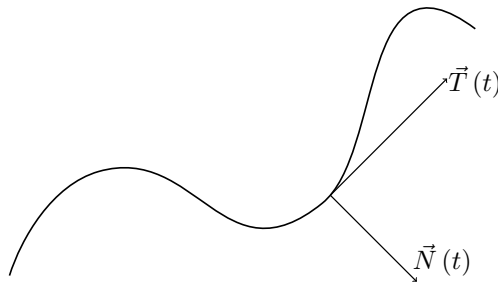


# 1 Lecture 9

## 1.1 Normal Vectors - Continued

Yesterday we saw that

$$\vec{N}(t) = \frac{\frac{d\vec{T}}{dt}}{\left| \frac{d\vec{T}}{dt} \right|}$$



**Example.** Consider the circle

$$\vec{r}(t) = (\cos t, \sin t), 0 \leq t \leq 2\pi$$

The velocity is

$$\vec{v}(t) = \vec{r}' = (-\sin t, \cos t)$$

We have  $|\vec{v}(t)| = 1$ , since

$$\vec{v}(t) \cdot \vec{v}(t) = (\sin^2 t + \cos^2 t) = 1$$

We find that  $\vec{T}(t) = \vec{v}(t)$ . To find  $\vec{N}$ , we need first

$$\frac{d\vec{T}}{dt} = \frac{d\vec{v}}{dt} = (-\cos t, -\sin t)$$

We check that  $\left| \frac{d\vec{T}}{dt} \right| = 1$ , then

$$\vec{N}(t) = (-\cos t, -\sin t) = -\vec{r}(t)$$

We compute more explicitly:

