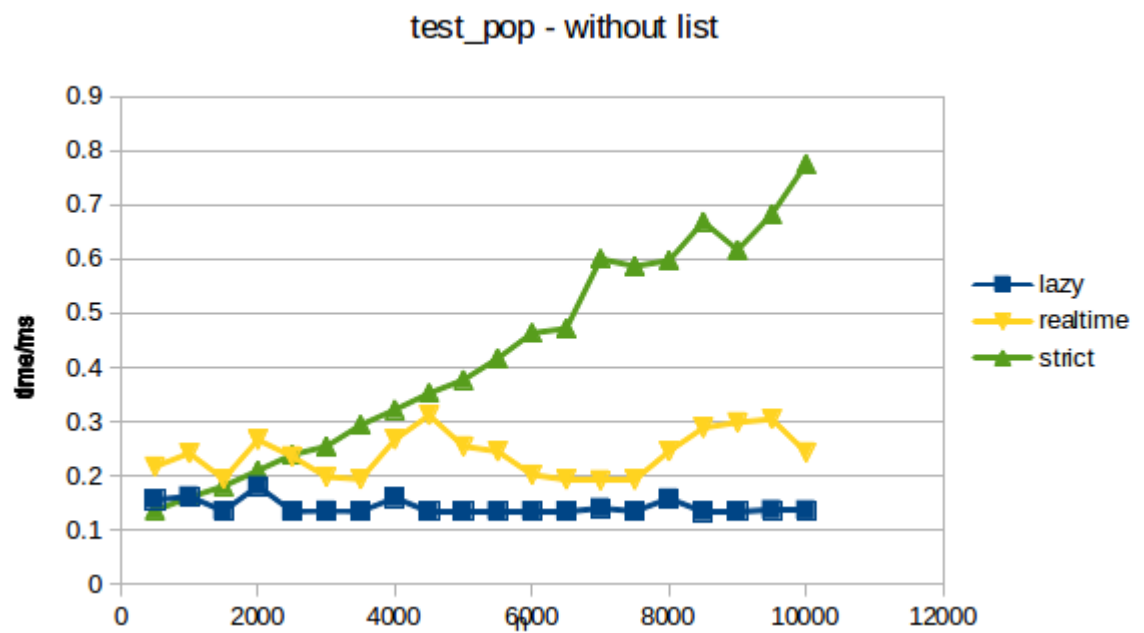
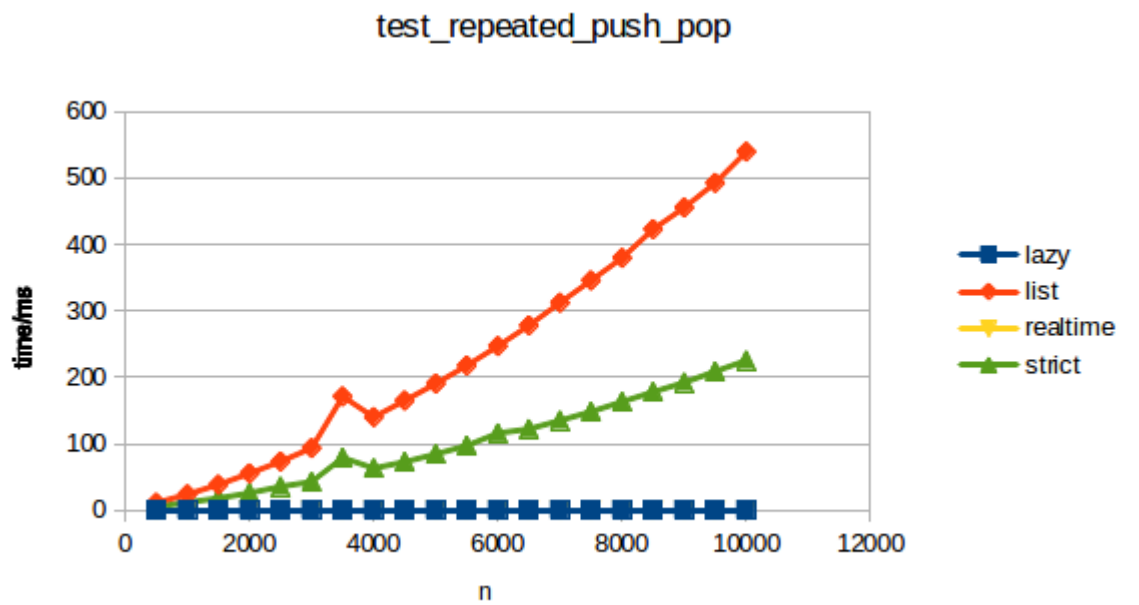
## 5.2 Computer Specs:

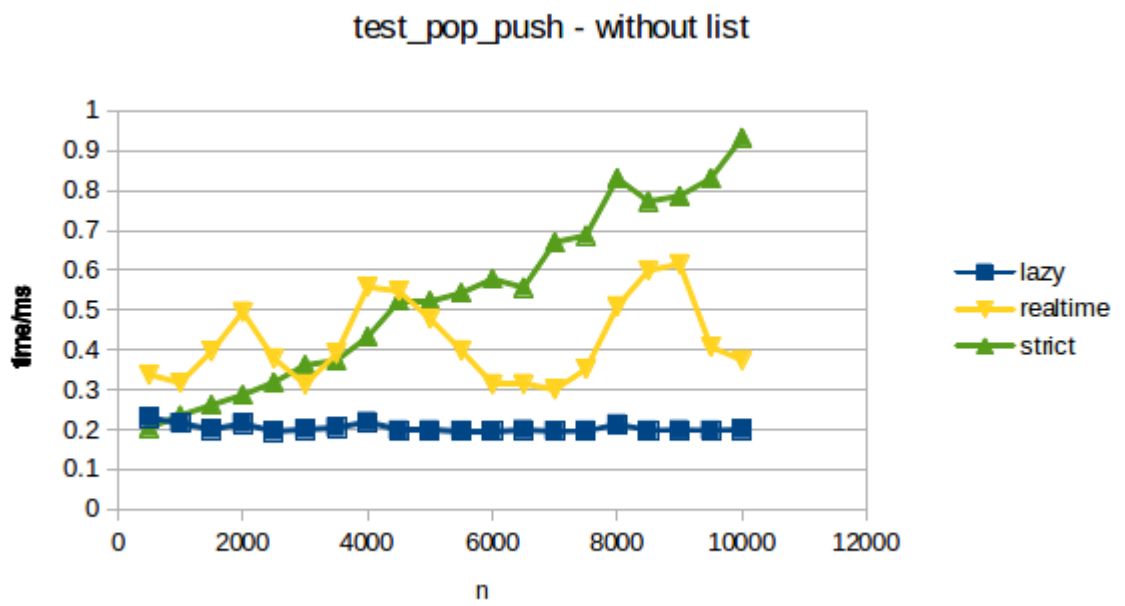
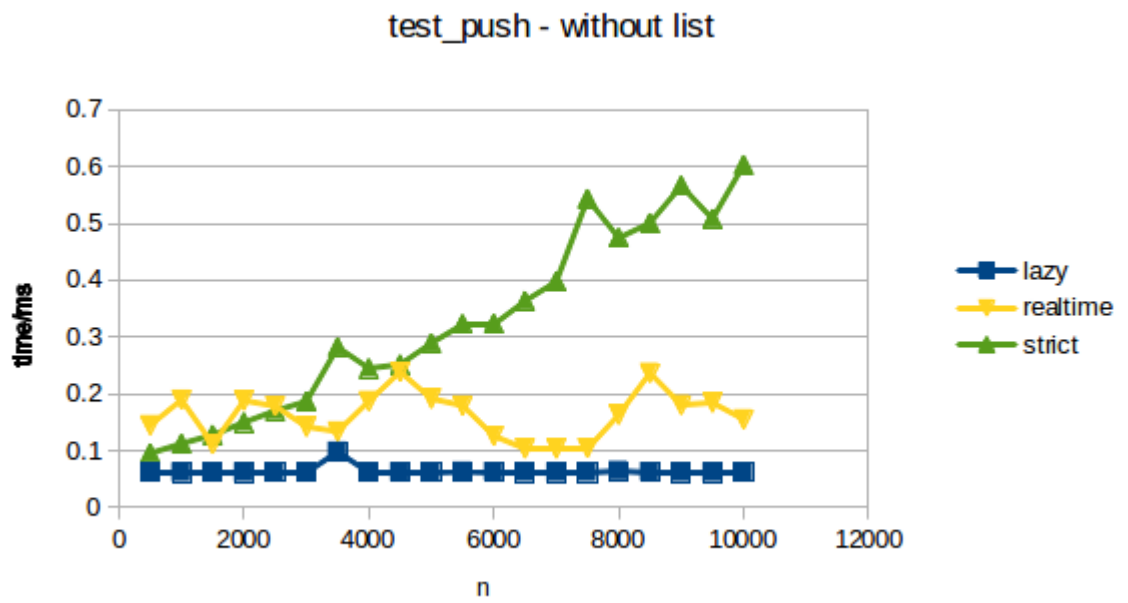
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OS:	Ubuntu 12.10
CPU:	Intel Atom Dual Core 1.8GHz
Memory:	2 GB

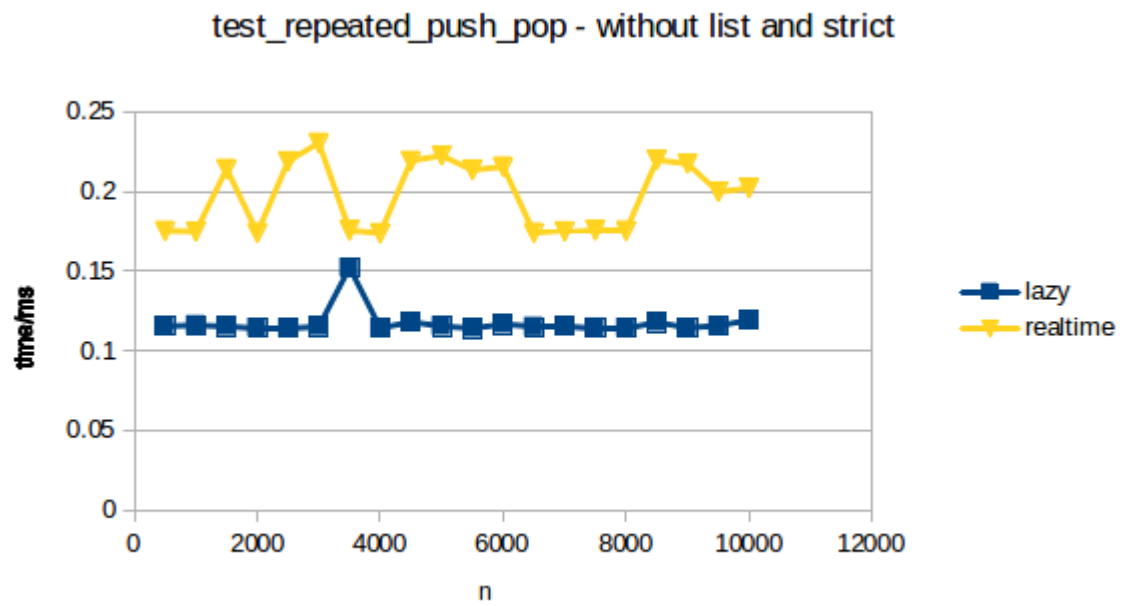
## 5.3 Result











## 5.4 Conclusions

TODO: Write, Kris can easily do this

## References