

Location Choices over the Life Cycle: The Role of Relocation for Retirement

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Abstract

The location choice of an individual is shaped by the trade-off between job opportunities, prices, and access to amenities. I provide evidence that the determinants of this trade-off change over the individual's life cycle: the productivity of a location is more valuable for workers than retirees, and changes in spending patterns with age imply that younger and older individuals value different types of local amenities. I develop an overlapping generations spatial equilibrium model with location choices for both work and retirement periods. I quantify the model to match the distributions of young and old individuals across U.S. commuting zones and the observed mobility patterns around the retirement age. I show that differences in local exogenous productivities and amenities lead to the geographic sorting by age, which is further amplified by an endogenous adjustment of amenities and productivities to the location's age composition. I estimate that the reduction in mobility frictions observed between 1960 and 2010 allowed individuals to increasingly separate locations for work and retirement, which generated welfare gains of around 6.3 percent. I use the model to study local and aggregate effects of place-based policies that promote the reallocation of retirees to less productive cities.

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1 Introduction

An individual’s location choice is shaped by the trade-off between job opportunities, housing prices, and the access to amenities (Rosen (1979), Roback (1982), Allen & Arkolakis (2014), Desmet & Rossi-Hansberg (2013)). The determinants of this trade-off can vary significantly over the life cycle: after retirement individuals no longer directly benefit from location’s productivity, but they are still affected by local prices. Moreover, younger and older individuals might value local amenities differently due to the changes in preferences and spending patterns with age. Yet, the literature on economic geography has mostly focused on a static location choice, abstracting from modelling the life cycle.

Understanding the life cycle component of location choices becomes especially important with an ageing population trend. Indeed, the growing population of retirees might fuel the development of cities attractive for the old: for instance, between 2010 and 2020, the retirement community Villages was the fastest-growing metro area in the U.S. Recognizing this, some states and cities put in place a range of policies aimed at attracting retirees to move there.¹ However, local and aggregate effects of such policies have been largely unexplored.

In this paper, I study the role of the life cycle for individuals’ location choices and for the distribution of economic activity across space. First, I provide new empirical evidence on the sorting by age across the U.S. commuting zones (CZs). Second, I develop a theoretical framework of location choices for work and retirement periods. I use this framework to estimate the differences in the CZs values for young and old residents, and to quantify the gains from a higher life cycle mobility. I further evaluate the determinants of a city’s ability to grow by attracting retirees, and I quantify the affects of place-based policies that incentivize the relocation of the old to less productive cities. Finally, I study the implications of the ageing population for the distribution of economic activity across cities.

I start by documenting a sorting pattern by age and CZ productivity: a 1% higher CZ wage is associated with a 0.9% lower CZ old-to-young ratio.² I show that this cross-sectional relationship is driven by changes in the mobility patterns with age: more productive locations receive an inflow of individuals in the younger age cohort and an outflow of individuals in the older age cohort. Moreover, I document that the CZ age composition is correlated with the composition of its establishments: CZs with a higher old-to-young ratio have a higher number health-care centers and recreation centers per capita, but a lower number of clothing stores, movie theatres, and childcare centers per capita. Using consumer expenditure data, I show that

¹ For example, Alabama’s state employee retirement system finances a series of golf courses in local cities. City Tallahassee in Florida gives direct reallocation subsidies for retirees to move there <https://www.nytimes.com/2018/06/08/business/florida-retirees.html>

²By old-to-young ratio I define the CZ ratio of 60+ years old to 25 – 59 years old

these differences are related to the shifts in expenditure patterns with age.³

The empirical evidence discussed above emphasizes two key changes over the life cycle that might affect the location choice: a decline in working hours, which makes location's productivity less important, and changes in expenditures on local services, which affect preferences for local amenities. Also, young and old individuals might differ in their preferences for location's natural and climate amenities.⁴ I develop a theoretical framework by introducing these life cycle changes into a spatial equilibrium model, building on [Allen & Arkolakis \(2014\)](#), [Monte et al. \(2018\)](#), and [Redding & Sturm \(2020\)](#). The key model ingredients are the following: (i) individuals choose locations for both work and retirement periods subject to mobility costs of moving for retirement; (ii) workers and retirees differ in their preferences for exogenous amenities of locations and for endogenous non-tradeable services and (iii) local services are provided by amenity developers and adjust to the local age composition due to differences in preferences of the young and the old. I also assume that productivity in the tradeable sector is subject to agglomeration spillovers that are modelled in a reduced-form way as in [Allen & Arkolakis \(2014\)](#).

I estimate the model using the data on the U.S. CZs and the data on the consumer spending patterns. In particular, I estimate the model-implied gravity equation for moving for retirement, and I find that mobility costs for the old increase significantly with distance between CZs. Given the data on young and old residents, wages, rents and estimated mobility costs, I show that I can uniquely recover amenities for the young and the old across locations so that the model fully rationalizes the data. I further calibrate the fixed component of mobility costs so that the model matches the aggregate share of individuals who relocate for retirement. I document significant heterogeneity in relative amenities for young and old residents across U.S. CZs, which is partially explained by differences in CZs geography, climate, and composition of non-tradeable establishments. Next, I quantify the endogenous adjustment of amenities to the location's age composition by estimating the heterogeneity between younger and older age groups in expenditure shares on local services.

Using the fully calibrated model, I show that differences in exogenous productivities and exogenous amenities across locations lead to the geographic sorting by age. Sorting is further amplified by the endogenous adjustment of location's productivity and amenities to location's age composition. To build an intuition for this result, consider the CZs of New York (NY) and Sarasota (FL). According to the model estimates, New York is endowed with a higher exogenous productivity, whereas Sarasota is endowed with better exogenous amenities for the old. Because

³I show that while the share of spending on health care services increases significantly with age, the share of spending on clothing and childcare services declines with age.

⁴In line with the findings in [Lu \(2020\)](#) and [Schneider & Green \(1992\)](#) I show that the CZ old-to-young ratio is positively correlated with better climate (warmer winters and cooler summers) and natural amenities (percentage of water area and topography)

retirees no longer benefit from local wages, they are less willing to pay high prices in exchange for productivity. Moreover, retirees are attracted by better amenities for the old in Sarasota. Therefore, the model predicts a net reallocation of retirees from a more productive to a more amenable city. As a result, housing constraints relax in New York, tighten in Sarasota, and push more young towards New York. This further magnifies productivity differences in two cities due to the presence of productivity spillovers. Additionally, the composition of local establishments shifts with local expenditures, which makes New York even more amenable for the young (e.g., more bars and restaurants) and Sarasota even more amenable for the old (e.g., more health care facilities).

I further illustrate how the model explains the documented empirical facts on geographic sorting by age. I compute that the decline in working hours after retirement is key for reproducing the observed negative relationship between the CZ old-to-young ratio and the CZ wage. I also find that the endogenous adjustment of local services to the differences in expenditure shares between the young and the old explains most of the documented correlation between the CZ old-to-young ratio and the CZ composition of establishments.

The model estimates show that the value of a given location differs significantly for its younger and older residents. This implies large gains from separating locations for work and retirement periods. I estimate that moving from an area at the 25th percentile of the value for old to an area at the 75th percentile is equivalent to increasing the individual's income by a factor of two. This large dispersion in the location-specific utilities of the old is sustained by significant mobility costs that retirees face. I show that a decline in mobility frictions allows the old to increasingly choose CZs that are cheaper and more amenable for the old, and also allow the young to increasingly choose CZs that are more productive and more amenable for the young.

Using the MSA-level data, I show that sorting by age and location productivity increased significantly over the 1960 and 2010 period. I also document that the share of individuals who moved between states around the retirement age increased by around 22 percent from 1960 to 2000.⁵ I use this evidence together with the modelling framework to decompose the changes in geographic sorting by age over time into the changes caused by mobility frictions and into the changes caused by location-specific factors. I compute that the model implied decline in mobility frictions is equal to 36 percent and that this decline explains most of the increase in sorting over the 1960-2010 period. I estimate that the resulting welfare gains from higher life cycle mobility are equal to 6.3 percent.

⁵Using U.S. Census samples for years 1960 and 2010, I compute the share of individuals of age 55+ who changed their state of residence over the 5 year window. Same for the age group 25 – 55. The increase in the mobility of the younger age group was only around 4 percent. The comparison is available only for 1960 and 2000 Censuses due to the data availability issues.

To study the local effects of policies aimed at attracting retirees, I compute the elasticity of local retiree population with respect to a local subsidy for the relocating old. This elasticity determines the impact of policies that aim to attract retirees to move to a particular location. I find that the elasticity varies from around 0 to almost 1.4 across U.S. CZs. The response is significantly higher in locations with smaller working age population, larger share of older individuals and in locations that are closer to more populated CZs. I show that an inflow of retirees increases the variety of locally provided services, with a large shift toward the services valued more by older residents. This effect is further magnified for the less productive cities as relocating retirees bring the accumulated savings with them. Next, I evaluate place-based policies that subsidize the reallocation of retirees to smaller cities through a universal lump-sum tax paid by workers. I show that such policies contribute to a more equal distribution of amenities across cities, and, as compared to the place-based policies targeted at workers, lead to an increase in the aggregate productivity. However, these policies are not welfare improving, because the efficient allocation does not feature higher sorting of younger and older individuals.

Finally, I show that the ageing population trend increases the importance of retirement for location choices and increases the role of reallocating retirees for the spatial equilibrium. I show that predicted changes in demographics between 2020 and 2040 are expected to generate a significant shift in the distribution of economic activity across space with a reallocation of activity towards cities that are more attractive for the older age group.

Relationship to the literature. The paper relates and contributes to the studies on quantitative economic geography models that include static environments [Roback \(1982\)](#), [Allen & Arkolakis \(2014\)](#), [Redding & Sturm \(2020\)](#) summarized in [Redding & Rossi-Hansberg \(2017\)](#), and recent dynamic models [Desmet & Rossi-Hansberg \(2014\)](#), [Eckert & Peters \(2018\)](#) and [Allen & Donaldson \(2018\)](#). This paper extends existing frameworks to study the role of the individual’s life cycle: I model the location choices both for work and retirement periods, and allow for the transfer of individual’s accumulated savings across locations and time.⁶ I show how the extended model can be mapped to the data, and how it can be used for the counterfactual analysis.

The paper is related to the recent studies that model the location choice as a part of the individual dynamic problem ([Bilal & Rossi-Hansberg \(2018\)](#) and [Giannone et al. \(2019\)](#)). In my paper, I contribute to this line of work by studying how the changes in working hours and preferences over the life cycle affect location choices, and how these changes interact with spatial spillovers.⁷ Moreover, to the best of my knowledge, this paper is the first to study the changes in

⁶In the models introduced in [Desmet & Rossi-Hansberg \(2014\)](#), [Eckert & Peters \(2018\)](#) and [Allen & Donaldson \(2018\)](#) individuals consume all of the earnings made during the period, and there are no changes in working hours and preferences over time

⁷[Bilal & Rossi-Hansberg \(2018\)](#) do not model changes in working hours and preferences with age. [Giannone et al. \(2019\)](#) model features the decline in working hours after retirement, but younger and older individuals have same preferences for locations’ amenities. Another major difference is that the model in this paper allows

geographic sorting by age, and to model the local and aggregate effects of place-based policies targeting retirees.

A growing literature considers how heterogeneous preferences for consumption amenities reinforce sorting of high and low skilled households within or across cities. ([Diamond \(2016\)](#), [Guerrieri et al. \(2013\)](#), [Couture et al. \(2019\)](#), [Su \(2020\)](#), [Hoelzlein \(2019\)](#)). Closest to this paper, [Almagro & Dominguez-Ino \(2019\)](#) identifies significant heterogeneity across different demographic groups in their valuation of different amenities, and significant heterogeneity in response of amenities to demographic composition of city neighbourhoods. Motivated by these findings, I further study an endogenous city-level adjustment of amenities in a response to a changing age composition and how this endogenous response amplifies the sorting patterns of the young and the old across cities. In terms of modelling amenity spillovers, I follow the recent studies that microfound amenity spillovers through the endogenous entry of establishments producing non-tradable goods ([Almagro & Dominguez-Ino \(2019\)](#), [Couture et al. \(2019\)](#), [Hoelzlein \(2019\)](#)).

The paper complements the research on the local and aggregate effects of place-based policies. [Kline & Moretti \(2014\)](#) estimate that positive local agglomeration externalities created by a local productivity shock are offset by losses in other parts of the country. [Glaeser & Gottlieb \(2008\)](#) also argue that due to the constant elasticity of spillovers there are no gains from reallocating workers across cities. However, [Fajgelbaum & Gaubert \(2020\)](#) and [Rossi-Hansberg et al. \(2019\)](#) show that due to the differences in spatial spillovers that heterogeneous workers generate, there is a room for place-based policies that target the sorting of workers across space. In this paper, I extend their results for the dynamic life cycle setting, where individuals contribute to local spillovers differently as they age. Besides, I model endogenous amenities through the entry of local establishments, rather than introducing them in a reduced form way. Consistent with the findings in the literature, I show that the presence of productivity spillovers and location preference shocks requires optimal place-based policies targeted at workers. I further show that differences between young and old in spatial spillovers don't require additional policies targeted at the sorting by age and location.

The paper relates to the literature that studies the determinants of the mobility flows for retirement using the individual-level mobility data around the retirement age ([Lu \(2020\)](#), [Schneider & Green \(1992\)](#), [Duncombe et al. \(2001\)](#)). Retirees were found to be attracted to places with favourable climate and natural amenities and to places with lower taxes and lower living costs. [Rosenthal & Strange \(2004\)](#) show that couples near retirement age tend to move away from places with favourable business environments and towards places with high values

for the closed form solutions for the distribution of individuals across locations, which allows me to invert the model and recover the differences in the values of locations for different demographic groups.

of amenities. I further show that differences in migration patterns by age are reflected in the demographic composition of the U.S. CZs: more productive CZs have significantly lower share of old in their total population. I further argue that the valuation of local amenities might differ for young and old, and I use the aggregate data on the demographics of the U.S. CZs combined with the spatial structure of the model to recover these differences. I show that places most amenable for the old are often different from the places most amenable for the young, and I argue that part of these differences comes from the endogenous adjustment of local services to individuals' preferences.

The remainder of the paper proceeds as follows. Section 2 describes the data and definitions used in the paper. Section 3 presents empirical analysis with the description of empirical facts. Section 4 introduces the theory and section 5 discusses its efficiency properties. Sections 6 and 7 describe the calibration of the model and its quantitative analysis. Section 8 describes counterfactual exercises. Section 9 concludes.

2 Data

This paper uses the 5 percent samples of the U.S. Censuses for the years 1960, 1980, 1990, 2000 and 1 percent samples of American Community Survey for the years 2012 -2016 which I aggregate into a single observation corresponding to the year 2014. The data is from Integrated Use Microdata Series (IPUMS), [Ruggles et al. \(2015\)](#). The IPUMS data provide detailed economic and demographic information at the individual level, including data on wages, housing costs, age, education, and geographic location of residence.

To proxy for amenities, I use establishment-level data from the County Business Patterns for year 2014 and climate and geography data from United States Department of Agriculture⁸. The expenditure level data come from the NBER extracts of the Consumer Expenditure Survey (CEX), which includes all waves from 1980 through 2003. The CEX data provide household level observations on expenditures made in a wide set of consumption categories.

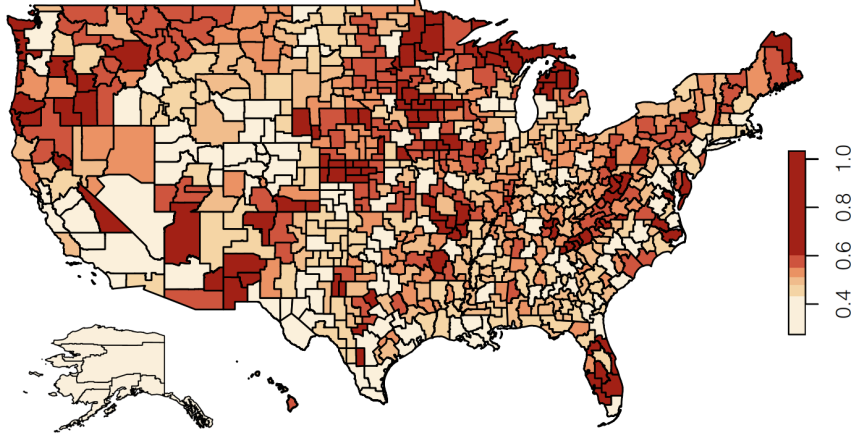
2.1 Definitions

Commuting Zones. The unit of geography is a commuting zone (CZ), which is an aggregation of the U.S. counties that partitions the U.S. and is designed to proxy for the local labor markets. I use time consistent mapping between Census Pumas and 741 US commuting zones provided by [Autor & Dorn \(2013\)](#).

Age groups. I define by the younger age group individuals whose age is between 25 and 59 years, and by the older age group individuals older than or equal to 60. Using IPUMS data

⁸<https://www.ers.usda.gov/data-products/natural-amenities-scale>

Figure 1: Demographic composition of US CZs (age 60+ to age [25, 60))



The figure shows the distribution of the ratio of older residents (age 60+) to younger residents (age 25-59) across 741 U.S. CZs for the year 2014 (average across 2011-2016 ACS)

and age group definitions, I compute the young and the old population of each CZ in the U.S.

Composition adjusted wages. To proxy for the CZ productivity, I use the IPUMS data on the average wages earned by CZ workers.⁹ I adjust wages for the differences in worker's age, sex, race, nativity and highest completed education. More details are in Appendix C. The resulting composition adjusted wages control for the differences in observable characteristics of the CZ workforce.

Quality adjusted rents. To proxy for the local prices, I use the IPUMS data on the average rents paid by the households in a given location. I adjust rents for the observed quality characteristics of the rented unit, so that to compare prices of similar units of housing across locations. More details are in Appendix C.

Amenities. I follow [Diamond \(2016\)](#) and [Almagro & Dominguez-Ino \(2019\)](#) in measuring the availability of local amenities by using the densities of establishments in different service industries. Details on the construction of the industry groups are in Appendix C. To proxy for CZ natural and climate amenities, I use the data from USDA on January hours of sun, January average temperature, July average temperature, topography and percentage of water area. This data is available only for 722 continental CZs.

Figure 2: Sorting of young and old by productivity



The figure plots CZ's ratio of individuals older than 60 to individuals between ages 25 and 60 against CZ's average wage earned by workers. Both variables are logs of the averages of demeaned values across 1980, 1990, 2000 and 2014 samples. CZs' wages are adjusted for the differences in CZs' demographics. β stands for the OLS regression coefficient and robust standard errors are in parenthesis. Regressions are weighted by location's average population across same samples. The size of each CZ circle is proportionate to its average populations.

3 Motivating empirical evidence

This section uses the data described above to document new facts on the geographic sorting by age. First, I show that there exists significant dispersion in the old-to-young ratios across U.S. CZs. Second, I document that CZ productivity is negative related to its old-to-young ratio. I show that this cross-sectional relationship arises from changes in mobility patterns with age: younger individuals tend to move to more productive CZs and then relocate to less productive CZs around the retirement age. Third, I show that CZ old-to-young ratio is correlated with the composition of its establishments in a way that is related to the shifts in expenditure patterns with age.

3.1 Geographic sorting by age

Figure 1 shows the distribution of the older age group relative to the younger age group across the U.S. CZs. There exists significant heterogeneity in the old-to-young ratios across U.S. CZs which vary from around 0.28 to almost 1. The highest ratio of old to young is in CZ Ocala in Florida, which is the home to one of the largest retirement communities in the U.S. Villages with lots of amenities specifically designed for older residents.¹⁰ The lowest ratio is in the CZ

⁹By workers I define individuals of age 17-64, who work more than 44 weeks and more than 34 hours a week

¹⁰Villages is an age-restricted community, that legally discriminates on the basis of age, and limits residency only to individuals older than 55. The available amenities include golf and country clubs, swimming pools and other recreational activities

Kodiak in Alaska.

To evaluate the magnitude of the geographic sorting by age, I compute the average dissimilarity index for the younger and the older age groups across Census samples of 1980, 1990, 2000 and 2014.¹¹ The resulting value is 0.085, which indicates that 8.5% of older individuals need to be reallocated in order to distribute them evenly across all U.S. CZs. The same index for high and low skill workers, geographic sorting of which has been widely studied in the literature, is equal to 0.143. While the degree of geographic sorting by age is lower than the degree of geographic sorting by skill, it is still large, and its magnitude might be dampened by mobility frictions that older individuals face.

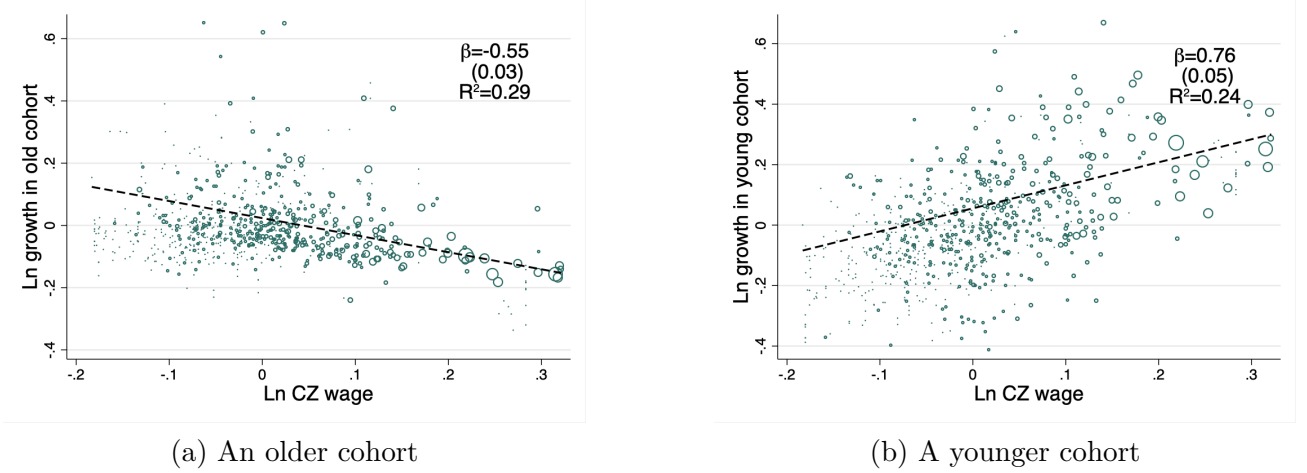
3.2 Sorting by age and location’s productivity across the U.S. CZs

One potential reason behind the geographic sorting by age is that after retirement individuals no longer benefit from location’s job opportunities. To explore this hypothesis, I study whether geographic sorting by age is systematically related to the differences in locations’ productivities. For each CZ, I compute the average composition adjusted wages and the average ratio of old to young residents across Census samples of 1980, 1990, 2000 and 2014. Figure 2 shows that the CZ old-to-young ratio is significantly and negatively related to the CZ productivity with the elasticity of -0.9 . As shown in Appendix A, the result is robust to considering retirees instead of old, to considering different age cut-offs and to using equal weights for the CZs.

Next, I study how the observed cross-sectional relationship between the CZ productivity and its age composition is related the changes in the mobility patterns with age. First, I explore the reallocation patterns of different age cohorts across U.S. CZs over a ten year period. I consider a cohort of older individuals (age 47-56) and follow them in the next decade when they potentially retire (57-66). Similarly, I consider a cohort of younger individuals (age 15-25) and follow them in the next decade when they potentially start working. Denote by $L_{m,t}^c$ the population size of a cohort c in location m and Census year t . For each CZ m , I compute the ratio $L_{m,t+10}^c/L_{m,t}^c$ to proxy for the reallocation patterns of the cohorts: a higher ratio implies that CZ m has a higher net inflow of individuals of cohort c over the ten year period. I use average values for 1980-1990, 1990-2000 and 2000-2010 Censuses to partially smooth the time effects for a particular cohort. Figure 3 shows that more productive CZs on average experience an outflow of individuals from the older cohort and an inflow of individuals from the younger cohort, suggesting that individuals move to more productive locations when young and then relocate to less productive locations for retirement.

¹¹The dissimilarity index is defined as $\frac{1}{2} \left| \frac{L_i^o}{\sum_i L_i^o} - \frac{L_i^y}{\sum_i L_i^y} \right|$ where L_i^o is the size of the older age group in the location i , and L_i^y is the size of the younger age group in i

Figure 3: Reallocation of young and old cohorts across CZs



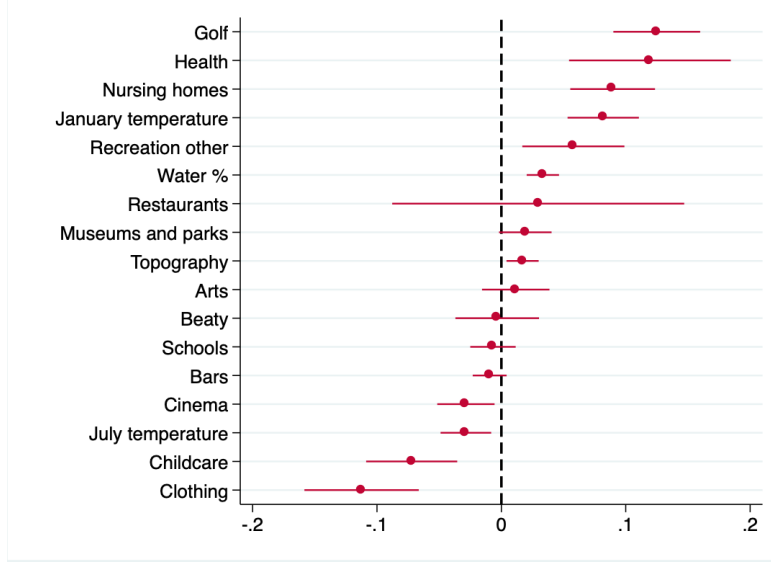
Regressions weighted by the CZ average total population across samples 1980-2010. Wages are adjusted for the location demographics. An older cohort denotes individuals who fall into the age category 47-57 in the Census year t and a younger cohort denotes individuals who fall into the age category 15-25 in the Census year t . For each CZ in the US I compute the growth in the population of a given cohort over the ten year period t and $t + 10$. Growth rates are averages across 1980-1990, 1990-2000 and 2000-2010. Wages are averages across sample years 1980-2010. Both variables are in logs.

In Appendix D, I use the data on individual's location five years ago to show that older movers have a lower probability of moving to a more productive location but a higher probability of moving to a location with a higher share of old. I also show that the largest change in mobility patterns happens around the retirement age (56-65).

3.3 CZ age composition and its amenities

Another potential reason behind the geographic sorting by age is that younger and older individuals value location's amenities differently. This section explores whether location's age composition is related to the observable measures of its amenities. I consider climate and natural variables from USDA and measures of the variability of local services. The latter is approximated by the number of CZ establishments in different non-tradeable industries per thousand residents. Figure 4 shows the results from the regression of the CZ old-to-young ratio on a set of its amenities controlling for CZ wages, population and prices. I find that CZs with a higher ratio of old to young residents have a significantly higher number of health care centers, nursing homes and recreational facilities (such as golf and country clubs) per capita, but lower number of clothing stores, childcare centers and bars per capita. In line with the results of previous studies (Lu (2020), Schneider & Green (1992)), CZs with a higher old-to-young ratio tend to have more favourable climate (warmer winters and cooler summers)

Figure 4: CZ age composition and its amenities



The figure plots point estimates and 95% confidence intervals from the single regression of the log of CZ share of old (residents of $age \geq 60$ relative to residents $25 \leq age < 60$) on the set of local amenities. Logs of CZ population, wages and rents are included as controls. Standard errors are robust to heteroskedasticity. Demographics data is from 2012-2016 ACS. Establishment counts are from CBP year 2014. Data on natural amenities is from USDA. Details on the construction of establishment categories are in appendix C.4

and more favourable natural amenities (higher percentage of water area and higher topography).

There might be two potential reasons why the composition of local establishments correlates with demographics. First, locations can differ in exogenous factors that affect the variety of some services more than the others. For example, some places can be more suitable for the entry of health care services which makes them relatively more attractive for older residents. Second, the variety of local services can adjust endogenously to local demographics as the number of firms can respond to local expenditures, making the composition of local establishments more aligned with preferences of its residents. Later, I will use the evidence on the differences in expenditure shares between younger and older age groups and the model structure to separate the two channels.

3.4 Differences in expenditure shares by age

If younger and older individuals differ in their preferences for locally provided services, these differences should be reflected in their expenditure patterns. Using the consumer expenditure data (CEX), I compute expenditure shares at the household level on a set of consumption categories roughly corresponding to local industries considered in the previous section. The

TABLE 1
AGE AND EXPENDITURE SHARES ON LOCAL SERVICES

	(1) Restaurants	(2) Bars	(3) Clothing	(4) Childcare	(5) Recreation	(6) Beauty	(7) Health	(8) NursingH
Age ≥ 60	−0.54*** (0.015)	−0.63*** (0.02)	−0.73** (0.012)	−0.96*** (0.014)	−0.58*** (0.015)	0.23*** (0.014)	1.26*** (0.014)	0.22*** (0.008)
Obs	77842	77842	77842	77842	77842	77842	77842	77842
R squared	0.16	0.12	0.18	0.05	0.17	0.03	0.17	0.3
Controls	✓	✓	✓	✓	✓	✓	✓	✓
Time FE	✓	✓	✓	✓	✓	✓	✓	✓

p -value *** $p \leq 0.01$. Robust standard errors are given in parenthesis. Dependent variable is the log of the expenditure share on a particular spending category. For the cases when expenditure shares are zero, I bottom code the expenditure data at 1 dollar. Regressions include a set of controls for sex, race, education and marital status. Category restaurants stands for the food outside of home, nightclubs stands for the alcohol consumption outside of home, and beauty stands for personal care services. More details on the construction of spending categories are in Appendix C.3

available groups are: food outside of home, alcohol consumption outside of home, clothing, personal care services, health services, low level education and childcare services, recreational services and nursing home services. More details on the data construction and the composition of the categories are in the Appendix C.3. To evaluate the effect of household's head age on the expenditure shares, I estimate the following specification for each service category:

$$\log(s_{it}^n) = \alpha + \beta \text{age}_{\geq 60} + \delta X_{it} + \psi_t + \epsilon_{it}$$

where s_{it}^n is the share of the consumption category n in individual's i total expenditures at year t , $\text{age}_{\geq 60}$ is the dummy for the age 60 or older, ψ_t is the time fixed effect and X_{it} if the set of demographic controls for race, sex, marital status and education.

Table 1 presents the estimation results. In line with the cross-sectional evidence on CZ amenities and its age composition, I find that the older demographic group spends a significantly higher share of their expenditures on health care services, nursing home, and significantly less on childcare, restaurants, nightclubs and clothing. The magnitude of the differences is large: for example, older individuals spend nearly twice more on health care services and twice less on childcare services. These effects can be directly related to changes in family composition and health care needs with age. Declining expenditure shares on clothing and restaurants are in line with the findings in Aguiar & Hurst (2013), where the authors argue that these services are complementary to working hours. Similarly, expenditures on other categories, such as personal care services, might increase with age due to their complementarity with leisure time. The main

discrepancy with the previous findings is that the share spend on recreation category actually declines with age. This result might mask significant heterogeneity in the subcomponents of the recreation consumption group in the data. ¹²

The empirical results above are consistent with the evidence documented in [Su \(2019\)](#) on the frequency of visits to local amenities by different age groups. She finds that the older age group (≥ 40) visits medical facilities and personal care facilities more often, while restaurant and bars less often as compared to the younger age group.

4 Theoretical Framework

This section introduces a model to formalize how changes in working hours and preferences for location’s amenities over the life cycle affect location choices and spatial equilibrium. The setup shares many features of the models in [Allen & Arkolakis \(2014\)](#), [Allen & Donaldson \(2018\)](#) and [Monte et al. \(2018\)](#). The key new element is that individuals live for two periods: “young” and “old”, and they choose locations for both periods subject to mobility frictions of relocating when old. The model allows for the heterogeneity in individual’s preferences, in locations’ amenities for the young and the old, and in locations’ productivities. Further, I model an endogenous adjustment of locations’ amenities to expenditures of location’s residents, similar to [Almagro & Dominguez-Ino \(2019\)](#) and [Couture et al. \(2019\)](#). The sections below describe the model setup, how the spatial equilibrium is determined, and discuss the efficiency properties of the model.

4.1 Setup

The economy consists of a set of discrete locations, which are indexed by $i = 1, \dots, J$. Locations differ in terms of their exogenous land endowments, exogenous productivities in the tradeable sector, and exogenous amenities.

There are three types of producers in each location. First, perfectly competitive firms produce a single freely tradeable good using local labor with the production function featuring agglomeration externalities. Second, each location has construction firms who use local land endowment and a final good to produce housing with a decreasing returns to scale production technology. Finally, each location has a free entry of amenity developers who compete for local housing to produce differentiated varieties in two categories of non-tradeable services.

Economy is populated by overlapping generations of individuals. Each cohort has an initial size L , and is replaced by a new cohort after T periods. I assume that individuals can be in two states: “young” and “old”. In the young state individuals inelastically supply one unit

¹²while it includes recreational activities such as fees for sporting events and country clubs, it also includes expenditures on pets and repair of recreational equipment

of labor in the tradeable sector in return for the location specific wages, and in the old state they retire and receive no labor income. Individuals in two states differ in their preferences for location specific exogenous amenities and in their preferences for two categories of locally provided services.

Agents live for $T = t_y + t_o$ periods in total, where the first t_y periods correspond to the young state, and the rest t_o periods to the old state. They choose a pair of locations (i, j) , where i is the location for the first t_y young periods and j is the location for the following t_o old periods. The first location choice is free of costs, but reallocation for the old period is subject to location pair specific mobility costs μ_{ij} .

The model structure implies that in each period of time the economy is populated by $t_y L$ young individuals and $t_o L$ old individuals. I denote by $\rho = t_o/t_y$ the relative length of the old period, which is also the relative number of old individuals in the economy. The model is static and aims at capturing the long-run steady state of the economy. For simplicity, there is no capital accumulation and the gross saving rate is equal to one.

4.1.1 Consumer preferences

The preferences of a consumer ω who lives in location i when young and in location j when old are determined as:

$$U_{ij\omega} = \sum_{t=1}^{t_y} \ln(u_{it}^y \epsilon_{i\omega}^y) + \sum_{t=t_y+1}^T \ln(u_{jt}^o \epsilon_{j\omega}^o) - t_o \ln(\mu_{ij}) \quad (1)$$

where u_{it}^y and u_{it}^o are the common components of the per period utility of young and old residents in location i at the age t , μ_{ij} is the cost of moving from i to j in terms of the consumption units of the old period, $\epsilon_{i\omega}^y$ and $\epsilon_{j\omega}^o$ are idiosyncratic preferences of individual ω for living in location i when young and in location j when old.

Define preference shock for each location path $\epsilon_{ij\omega}$ as $\ln \epsilon_{ij\omega} = t^y (\ln \epsilon_{i\omega}^y + \rho \ln \epsilon_{j\omega}^o)$. I assume that $\epsilon_{ij\omega}$ is drawn independently from an extreme-value (Fréchet) distribution:

$$F(\epsilon_{ij\omega}) = e^{\epsilon_{ij\omega}^{-\theta}}, \quad \theta > 1$$

where $\theta > 1$ controls the dispersion of idiosyncratic utility. I assume that individuals learn their realisation of the preference shocks for each path (i, j) in the young state before making location choices.

The per period common utility of young and old consumers in location i is:

$$u_{it}^y = A_i^y (c_t^y)^{\delta_c} (h_t^y)^{\delta_h} (Q_{it}^y)^{\delta_b} \quad u_{it}^o = A_i^o (c_t^o)^{\delta_c} (h_t^o)^{\delta_h} (Q_{it}^o)^{\delta_b} \quad (2)$$

where A_i^y and A_i^o are the valuations of location i exogenous amenities by young and old residents, c is the consumption of the tradeable good, h is the consumption of housing, and Q_i is the consumption of the bundle of non-tradeable services in location i . I assume that $\delta_h + \delta_c + \delta_b = 1$.

In the empirical section 3.4, I show that younger and older demographic groups systematically differ in their expenditures on local services. As argued in Aguiar & Hurst (2013) some consumption goods might be complementary to working hours (e.g. clothing, food outside of home), while others might be complementary to leisure (e.g. golf clubs). Besides, young and old might differ in their preferences health care services and childcare. To account for this, I assume that there are two categories of services that enter the bundle of non-tradeables in each location. The first group corresponds to services that are valued more by young, and the second group corresponds to services that are valued more by old:

$$Q_i^y = Q_{1i}^{\alpha_1^y} Q_{2i}^{1-\alpha_1^y} \quad Q_i^o = Q_{1,i}^{\alpha_1^o} Q_{2i}^{1-\alpha_1^o}$$

where $\alpha_1^y > \alpha_1^o$. Within a group of services competitive amenity developers in location i offer varieties that are imperfect substitutes. Individuals have CES preferences over the varieties with the common elasticity of substitution parameter σ :

$$Q_{si} = \left(\int_{m=1}^{N_{si}} q_{ms}^{\frac{\sigma-1}{\sigma}} \right)^{\frac{\sigma}{\sigma-1}}$$

where $s = 1, 2$ denotes the group of services, q_{ms} denotes the quantity of the variety m consumed in the category s , and N_{si} denotes the number of varieties in the category s in the location i .

4.1.2 Production of the tradeable good

A continuum of firms in each location produces under perfectly competitive conditions a single homogeneous product that is freely tradeable across locations. The production function is linear in labor with location-specific productivity level z_i :

$$y_i(\omega) = z_i l_i(\omega)$$

The productivity level z_i is determined as:

$$z_i = Z_i \left(\int l_i(\omega) d\omega \right)^{\gamma^P} = Z_i (L_i^y)^{\gamma^P} \quad (3)$$

where Z_i is the exogenous component that is allowed to vary across locations, and γ^P is the parameter that governs any potential agglomeration externalities operating through the size

of local production, modelled in a structural way as in [Allen & Arkolakis \(2014\)](#) and [Allen & Donaldson \(2018\)](#). As only young individuals supply labor, the agglomeration spillover is determined by the number of young in a given location. The price of the final good is the same across all locations and is normalised to be equal to one.

4.1.3 Housing sector

Producers in the construction sector in location i use intermediary input I_i and the fixed supply of land \bar{H}_i to produce housing H_i according to the following decreasing returns to scale production function:

$$H_i = \bar{H}_i I_i^{\frac{1}{1+\epsilon_h}}$$

Intermediary input is produced one to one with the final consumption good $I_i = c_{ih}$. Housing units are rented to location residents and to amenity developers at the rental rate R_i . The profit maximisation problem of the producers is:

$$\max_{I_i} R_i \bar{H}_i I_i^{\frac{1}{1+\epsilon_h}} - I_i$$

I assume that construction firms are owned by local landlords who spend profits on the consumption of the tradeable good.

4.1.4 Production of non-tradeable services

There is an infinite mass of potential amenity developers outside of the city who can produce a single variety in a given sector s . To produce q units of a variety, a developer needs to rent kq units of housing, so the marginal cost of production is location-specific and equal to kR_i . A developer in location i producing variety m in category s solves the following profit maximisation problem:

$$\max_{p_{msi}} q_{msi}(p_{msi})(p_{msi} - kR_i)$$

Amenity developers can freely enter each category of services in each location. To produce a variety they need to pay location-service specific operating costs F_{si} in terms of the rented housing units.

4.2 Consumer problem

Young individuals in location i inelastically supply one unit of labor in a location of choice and earn per period location specific wage w_i . This income is spend on the consumption of the tradeable good, housing and local services during young and old periods. Because the interest

rate and the discount rate are both assumed to be equal to one, the resulting optimal choices within the young and old periods are constant over time: $x_t^y = x^y$, $x_t^o = x^o$, for $x = c, h, q_{ms}$, $s = 1, 2$ and $\forall m$. Consider the consumption choice problem of an individual who chose the location path (i, j) . Using (1) and (2), I reformulate the problem as:

$$\max_{c^y, c^o, h^y, h^o, q_{ms}^y, q_{ms}^o} \ln A_i^y (c^y)^{\delta_c} (h^y)^{\delta_h} (Q_i^y)^{\delta_b} + \rho \ln A_j^o (c^o)^{\delta_c} (h^o)^{\delta_h} (Q_j^o)^{\delta_b} - \rho \ln \mu_{ij} + \ln \epsilon_{ij\omega} \quad (4)$$

s.t.

$$c^y + R_i h^y + \sum_{s=1}^2 \int_{m=1}^{N_{si}} p_{msi} q_{ms}^y + \rho (c_{ij}^o + R_j h_{ij}^o + \sum_{s=1}^2 \int_{m=1}^{N_{sj}} p_{msj} q_{ms}^o) = w_i \quad (5)$$

where p_{msi} denotes the price of variety m of category s in location i .

The resulting solution for the consumption of the final good and housing is:

$$c_{ij}^y = c_{ij}^o = \frac{\delta_c w_i}{1 + \rho} \quad h_{ij}^y = \frac{\delta_h w_i}{R_i(1 + \rho)} \quad h_{ij}^o = \frac{\delta_h w_i}{R_j(1 + \rho)} \quad (6)$$

The resulting demand for each variety m in categories $s = 1, 2$ is:

$$q_{msij}^y = \alpha_s^y \delta_b \frac{w_i}{1 + \rho} \frac{1}{P_{si}} \left(\frac{P_{si}}{p_{msi}} \right)^\sigma \quad q_{msij}^o = \alpha_s^o \delta_b \frac{w_i}{1 + \rho} \frac{1}{P_{sj}} \left(\frac{P_{sj}}{p_{msj}} \right)^\sigma \quad (7)$$

where the price index is $P_{si} = \left(\int_{m=1}^{N_{s,i}} p_{msi}^{1-\sigma} \right)^{\frac{1}{1-\sigma}}$.

4.3 Endogenous amenities and consumers indirect utility

Denote by L_{ij} the number of individuals who choose a location path (i, j) . Then, the total number of young and old individuals in the location i is:

$$L_i^y = t^y \sum_j L_{ij} \quad L_i^o = t^o \sum_j L_{ji}$$

The total demand for variety m of a group s in the location i is the sum of quantities demanded by young and old residents:

$$q_{msi} = t^y \sum_j L_{ij} q_{msij}^y + t^o \sum_j L_{ji} q_{msji}^o = \frac{1}{P_{si}} \left(\frac{P_{si}}{p_{msi}} \right)^\sigma t^y \left(L_i^y \delta_b \alpha_s^y \frac{w_i}{1 + \rho} + \rho \sum_j L_{ji} \delta_b \alpha_s^o \frac{w_j}{1 + \rho} \right)$$

The resulting elasticity of the demand for each variety is invariant across locations and is equal to $-\sigma$.

Amenity developers will optimally charge constant markup over their marginal costs:

$$p_{msi} = \frac{\sigma}{\sigma - 1} k R_i \quad (8)$$

Given that all firms in the service group s in location i are symmetric, in equilibrium $q_{msi} = q_{si}$ and $p_{msi} = p_{si}$. Then, the quantity demanded can be simplified as:

$$q_{si} = \frac{t^y}{N_{si} p_{si}} \left(L_i^y \delta_b \alpha_s^y \frac{w_i}{1 + \rho} + \rho \sum_j L_{ji} \delta_b \alpha_s^o \frac{w_j}{1 + \rho} \right) \quad (9)$$

The number of firms in each category adjusts so that the operating profit of the developer just offsets the fixed operating cost:

$$q_{si}(p_{si} - k R_i) = F_{si} R_i \quad (10)$$

Substituting the equilibrium prices (8) and quantities (9) into the free entry condition (10), I can get the expression for the number of firms in each location and each group of services:

$$N_{si} = \frac{\frac{t^y}{1 + \rho} \left(L_i^y \delta_b \alpha_s^y w_i + \rho \sum_j L_{ji} \delta_b \alpha_s^o w_j \right)}{F_{si} R_i \sigma} \quad (11)$$

The number of firms in each service category is proportional to local expenditures on this service category and inversely proportional to local housing prices. As young and old differ in their preferences, location demographic composition affects local expenditures and determines the composition of local establishments. Besides, the location of origin for the older residents affects local expenditures by determining the retiree income.

Combining the solution to the consumer problem (6)-(7) and the equilibrium number of firms (11), I derive the indirect utility for each location path (i, j) ¹³:

$$V_{ij\omega} = \ln \left(\frac{w_i a_i^y}{R_i^{(1-\delta_c)}} \right) + \rho \ln \left(\frac{w_i a_j^o}{R_j^{(1-\delta_c)}} \right) - \rho \ln(\mu_{ij}) + \ln(\epsilon_{ij\omega}) \quad (12)$$

where local amenities are determined as:

$$a_i^y = A_i^y \left(N_{1i}^{\alpha_1^y} N_{2i}^{(1-\alpha_1^y)} \right)^{\frac{\delta_b}{\sigma-1}} \quad a_i^o = A_i^o \left(N_{1i}^{\alpha_1^o} N_{2i}^{(1-\alpha_1^o)} \right)^{\frac{\delta_b}{\sigma-1}} \quad (13)$$

The endogenous number of establishments in a given service category N_{si} affects consumer utility through a love of variety effect. As young and old consumers have different preferences

¹³the results are equal up to a constant, which is a monotonic transformation that does not affect the final results

over local services, higher presence of individual's own demographic group makes composition of local establishment more aligned with individual's preferences.

4.4 Consumer location choice problem

I will further work with the exponential transformation of the original utility function. Denote by W_{ij} the exponent of the deterministic part of the indirect utility (12) :

$$W_{ij} = \frac{w_i^{(1+\rho)} a_i^y (a_j^o)^\rho}{R_i^{1-\delta_c} R_j^{\rho(1-\delta_c)} \mu_{ij}^\rho}$$

Individuals choose a location path that maximizes their utility:

$$\max_{ij} W_{ij} \epsilon_{ij\omega}$$

Due to the Freshet assumption on the distribution of the preference shocks, the share of individuals that chooses a location path (i, j) is given by:

$$\frac{L_{ij}}{L} = \frac{W_{ij}^\theta}{\sum_{k=1}^J \sum_{m=1}^J W_{km}^\theta}$$

The expected lifetime utility of individuals can be computed as:

$$U = E(\max_{ij} W_{ij}) = \left(\sum_{k=1}^J \sum_{m=1}^J W_{km}^\theta \right)^{\frac{1}{\theta}} \quad (14)$$

Summarizing, I can write bilateral migration flows for retirement as:

$$L_{ij} = \underbrace{\mu_{ij}^{-\theta\rho} \left(\frac{w_i^{(1+\rho)} a_i^y}{R_i^{1-\delta}} \right)^\theta}_{\text{Value of i for y}} \underbrace{\left(\frac{a_j^o}{R_j^{(1-\delta)}} \right)^{\rho\theta}}_{\text{Value of j for o}} LU^{-\theta} \quad (15)$$

Migration flows are higher into destination locations j that have better amenities for old and lower rents, out of origin locations that are more attractive for young, and among location pairs that have lower mobility costs.

4.5 Housing market

Profit maximisation problem of firms in the construction sector problems implies the following housing supply function:

$$H_i = d_h \bar{H}_i (R_i)^{\frac{1}{\epsilon_h}} \quad (16)$$

where $d_h = (1 + \epsilon_H)^{\frac{1}{\epsilon_h}}$. The parameter ϵ_h governs the inverse elasticity of the housing supply.

Given the rental rate R_i , the amount of housing demanded by consumers is:

$$H_i^h = t^y \sum_j L_{ij} h_{ij}^y + t^o \sum_j L_{ji} h_{ji}^o = \frac{t^y}{(1 + \rho)R_i} \left(L_i^y \delta_h w_i + \rho \sum_j L_{ji} \delta_h w_j \right)$$

The amount of housing demanded by amenity developers is equal to the housing used in producing local services including fixed entry costs:

$$H_i^d = t^y L_i^y k \sum_{s=1}^2 \int_{m=1}^{N_{si}} q_{ms,ij}^y + t^o \sum_j L_{ji} k \sum_{s=1}^2 \int_{m=1}^{N_{si}} q_{msji}^o + \sum_{s=1}^2 N_{si} F_{si}$$

The housing clearing condition is then:

$$H_i = H_i^h + H_i^d$$

Using (8) and (11), I simplify the condition to:

$$H_i = (1 - \delta_c) \frac{t^y}{(1 + \rho)R_i} \left(L_i^y w_i + \rho \sum_j L_{ji} w_j \right) \quad (17)$$

A fixed fraction $(1 - \delta_c)$ of individual's income is spend on local housing either directly through housing consumption or indirectly through the consumption of local services.

4.6 Equilibrium

Definition 1. For any time-invariant geography vector $\{\bar{H}_i, Z_i, A_i^y, A_i^o, \mu_{ij}\}$ a steady-state equilibrium is a vector of endogenous variables $\{L_i^y, L_i^o, R_i, w_i, N_{1i}, N_{2i}, a_i^y, a_i^o\}$ such that for any i :

1. Firms in the tradeable sector earn zero profits: $w_i = z_i$. Local productivity z_i satisfies equation (3);
2. The mobility flows between locations are consistent with individual optimal location choices (15);
3. The number of young and old in each location is determined as:

$$L_i^y = t_y \sum_j L_{ij} \quad L_i^o = t_o \sum_j L_{ji} \quad (18)$$

4. Housing supply H_i satisfies (16)

5. *Housing markets clear such that equation (17) holds*
6. *The number of firms in each service category is determined by the free entry condition of amenity developers such that equation (11) holds;*
7. *Local amenities satisfy equation (13).*

From equilibrium conditions, I can express the number of young and old in each location as a function of location amenities, wages and rents:

$$\frac{L_i^y}{L} = t_y \underbrace{\left(\frac{w_i^{(1+\rho)} a_i^y}{R_i^{1-\delta_c} U} \right)^\theta}_{\text{Value for young}} \underbrace{\sum_j \left(\frac{(a_j^o)^\rho}{R_j^{\rho(1-\delta_c)} \mu_{ij}^\rho} \right)^\theta}_{\text{Retirement option}} \quad (19)$$

$$\frac{L_i^o}{L} = t_o \underbrace{\left(\frac{a_i^o}{R_i^{(1-\delta_c)}} \right)^{\theta\rho}}_{\text{Value for old}} \underbrace{\sum_j \left(\frac{w_j^{(1+\rho)} a_j^y}{R_j^{1-\delta_c} \mu_{ji}^\rho U} \right)^\theta}_{\text{Proximity to young}} \quad (20)$$

The dynamic nature of the location choice problem and the presence of mobility costs for retirement make young and old location choices interconnected. The number of young in each location depends not only on the attractiveness of this location for young, but also on how easy it is to move from this location to a location valuable for retirement. Similarly, the number of old in each location depends both on the attractiveness of this location for old determined by amenities for old and rents, and on the proximity of this location to the locations valuable for young.

As argued in the literature, the presence of spillovers might lead to the equilibria multiplicity. Unfortunately, the existence and uniqueness techniques developed in [Allen et al. \(2015\)](#) do not directly apply to the model developed in the paper. Therefore, I proceed with numerical analysis and show that for the calibrated parameter values the solution exists and is stable.

4.7 Adjusted fundamentals

Combining equations 11 and 13, I derive the following equations for the endogenous amenities in the model:

$$a_i^y = \frac{A_i^y}{\sigma F_{1,i}^{\alpha_1^y} F_{2,i}^{\alpha_2^y}} \left(\frac{E_{1,i}^{\alpha_1^y} E_{2,i}^{\alpha_2^y}}{R_i} \right)^{\frac{\sigma_b}{\sigma-1}} \quad a_i^o = \frac{A_i^o}{\sigma F_{1,i}^{\alpha_1^o} F_{2,i}^{\alpha_2^o}} \left(\frac{E_{1,i}^{\alpha_1^o} E_{2,i}^{\alpha_2^o}}{R_i} \right)^{\frac{\sigma_b}{\sigma-1}} \quad (21)$$

where $E_{s,i}$ is total expenditure on a category s in the city i and is determined by $E_{s,i} = t^y (L_i^y \delta_b \alpha_s^y \frac{w_i}{1+\rho} + \rho \sum_j L_{ji} \delta_b \alpha_s^o \frac{w_j}{1+\rho})$.

Define by adjusted amenities for young and old the exogenous component of the equations 21:

$$\tilde{A}_i^y = \frac{A_i^y}{\sigma F_{1,i}^{\alpha_y^y} F_{2,i}^{\alpha_y^y}} \quad \tilde{A}_i^o = \frac{A_i^o}{\sigma F_{1,i}^{\alpha_o^o} F_{2,i}^{\alpha_o^o}} \quad (22)$$

Adjusted exogenous amenities are determined both by location exogenous characteristics such as climate and nature (A_i), and by location specific fixed costs of entry in non-tradable industries $F_{s,i}$. Therefore, spatial variation in the relative exogenous amenities for young and old can be rationalised not only by the differences in the valuation of climate and nature, but also by the differences in the preferences for local services. For example, if due to some exogenous reasons local entry costs into the health care industry are low, this would be reflected as relatively higher exogenous amenity for old.

Given the exogenous fundamentals $\{\tilde{A}_i^y, \tilde{A}_i^o, Z_i, \bar{H}_i, \mu_{ij}\}$, I can solve for the equilibrium set of variables $\{L_{ij}, w_i, R_i, a_i^y, a_i^o\}$ using equations 3, 18, 15, 17, 21 and 22. Therefore, I don't need to estimate the fixed cost of entry $F_{s,i}$ to compute the main equilibrium outcomes of the model.

5 Efficient Allocation and Policy

As argued in Fajgelbaum & Gaubert (2020) and Rossi-Hansberg et al. (2019), differences in productivity and amenity spillovers between demographic groups can lead to their inefficient sorting across space. I explore this idea in my setting, where differences in spillovers arise due to individual's lifecycle, and where amenity adjustment is modelled through the entry of variety producers.¹⁴

Consider a planning problem where a planner can redistribute the final good across consumers and construction producers, and reallocate housing units between local residents and local non-tradable sectors to maximise the expected lifetime utility of the individuals. The planner can't directly choose location of consumers, so the planner is bounded by the spatial mobility constraint 15. The planner also can't condition on the realization of the individual's preference shocks for location pairs. The planner problem is defined formally in Appendix B.2.

Proposition 1. *In an efficient allocation the following should hold:*

$$\underbrace{x_{ij}}_{\text{consumption cost}} + \underbrace{\lambda}_{\text{opport}} = \underbrace{z_i^* + \gamma^P z_i^*}_{\text{marginal product in } i} - \frac{x_{ij}}{\theta(1 + \rho)} \quad (23)$$

¹⁴ Rossi-Hansberg et al. (2019) considers only differences in productivity spillovers in the tradable sectors. Fajgelbaum & Gaubert (2020) considers both differences in amenity spillovers and productivity spillovers, but both are modelled in a reduced form way

$$\underbrace{R_i^* N_{si} F_{si}}_{\text{housing cost}} = \underbrace{\frac{\sigma}{\sigma-1} \frac{1}{\sigma} \frac{\delta_b}{1+\rho} \left(\alpha_s^y \sum_j x_{ij} L_{ij} + \rho \alpha_s^o \sum_j x_{ji} L_{ji} \right)}_{\text{utility gain}} \quad (24)$$

for $s = 1, 2$, where $x_{ij} = c_{ij}^y + \rho c_{ij}^o + R_i^* (h_{ij}^y + \sum_{s=1,2} N_{si} k q_{sij}^y) + \rho R_j^* (h_{ij}^o + \sum_{s=1,2} N_{sj} k q_{sij}^o)$ is the cost along the path, R_i^* is the multiplier under the housing constraint of the city i and λ is the multiplier under the labor allocation constraint

Condition (23) shows that social planner equalises the marginal cost and benefit of allocating an individual to the location path $\{i, j\}$. The marginal cost is the consumption levels along that path, the tightening of the housing constraints and the opportunity cost of allocating the individual on a different path. The marginal benefit is the marginal productivity of the individual when she is working in the location i , including the productivity spillover γ^P . In equilibrium, the individual expenditures x_{ij} are equal to location i wage: $w_i = z_i$. So the planner's optimality condition with respect to L_{ij} differs from the equilibrium one due to the presence of productivity spillovers γ^P , and also due to the dispersion in the location-specific preference shocks θ . The intuition for the latter is that the dispersion of the preference shocks leads to the variation in the marginal utilities across consumers. The planner finds it optimal to redistribute the final good away from individuals with lower marginal utility and towards the individuals with higher marginal utility. However, the planner can't condition on the preference shock realizations, so she uses that fact that more productive locations attract individuals with on average worse preference draws.

Condition (24) shows that the planner chooses the optimal mass of firms in two sectors by equalising the housing costs associated with entry with the utility gains from a higher variety of services. As compared to the equilibrium outcome, the planner internalises the love of variety gains and wants to redistribute the housing away from the residential use and towards services in the same proportion across locations equal to $\frac{\sigma}{\sigma-1}$. Therefore, the presence of endogenous amenities does not contribute to an inefficient allocation of young and old across cities. This result differs from the findings in [Fajgelbaum & Gaubert \(2020\)](#), where differences in reduced-form amenity spillovers require policies targeted at the sorting of heterogeneous agents.

Overall, depending on the trade-off between productivity spillovers and distributional inefficiency due to the preference shocks, the planner either wants to increase or decrease the concentration of young individuals in more productive cities. As location choices of young are affected by location choices of old through housing prices, one way to affect the allocation of workers is through the reallocation of retirees. In the quantitative section, I further explore whether policies that incentivise the reallocation of retirees to less productive cities are welfare improving.

6 Model calibration

This section discusses quantification of the model parameters. Section 6.1 describes the data and mapping of the model endogenous variables to empirical moments. Section 6.2 describes calibration of the structural parameters. Section 6.3 discusses the tree-step estimation procedure to recover the exogenous geography parameters.

6.1 Data

The model is calibrated to the mean outcomes across 1980, 1990, 2000 Censuses and 2012-2016 ACS. As in the empirical section, I define locations by 741 CZs in the U.S. I approximate L_i^o by the number of CZ residents older than 60.¹⁵ Similarly, I approximate L_i^y by the number of CZ residents between ages 25 and 60. I use average composition adjusted wages of local workforce as my measure of w_i , and I use average quality adjusted rents paid by local residents as my measure of R_i . Therefore, for 741 commuting zones in the U.S. I observe the vector of wages, rents and location choices $\{w_i, R_i, L_i^y, L_i^o\}$. More details on the construction of the variables are in the Appendix C

To estimate the mobility costs μ_{ij} , I additionally need the data on location choices for each location path L_{ij} . In the Census IPUMS data for the years 2000 I observe individual age, current location and location five years ago. As the retirement decision is not directly observed, I assume that the reallocation for retirement reasons occurs in a 20 year window around the average retirement age of 64. So I approximate the location choices L_{ij} with $\hat{L}_{ij} = \sum_{a=57}^{77} L_{ij}^5(a)$, where $L_{ij}^5(a)$ is the number of individuals of age a who were in the location i five years ago and currently are in the location j . While \hat{L}_{ij} represents only a subsample of all moves for retirement due to the limited 5 year window, I show in the Appendix E.3 that if individuals move for retirement with some constant probability for each year within the reallocation window, then this data limitation does not affect the estimation of mobility costs.

Finally, I use the consumer expenditure data (CEX) provided by NBER CEX extracts to estimate the differences in the expenditure shares on local services by age group. More details on the CEX dataset and the construction of the consumption groups are in Appendix C.3.

6.2 Calibrated parameters

I use CEX data for the 1980-2000 period to compute the average share of housing in consumer expenditure $\delta_h = 0.36$ ¹⁶. I calibrate the expenditure share on local non-housing goods δ_b to

¹⁵the average retirement age in the US is 64, but as shown in the empirical sections individuals might decide on changing location for retirement reasons earlier than actual retirement

¹⁶ Total expenditures exclude savings and contributions to retirement plans. Housing costs include both housing rent (imputed rent for homeowners) and utilities

TABLE 2
CALIBRATED PARAMETERS

	Value	Description	Strategy	Source
γ^P	0.06	productivity spillover	Literature	Rosenthal & Strange (2004)
θ	3.35	preference shocks shape	Calibrated	Hornbeck & Moretti (2018)
δ_h	0.36	share spend on housing	Calibrated	CEX data
δ_b	0.224	share spend on local goods	Calibrated	based on Moretti (2013)
σ	5	Substitution elasticity for amenities	Literature	Hoelzlein (2019)
$1/\epsilon_h$	1.75	elasticity of housing supply	Literature	Saiz (2010)
α_1^y	0.711	share spend on local good 1 by young	Calibrated	CEX data
α_1^o	0.464	share spend on local good 1 by old	Calibrated	CEX data
ρ	0.5	length of old period	Calibrated	Old to young ratio

match the estimate from [Moretti \(2013\)](#) that 35 percent of non-housing costs varies systematically with housing prices.¹⁷

Parameters α_1^y and α_1^o govern the degree of heterogeneity in the expenditure shares on local goods between young and old groups. I calibrate these parameters following the analysis in the section 3.4. In particular, I assume that expenditure patterns on local goods can be approximated by 8 consumption categories corresponding to local services in the CEX data (see Appendix C.3 for the details). Then I compute predicted expenditure shares on these categories for younger and older age groups. Table 3 presents the results and describes the estimation procedure. In line with the results in the section 3.4, there exists significant heterogeneity between younger and older demographic groups in their expenditure patterns: e.g. the older group spends much more on healthcare services, while the younger group spends more on clothing, restaurants and childcare. I further aggregate the expenditure categories into two broader groups. Group 1 includes categories where the younger group spends a higher share of their income than the older group: restaurants, bars, clothing, childcare services and recreation. Other categories are included in the group 2: healthcare, nursing homes and beauty services. The resulting parameters $\alpha_1^y = 0.711$ and $\alpha_1^o = 0.464$ are the expenditure shares on the first category for the younger and older age groups correspondingly.

Parameter σ governs the elasticity of demand for consumption amenities. [Dolfen et al. \(2019\)](#) estimate elasticity of demand $\sigma = 6.1$ for the offline retail stores in the U.S, [Couture et al. \(2019\)](#) estimate $\sigma = 6.5$ for the U.S. restaurants, gyms, movie-theatres, and outdoor amenities, [Su \(2019\)](#) reports values between 3.69 and 16 for disaggregated local sectors, and in particular estimates $\sigma \in [4.26, 7.11]$ for medical facilities. As I use aggregated sectors, I follow [Hoelzlein \(2019\)](#) and choose $\sigma = 5$ which is towards the lower end of the empirical estimates.

¹⁷ The paper estimates the local component of non-housing costs by regressing changes in consumer price indices for individual cities (reported by BLS) on housing price changes within cities

TABLE 3
PREDICTED EXPENDITURE SHARES ON LOCAL SERVICES

	(1) Restaurants	(2) Bars	(3) Clothing	(4) Childcare	(5) Recreation	(6) Beauty	(7) Health	(8) NursingH
$25 \leq age < 60$	0.223	0.025	0.262	0.035	0.165	0.05	0.24	0
$age \geq 60$	0.17	0.014	0.155	0.004	0.121	0.056	0.476	0.004

Table shows the predicted expenditure shares for younger and older age groups. First, I compute the total expenditures on 8 categories and the shares corresponding to each separate group. Then, I regress the resulting shares on age dummy (≥ 60), time fixed effects and a set of controls for sex, race, education and marital status. Finally, I compute the predicted values for the two age group dummy variables, keeping all the controls at their average values.

In the model, parameter θ governs the elasticity of the individual location choices with respect to location fundamentals. I calibrate θ so that the average employment response to exogenous local TFP shocks matches the estimates from [Hornbeck & Moretti \(2018\)](#).¹⁸

Finally, I set $\rho = 0.5$ to match the aggregate ratio of older to younger demographic groups in the data. Parameters L and t_y are normalised, as they only affect the scaling of the model variables.

Parameters from the Literature I set productivity spillover $\gamma^P = 0.06$ based on the empirical estimates of productivity spillovers summarized in [Rosenthal & Strange \(2004\)](#).¹⁹ [Saiz \(2010\)](#) estimates developed land supply elasticities for 95 metropolitan statistical areas in the United States. I calibrate $1/\epsilon_H$ to the population-weighted average of these elasticities equal to 1.75.

6.3 Mapping of the model to the data

I now describe the three step estimation procedure to recover exogenous geography $\{\mu_{ij}, \tilde{A}_i^y, \tilde{A}_i^o, Z_i, \bar{H}_i\}$ for U.S. CZs. First, I estimate the gravity for retirement flows to evaluate how mobility costs vary with the distance between locations. Second, I calibrate composite amenities $\{a_i^y, a_i^o\}$ and fixed component of mobility costs, so that the model exactly matches the data $\{L_i^y, L_i^o, w_i, R_i\}$ and the share of old who relocate for retirement. Finally, I decompose the model implied composite amenities, observed wages and housing prices into exogenous and endogenous components using the calibrated structural parameters described in section 6.2.

¹⁸[Hornbeck & Moretti \(2018\)](#) estimate that a 1% increase in city manufacturing TFP during the period 1980-1990 is associated with an average local employment increase by 4.16%.

¹⁹the empirical estimates are found to be in the rage of 3% – 8%

6.3.1 Gravity for retirement flows

I assume that mobility costs are a constant elasticity function of the physical distance between locations and a stochastic error for all pairs of commuting zones with positive commuting flows:

$$\ln \mu_{ij} = \begin{cases} \ln \kappa + \xi \ln \text{dist}_{ij} + \epsilon_{ij} & \text{if } i \neq j \\ 0 & \text{if } i = j \end{cases} \quad (25)$$

where κ is the fixed cost of reallocation, ξ is the elasticity of the mobility cost with respect to distance and ϵ_{ij} is an unobserved idiosyncratic component of commuting costs specific to a commuting zone pair. In my baseline specification, I follow [Redding & Sturm \(2020\)](#) and assume prohibitive mobility costs ($\mu_{ij} \rightarrow \infty$) for the pairs of commuting zones with zero retirement flows. So I restrict my sample to CZs with positive retirement flows.

Combining the specification for mobility costs (25) and the gravity equation for migration flows (15), I derive the gravity equation for the log retirement flows:

$$\ln \left(\frac{L_{ij}}{L} \right) = -\theta \rho \xi \ln \text{dist}_{ij} + \psi_i + \pi_j + e_{ij}$$

where the location of origin fixed effect includes local wage, amenities for young and rents, and expected utility and fixed component of the mobility cost $\psi_i = (1 + \rho)\theta \ln w_i + \theta \ln a_i^y - (1 - \delta)\theta \ln R_i - \theta \ln(U) - \theta \ln \kappa$, the location destination fixed effect includes amenities for old and rents $\pi_j = \rho\theta \ln a_j^o - \rho\theta(1 - \delta) \ln R_j$, and the error term represents idiosyncratic error in mobility costs between commuting zones $e_{ij} = -\theta\epsilon_{ij}$.

In my baseline specification, I estimate the composite parameter $-\theta\xi\rho$ using OLS with origin and destination fixed effects. As described in the data section 6.1, I approximate flows L_{ij} with $\hat{L}_{ij} = \sum_{a=57}^{77} L_{ij}^5(a)$, where $L_{ij}^5(a)$ is the number of individuals of age a who were in the location i five years ago and currently are in the location j from the US Census data for the year 2000. I observe the non zero migration flows for 101445 pairs of commuting zones.²⁰

Estimation results for the baseline specification are presented in table 4 column (1). The elasticity of retirees migration flows with respect to distance is equal to -0.92 and is significant at the 1% level. From the regression R^2 , the gravity equation explains around 71% percent of the variation in bilateral mobility patterns, meaning that gravity framework works well for explaining the migration patterns for retirement. In column (2), I relax the assumption of infinite mobility costs for the commuting zone pairs with zero mobility flows, and estimate the gravity equation using the Poisson pseudo maximum likelihood estimator of [Santos & Tenreiro](#)

²⁰In the Census data I observe mobility at the PUMA level. I then redistribute the migration flows across PUMAs to migration flows across CZs using the probabilistic matching based on the [Autor & Dorn \(2013\)](#) crosswalk. More details are in Appendix E.2

TABLE 4
GRAVITY EQUATION FOR RETIREMENT FLOWS

Dependent Variable	(1) $\ln\left(\frac{L_{ij}}{L}\right)$	(2) $\ln\left(\frac{L_{ij}}{L}\right)$
$\ln dist_{ij}(-\theta\rho\xi)$	-0.92*** (0.005)	-1.42*** (0.014)
Estimation	OLS	Poisson PML
Observations	101445	548340
R^2	0.72	-
Origin and destination fixed effects	✓	✓

Notes: The dependent variable $\frac{L_{ij}}{L}$ is the share of individuals of age 57-77 who lives in the CZ i 5 years ago and live in the CZ j in 2000. The variable $dist_{ij}$ denotes the distance in miles between commuting zones i and j . Poisson PML is Poisson pseudo maximum likelihood estimator. p -value *** $p \leq 0.01$. Standard errors are clustered at the commuting zone level.

(2006) on a full sample of CZ pairs. I find a similar pattern of results with a higher elasticity of -1.42 .

The estimation above provide the first component of the mobility costs $dist_{ij}^{-\theta\rho\xi}$. In the next section, I discuss how to calibrate the fixed component of the mobility costs κ to match the share of old that reallocates for retirement

6.3.2 Recovering the composite amenities a_i^y and a_i^o and the fixed mobility cost κ

Given the estimated mobility costs μ_{ij} , I prove that I can uniquely recover composite location amenities a_i^y and a_i^o by inverting the equilibrium conditions for young and old location choices.

Proposition 2. *Given observed data on $\{L_i^y, L_i^o, w_i, R_i\}$ and estimated mobility costs μ_{ij} , there exist unique (up to scale) values of $\{a_i^y, a_i^o\}$ that satisfy model equilibrium conditions 26 and 27:*

$$\frac{L_i^y}{L} = \left(\frac{w_i^{(1+\rho)} a_i^y}{R_i^{1-\delta_c} U} \right)^\theta \sum_j \left(\frac{(a_j^o)^\rho}{R_j^{\rho(1-\delta_c)} \mu_{ij}} \right)^\theta \quad (26)$$

$$\frac{L_i^o}{L} = \rho \left(\frac{a_i^o}{R_i^{(1-\delta_c)}} \right)^{\theta\rho} \sum_j \left(\frac{w_j^{(1+\rho)} a_j^y}{R_j^{1-\delta_c} \mu_{ij} U} \right)^\theta \quad (27)$$

Proof. See Appendix B.3 □

The model predicts high amenities for young in places that have high young population despite high housing prices, low wages and bad access to amenable places for retirement.

Similarly, the model predicts high amenities for old in places that have high old population despite bad access to the locations valuable for young and high housing prices.

Using the results from the proposition 2, for each value of the fixed cost κ I can uniquely recover the model implied amenities a_i^y and a_i^o . Then, I can compute the model implied aggregate share of individuals who moves for retirement:

$$Movers = 1 - \sum_i \frac{L_{ii}}{L} = 1 - \frac{\sum_i \left(w_i^{(1+\rho)} R_i^{-(1-\delta_c)(1+\rho)} a_i^y (a_i^o)^\rho \right)^\theta}{\sum_i \sum_j \left(w_i^{(1+\rho)} R_i^{-(1-\delta_c)} a_i^y R_j^{-(1-\delta_c)\rho} (a_j^o)^\rho \mu_{ij}^\rho \right)^\theta}$$

Parameter κ can be calibrated so that the model implied reallocation share matches the corresponding share in the data. Using Census data, I compute that 7.5% of individuals in the age group 60-65 changed a CZ within a 5 year period. This reallocation share misses all the moves that individuals make after the age of 65. Finkelstein et al. (2019) document that 10% of Medicare enrollees between ages 65 and 99 moved between CZs at least once over the 15 year period.²¹ Assuming that 20% of individuals move more than once²², this implies that roughly 14% of individuals in the older age group move within 20 year window. Therefore, I use this reallocation share as my target in the calibration.

I find that there exists significant dispersion in the relative amenities for old a_o/a_y across the U.S. commuting zones. Tables 5 and 6 list commuting zones with lowest and highest relative amenities for old:

CZ Name	State	a_o/a_y
Anchorage	Alaska	0.08
Fairbanks	Alaska	0.11
Bethel	Alaska	0.16
Unalaska	Alaska	0.17
Los Angeles	California	0.18

Table 5: CZ with lowest a_o/a_y

CZ Name	State	a_o/a_y
Port St. Lucie	Florida	16
Sarasota	Florida	13.6
Tampa	Florida	12.6
Miami	Florida	10
Toms River	New Jersey	5.8

Table 6: CZ with highest a_o/a_y

CZ with the worst relative amenities for old is Anchorage in Alaska, followed by Fairbanks in Alaska. These cities might be less attractive for older residents due to severe climate conditions.

²¹Finkelstein et al. (2019) use administrative data on Medicare enrollees for a 100% panel of Medicare beneficiaries (69 million enrollees) for the period 1999-2014. Over this period of time 7 million enrollees changed their CZ

²²Finkelstein et al. (2019) report that 2.4 million out of 7 million movers move more than twice

Places with the best amenities for old are Port St. Lucie in Florida, followed by Sarasota in Florida. These cities not only have much nicer natural amenities and better climate, but also lots of recreational activities for older residents such as golf and country clubs and swimming pools.

To study whether model implied amenities are systematically related to the observable measures of amenities, I regress the ratio a_o/a_y on a set of climate and geography variables and on densities of different local establishments. Table G2 shows results. As predicted by the model, amenities are related to the composition of local establishments: a_o/a_y is significantly higher in locations with higher densities of gold and country clubs, health and nursing care services and personal care services, but lower in locations with higher density of restaurants, movie theatres and childcare services. Besides, relative amenities for old are significantly higher in locations with higher percentage of the water area and with warmer winter temperatures.

6.4 Exogenous productivities, amenities and housing supplies

This section shows how given the structural parameters calibrated in section 6.2, composite amenities $\{a_i^y, a_i^o\}$ recovered in section 6.3.2 and data $\{L_i^y, R_i, w_i\}$, I can invert the remaining exogenous fundamentals of the model $\{\tilde{A}_i^y, \tilde{A}_i^o, Z_i, \bar{H}_i\}$. First, I compute model implied migration flows \hat{L}_{ij} according to the equation 15. This allows me to calibrate exogenous adjusted amenities for young and old across locations using model implied equation for amenities (22):

$$\tilde{A}_i^y = a_i^y \left(\frac{E_{1i}^{\alpha_1^y} E_{2i}^{(1-\alpha_1^y)}}{R_i} \right)^{\frac{\delta_b}{\sigma-1}} \quad \tilde{A}_i^o = a_i^o \left(\frac{E_{1i}^{\alpha_1^o} E_{2i}^{(1-\alpha_1^o)}}{R_i} \right)^{\frac{\delta_b}{\sigma-1}}$$

where E_{si} is the total expenditure in the city i on category s and can be approximated as:

$$\hat{E}_{s,i} = \left(L_i^y \delta_b \alpha_s^y \frac{w_i}{1+\rho} + \rho \sum_j \hat{L}_{ji} \delta_b \alpha_s^o \frac{w_j}{1+\rho} \right)$$

Given the observed wage vector $\{w_i\}$ and calibrated productivity spillover value γ^P , I can invert the exogenous productivities across locations:

$$Z_i = w_i (L_i^y)^{-\gamma^P}$$

Finally, I given the data $\{R_i, w_i, L_i^y\}$ and the predicted flows \hat{L}_{ij} , I recover exogenous housing

supplies $\{\overline{H}_i\}$ using model equations (16) and (17)

$$\overline{H}_i = \frac{(1 - \delta_c)}{d_h(1 + \rho)} R_i^{-(1 + \frac{1}{\epsilon_h})} (L_i^y w_i + \rho \sum \hat{L}_{ji} w_j)$$

where $d_h = (1 + \epsilon_H)^{\frac{1}{\epsilon_h}}$

7 Quantitative Analysis of the Model

In this section, I explore quantitatively the main features of the model. Section 7.1 studies how the life cycle affects the distribution of economic activity across space. Section 7.2 uses the model to analyse the drivers behind the motivating empirical facts documented in the empirical section. To summarize, I show that differences in location's exogenous amenities for young and old, and exogenous productivities lead to the geographic sorting by age, which is further amplified by an endogenous adjustment of productivities and amenities. I estimate that the adjustment of the number of firms to local expenditures is the key mechanism to explain the observed correlation between CZ old-to-young ratios and CZ composition of establishments. Finally, I show that the decline in working hours after retirement is driving the observed negative relationship between CZ old-to-young ratios and the CZ wages.

Section 7.3 studies the quantitative importance of mobility frictions of moving for retirement. Section 7.4 studies the determinants of the CZ's ability to grow by attracting retirees.

7.1 Life cycle and spatial equilibrium

To study the importance of the life cycle for the distribution of economic activity across cities, I compare the Gini coefficients for the main endogenous local variables in the full model (as in the data) with the restricted version of the model where all individuals are young workers who make one static location choice ($t^y = T$ and $t^o = 0$). To further isolate the role of reallocating retirees, I additionally compute the Gini coefficients for the case when older individuals don't move for retirement. Table 7 presents the results. Overall, life cycle contributes to a more equal distribution of location population sizes, rents and amenities. First, some cities have an exogenous advantage in their amenities for old, and this allows them to attract both young and old residents, which contributes to a more equal distribution of economic activity across space. Moreover, older individuals move out of more expensive cities towards smaller and cheaper places. Additionally, they bring their higher earnings with them, which further contributes to a more equal distribution of prices and amenities across locations.

TABLE 7
GINI COEFFICIENTS FOR THE MAIN LOCAL VARIABLES

	Population	Rents	Amenities young
Full model /Data	1	1	1
No mobility for retirement	1.02	1.13	1.01
No life cycle	1.21	2.17	1.04

The table shows the Gini coefficients for the local variables in the data (full model), in the model with no life cycle ($T^y = T$ and $t^o = 0$) and in the model with no mobility for retirement (I recompute local population, rents and amenities assuming that $L_i^o = \rho L_i^y$ and keeping L_y fixed at its observed level). Coefficients are normalised by the full model levels. The sample includes 741 U.S. CZs

7.2 Decomposing the sorting pattern by age and location

What are the drivers of the sorting of younger and older residents across locations? From the model equilibrium conditions (19) and (20), the ratio of old in location i to young in location i is determined as:

$$\ln \frac{L_i^o}{L_i^y} = \ln \rho + \rho \ln \frac{\left(a_i^o R_i^{-(1-\delta_c)}\right)^\theta}{\sum_j \left(\mu_{ij} a_j^o R_j^{-(1-\delta_c)}\right)^\theta} - \ln \frac{\left(w_i^{(1+\rho)} a_i^y R_i^{-(1-\delta_c)}\right)^\theta}{\sum_j \left(\mu_{ij} w_j^{(1+\rho)} a_j^y R_j^{-(1-\delta_c)}\right)^\theta} \quad (28)$$

Equation (28) implies that if older individuals can move across locations (mobility costs are finite), sorting of young and old across locations is governed by the dispersion in the differences of location values for young and old residents. This dispersion arises from three reasons. First, local wages are valued only by workers as retirees supply zero working hours. Second, young and old differ in their valuation of local amenities. Besides, as the relative length of the older period ρ is less than one, old are less sensitive to the variation in all location fundamentals. I further confirm that in the model with fully symmetric geography the variation in the share of old across locations is zero.

To isolate the role of exogenous geography, I simulate the model where I shut down the endogenous responses of amenities and productivity ($\sigma = \infty$ and $\gamma^p = 0$). I find that the resulting model explains 93% of the variance of (log) ratio of old to young, implying that the remaining 7% result from the amplification of location differences through the endogenous adjustment of amenities and productivities. I further compute that of this seven percent, two percent is attributed to the endogenous adjustment of the composition of local establishments to the young and old preferences.²³ One concern is that the aggregation procedure made in the paper might miss richer heterogeneity in young and old expenditure shares on local services. However, even in the extreme case when $\alpha_1^y = 1$ and $\alpha_1^o = 0$, that is when young and old

²³I consider the full version of the model, where I restrict $\alpha^y = \alpha^o$ and compute how much of the variance in the ratio of old to young this model accounts for.

consume completely different sets of local services, the contribution of endogenous amenities to the variance in the ratio of old to young is only 6%. The reason is that amenity gains from a higher alignment of preferences with the composition of services are limited by the share spend on the local goods δ_b and by the love of variety gains governed by σ .

Even though the contribution of endogenous amenities to the sorting of young and old is quantitatively small, I show that this mechanism can match the evidence on the correlation between the composition of location establishments and location demographics described in section 3.3. In particular, to directly relate the empirical evidence to the model outcomes, I aggregate establishments into two broad service categories as in the calibration section 6.2, and then I compute the elasticity of the composition establishments with respect to CZ demographic composition by running the following OLS regression:

$$\ln \frac{N_{2i}}{N_{1i}} = \beta_o + \beta_1 \ln \frac{L_i^o}{L_i^y} + X_i + \epsilon_i$$

where X_i include controls for log location wages and rents. Then I run the same specification on the model simulated data, where I assume that the fixed costs of entry $F_{s,i}$ are symmetric across locations. Figure 8 presents the results and shows that the model implied elasticity $\beta_1 = 0.24$ is close to the OLS estimate $\beta_1 = 0.29$ in the data. This moment was not directly targeted in the calibration. In the model, it is disciplined only through the differences in expenditure shares by age recovered from the CEX data, and through the endogenous firms' entry mechanism which was calibrated based on the estimates from the literature. Therefore, the endogenous adjustment of local firms to local expenditures is the key mechanism to explain the relationship between local amenities and demographics, but it has a limited role in explaining the sorting pattern by age and location.

Another empirical fact documented in the paper is that CZ wage is negatively correlated with CZ old-to-young ratio. The model was calibrated to fully match the distribution of young and old across CZs. Therefore, it fully matches the elasticity of the ratio of old to young with respect to the CZ productivity reported in section 3.2. To isolate the role of differences in working hours in generating this pattern, I consider a version of the model where the only change over the life cycle is retirement.²⁴ In the restricted model, the elasticity of the ratio of old to young w.r.t. CZ wages is -0.7 versus -0.9 in the data.²⁵ Therefore, most of the negative relationship between CZ wages and demographics is attributed to the decline in working hours after retirement, and the rest is attributed to relative amenities for old being better in less productive locations.

²⁴ I assume that $\tilde{A}_i^o = \tilde{A}_i^y$ and that $\alpha^o = \alpha^y$

²⁵ I run the same regression as on figure 2 using the data simulated from the restricted version of the model

TABLE 8
COMPOSITION OF LOCAL ESTABLISHMENTS:
MODEL VS DATA

	(1)	(2)
Dependent Variable	N_2/N_1 data	N_2/N_1 model
L_i^o/L_i^y	0.29* (0.15)	0.24*** (0.003)
Controls	✓	✓

p-value *** $p \leq 0.01$, ** $p \leq 0.05$, * $p \leq 0.1$. Robust standard errors are given in parenthesis. All variables are in logs. Observations weighted by CZ sum of young and old population. N_1 includes establishments in hospital, nursing care homes and beauty services. N_2 includes restaurants, clothing, and childcare services. Both regressions include CZ wages and rents as controls, and include observations for 722 U.S. continental CZs.

7.3 The role of mobility costs of moving for retirement

In the model, young individuals are fully mobile, so their expected life time utility is equalised across space. However, this is no longer true for the utility of older residents, who face mobility costs of reallocation across cities. I find that the per period utility of older residents varies significantly across the U.S. CZs: moving from an area at the 25th percentile of the value for old to an area at the 75th percentile is equivalent to increasing the individual's income by a factor of 2.06.²⁶ These differences are driven by the fact that locations that are most valuable for the work period are often different from locations that are best for the retirement, so a worse utility for the older residents is offset by a higher utility during the work period and vice versa.

I further show that lower mobility costs allow individuals to increasingly separate locations for work and retirement, which improves the allocation of both young and old individuals w.r.t. CZ fundamentals. In particular, I use 2 and 12 to derive the sum of the location values for young and old residents²⁷

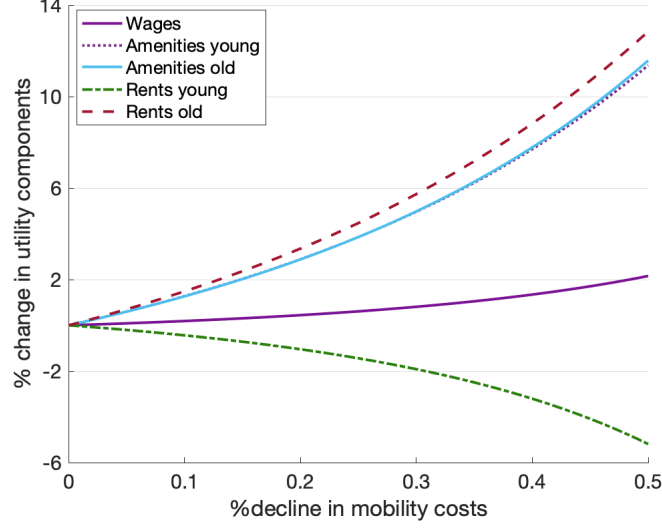
$$V = \sum_i L_i^y \left((1 + \rho) \ln w_i + \ln a_i^i - (1 - \delta_c) \ln R_i \right) + \sum_i L_i^o \left(\ln a_j^o - (1 - \delta_c) \ln R_j \right)$$

Figure 5 shows how different components of V respond to a decline in the fixed mobility cost for retirement κ . Due to lower mobility costs for retirement, young individuals are increasingly choosing locations that are more amenable for young and more productive, and old individuals are increasingly choosing locations that are cheaper and more amenable for old. The gains

²⁶Per period utility of older residents in a location i who lived in j when young is $u_{ji}^o = \frac{w_j a_i^o}{R_i^{1-\delta_c}}$

²⁷It is a sum of the common components of individual's utilities from living in a given location: $\sum_i (L_i^y u_i^y + L_i^o u_i^o)$.

Figure 5: Gains from lower mobility costs for retirement



This figure decomposes the changes in the sum of location values V in response to a decline the fixed component of the mobility cost for retirement κ . The horizontal axes shows the percentage decline change in κ . The vertical axes shows the resulting percentage changes in the different components of V . Wage is $L_i^y(1 + \rho) \ln w_i$, amenity for young is $L_i^y \ln a_i^y$, amenity for old is $L_i^o \ln a_i^o$, rent young is $L_i^y(1 - \delta_c) \ln R_i$ and rent old is $L_i^o(1 - \delta_c) \ln R_i$

for the younger age group are partially offset by the higher rental prices: young residents who expect to later reallocate for retirement are more willing to pay higher prices in exchange for the location value for young.

To sum up, the results in this section suggest that there are large gains from reducing mobility frictions of moving for retirement due to the significant differences in location's value for its younger and older residents.

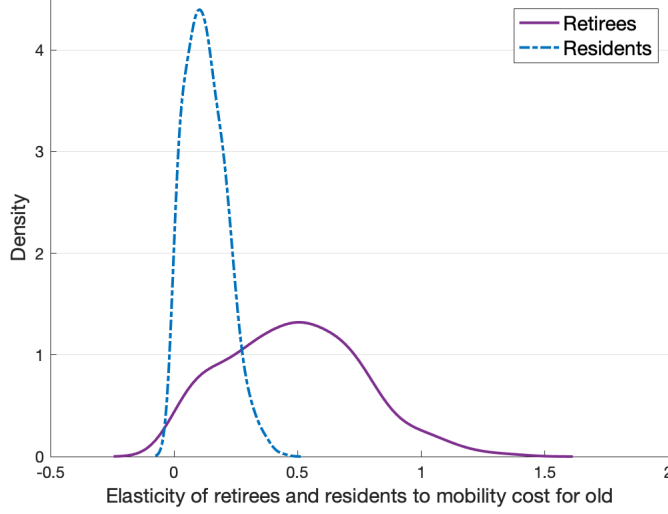
7.4 Local Retirement Elasticities

There exist numerous examples of cities and states trying to attract retirees to relocate there.²⁸ What determines the ability of the city to grow by attracting retirees? To answer this question, I follow the approach of Monte et al. (2018) for studying local employment elasticities. For each CZ i , I compute the response of the local retiree population to a 1 percent decline in the retiree's mobility costs of moving to a location i .²⁹ In this way, I proxy for the effects of policies that target older movers such as relocation subsidies and assistance with moving. Figure 6 shows the estimated kernel density for the distribution of the general equilibrium elasticity across 741 treated CZs. The mean estimated elasticity 0.5 is significantly lower than mean

²⁸see Reeder (1998)

²⁹I compute 741 counterfactuals where I shock the mobility costs of moving to CZ i μ_{ji} by the factor of 0.99 for $j \neq i$, keeping all other model parameters fixed

Figure 6: Local retirement elasticities



The figure plots the kernel density for the distribution of retirees and residents elasticities in response to a decline in the mobility costs for incoming retirees. Elasticities are computed from the model simulations for 741 U.S. CZs

employment elasticity to productivity shocks (around 3.9) due to the high level of mobility costs for retirement. Importantly, there exists significant heterogeneity in the predicted elasticities, which vary from as low as 0.001 to almost 1.4.

To study the determinants of this large variation in elasticities, I regress them on a set of CZ observable characteristics. Table 9 shows the results. In column 1, I include log CZ young population as the only control, and I find a strong and negative relationship between the two variables which explains a significant portion of the variation in elasticities (R^2 is 0.65). Places that are less attractive for younger residents have a larger pool of potential reallocating retirees relative to their current population size, so they are more successful at increasing their retiree population. In columns 2 and 3 I add log CZ old to young ratio and total young population in nearby CZs as additional controls, which raises the R^2 to 0.95.³⁰ Both controls capture the attractiveness of a CZ for the retirees in other locations and are positively associated with the retirement elasticity. Adding more observable controls such as wages, rents in the location and in nearby locations does not improve the regression fit.

Figure 6 shows that as compared to the retirement elasticities the predicted total population elasticities are much lower and vary from around 0 to just 0.5. The reason is that reallocating retirees increase the local housing prices which makes the location less attractive for the younger

³⁰ total young population in nearby CZs for the CZ i is the inverse mobility cost weighted sum of L_y in CZs other than i

TABLE 9
DETERMINANTS OF THE LOCAL
RETIREMENT ELASTICITIES

	(1)	(2)	(3)
$\ln L_y$	-0.22*** (0.007)	-0.19*** (0.004)	-0.21*** (0.005)
$\ln \frac{L_o}{L_y}$		0.96*** (0.03)	0.8*** (0.04)
$\ln \bar{L}_{-i}^y$			0.91*** (0.08)
Obs.	741	741	741
R-squared	0.65	0.92	0.95

p -value *** $p \leq 0.01$. Robust standard errors are given in parenthesis. The dependent variables is the model simulated elasticity of the CZ old population w.r.t. the decline in the mobility costs for reallocating retirees. \bar{L}_{-i}^y is the inverse mobility cost weighted sum of young individuals in CZs other than i .

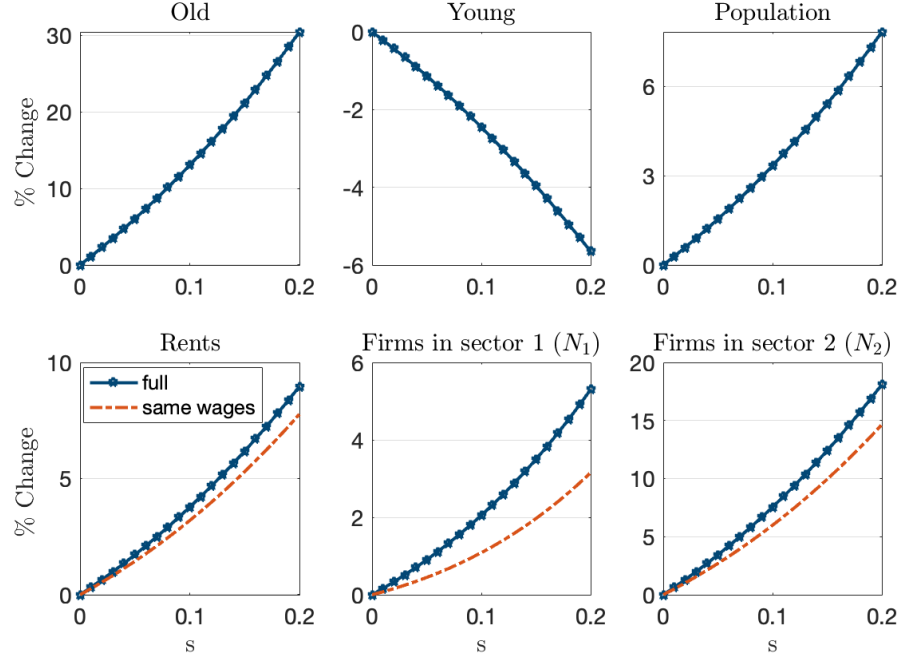
residents and dampens the response of total population to mobility costs.

Overall, the results in this section suggest that same local policies targeted at attracting retirees can have heterogeneous affects across treated cities. Locations that grow the most are the ones that are smaller, have larger share of older residents and are closer to more populated CZs. However, the total affect of such policies is significantly dampened by the high mobility costs that retirees face and by the rising local prices that drive out workers.

8 Counterfactual Exercises

This section describes counterfactual exercises of the model. Section 8.1 studies the local and aggregate effects of place-based policies that target older individuals to relocate to less productive cities. Section 8.2 discusses the implications of the ageing shift predicted over 2014-2040 period. Section 8.3 shows that geographic sorting by age has increased over 1960-2010 period and argues that declining mobility frictions for old was the main factor behind these changes.

Figure 7: Local effects of the policy that subsidises the reallocation of old to less productive cities



Simulated local changes due to the introduction of a subsidy s measured as a percentage of individuals' average wages in the economy given to any old individual moving to a treated city. The policy is financed via a lump sum tax paid by all workers in the economy. Treated cities are the smallest CZs in U.S. that represent 1 percent of total population.

8.1 Place-based policies targeted at retirees

The previous section shows that smaller cities gain relatively more from subsidising the reallocation for retirement. Should policy promote the development of smaller/less-productive cities by this channel? Existing literature has largely focused on the affects of place-based policies that subsidize firms locating in less developed cities or regions. This type of policies aims at reducing the spatial disparities and increasing the aggregate efficiency. However, as argued in [Kline & Moretti \(2014\)](#) positive local impacts of such policies are counterbalanced by losses in other locations and lead to the aggregate losses in the welfare and TFP. [Gaubert \(2018\)](#) further shows that such policies actually increase the spatial disparities in GDP per capita in the U.S. Related to the questions in this paper, some states indeed try to boost their less developed areas by attracting the retirees to reallocate there.³¹ Analysis from the previous section shows that smaller cities benefit from such policies relatively more in terms of their

³¹For example, Alabama provides state assistance to rural communities in retiree attraction, including planning and technical assistance coordinated marketing efforts, financial assistance, and amenity development. More examples are in [Reeder \(1998\)](#)

population size. However, the efficiency of this policy depends on whether the optimal allocation features higher or lower sorting of the young and the old given the calibrated parameters.

In this section, I study quantitatively local and aggregate effects of the policies that incentivise the old to reallocate to less productive cities. I consider counterfactuals in which older individuals are given a subsidy s to move to the least productive cities in the U.S (cities in the 25th quantile by productivity). Figure 7 shows the local effects of the policy as a function of the subsidy level s . For example, a 10% subsidy in terms of the average wages in the economy which costs 0.04% of GDP (as the policy considered in Gaubert (2018)) increases the total population of treated cities by 3.2%, increases rents by 4.6% and increases the number of firms in sectors 1 and 2 by 2.01% and 9.5% respectively. The red dotted line on figure 7 shows what response of local variables would be if relocating old had same wages as the workers in the treated city. The difference between the two lines shows that local policy effects are amplified by higher earnings of relocating retirees.

The counterfactual exercise allows me to compute the general equilibrium effect of the policy on the welfare, TFP. Appendix figure H7 shows that aggregate welfare is monotonically decreasing in the subsidy level s , while the reverse holds for aggregate TFP. While reallocation of retirees improves productive efficiency, this is achieved by very costly mobility of old, which does not offset the TFP gains. From the optimal policy perspective, it turns out that for the calibrated parameters gains from productivity spillovers are offset by a worse distributional efficiency due to the preference shocks. So higher sorting by age and productivity caused by the subsidy does not improve welfare.

I further study how the policy affects the dispersion of spatial outcomes according to the Gini coefficient for the endogenous spatial variables. I find that the type of the place-based policy that I study contributes to a more equal distribution of amenities and rents across CZs, but a more unequal distribution of wages in the tradeable sector. However, as I don't model the employment in the local service sector, the analysis might miss the additional response from employment and wages there.

8.2 Ageing population and changes in the city size distribution (in progress)

Over the 2020-2040 period the relative size of the older age group is predicted to increase by around 36%.³² Through the lens of the model, this change corresponds to an increase in the relative length of the old period ρ , which makes the older period more important for the individual's location choices and for the equilibrium outcomes.

³²The prediction is for the age groups 20-64 and 65+ from <https://www.urban.org/policy-centers/cross-center-initiatives/program-retirement-policy/projects/data-warehouse/what-future-holds/us-population-aging>

By running the counterfactual increase in ρ by 36 percent, I estimate that the ageing shift between 2030 and 2040 is expected to generate a significant shift in spatial distribution of cities: 13 percent of workers and 16 percent of retirees are expected to change their location. I find that CZs that are more attractive for old are predicted to gain both in terms their retiree and working age population, which further increases their wages and amenities.

8.3 Changes in geographic sorting by age, 1960-2010

Figure 8 shows that a pattern of sorting by age and productivity documented in recent decades was not present in an earlier Census sample of 1960.³³ I further compute that the dissimilarity index for the younger and the older age groups has increased by 38% over this period from around 0.06 in 1960 to around 0.08 in 2010.³⁴ These changes might be related to an increased mobility for retirement: the share of individuals of age 55 and older who moved between states within a 5 year window has increased by around 21% over 1960-2010.³⁵ By comparison, the share of individuals in the younger age group (25-55) who moved between states has increased only by around 4%.

This section studies the drivers behind the changes in geographic sorting by age over time. In particular, I recalibrate my model to the MSA-level data for 1960 and 2010 years, treating these two time periods as different steady states of the model. I keep all the structural parameters as in the main quantification part, except for the fixed component of the mobility cost (κ) and the relative length of the old period ρ . I recalibrate κ for year 1960 so that the share of individuals who reallocate between states for retirement is by 22 percent lower than in 2010.³⁶ I find that mobility friction in 1960 should have been 36% lower than in 2010. More details on the calibration procedure are in Appendix F. The main reason behind this large model-implied changes in mobility costs is that in 1960 population was much more concentrated in the most productive U.S. MSAs, and most of these locations actually had old-to-young ratios above national average. So to rationalise low mobility flows in that period the model requires relatively large mobility costs.

I compute that reducing mobility costs from the level observed in 1960 to their 2010 level leads to a 6.3 percent increase in welfare, which is equivalent to increasing an individual's income

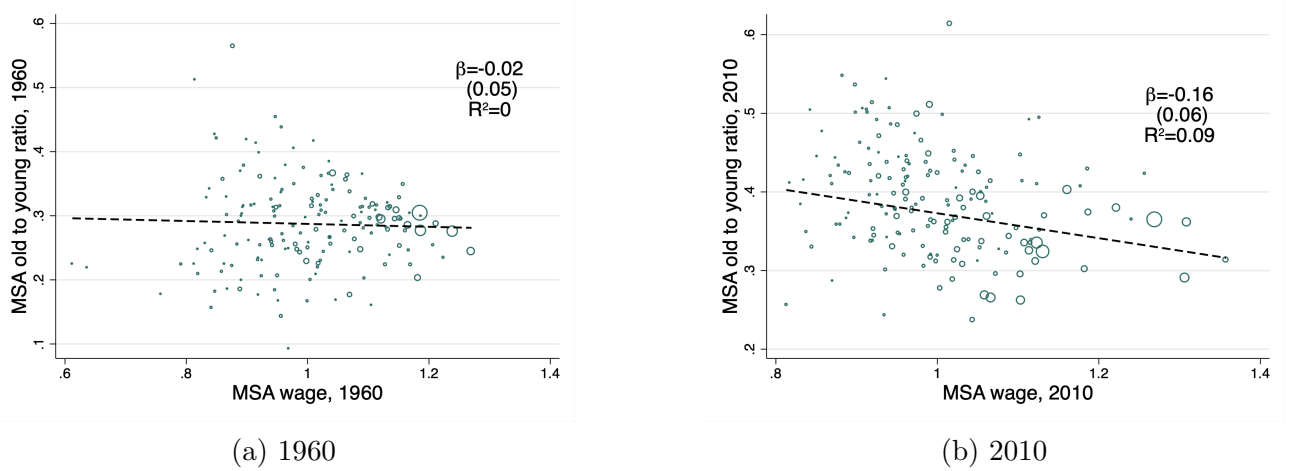
³³As there is no mapping between geography units and CZs for historical samples in Census data, I chose to make historical comparisons at the MSA level

³⁴The dissimilarity index is defined as $\frac{1}{2} \left| \frac{L_i^o}{\sum_i L_i^o} - \frac{L_i^y}{\sum_i L_i^y} \right|$ where L_i^o is the size of the older age group in the location i , and L_i^y is the size of the younger age group in i . I include 169 common MSAs and one location corresponding to all the areas outside of the MSAs in the computation

³⁵I compute that 3.97% of individuals older than 55 moved between U.S. states in 1960, while the corresponding number for 2010 is 4.83%. I choose a lower age cut-off than in the definition of the older age group as individuals might reallocate for retirement earlier than their actual retirement

³⁶I map each MSA to a single state and compute the share of old who relocates between states

Figure 8: Sorting by age and productivity, MSA level



Regressions weighted by the MSA total population. Older age group includes individuals of age 60+ and younger age group includes individuals of age 25 – 60. Wages are adjusted for the location demographics. Regressions include 169 MSAs present in both years. Wages and old to young ratios are normalised by the MSA mean values in the corresponding year.

by 4.9 percent. In terms of size, the welfare gains from lower mobility costs for retirement are in the upper range of the estimates of welfare gains from reduction in commuting costs over 1990-2010 provided in [Monte et al. \(2018\)](#).³⁷ Table 10 shows that the calibrated decline in the mobility costs explains around 73% of the increase in the correlation between MSA old to young ratio and MSA wages over 1960-2010 period. The reason is that lower mobility costs allow individuals to increasingly separate locations for work and retirement, which drives higher sorting by age and location's productivity.

The results described above are based on the MSA recalibration of the model for 1960 and 2010 Census years. For robustness, I perform a similar exercise using the main calibration of the model for the U.S. CZs over 1980-2014 time period. I find that a 22 percent increase in mobility for retirement corresponds to a 27 percent decline in mobility costs and to a 7.05 percent increase in aggregate welfare. The welfare gains are slightly larger as the number of CZ exceeds the number of MSAs (741 vs 169), which increases the gains from having an option to reallocate due to the assumption on the presence of preference shocks for each location path. However, the main drawback of this exercise is that it does not allow for the changes in location-specific fundamentals over time when calibrating the model implied change in mobility costs.

³⁷[Monte et al. \(2018\)](#) estimate reducing the commuting costs by the seventy-fifth, fiftieth, and twenty-fifth percentiles of the empirical distribution of changes in the ease of commuting between 1990 and 2010 leads to 6.89, 3.26 and 0.89 percent welfare gains

TABLE 10
CHANGES IN SORTING 1960-2010

	1960	Simulation	2010
$corr(W_i, \frac{L_i^o}{L_i^y})$	0.01	-0.2	-0.27

All variables are normalized by the year means. Column two computes the correlation of the simulated W_i and $\frac{L_i^o}{L_i^y}$ in a model that was calibrated to year 1960 at the MSA level and where mobility costs were set at 2010 level.

9 Conclusion

This paper argues on the importance of the life cycle for location choices and for the distribution of economic activity across space. By building and estimating the model of location choices for work and retirement periods, I quantify the differences in locations' values for their younger and older residents. I find that these differences arise from changes in working hours and preferences for local amenities with age, and that they imply large gains from life cycle mobility. I also estimate that mobility frictions preclude retirees from moving to better places and lead to a significant dispersion in location-specific utilities of older individuals.

I document that geographic sorting by age has increased dramatically over 1960-2010 period. Using the model structure, I argue that this increase in sorting is related to the decline in mobility frictions of relocating for retirement, which allowed individuals to increasingly separate locations for work and retirement period. I estimate the resulting welfare gains to be equal to 6.3%. However, I show that policies that target higher sorting of young and old through place-based transfers are not welfare improving. This suggests that it is important to further study the frictional components of the mobility costs that older individuals face and how and why they have changed over time.

The paper also shows that smaller cities benefit the most from local policies aimed at attracting retirees: they experience an increase in total population and an increase in the variety of local services. Therefore, such policies can be considered for the purpose of reducing spatial disparities, and they differ from similar policies targeted at workers as they do not distort production efficiency. Another direction for the future research is to model the response of the employment in the non-tradeable sector to the inflow of savings of relocating old. This would help to better understand the scope of place-based policies targeted at the old for reducing spatial disparities and inequality.

References

- Aguiar, M. & Hurst, E. (2013). Deconstructing life cycle expenditure. *Journal of Political Economy*, 121(3), 437–492.
- Allen, T. & Arkolakis, C. (2014). Trade and topography of the spatial economy. *The Quarterly Journal of Economics*, 129(3), 1085–1140.
- Allen, T., Arkolakis, C., & Li, X. (2015). On the existence and uniqueness of trade equilibria. *mimeo, Dartmouth and Yale Universities*.
- Allen, T. & Donaldson, D. (2018). The geography of path dependence. *Unpublished manuscript*.
- Almagro, M. & Dominguez-Ino, T. (2019). Location sorting and endogenous amenities: Evidence from amsterdam.
- Autor, D. & Dorn, D. (2013). The growth of low-skill service jobs and the polarization of the us labor market. *American Economic Review*, 103(5), 1553–97.
- Bilal, A. & Rossi-Hansberg, E. (2018). Location as an asset. *National Bureau of Economic Research*, No. w24867.
- Couture, V., Gaibert, C., Handbury, J., & Hurst, E. (2019). Income growth and distributional effects of urban spatial sorting. *National Bureau of Economic Research*, (No. w26142).
- Desmet, K. & Rossi-Hansberg, E. (2013). Urban accounting and welfare. *American Economic Review*, 103(6), 2296–2327.
- Desmet, K. & Rossi-Hansberg, E. (2014). Spatial development. *American Economic Review*, 104(4), 1211–43.
- Diamond, R. (2016). The determinants and welfare implications of us workers diverging location choices by skill: 1980-2000. *American Economic Review*, 106(3), 479–524.
- Dolfen, P., Einav, L., Klenow, P. J., Klopach, B., Levin, J. D., & Best, W. (2019). Assessing the gains from e-commerce. *National Bureau of Economic Research*, (No w.25610).
- Duncombe, W., Robbins, M., & Wolf, D. A. (2001). Retire to where? a discrete choice model of residential location. *International Journal of Population Geography*, 7(4), 281–293.
- Eckert, F., Gvirtz, A., Liang, J., & Peters, M. (2020). A method to construct geographical crosswalks with an application to us counties since 1790. *NBER Working Paper No. 26770*.

- Eckert, F. & Peters, M. (2018). Spatial structural change. *Unpublished manuscript*.
- Fajgelbaum, P. D. & Gaubert, C. (2020). Optimal spatial policies, geography, and sorting. *The Quarterly Journal of Economics*, 135(2), 959–1036.
- Finkelstein, A., Gentzkow, M., & Williams, H. L. (2019). Place based drivers of mortality: Evidence from migration. *National Bureau of Economic Research*, (No. w25975).
- Gaubert, C. (2018). Firm sorting and agglomeration. *American Economic Review*, 108(11), 3117–53.
- Giannone, E., Li, Q., Paixao, N., & Pang, X. (2019). Unpacking moving.
- Glaeser, E. L. & Gottlieb, J. D. (2008). The economics of place-making policies. *National Bureau of Economic Research*, (No. w14373).
- Guerrieri, V., Hartley, D., & Hurst, E. (2013). Endogenous gentrification and housing price dynamics. *Journal of Public Economics*, (pp. 45–60).
- Hoelzlein, M. (2019). Two-sided sorting and spatial inequality in cities.
- Hornbeck, R. & Moretti, E. (2018). Who benefits from productivity growth? direct and indirect effects of local tfp growth on wages, rents and inequality. *National Bureau of Economic Research*, (No. w24661).
- Kline, P. & Moretti, E. (2014). Local economic development, agglomeration economies, and the big push: 100 years of evidence from the tennessee valley authority. *The Quarterly Journal of Economics*, 129(1), 275–331.
- Lu, J. (2020). Household residential location choice in retirement: The role of climate amenities. *Regional Science and Urban Economics*, 84.
- Monte, F., Redding, S., & Rossi-Hansberg, E. (2018). Commuting, migration and local employment elasticities. *American Economic Review*, 108(12), 3855–90.
- Moretti, E. (2013). Real wage inequality. *American Economic Journal: Applied Economics*, 5(1), 65–103.
- Redding, H. S. S. J. & Sturm, D. M. (2020). The making of the modern metropolis: evidence from london. *The Quarterly Journal of Economics*.
- Redding, S. & Rossi-Hansberg, E. (2017). Quantitative spatial economics. *Annual Review of Economics*, 9(1).

- Reeder, R. J. (1998). Retiree-attraction policies for rural development. *Agriculture Information Bulletin*, (741).
- Roback, J. (1982). Wages, rents, and the quality of life. *the Journal of Political Economy*, (pp. 1257–1278).
- Rosen, S. (1979). Wages-based indexes of urban quality of life. *Current Issues in Urban Economics*.
- Rosenthal, S. S. & Strange, W. C. (2004). Evidence on the nature and sources of agglomeration economies. *Handbook of regional and urban economies*, 4(2119-2171).
- Rossi-Hansberg, E., Sarte, P.-D., & Schwartzman, F. (2019). Cognitive hubs and spatial redistribution. *National Bureau of Economic Research*, (w26267).
- Ruggles, S., Genadek, K., Goeken, R., Grover, J., & Sobek, M. (2015). Integrated public use microdata series: Version 6.0 (machine readable database).
- Saiz, A. (2010). The geographic determinants of housing supply. *Quarterly Journal of Economics*, 125(3), 1253–96.
- Santos, S. J. & Tenreyro, S. (2006). The log of gravity. *The Review of Economics and Statistics*, 88(4), 641–658.
- Schneider, M. & Green, B. (1992). A demographic and economic comparison of nonmetropolitan retirement and nonretirement counties in the us. *Journal of Applied Sociology*, (pp. 63–84).
- Su, Y. (2019). Measuring the value of urban consumption amenities: A time use approach. *Available at SSRN 3454631*.
- Su, Y. (2020). The rising value of time and the origin of urban gentrification.

Appendices

A Robustness Checks for the Empirical Results

First, I consider whether the results change if I consider retirees instead of just old. I define retirees as individuals with age 50 and higher who is out of the labor force. For each location I compute the ratio of retirees to workers. The results are presented on the figure A1. The results are stronger than in case of old and young, which might be driven by workers retiring earlier in less productive commuting zones.

Figure A1: Sorting of retirees and workers across the US CZs

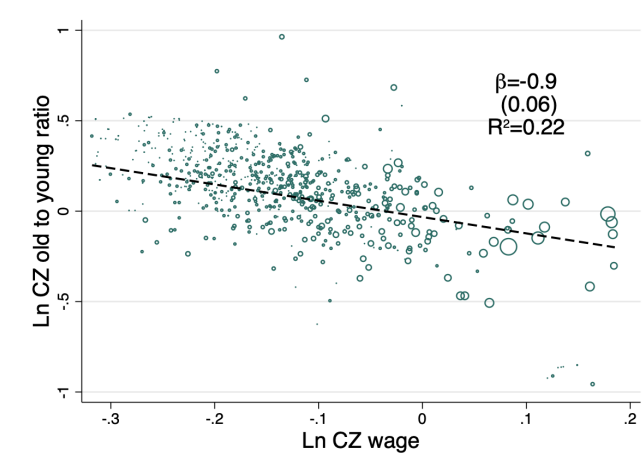


Average values for the years 1980, 1990, 2000 and 2014. Regressions weighted by location population. Wages are adjusted for the location demographics.

Second, I consider whether the results are sensitive to the age cut-off. As shown in the figure A2, patterns of sorting by age and productivity are the same if we consider a cut-off of 65+. I also check if the results are robust to the weighting: the original regression uses observations weighted by the CZ population size. If observations are not weighted, the correlation between location productivity and share of old is even stronger, as shown in the figure A3.

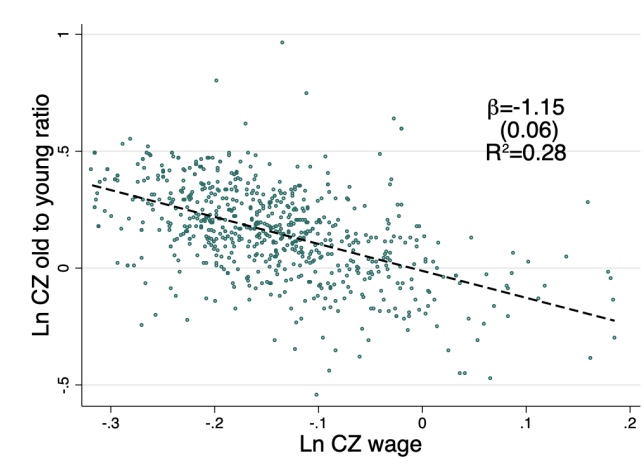
Finally, I provide an additional check that the original evidence on sorting is mostly driven by the fact that young and old value locations differently, rather than by the fact that they respond to shocks in a different way. In particular, I compute whether the lagged location productivity (year 1970) is correlated with location current share of old (year 2014). The results are similar to the original evidence on sorting and are presented on the figure A4, suggesting that time persistent differences in CZ productivities are driving the sorting pattern.

Figure A2: Sorting of young and old (65+) across the US CZs



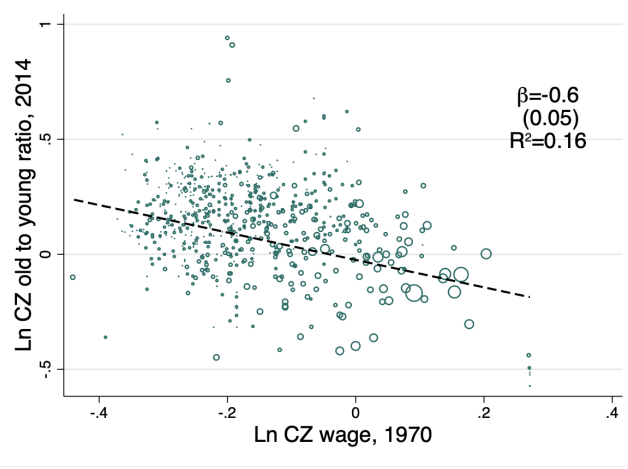
Average values for the years 1980, 1990, 2000 and 2014. Regressions weighted by location population. Wages are adjusted for the location demographics.

Figure A3: Sorting of young and old across the US CZs (no weights)



Average values for the years 1980, 1990, 2000 and 2014. Wages are adjusted for the location demographics.

Figure A4: Sorting of young and old across the US CZs: lagged productivity



Regressions weighted by location population. Wages are adjusted for the location demographics.

B Proofs for the Theoretical Part

B.1 Relative length of old period

The model in the main text is equivalent to the following set-up. Suppose that individuals spend t_1 periods being "young" and t_2 periods being "old". Let $\rho = t_2/t_1$ denote the relative length of the old period. I assume that the discount rate and the interest rate are both equal to 1. Individuals choose a pair of locations $\{i, j\}$, where i is where they live for the t_1 young periods, and j is where they live for the t_2 old periods. Conditional on the location path $\{i, j\}$, the individual problem is:

$$\begin{aligned} & \max_{c_t^y, c_t^o, h_t^y, h_t^o, q_{m,s,t}^y, q_{m,s,t}^o} \sum_{t=1}^{t=t_1} u(c_t^y, h_t^y, q_{m,s,t}^y) + \sum_{t=t_1+1}^{t=T} u(c_t^o, h_t^o, q_{m,s,t}^o) \\ \text{s.t. } & \sum_{t=1}^{t=t_1} \left(c_t^y + R_{i,t} h_t^y + \sum_{s=1}^2 \sum_{m=1}^{N_{s,i,t}} p_{m,s,i,t} q_{m,s,t}^y \right) + \sum_{t=t_1+1}^T \left(c_t^o + R_{i,t} h_t^o + \sum_{s=1}^2 \sum_{m=1}^{N_{s,i,t}} p_{m,s,i,t} q_{m,s,t}^o \right) = \sum_{t=1}^{t=t_1} w_i \end{aligned}$$

where w_i is the wage that individual receives each period that she is young from supplying one unit of labor and where I assumed that the discount factor and the interest rate are equal to one.

As the model is stationary, in equilibrium all the prices will be constant through time. Then, in the optimal solution to this problem individuals will choose same consumption levels within young and old period: $c_t^y = c_y$, $h_t^y = h^y$, $c_t^o = c^o$, $h_t^o = h^o$, $q_{m,s,t}^y = q_{m,s}^y$ and $q_{m,s,t}^o = q_{m,s}^o$. Then

the problem is equivalent to:

$$\begin{aligned} & \max_{c^y, h^y, c^o, h^o} t_1 u(c^y, h^y, a_i) + t_2 u(c^o, h^o, a_j) \\ \text{s.t. } & t_1 \left(c^y + R_i h^y + \sum_{m=1}^{N_{s,i}} p_{m,s,i} q_{m,s}^y \right) + t_2 \left(c^o + R_i h^o + \sum_{m=1}^{N_{s,i}} p_{m,s,i} q_{m,s}^o \right) = t_1 w_i \end{aligned}$$

Which is equivalent to the consumer problem in the main text, if we normalize utility by young period length t_1 .

B.2 Social planner problem

Definition 2. *Social planner chooses consumption $\{c_{ij}^{y,o}, h_{ij}^{y,o}, q_{1ij}^{y,o}, q_{2ij}^{y,o}\}$ and a mass of firms in two non-tradeable sectors $\{N_{1i}, N_{2i}\}$ to solve*

$$\max LU$$

subject to

- *spatial mobility constraint:*

$$\ln \left(\frac{L_{ij}}{L} \right)^{\frac{1}{\theta}} = \ln \left(A_i^y (c_{ij}^y)^{\delta_c} (h_{ij}^y)^{\delta_h} (Q_i^y)^{\delta_b} \right) + \rho \ln \left(A_i^o (c_{ij}^o)^{\delta_c} (h_{ij}^o)^{\delta_h} (Q_i^o)^{\delta_b} \right) - \ln U$$

$$\text{where } Q_i^a = \left(N_{1i}^{\frac{\sigma}{\sigma-1}} q_{1ij} \right)^{\alpha_1^a} \left(N_{2i}^{\frac{\sigma}{\sigma-1}} q_{2ij} \right)^{\alpha_2^a} \text{ for } a = y, o$$

- *Housing production function*

$$H_i = \bar{H}_i I_i^{\frac{1}{1+\epsilon_h}}$$

- *Resource constraint:*

$$\sum_j \sum_i L_{ij} (c_{ij}^y + \rho c_{ij}^o) + \sum H_i I_i = \sum_j \sum_i L_{ij} Z_i (L_i^y)^{\gamma_P}$$

- *individual's allocation constraint:*

$$\sum_j \sum_i L_{ij} = L \tag{29}$$

- *Housing constraints:*

$$H_i = \sum_j L_{ij} \left(h_{ij}^y + \sum_{s=1,2} N_{s,i} k q_{sij}^y \right) + \rho \sum_j L_{ji} \left(h_{ji}^o + \sum_{s=1,2} N_{s,i} k q_{sji}^o \right) + \sum_{s=1,2} N_{s,i} F_{s,i}$$

Proposition 3. *In an efficient allocation the following should hold:*

$$\underbrace{x_{ij}}_{\text{consumption cost}} + \underbrace{\lambda}_{\text{opport}} = \underbrace{z_i^* + \gamma^P z_i^*}_{\text{marginal product in } i} - \frac{x_{ij}}{\theta(1+\rho)} \quad (30)$$

$$\underbrace{R_i^* N_{si} F_{si}}_{\text{housing cost}} = \underbrace{\frac{\sigma}{\sigma-1} \frac{1}{\sigma} \frac{\delta_b}{1+\rho} \left(\alpha_s^y \sum_j x_{ij} L_{ij} + \rho \alpha_s^o \sum_j x_{ji} L_{ji} \right)}_{\text{utility gain}} \quad (31)$$

for $s = 1, 2$, where $x_{ij} = c_{ij}^y + \rho c_{ij}^o + R_i^* (h_{ij}^y + \sum_{s=1,2} N_{s,i} k q_{sij}^y) + \rho R_j^* (h_{ji}^o + \sum_{s=1,2} N_{s,j} k q_{sji}^o)$ is the cost along the path, R_i^* is the multiplier under the housing constraint of the city i and λ is the multiplier under the labor allocation constraint

Proof. The Lagrangian of the planning problem is:

$$\begin{aligned} L = & \ln U - \sum_{ij} \omega_{ij} \left(\ln \left(A_i^y (c_{ij}^y)^{\delta_c} (h_{ij}^y)^{\delta_h} \left(N_{1i}^{\frac{\sigma}{\sigma-1}} q_{1ij} \right)^{\delta_b \alpha_1^y} \left(N_{2i}^{\frac{\sigma}{\sigma-1}} q_{2ij} \right)^{\delta_b \alpha_2^y} \right) + \right. \\ & \rho \ln \left(A_i^o (c_{ij}^o)^{\delta_c} (h_{ij}^o)^{\delta_h} \left(N_{1j}^{\frac{\sigma}{\sigma-1}} q_{1ij} \right)^{\delta_b \alpha_1^o} \left(N_{2j}^{\frac{\sigma}{\sigma-1}} q_{2ij} \right)^{\delta_b \alpha_2^o} \right) - \ln U - \ln \left(\frac{L_{ij}}{L} \right)^{\frac{1}{\theta}} \\ & + R_i^* \left(\bar{H}_i I_i^{\frac{1}{1+\epsilon_h}} - \sum_j L_{ij} \left(h_{ij}^y + \sum_{s=1,2} N_{s,i} k q_{sij}^y \right) - \rho \sum_j L_{ji} \left(h_{ji}^o + \sum_{s=1,2} N_{s,i} k q_{sji}^o \right) - \sum_{s=1,2} N_{s,i} F_{s,i} \right) \\ & + P^* \left(\sum_j \sum_i L_{ij} Z_i \left(\sum_j L_{ij} \right)^{\gamma^P} - \sum_j \sum_i L_{ij} (c_{ij}^y + \rho c_{ij}^o) - \sum H_i I_i \right) \\ & + \lambda \left(L - \sum_j \sum_i L_{ij} \right) \end{aligned}$$

Where $P^*, \lambda, \omega_{ij}, R_i^*$ are Lagrangian multipliers. Normalize $P^* = 1$. The first order conditions are:

$$[L_{ij}] : R_i^* (h_{ij}^y + \sum_{s=1,2} N_{s,i} k q_{sij}^y) + \rho R_j^* (h_{ji}^o + \sum_{s=1,2} N_{s,j} k q_{sji}^o) + c_{ij}^y + \rho c_{ij}^o = z_i (1 + \gamma^P) - \frac{\omega_{ij}}{\theta L_{ij}} - \lambda \quad (32)$$

$$[c_{ij}^y] : \frac{\delta_c \omega_{ij}}{c_{ij}^y} = L_{ij} \quad [c_{ij}^o] : \frac{\delta_c \omega_{ij}}{c_{ij}^o} = L_{ij} \quad (33)$$

$$[h_{ij}^y] : \frac{\delta_h \omega_{ij}}{h_{ij}^y} = R_i^* L_{ij} \quad [c_{ij}^o] : \frac{\delta_c \omega_{ij}}{h_{ij}^o} = L_{ij} R_j^* \quad (34)$$

$$[q_{sij}^y] : \frac{\delta_b \alpha_s^y \omega_{ij}}{q_{sij}^y} = L_{ij} R_i^* k N_{si} \quad [q_{sij}^o] : \frac{\delta_b \alpha_s^o \omega_{ij}}{q_{sij}^o} = L_{ij} R_j^* k N_{sj} \quad (35)$$

$$[N_{si}] : \frac{\sigma}{\sigma-1} \delta_b \alpha_s^y \sum_j \omega_{ij} + \rho \frac{\sigma}{\sigma-1} \delta_b \alpha_s^o \sum_j \omega_{ji} - R_i^* \sum_j L_{ij} q_{1ij}^y k - R_i^* \rho \sum_j L_{ji} q_{1ji}^o k - R_i^* F_{1i} = 0 \quad (36)$$

$$[I_i] : R_i \frac{1}{1 + \epsilon_H} \bar{H}_i I_i^{-\frac{\epsilon_H}{1+\epsilon_H}} - H_i = 0 \quad (37)$$

Substituting 35 into 36, I get the optimality condition for the number of firms in non-tradeable sector s :

$$\frac{1}{\sigma-1} \left(\delta_b \alpha_s^y \sum_j \omega_{ij} + \rho \delta_b \alpha_s^o \sum_j \omega_{ji} \right) = R_i^* F_{si} N_{si} \quad (38)$$

Denote by x_{ij} the total cost of putting an individual on a location path ij in terms of the consumption of the final good and tightening of the housing constraints (either directly or through consumption of non-tradeables):

$$x_{ij} = c_{ij}^y + \rho c_{ij}^o + R_i^* (h_{ij}^y + \sum_{s=1,2} N_{si} k q_{sij}^y) + \rho R_j^* (h_{ij}^o + \sum_{s=1,2} N_{sj} k q_{sij}^o)$$

From the FOCs the following holds the following holds:

$$\omega_{ij} = \frac{x_{ij} L_{ij}}{(1 + \rho)}$$

B.3 Proof of Proposition 4

Denote $x_i = (a_i^y)^{-\theta}$ and $y_i = (a_i^o)^{-\beta\theta}$. Then the system of equilibrium conditions transforms into:

$$x = \frac{L}{U^\theta} \sum_j K_{ij} y_j^{-1}$$

$$y = \frac{L}{U^\theta} \sum_j K_{ji} x_j^{-1}$$

where K_{ij} are known positive values. The corresponding matrices of coefficients are:

$$B = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} \quad \Gamma = \begin{pmatrix} 0 & -1 \\ -1 & 0 \end{pmatrix}$$

Then matrix A can be found as:

$$A \equiv \Gamma B^{-1} = \begin{pmatrix} 0 & -1 \\ -1 & 0 \end{pmatrix}$$

taking the absolute value of matrix coefficients we get that:

$$A^p = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$$

The spectral radius of the matrix is equal to 1. Applying the results from [Allen et al. \(2015\)](#), I get that the solution of the system exists and is unique up to the scale. So is the solution for a_i^y, a_i^o .

C Data Appendix

C.1 Composition adjusted wages

To compute composition adjusted wages, I compute individual log hourly wages for the subsample of workers: individuals of age 17-64, who work more than 44 weeks and more than 34 hours a week. Then, for each sample year I regress log hourly wages on the set of demographic controls: age, sex, race, nativity and highest completed education:

$$\ln w_{i,t} = \alpha + \beta X_{i,t} + \epsilon_{i,t}$$

Then, composition adjusted wages for residents in each location j can then be constructed as:

$$\ln w_{i,j,t}^{adj} = \ln w_{i,j,t} - \sum_k \beta_t^k (X_{i,t}^k - \bar{X}_t^k)$$

where $w_{i,j,t}$ is the individual i wage in a location j at the time t , and \bar{X}_t^k is the average of the demographic control k in year t across all individuals. City j composition adjusted wage is computed as the average of the composition adjusted wages of its citizens.

C.2 Quality adjusted rents

In order to be able to compare rent prices across CZs, I need to adjust them for the differences in the quality of the rented housing. I use gross rent which is monthly rental cost of the housing unit, including contract rent plus additional costs for utilities (water, electricity, gas) and fuels (oil, coal, kerosene, wood, etc.).

- **Year build.** Six indicator variables for the year build (0-1 years, 2-5 years, 6-10 years, 11-20 years, 21-30 years, 31+)
- **Number of bedrooms.** Six indicator variables (0 bedrooms, 1, 2, 3, 4, 5+)
- **Kitchen facilities.** Indicator for the presence of the kitchen facilities
- **Plumbing facilities.** Indicator for the presence of the plumbing facilities

Then, for each sample year for the subsample of renters I regress log rents on the set of demographic controls defined above.

$$\ln R_{i,t} = \alpha + \beta X_{i,t} + \epsilon_{i,t}$$

Then, quality adjusted rents for residents of each location j can then be constructed as:

$$\ln R_{i,j,t}^{adj} = \ln R_{i,j,t} - \sum_k \beta_t^k (X_{i,t}^k - \bar{X}_t^k)$$

where $R_{i,j,t}$ is the individual i rent paid in a location j at the time t , and \bar{X}_t^k is the average of the quality control k in year t across all individuals. City j quality adjusted rents are computed as the average of the quality adjusted rents of its citizens.

C.3 CEX data

I use data extracts from the Consumer Expenditure Survey's quarterly interview survey compiled by Ed Harris and John Sabelhaus and provided by NBER. The dataset includes households interviewed between the first quarter of 1980 and the second quarter of 2003. The interviews are conducted during five consecutive quarters: first quarter collects demographic data for each household member, and subsequent four interviews collect data on household level expenditures. The NBER extract aggregates the four interviews into a single observation per household, summing all quarterly expenditures.

As expenditure level data is provided at the household level data, I restrict the sample to the single households, married couples and married couples with children under the age of 21. For each household I define a household head using the procedure developed in [Aguiar & Hurst \(2013\)](#): a head is defined as an individual who identifies herself or himself as a household head in the survey, and if there are multiple heads, the head is identified by sex, employment, age and marital status. To match expenditure data to demographics, I use the demographic data for the identified household head.

Harris and Sabelhaus aggregate expenditures into 47 broad categories. I compute total expenditure using all available categories, and then consider a subsample of categories that is most closely related to locally provided services:

- Food outside of home: includes food and non-alcoholic beverages at Restaurants, Cafes and fast food places, food at school and boarding places.
- Nightclubs: includes alcoholic beverages at restaurants, cafes and bars.
- Clothing: includes expenditures on clothing and shoes, jewelry and watches and tailoring.
- Personal care services: includes expenditures on barbershops, beauty parlors and health clubs.
- Health care services: includes expenditures on drugs and hospitals both out of pocket and included in medical insurance.
- Nursing Homes: includes care in Convalescent or Nursing Home
- Recreation (other recreation category in NBER extract): includes expenditures on repair and rental of recreational equipment, expenditures on pets, expenditures on country clubs, health clubs, swimming pools and other clubs, admission fees for entertainment activities and sporting event.
- Childcare services: includes expenditures on day care centers, nursery schools, elementary and secondary education.

I further restrict my subsample to households that report positive expenditures for the sum of 8 local service categories, and restrict household head to be older than 25. This leaves a sample of 77844 households.

C.4 Amenities

I use establishments counts at the county level in the following NAICS codes as proxies for local amenities:

- Food Services and Drinking places (NAICS 722 except 7224)
- Drinking places (NAICS 7224)
- Clothing and Accessory stores (NAICS 448)
- Golf Courses and Country clubs (NAICS 71391)

- Other recreation (NAICS 7139 except 71391).
- Performing Arts, Spectator Sports, and Related Industries (NAICS 711)
- Motion picture theatres (NAIC 512131)

I further use crosswalks from counties to pumas and from pumas to commuting zones provided by [Autor & Dorn \(2013\)](#). To compute establishment density I scale total number of establishments by commuting zone total population size to get establishment counts per 1000 residents.

Besides, I use geographic amenities data constructed by the United States Department of Agriculture³⁸. These measures are warm winter, winter sun, temperate summer, low summer humidity, topographic variation, and water area. The data is available at the county level. I use crosswalks provided by [Eckert et al. \(2020\)](#) to map the data to Commuting zones. The data is available for 722 CZs out of 741.

D Changes in the individual-level mobility patterns with age

This section studies how the direction of individual's mobility between CZs changes with age. I use 2000 Census sample to identify the subsample of movers: individuals who changed their CZ within a 5 year window. For each mover, I compute the difference between the fundamentals of the destination and origin CZs. I study how the probability of moving up (to a commuting zone with at least 1% higher fundamental of interest) depends on individual age:

$$\text{Up}_{i,j} = \alpha + \beta X_{i,t} + \sum_{i=1}^5 \gamma_i \text{age group}_{i,t} + \psi_j + \epsilon_i$$

Where $X_{i,t}$ is a set of demographic controls for race, sex, nativity and education and ψ_j are location fixed effects. Age groups are 25 – 35, 36 – 45, 46 – 55, 56 – 65, 66+.

Table [D1](#) shows the results. As hypothesised, older individuals are significantly less likely to move to a more productive location as compared to young. The highest difference happens around the retirement age (age group 55-65). Older individuals are also less likely to move to a more populated and expensive location, except for the oldest group of 66+. This group does not move to cheaper places, but still moves to places with a significantly higher share of old, indicating the reallocation for amenity reasons.

³⁸<https://www.ers.usda.gov/data-products/natural-amenities-scale>

TABLE D1
DIRECTION OF INDIVIDUAL MOBILITY BY AGE

	Higher Wage	Higher Pop.	Higher Rent	Higher old share
[36 – 45]	-0.023*** (0.002)	-0.022*** (0.002)	-0.021*** (0.002)	0.02*** (0.002)
[46 – 55]	-0.047*** (0.003)	-0.04*** (0.003)	-0.035*** (0.003)	0.043*** (0.003)
[56 – 65]	-0.088*** (0.005)	-0.066*** (0.005)	-0.047*** (0.003)	0.099*** (0.006)
66+	-0.043*** (0.005)	-0.027*** (0.004)	-0.004 (0.004)	0.084*** (0.007)
Obs.	1,091,989	1,091,989	1,091,989	1,091,989
R-squared	0.307	0.335	0.299	0.299
CZ FE	YES	YES	YES	YES
Controls	YES	YES	YES	YES

Results relative to the youngest group 25-35. Standard errors in parentheses are clustered at the CZ level

E Mobility Costs Estimation

E.1 Distance between CZs

I use the data from the county distance database³⁹ that computes great-circle distances calculated using the Haversine formula based on internal points in the geographic area for all pairs of counties in the US. To compute the distances between the CZs, I map each 1990 county to a single 1990 CZ using the crosswalk in [Eckert et al. \(2020\)](#) based on the largest area of the intersection.⁴⁰ Then I compute a distance between CZs as an area weighted average distance between counties in two CZs.

E.2 Mobility Data

For the main regression I use Census IPUMS data for the year 2000 that provides individual level data on the current location and location 5 years ago at the PUMA level. I aggregate all migration PUMAs to commuting zones and compute $L_{ij}^5(a)$ - the number of individuals of age a who were in the CZ i five years ago and are currently in the CZ j using the crosswalk weights between migration PUMAs and CZs. As the crosswalks weights provide many to many mapping, for each PUMA to PUMA migration flows, I find all CZs corresponding to origin and

³⁹<https://www.nber.org/research/data/county-distance-database>

⁴⁰because 1990 CZs were constructed as a collection of 1990 counties, a one to one mapping works well

destination PUMAs, and I allocate the weight of the observation to CZ flows according to the area intersection weights provided in [Autor & Dorn \(2013\)](#).

E.3 Estimating mobility regression

In the data I observe $L_{ij}^5(a)$. I use five year mobility data for individuals of age $a \in [63, 72]$. I further assume that conditional on reallocation, the probability that it happens at age a is p_a :

$$p(a) = p\lambda^{(a-58)} \quad \frac{p(1 - \lambda^{15})}{1 - \lambda} = 1$$

That is probabilities decline with age at the rate λ , and the sum of probabilities between ages 60 and 75 should be equal to one.

Let Π_5 be the probability that an individual is in the same location as 5 years ago. Then:

$$1 - \Pi_5(a) = (1 - \Pi)p_a^*$$

where $p_a^* = p\lambda^{(a-65)}(1 + \lambda + \lambda^2 + \lambda^3 + \lambda^4)$ is the probability of reallocation within the last 5 years.

Given the assumptions made above, the probability that an individual of age $a \in [63, 72]$ is in the same location as 5 years ago is:

$$\Pi_5(a) = \Pi(a) + (1 - \Pi(a))(1 - p_a^*)$$

$$\Pi(a) = \frac{1}{p_a^*}(\Pi_5 - (1 - p_a^*))$$

Given the assumptions made in the previous section:

$$\frac{L_{ij}^5(a)}{L} = \pi_{ij}p_a^*$$

$$\sum_{a=63}^{a=72} \frac{L_{ij}^5(a)}{L} = \pi_{ij} \sum_a p_a^*$$

Therefore, the share of individuals who moved from i to j within a 5 year window corresponds to the share of individuals who move from i to j up to the scale. As the scale parameter will be absorbed in the fixed effects, I can use $\sum_{a=63}^{a=72} L_{ij}^5(a)$ as a proxy for L_{ij} in the main regression.

F MSA calibration

Due to the data availability issues, historical comparison between 1960 and 2010 is available only at the MSA level. This section provides additional details on the mapping of the model to the MSA data for the years 1960 and 2010. I select 169 MSAs available in the Census data for both time periods.⁴¹ Using the Census data I construct the vectors of wages, rents, young and old location choices $\{W_{i,t}, R_{i,t}, L_{i,t}^y, L_{i,t}^o\}$ corresponding to 169 US MSAs for years $t = 1960, 2010$.⁴² I keep all the structural parameters fixed at their calibrated values described in section 6.2, except for the relative length of the old period ρ and the fixed mobility cost κ . I recalibrate ρ_t for each year $t = 1960, 2010$ so that to match the ratio of the sizes of the older and younger age groups.

I take mobility costs for year 2010 to be equal to the calibrated mobility costs for the full model (see section 6.3), where the quantification was based on the 5 year window mobility data for the year 2010. I further calibrate the mobility costs for 1960 to match the evidence on an increase in the older population mobility during 1960-2010 period. Due to the data limitations, I can only compare the individual level mobility data across U.S. states within a 5 year window. I compute that mobility around retirement age increased by around 21% over 1960-2010.⁴³ I further calibrate the fixed component of mobility costs for retirement model in 1960 together with the amenities for young and old $\{a_{60}^y, a_{60}^o\}$ so that the share of older individuals who reallocate is 22 percent lower than in 2010.⁴⁴ The calibration procedure follows the same steps as in the main text of the paper. This allows me to compute that a model implied decline in mobility costs is equal to 36 percent. The following steps are the same as in the main calibration, except for the different vectors of the data.

⁴¹169 MSAs available in both time periods cover 58 percent of the population in 1960 and 67 percent of the population in 2010

⁴²Construction of the samples $\{W_{i,t}, R_{i,t}, L_{i,t}^y, L_{i,t}^o\}$ follows the same steps as in the main calibration, see section C

⁴³I compute that 3.97% of individuals older than 55 moved between U.S. states in 1960, while the corresponding number for 2010 is 4.83%. In contrast, the rise in the mobility of the younger age group (25-55) was much lower and equal to 4.4%.

⁴⁴Here I implicitly assume that an increase in mobility across MSAs over the same time period is the same as across MSAs

G Additional tables

TABLE G2
DETERMINANTS OF MODEL IMPLIED
AMENITIES

Dependent Variable	(1) a_i^o/a_i^y	(2) a_i^o/a_i^y
Golf and Country clubs	0.34*** (0.06)	1*** (0.12)
Hospitals	0.34*** (0.06)	1.14*** (0.31)
Personal care	0.36*** (0.06)	0.92*** (0.16)
Nursing homes	0.33*** (0.06)	0.48*** (0.17)
% Water area	0.08*** (0.023)	0.39*** (0.07)
January temperature	0.16*** (0.06)	0.05 (0.08)
Food & drinking	-0.2 (0.18)	-1.9*** (0.53)
Movie theatres	-0.4*** (0.05)	-0.53*** (0.13)
Childcare	-0.17*** (0.06)	0.12 (0.13)
Schools	-0.05 (0.03)	-0.2* (0.11)
Museums and Parks	-0.07* (0.04)	0.32*** (0.11)
Clothing	-0.06 (0.06)	0.58** (0.15)
Arts	-0.008* (0.05)	-0.34*** (0.11)
July temperature	0.16 (0.09)	0.23*** (0.08)
Topography	-0.0016 (0.02)	0.14*** (0.06)
Observations	722	722
R-squared	0.36	0.67
Weighted by CZ population		✓

p -value *** $p \leq 0.01$, ** $p \leq 0.05$, * $p \leq 0.1$. Robust standard errors are given in parenthesis. All variables are in logs are in logs. Includes 722 mainland commuting zones.

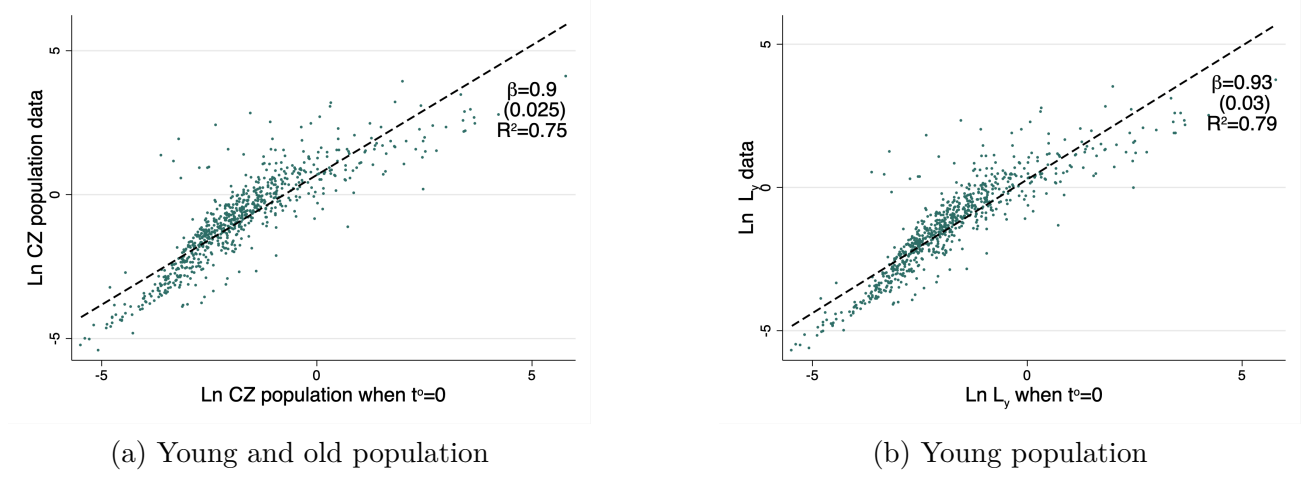
TABLE G3
LOCAL EFFECTS OF THE PLACE-BASED
POLICIES TARGETED AT RETIREES

L	L^y	L^o	N^y	N^o	a^y	a^o	R
5.36	-3.4	19.43	3.01	10.6	0.3	0.4	3.8

The table shows the percentage response of the corresponding local variables to a 10% subsidy for retirees for moving into a city. N^y denotes the number of firms in the non-tradeable category 1 that is valued more by young. N^o denotes the number of firms in the non-tradeable category 2 that is valued more by old.

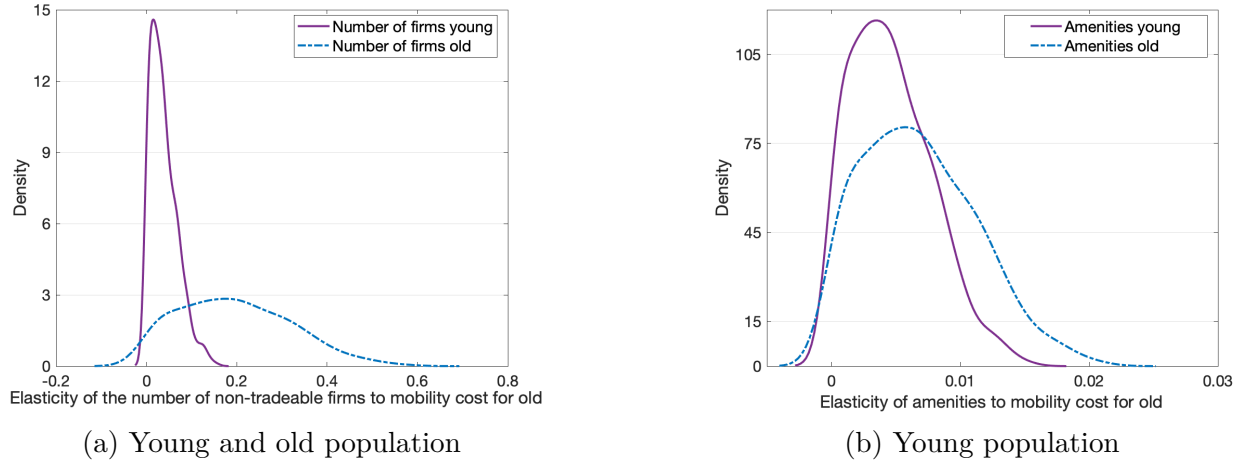
H Additional figures

Figure H5: Fit of the model with no life cycle



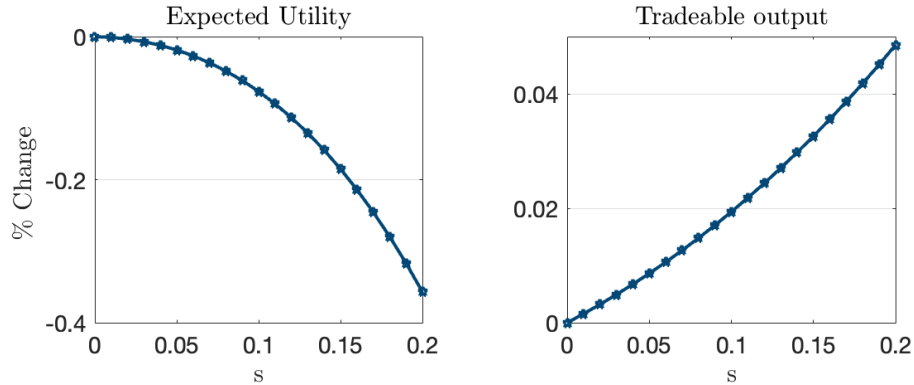
The left graph shows on the vertical axes the log of the CZ population and the horizontal axes the log of the predicted CZ population in a model with no life cycle ($t_o = 0$) and ($t_y = T$). The right graph shows on the vertical axes the log of the number of younger rage group (age 25-60) and on the horizontal axes the log of the predicted number of younger residents in the model with no life cycle. β is the resulting regression coefficient. Robust standard errors are in parenthesis

Figure H6: Elasticities of amenities and number of non-tradeable firms to the mobility of old



The left graph shows the kernel density of the distribution of the number of firms in two non-tradeable sectors (sector 1 preferred more by young and sector 2 preferred more by old in response to a decline in the mobility costs of retirees to move to a CZ). The right graph shows same density for the amenities of young and old

Figure H7: Aggregate effects of the policy that subsidises the reallocation of old to smaller cities



Aggregate effects of the policy that introduces of a subsidy s measured as a percentage of individuals' average wages given to any old individual moving to a treated city. The policy is financed via a lump sum tax paid by all workers in the economy. Treated cities are the cities in 25th quantile by productivity