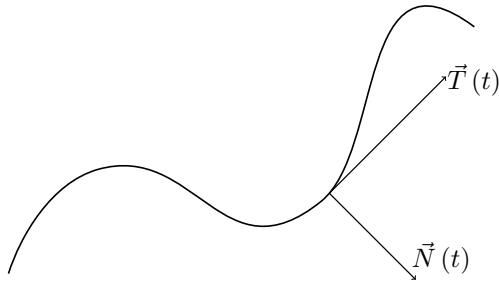


1 Lecture 9

1.1 Normal Vectors - Continued

Yesterday we saw that

$$\vec{N}(t) = \frac{\frac{d\vec{T}}{dt}}{\left| \frac{d\vec{T}}{dt} \right|}$$



Example. Consider the circle

$$\vec{r}(t) = (\cos t, \sin t), 0 \leq t \leq 2\pi$$

The velocity is

$$\vec{v}(t) = \vec{r}' = (-\sin t, \cos t)$$

We have $|\vec{v}(t)| = 1$, since

$$\vec{v}(t) \cdot \vec{v}(t) = (\sin t)^2 + (\cos t)^2 = 1$$

We find that $\vec{T}(t) = \vec{v}(t)$. To find \vec{N} , we need first

$$\frac{d\vec{T}}{dt} = \frac{d\vec{v}}{dt} = (-\cos t, -\sin t)$$

We check that $\left| \frac{d\vec{T}}{dt} \right| = 1$, then

$$\vec{N}(t) = (-\cos t, -\sin t) = -\vec{r}(t)$$

We compute more explicitly:

