

Part 1:

	INCOME	STUDENT	CREDIT	CLASS
YOUTH	HIGH	NO	FAIR	NO
YOUTH	HIGH	NO	EXCELLENT	NO
YOUTH	MED	NO	FAIR	NO
YOUTH	LOW	YES	FAIR	YES
YOUTH	MED	YES	EXCELLENT	YES

GAIN

$$INFO(D) = -\frac{3}{5} \log_2 \left(\frac{3}{5} \right) - \frac{2}{5} \log_2 \left(\frac{2}{5} \right) = 0.971$$

$$INFO_{(student)}(D) = \underbrace{\frac{3}{5} \left(-\frac{3}{3} \log_2 \frac{3}{3} \right)}_{NO} + \underbrace{\frac{2}{5} \left(-\frac{2}{2} \log_2 \frac{2}{2} \right)}_{YES} = 0 + 0$$

$$INFO_{(credit)}(D) = \underbrace{\frac{3}{5} \left(-\frac{2}{3} \log_2 \frac{2}{3} - \frac{1}{3} \log_2 \frac{1}{3} \right)}_{FAIR} + \underbrace{\frac{2}{5} \left(-\frac{1}{2} \log_2 \frac{1}{2} - \frac{1}{2} \log_2 \frac{1}{2} \right)}_{EXCELLENT} = .551 + 0.4 = 0.951$$

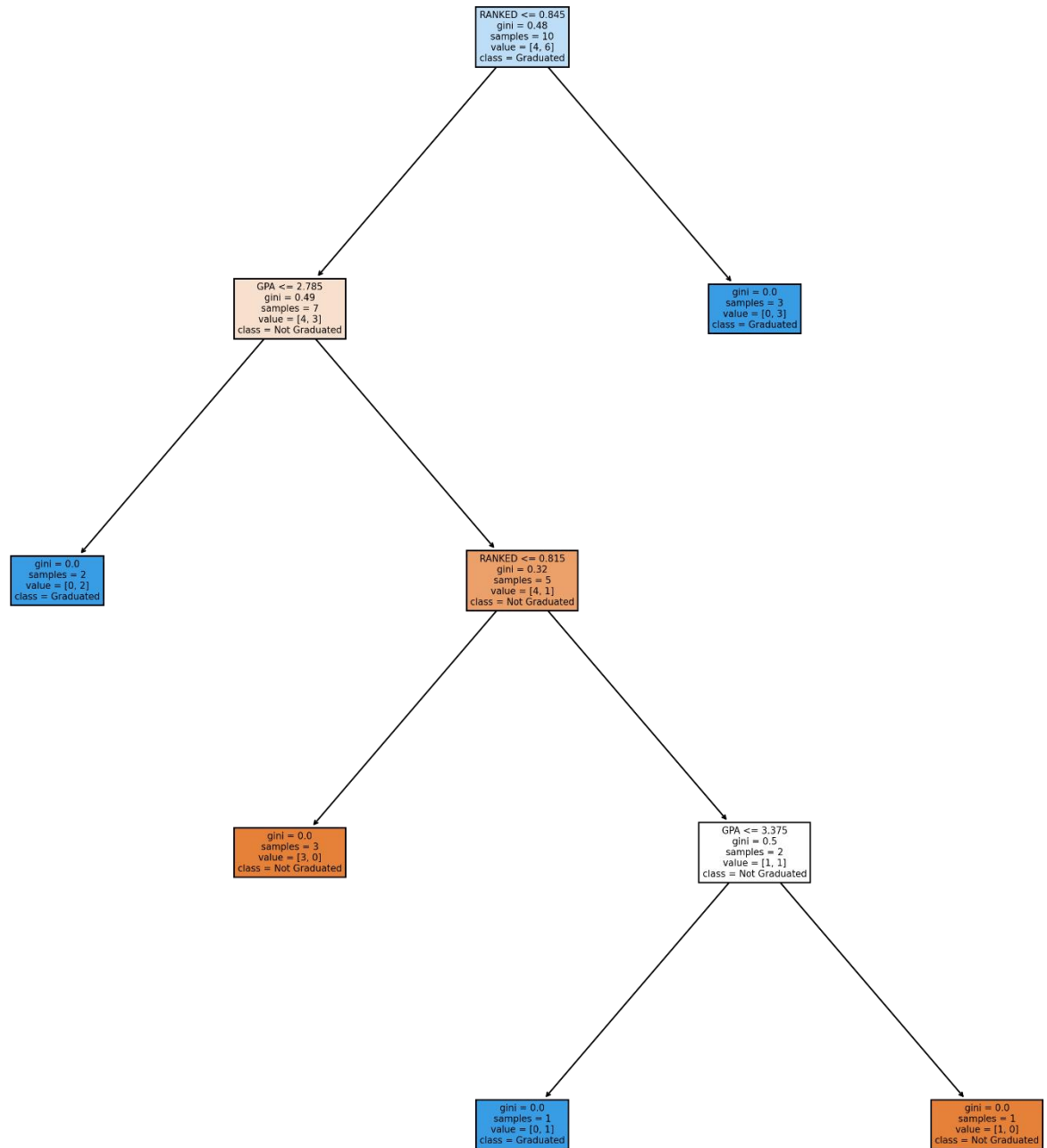
$$INFO_{(income)}(D) = \underbrace{\frac{2}{5} \left(-\frac{2}{2} \log_2 \frac{2}{2} \right)}_{HIGH} + \underbrace{\frac{1}{5} \left(-1 \log_2 1 \right)}_{LOW} + \underbrace{\frac{2}{5} \left(-\frac{1}{2} \log_2 \frac{1}{2} - \frac{1}{2} \log_2 \frac{1}{2} \right)}_{\substack{NO \\ YES \\ MED}} = 0 + 0 + 0.4 = 0.4$$

$$GAIN_{(income)} = INFO(D) - INFO_{(income)}(D) = 0.971 - 0.4 = 0.571$$

$$GAIN_{(student)} = INFO(D) - INFO_{(student)}(D) = 0.971 - 0 = 0.971$$

$$GAIN_{(credit)} = INFO(D) - INFO_{(credit)}(D) = 0.971 - 0.951 = 0.020$$

Part 2:



Root + decision node RANK ≥ 0.845 : True= 3 students graduated (leaf/terminal node); False= 7 students

Decision node GPA ≤ 2.785 : True= 2 students graduated (leaf/terminal node); False= 5 students

Decision node RANK ≤ 0.815 : True= 3 students not graduated(leaf/terminal node); False= 2 students

Decision node GPA ≤ 3.375 : True= 1 student graduated(leaf/terminal node); False= 1 student(leaf/terminal node)