# Einführung in Visual Computing

186.822

# Clipping

Werner Purgathofer



#### Viewing in the Rendering Pipeline object capture/creation scene objects in object space modeling vertex stage viewing ("vertex shader") projection transformed vertices in clip space clipping > homogenization scene in normalized device coordinates viewport transformation rasterization pixel stage shading ("fragment shader") raster image in pixel coordinates

## Overview: Clipping



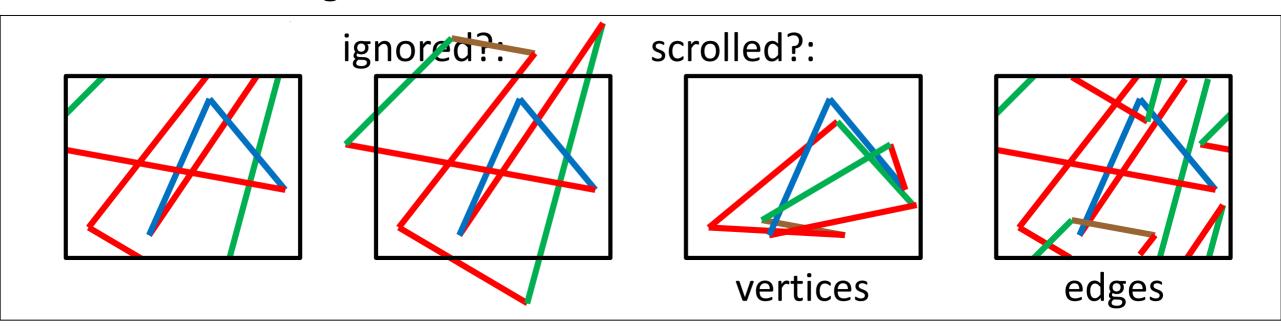
- line clipping
- polygon clipping
- triangle clipping



#### Clipping



- partly visible or completely invisible parts
- must not be ignored and must not be drawn



■ ⇒ must be cut off (as early as possible)



#### **Clipping Operations**



- remove objects outside a clip window
  - clip window: rectangle, polygon, curved boundaries
  - applied somewhere in the viewing pipeline
  - can be combined with scan conversion
  - objects to clip: points, lines, triangles, polygons, curves, text, ...



### 3 Principle Possibilities for Clipping



- analytically in world coordinates
  - reduces WC → DC transformations

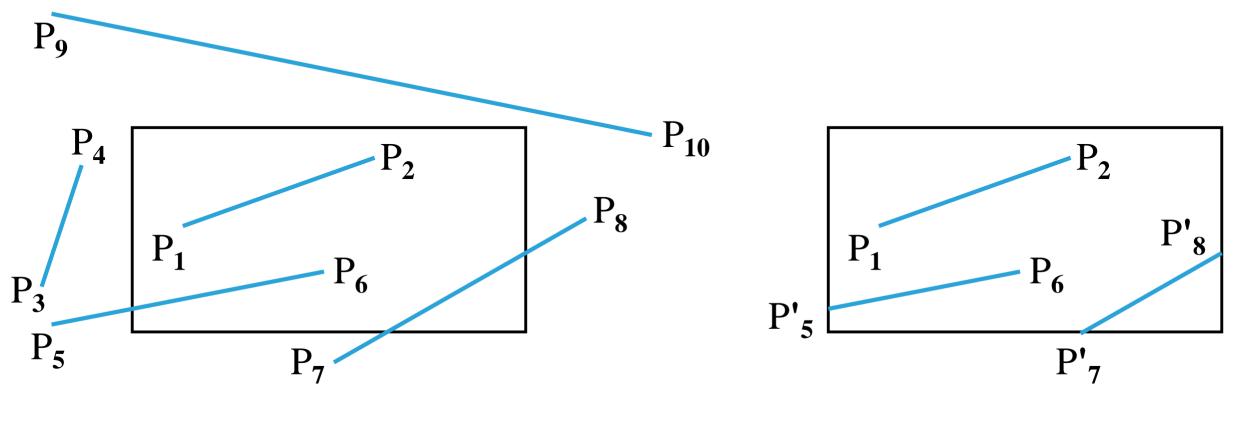
- analytically in clip coordinates
  - simple comparisons

- during raster conversation
  - = as part of the rasterization algorithm
    - may be efficient for complex primitives



## Line Clipping (1)





before clipping

after clipping

[line clipping against a rectangular clip window]



## Line Clipping (2)



- goals
  - eliminate simple cases fast
  - avoid intersection calculations

```
for endpoints (x_0, y_0), (x_{end}, y_{end})

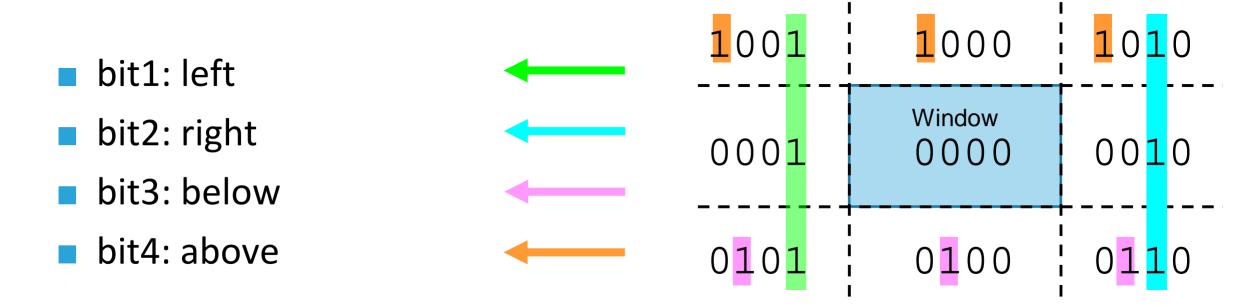
intersect parametric representation x = x_0 x_{end} - x_0 y = y_0 + u \cdot y_{end} - y_0 with window borders:

intersection \Leftrightarrow 0 < u < 1
```





assignment of region codes to line vertices



binary region codes assigned to line endpoints according to relative position with respect to the clipping rectangle

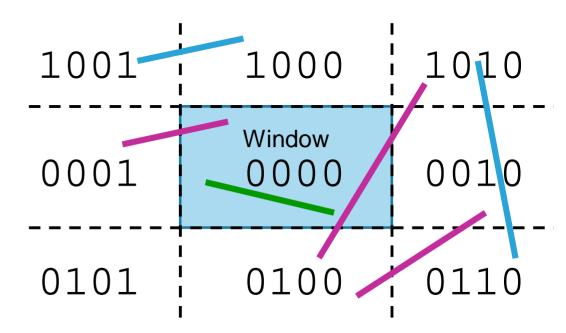




"or" of codes of both points =  $0000 \Rightarrow$  line entirely *visible* 

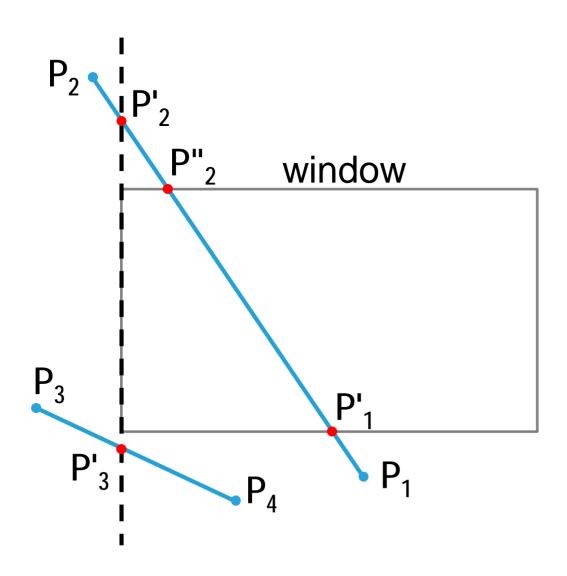
■ "and" of codes of both points  $\neq$  0000  $\Rightarrow$  line entirely *invisible* 

 $\blacksquare$  all others  $\Rightarrow$  *intersect!* 









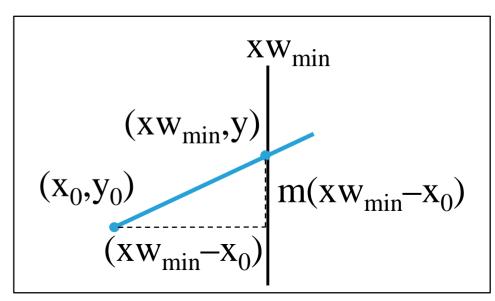
lines extending from one coordinate region to another may pass through the clip window, or they may intersect clipping boundaries without entering the window





- remaining lines
  - intersection test with bounding lines of clipping window
  - left, right, bottom, top
  - discard an outside part
  - repeat intersection test up to four times

vertical: 
$$(x = xw_{min})$$
  
 $y = y_0 + m(xw_{min} - x_0)$ 



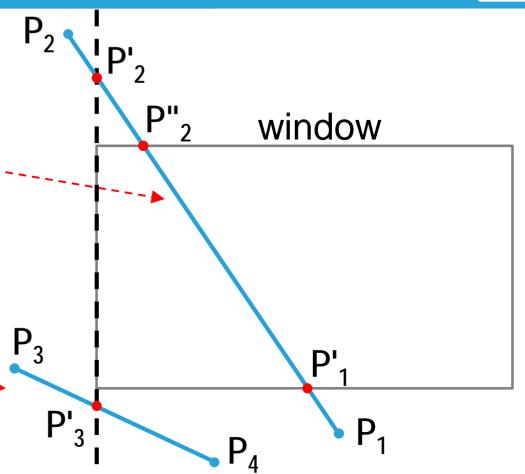
vertical:  $y = y_0 + m(xw_{min} - x_0)$ ,  $y = y_0 + m(xw_{max} - x_0)$ horizontal:  $x = x_0 + (yw_{min} - y_0)/m$ ,  $x = x_0 + (yw_{max} - y_0)/m$ 





passes through clipping window

intersects boundaries without entering clipping window



vertical: 
$$y = y_0 + m(xw_{min} - x_0)$$
,

horizontal: 
$$x = x_0 + (yw_{min} - y_0)/m$$
,  $x = x_0 + (yw_{max} - y_0)/m$ 

$$y = y_0 + m(xw_{max} - x_0)$$

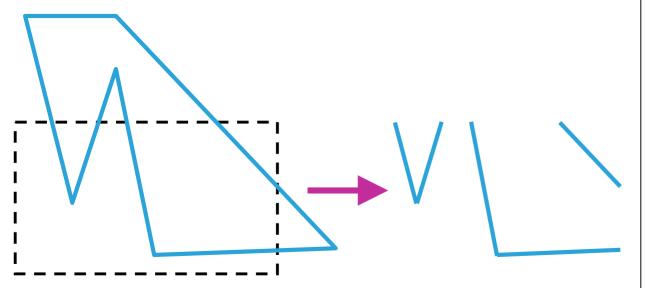
$$x = x_0 + (yw_{max} - y_0)/m$$



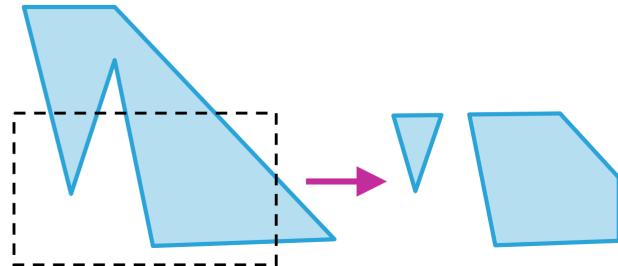
#### Polygon Clipping



- modification of line clipping
- goal: one or more closed areas



display of a polygon processed by a line-clipping algorithm

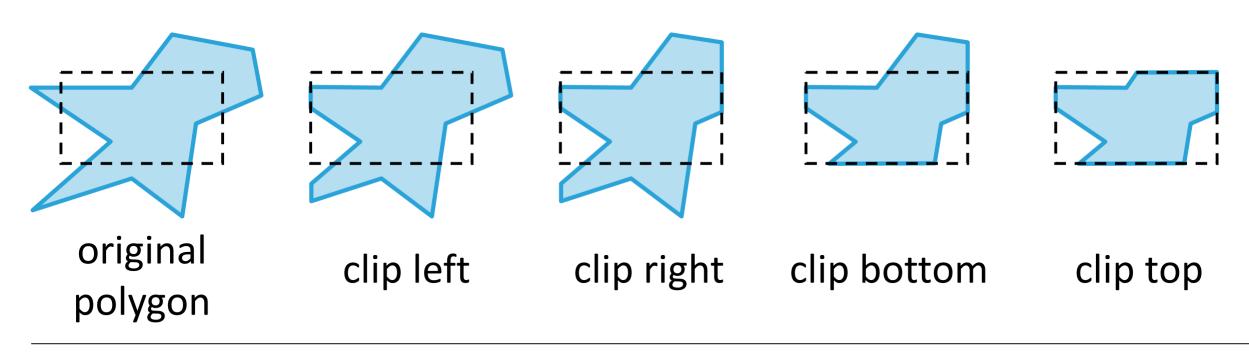


display of a correctly clipped polygon





- processing polygon boundary as a whole against each window edge
- output: list of vertices

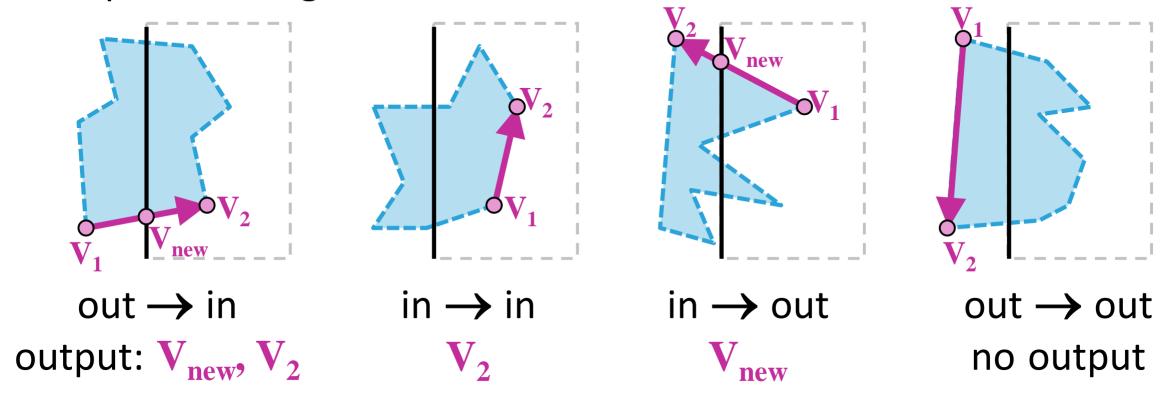


clipping a polygon against successive window boundaries





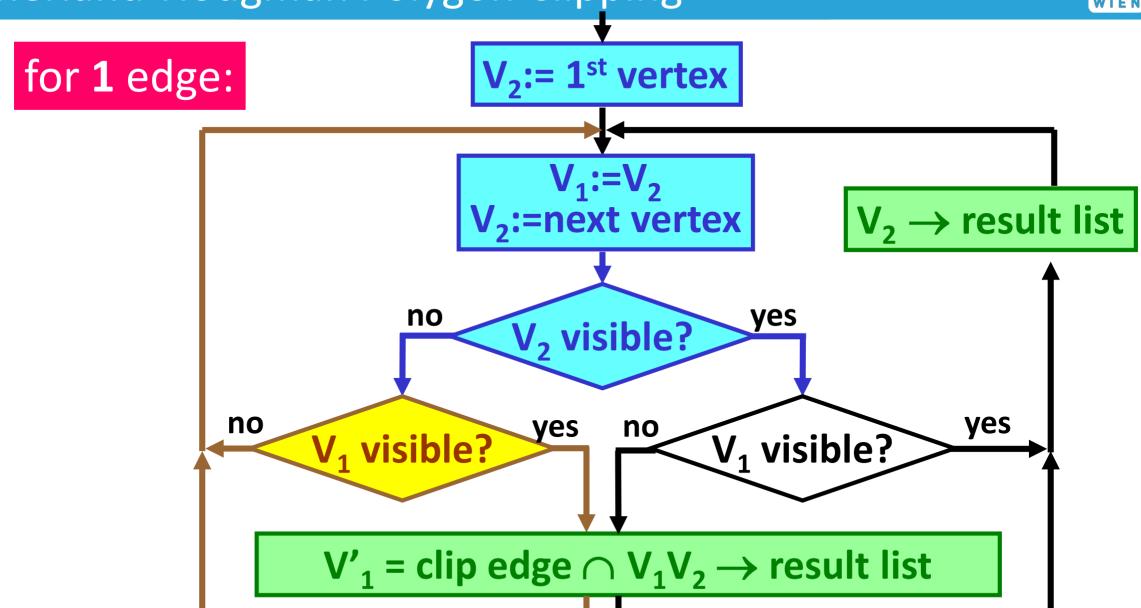
four possible edge cases



successive processing of pairs of polygon vertices against the left window boundary







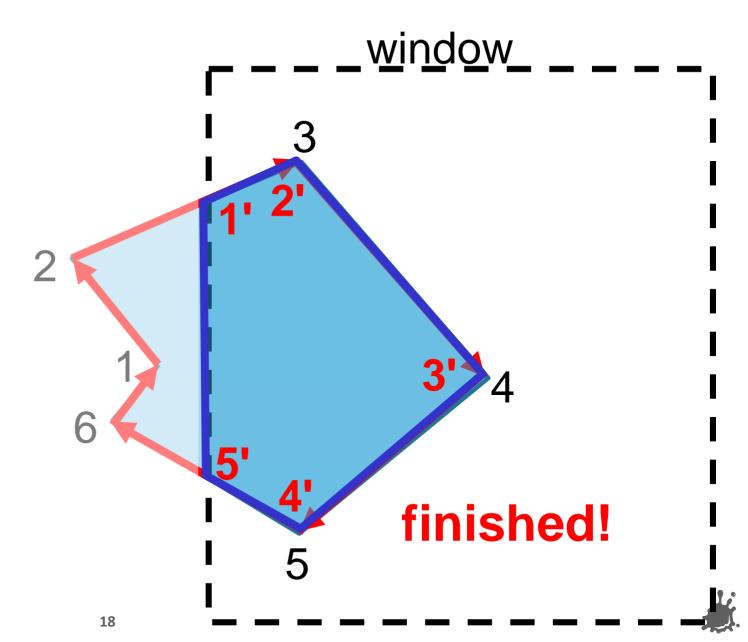


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clipping a polygon against the left boundary of a window, starting with vertex 1.

primed numbers are used to label the points in the output vertex list for this window boundary



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#### Polygon Clip: Combination of 4 Passes



the polygon is clipped against each of the 4 borders separately,
 that would produce 3 intermediate results.

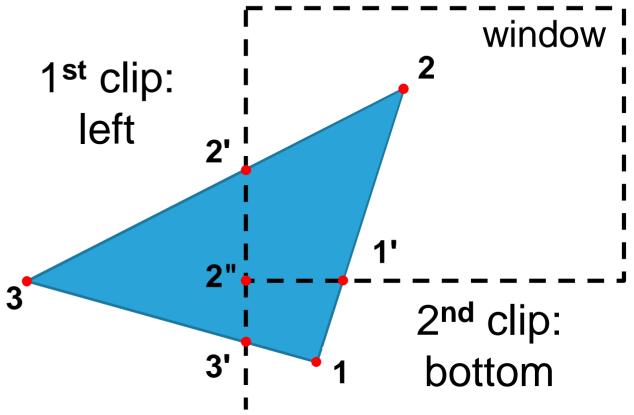
by calling the 4 tests recursively,
 (or by using a clipping pipeline)
 every result point is immediately processed on,
 so that only one result list is produced



#### Sutherland-Hodgman Clipping Example



 pipeline of boundary clippers to avoid intermediate vertex lists

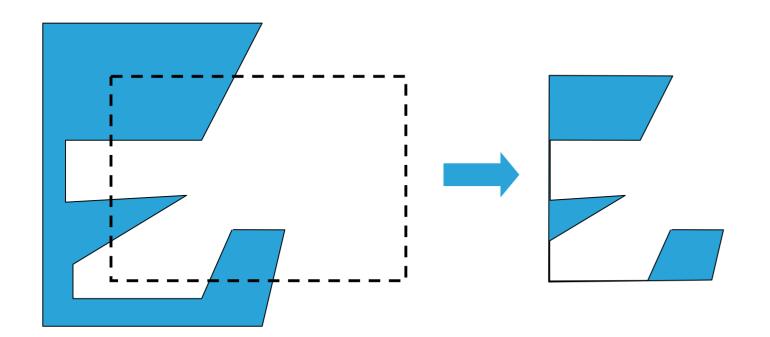


Processing the polygon vertices through a boundary-clipping pipeline. After all vertices are processed through the pipeline, the vertex list for the clipped polygon is {1', 2, 2', 2"}





- extraneous lines for concave polygons:
  - split into separate parts or
  - final check of output vertex list



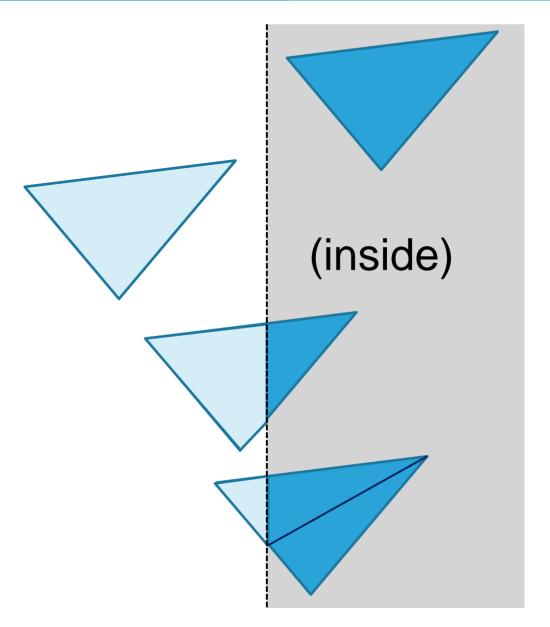
clipping the concave polygon with the Sutherland-Hodgeman clipper produces three connected areas



#### Clipping of Triangles



- often b-reps are "triangle soups"
- clipping a triangle triangle(s)
- 4 possible cases:
  - inside
  - outside
  - triangle
  - quadrilateral → 2 triangles

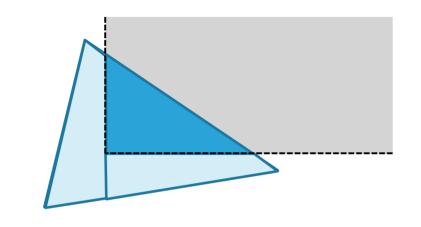


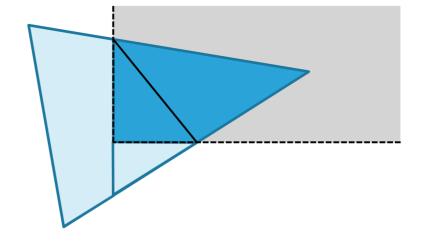


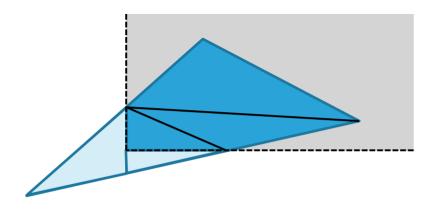
## Clipping of Triangles

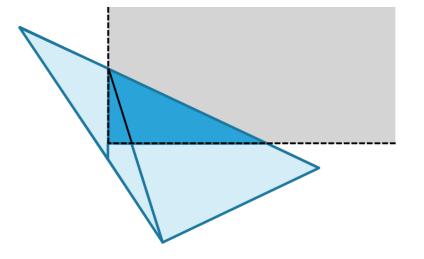


corner cases need no extra handling!







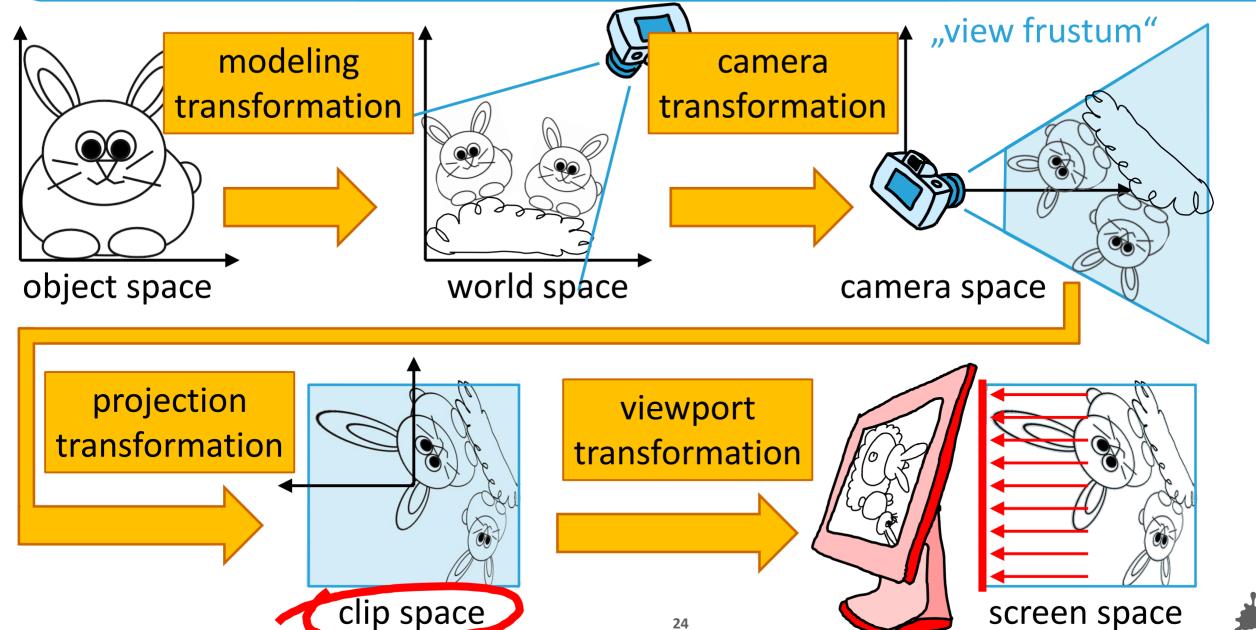




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#### From Object Space to Screen Space







#### Clipping in Clip-Space

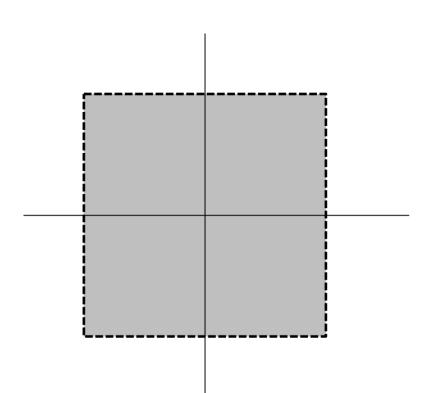


- clipping against  $x = \pm 1$ ,  $y = \pm 1$ ,  $z = \pm 1$
- (x,y,z) inside?
- only compare one value per border!



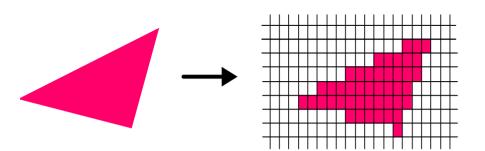
$$x = \pm h$$
,  $y = \pm h$ ,  $z = \pm h$ 

- clips points that are behind the camera!
- reduces homogenization divisions

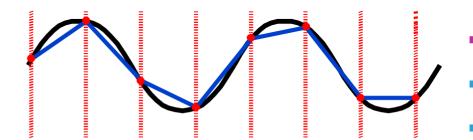




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## Antialiasing

Werner Purgathofer







#### **Antialiasing** in the Rendering Pipeline object capture/creation scene objects in object space modeling vertex stage viewing ("vertex shader") projection transformed vertices in clip space clipping + homogenization scene in normalized device coordinates viewport transformation rasterization pixel stage shading ("fragment shader") raster image in pixel coordinates

#### Aliasing and Antialiasing



what is aliasing? ['eiliæsiη]

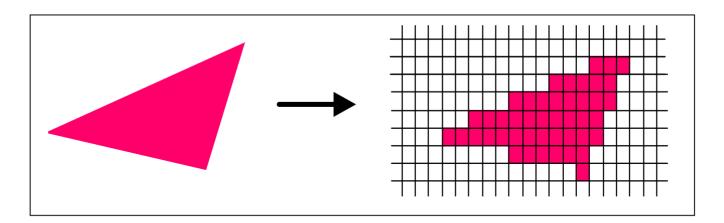
what is the reason for aliasing?

what can we do against it?



#### What is Aliasing?





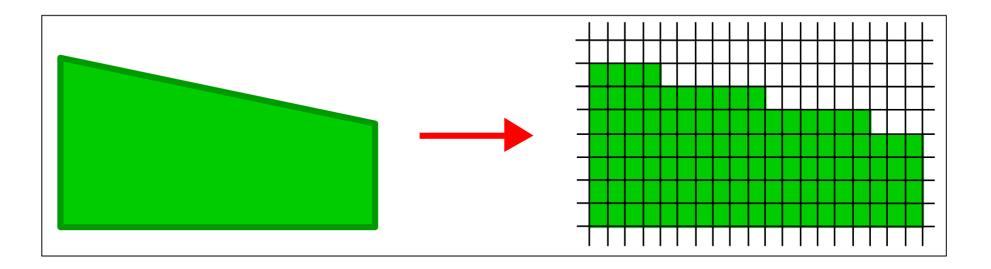
errors that are caused by the discretization of analog data to digital data

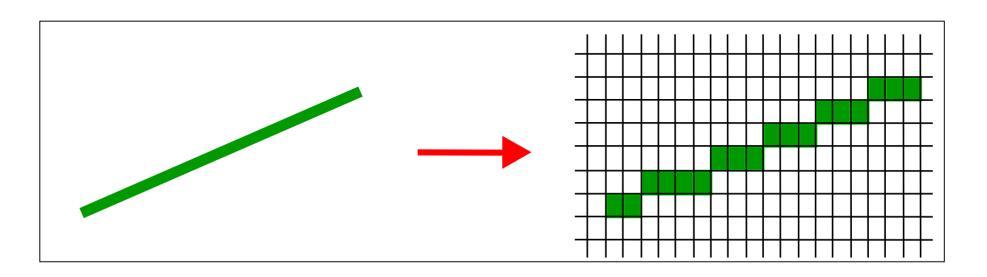
- too bad resolution
- too few colors
- too few images / sec
- geometric errors
- numeric errors



## Aliasing: Staircase Effect



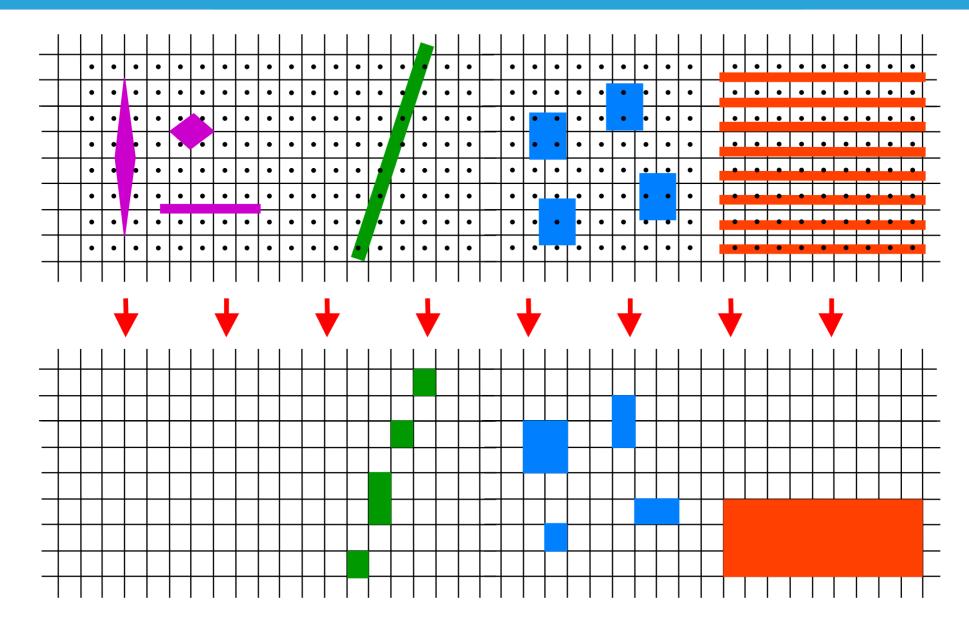






### **Various Aliasing Effects**

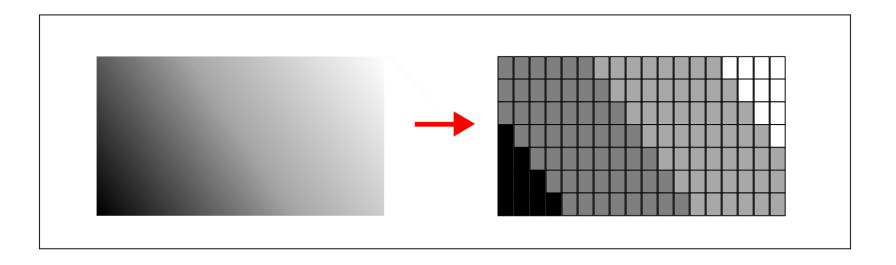






### Aliasing from too few Colors





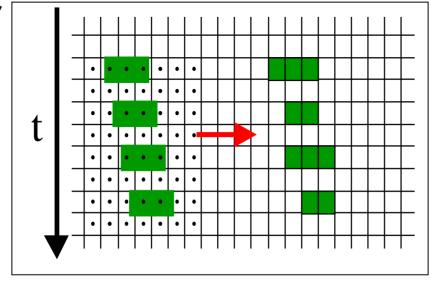
artificial color borders can appear

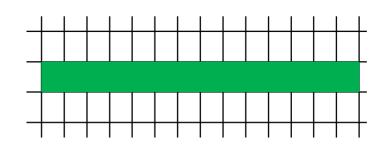


#### Aliasing in Animations

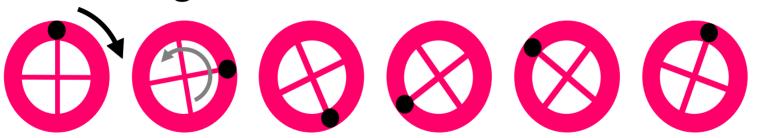


- jumping images
- "worming"





backwards rotating wheels





#### Solutions against Aliasing?



- 1. improve the devices
  - higher resolution
  - more color levels
  - faster image sequence

expensive or incompatible

- 2. improve the images = *antialiasing* 
  - postprocessing
  - prefiltering!

software!



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#### Nyquist-Shannon Sampling Theorem



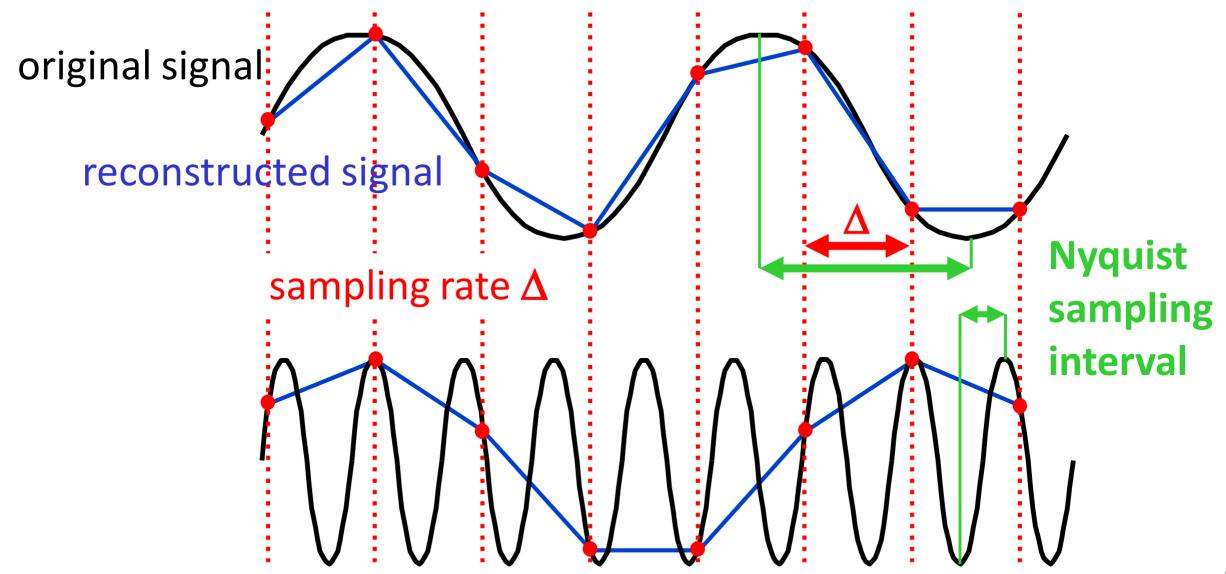
a signal can only be reconstructed without information loss if the sampling frequency is at least twice the highest frequency of the signal

this border frequency is called "Nyquist Limit"



#### **Nyquist-Shannon Sampling Theorem**







#### Antialiasing: Nyquist Sampling Frequency



a signal can only be reconstructed without information loss if the sampling frequency is at least twice the highest frequency of the signal

Nyquist sampling frequency:  $f_s = 2 f_{\rm max}$ 

$$\Delta x_s = \frac{\Delta x_{cycle}}{2}$$
 with  $\Delta x_{cycle} = 1/f_{max}$ 

i.e. sampling interval ≤ one-half cycle interval



## **Antialiasing Strategies**

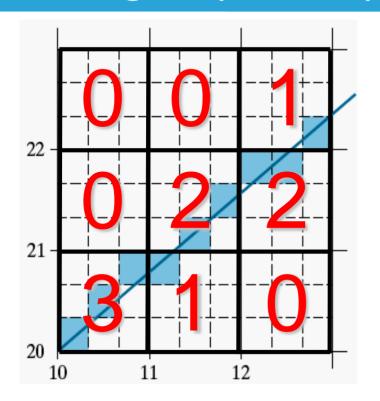


- supersampling straight-line segments
- subpixel weighting masks
- area sampling straight-line segments
- filtering techniques
- compensating for line-intensity differences
- antialiasing area boundaries
  - (adjusting boundary pixel positions)
  - adjusting boundary pixel intensity



#### Antialiasing: Supersampling Lines

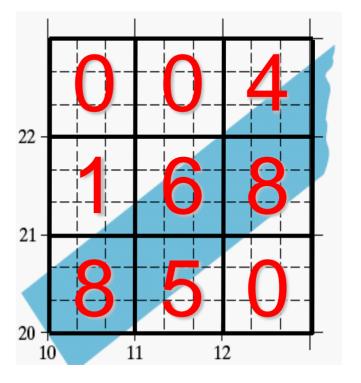




#### mathematical line

3 = max. intensity

 $0 = \min$  intensity



#### line of finite width

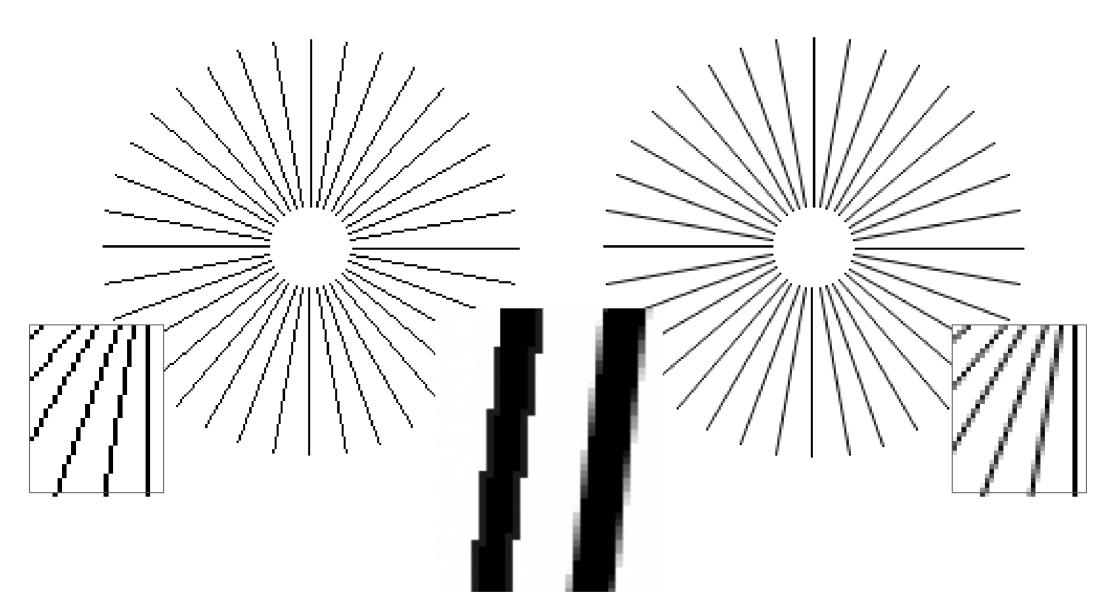
9 = max. intensity

 $0 = \min$  intensity



# Antialiasing



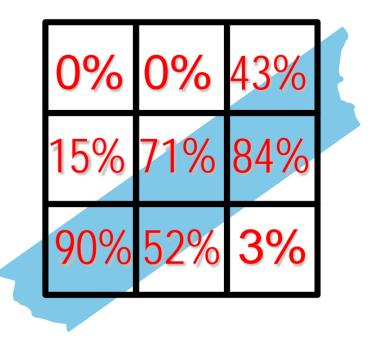




#### Antialiasing: Area Sampling Lines



- calculate the pixel coverage exactly
- can be done with incremental schemes





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#### Antialiasing: Pixel Weighting Masks



1	2	1
2	4	2
1	2	1

- more weight for center subpixels
- must be divided by sum of weights
- subpixel grids can also include some neighboring pixels

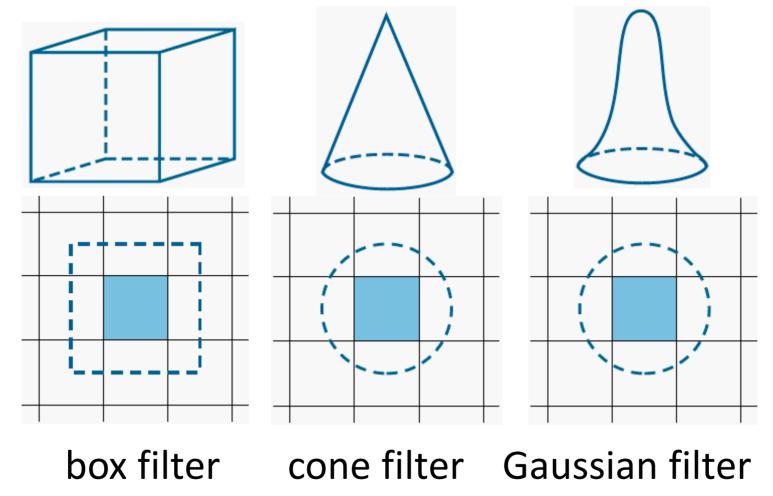
relative weights for a grid of 3x3 subpixels



## Antialiasing: Filtering Techniques

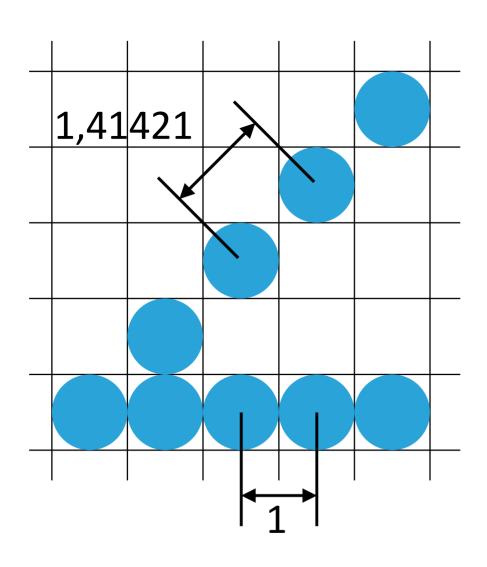


continuous overlapping weighting functions to calculate the antialiased values with integrals



#### Antialiasing: Intensity Differences



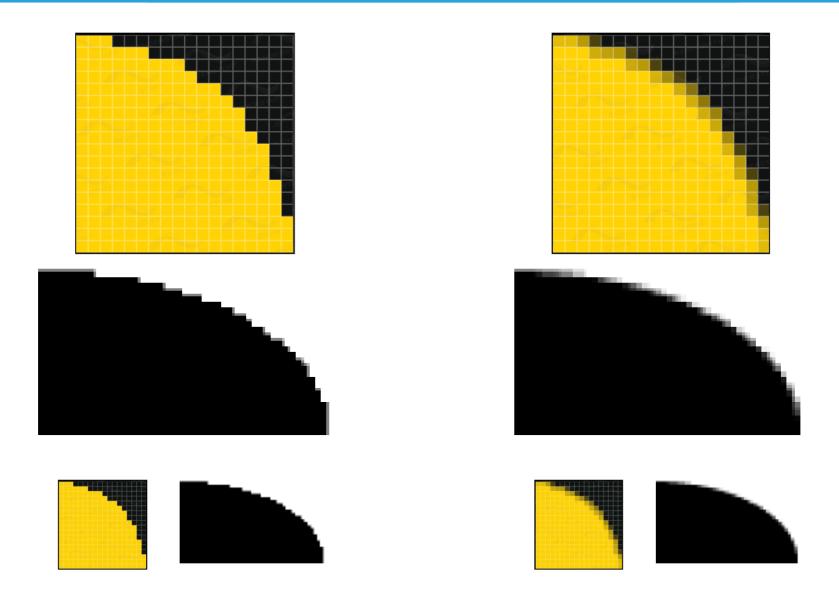


- unequal line lengths displayed with the same number of pixels in each line/row have different intensities
- proper antialiasing compensates for that!



# **Antialiasing Area Boundaries**

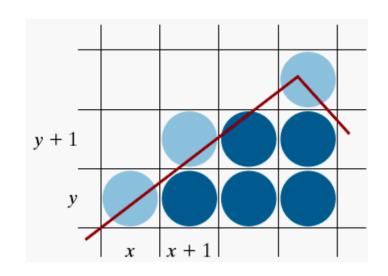




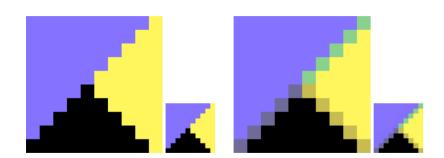


## Antialiasing Area Boundaries (1)

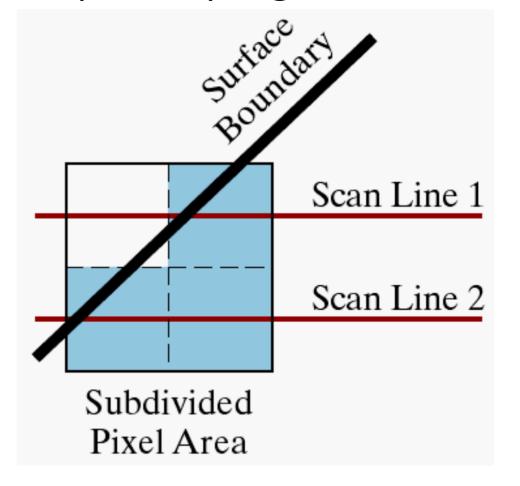




adjusting pixel intensities along an area boundary



# alternative 1: supersampling



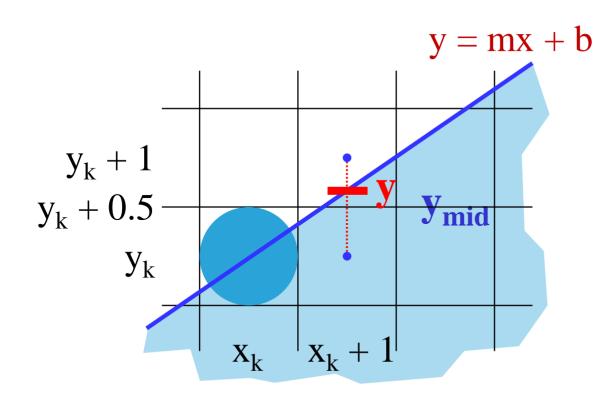


#### Antialiasing Area Boundaries (2)



#### alternative 2: similar to Bresenham algorithm

$$p' = y - y_{mid} = [m(x_k + 1) + b] - (y_k + 0.5)$$



$$p'<0 \Rightarrow y \text{ closer to } y_k$$
  
 $p'>0 \Rightarrow y \text{ closer to } y_{k+1}$ 

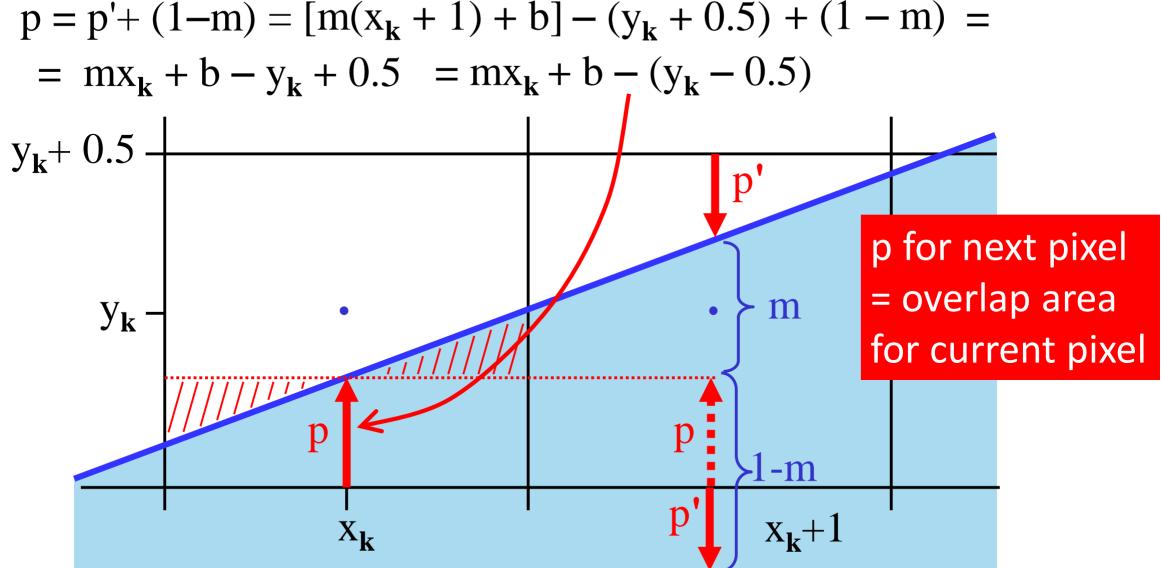
$$p = p' + (1-m)$$
:  
 $p < 1-m \Rightarrow y \text{ closer to } y_k$   
 $p > 1-m \Rightarrow y \text{ closer to } y_{k+1}$ 

(and 
$$p \in [0,1]$$
)



#### Antialiasing Area Boundaries (3)

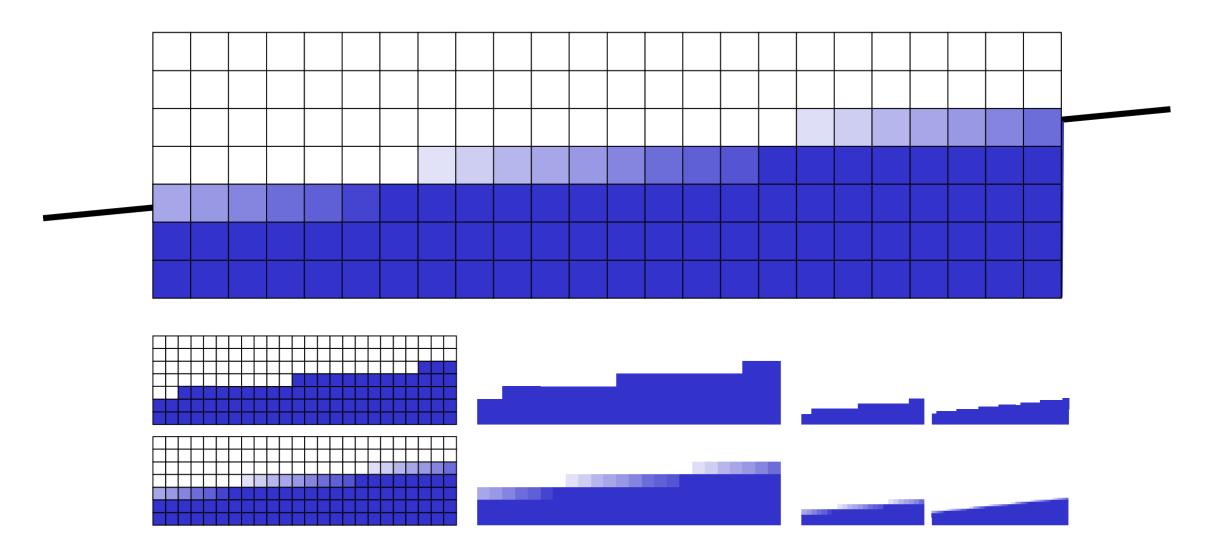






## Antialiasing Area Boundaries (4)







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## **Antialiasing Examples**



