

# Location Choices over the Life Cycle: The Role of Relocation for Retirement

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## Abstract

The location choice of an individual is shaped by the trade-off between job opportunities, prices, and access to amenities. I provide evidence that the determinants of this trade-off change over the individual's life cycle: the productivity of a location is more valuable for workers than retirees, and changes in spending patterns with age imply that younger and older individuals value different types of local amenities. To study the allocation of younger and older individuals across cities, I develop and quantify an overlapping generations spatial equilibrium model with location choices for both work and retirement periods. I show that differences in local exogenous productivities and amenities for the young and the old lead to the geographic sorting by age, which is further amplified by an endogenous adjustment of amenities and productivities to the location's age composition. I estimate that the reduction in mobility frictions observed between 1960 and 2010 allowed individuals to increasingly separate locations for work and retirement, which generated welfare gains of around 6.3 percent. Using the calibrated model, I evaluate local and aggregate effects of place-based policies that promote the reallocation of retirees to less productive cities.

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# 1 Introduction

An individual’s location choice is shaped by the trade-off between job opportunities, housing prices, and the access to amenities ([Rosen \(1979\)](#), [Roback \(1982\)](#), [Allen & Arkolakis \(2014\)](#), [Desmet & Rossi-Hansberg \(2013\)](#)). The determinants of this trade-off can vary significantly over the life cycle: after retirement individuals no longer directly benefit from a location’s productivity, but they are still affected by local prices. Moreover, younger and older individuals might value local amenities differently due to changes in preferences and spending patterns with age. Yet, the literature on economic geography has mostly focused on a static location choice, abstracting from modelling the life cycle.

Understanding the life cycle component of location choices becomes especially important with the ageing population trend. Indeed, the growing population of retirees might fuel the development of cities attractive for the old: for instance, the retirement community, The Villages, FL, was the fastest-growing metro over the period 2010-2020. Some states and cities put in place a range of policies aimed at attracting relocating retirees.<sup>1</sup> However, local and aggregate effects of such policies have been largely unexplored.

In this paper, I study the role of the life cycle for individuals’ location choices and for the distribution of economic activity across space. First, I provide new empirical evidence on the sorting by age across U.S. commuting zones (CZs). Second, I develop a structural framework of location choice over the life cycle: workers live for two periods and make a work-location decision in the first period, and a retirement-location decision in the second. I use my framework to estimate the values of CZs separately for its younger and older residents, and to quantify the gains from declining mobility costs for moving for retirement. I further evaluate the determinants of a city’s ability to grow by attracting retirees, and I quantify the effects of place-based policies that incentivize the relocation of the old to less productive cities.

I start by documenting sorting patterns by age and CZ productivity, proxied by its wage: a 1% higher CZ wage is associated with a 0.9% lower CZ old-to-young ratio.<sup>2</sup> I show that this cross-sectional relationship is related to the changes in the mobility patterns with age: more productive locations receive an inflow of individuals in the younger age cohort and an outflow of individuals in the older age cohort. Moreover, I document that a CZ age composition is correlated with the composition of its establishments: CZs with a higher old-to-young ratio have a higher number of health-care and recreation centers per capita, but a lower number of

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<sup>1</sup> For example, Alabama’s state employee retirement system finances a series of golf courses in local cities. City Tallahassee in Florida gives direct reallocation subsidies for retirees to move there: “Florida city Wants more Retirees and is Going After Them”(NYT article)

<sup>2</sup>The old-to-young ratio is defined as the ratio of 60+ years old to 25 – 59 years old. I adjust CZ wages for the differences in their demographic composition to proxy for location-specific wage component. I will further discuss the connection between spatial heterogeneity in wages and productivity in the model.

clothing stores, movie theatres, and childcare centers per capita. Using consumer expenditure data, I show that younger and older age groups differ in their demand for the services provided by these establishments.<sup>3</sup>

The empirical evidence on the geographic sorting by age emphasizes two key changes over the life cycle that might affect the location choice: a decline in working hours, which makes location's productivity less important, and changes in expenditures on local services, which affect preferences for local amenities. Also, young and old individuals might differ in their preferences for location's natural and climate amenities.<sup>4</sup> I develop a theoretical framework by introducing these life cycle changes into a spatial equilibrium model, building on [Allen & Arkolakis \(2014\)](#), [Monte et al. \(2018\)](#), and [Redding & Sturm \(2020\)](#). The key model ingredients are the following: (i) individuals choose locations for both work and retirement periods subject to mobility costs of moving for retirement; (ii) workers and retirees differ in their preferences for exogenous amenities of locations and for endogenous non-tradeable services and (iii) local services are provided by amenity developers and adjust endogenously to local expenditures. I also assume that the productivity of the tradeable sector is subject to agglomeration spillovers as in [Allen & Arkolakis \(2014\)](#). In the model, dynamics arise for two reasons: first, the young anticipate costly relocation for retirement, and second, workers only earn wages in the first period and so there is a savings decision embedded in their work decision.

I estimate the model using cross-sectional data on U.S. CZs, data on mobility patterns around the retirement age, and data on the consumer spending patterns. In particular, I estimate a model-implied gravity equation for moving for retirement, and I find that mobility costs for the old increase significantly with the distance between CZs. I further calibrate the fixed component of mobility costs for the old and the composite amenities for the young and the old across CZs to match data on different locations' young and old residents, wages, and rents, and to match the aggregate share of individuals who relocate for retirement. I document significant heterogeneity in CZ amenities for the old relative to the young, which is partially explained by differences in CZs geography, climate, and composition of non-tradeable establishments. Next, I quantify the endogenous adjustment of amenities to the location's age composition by estimating the heterogeneity between younger and older age groups in expenditure shares on local services.

Using the fully calibrated model, I show that differences in exogenous productivities and exogenous amenities across locations lead to geographic sorting by age. Sorting is further amplified by an endogenous adjustment of location's productivity and amenities to location's

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<sup>3</sup>I show that older individuals spend more on health care services but less on clothing, childcare and food outside of home.

<sup>4</sup>I show that the CZ old-to-young ratio is positively correlated with better climate (warmer winters and cooler summers) and natural amenities (percentage of water area and topography). This is consistent with the findings in [Lu \(2020\)](#) and [Schneider & Green \(1992\)](#) that older individuals increasingly move to locations with better climate and natural amenities

age composition. To build intuition for this result, consider the CZs of New York (NY) and Sarasota (FL). According to the model estimates, New York is endowed with a higher exogenous productivity, whereas Sarasota is endowed with better exogenous amenities for the old. Because retirees no longer benefit from local wages, they are less willing to pay high prices in exchange for productivity. Moreover, retirees are attracted by better amenities for the old in Sarasota. Therefore, the model predicts a net reallocation of retirees from a more productive to a more amenable city. As a result, housing constraints relax in New York, tighten in Sarasota, and push more young towards New York. This further magnifies productivity differences in two cities due to the presence of productivity spillovers. Additionally, the composition of local establishments shifts with local expenditures, which makes New York even more amenable for the young (e.g., more bars and restaurants), and Sarasota even more amenable for the old (e.g., more health care facilities).

I further illustrate how the model explains the documented empirical facts on the geographic sorting by age. I compute that if the only change over the life cycle was the decline in working hours after retirement, that is if the old had the same preferences as the young, then the elasticity of the old-to-young ratio with respect CZ's wages would be equal to  $-0.7$  as compared to  $-0.9$  in the data. Therefore, most of the observed negative relationship between CZ wages and demographics is attributed to the decline in working hours after retirement, and the rest is attributed to relative amenities for the old being better in less productive locations. Next, I find that the endogenous adjustment of local services to the differences in expenditure shares between the young and the old explains most of the documented correlation between the CZ old-to-young ratio and the CZ composition of establishments.

The model estimates show that the value of a given location differs significantly for its younger and older residents. This implies large gains from separating locations for work and retirement periods. I estimate that moving from an area at the 25th percentile of the value for the old to an area at the 75th percentile is equivalent to increasing the individual's income by a factor of two. This large dispersion in the location-specific utilities of the old is sustained by significant mobility costs that retirees face. This also implies that location decisions for the work period depend on how easy it is to move from the location to places that are valuable for retirement. In particular, the model estimates show that at least thirty percent of the spatial variation in working age population across the U.S. CZs can be explained by the locations' values for the old. I further show that a decline in mobility frictions allows the old to increasingly choose CZs that are cheaper and more amenable for the old, and also allows the young to increasingly choose CZs that are more productive and more amenable for the young.

Using the MSA-level data, I show that the sorting by age and location's productivity significantly increased from 1960 to 2010. I also document that the share of individuals who

moved between states around the retirement age increased by 22 percent from 1960 to 2000.<sup>5</sup> Using the modelling framework, I decompose the changes in geographic sorting by age over time into the changes caused by mobility frictions and into the changes caused by location-specific factors. I compute that the model implied decline in mobility frictions explains most of the increase in sorting over the 1960-2010 period. I estimate that the resulting welfare gains from higher life cycle mobility are equal to 6.3 percent.

To study the local effects of place-based policies targeted at retirees, I compute the elasticity of local retiree population with respect to a local subsidy for the relocating old.<sup>6</sup> I do this separately for each CZ. This elasticity determines the impact of policies that aim to attract older movers. I find that the elasticity varies from around 0 to almost 1.4 across U.S. CZs. The response is significantly higher in locations with a smaller working age population, a larger share of older individuals and in locations that are closer to more populated CZs. I show that an inflow of retirees increases the variety of locally provided services, and that this effect is magnified for less productive cities as retirees relocating from more productive cities bring accumulated savings with them. Next, I evaluate place-based policies that subsidize the reallocation of retirees to less productive cities through a universal lump-sum tax paid by workers. I show that such policies contribute to a more equal distribution of amenities across cities, and, as compared to the place-based policies targeted at workers, lead to an increase in the aggregate productivity. However, these policies are not welfare improving, because the efficient allocation does not feature higher sorting of younger and older individuals.

Finally, I show that the ageing population trend increases the importance of retirement for location choices and increases the role of reallocating retirees for the spatial equilibrium. I show that predicted changes in demographics between 2020 and 2040 are expected to generate a significant shift in the distribution of economic activity across space with a reallocation of activity towards cities that are more attractive for the older age group.

**Relationship to the literature.** The paper builds on the literature on quantitative spatial models that include static environments [Roback \(1982\)](#), [Redding & Sturm \(2008\)](#), [Allen & Arkolakis \(2014\)](#), [Redding & Sturm \(2020\)](#), and recent dynamic models [Desmet & Rossi-Hansberg \(2014\)](#), [Eckert & Peters \(2018\)](#) and [Allen & Donaldson \(2018\)](#). I extend existing frameworks by modelling the individual’s life cycle: I introduce the location choices

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<sup>5</sup>Using U.S. Census samples for years 1960 and 2010, I compute the share of individuals of age 55+ who changed their state of residence over the 5 year window. Same for the age group 25 – 55. I consider a lower age cut-off to capture the fact that individuals can move for retirement reasons before actual retirement. The increase in the mobility of the younger age group was only around 4 percent. The comparison is available only for 1960 and 2000 Censuses due to the data availability issues.

<sup>6</sup>Individuals are given a monetary transfer in case they move into the treated CZ for retirement. This counterfactual abstracts from modelling the financing side of the policy. This assumption will be relaxed in the policy exercise.

for both work and retirement periods, and allow for the transfer of individual’s accumulated savings across locations and time.<sup>7</sup> I show that the extended model remains tractable, and allows for the usage of model inversion techniques to recover the amenities for the young and the old across locations.

The paper is related to the recent studies that model the location choice as a part of the individual’s dynamic problem (Bilal & Rossi-Hansberg (2018) and Giannone et al. (2019)). These papers focus on understanding the role of financial constraints and housing for location decisions. In my paper, I contribute to this line of work by studying how the changes in working hours and preferences over the life cycle affect location choices. Bilal & Rossi-Hansberg (2018) do not model changes in working hours and preferences with age. Giannone et al. (2019) model features the decline in working hours after retirement, but younger and older individuals have same preferences for locations’ amenities. Another major difference is that the model in this paper has closed form solutions for the distribution of individuals across locations, so I can invert the model to solve for unobserved amenities for the young and the old across U.S. CZs. Model tractability also allows me to analyze efficiency properties of my model in order to discuss optimal sorting of the young and the old, and policies geared toward that.

A growing literature considers how heterogeneous preferences for consumption amenities reinforce sorting of high and low skilled households within or across cities. (Diamond (2016), Guerrieri et al. (2013), Couture et al. (2019), Su (2020), Hoelzlein (2019)). Closest to this paper, Almagro & Dominguez-Ino (2019) identify heterogeneous response of amenities to the demographic composition of city’s neighbourhoods. This paper further studies whether city-level amenities adjust to a city’s age composition, and quantifies the contribution of this mechanism to the sorting of the young and the old across cities. I follow the recent studies that microfound amenity spillovers through the endogenous entry of establishments producing non-tradable goods (Almagro & Dominguez-Ino (2019), Couture et al. (2019), Hoelzlein (2019)). I use the life cycle changes in the individual’s spending profiles (Aguiar & Hurst, 2013) to quantify the endogenous adjustment of amenities to the differences in the preferences of the young and the old.

The paper complements the research on the local and aggregate effects of place-based policies. Kline & Moretti (2014) and Glaeser & Gottlieb (2008) argue that due to the constant elasticity of spatial spillovers there are no gains from reallocating workers across cities. Fajgelbaum & Gaubert (2020) and Rossi-Hansberg et al. (2019) show that due to the differences in spatial spillovers that heterogeneous workers generate, there is a room for place-based policies that target the sorting of workers across space. In this paper, I extend

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<sup>7</sup>In the models introduced in Desmet & Rossi-Hansberg (2014), Eckert & Peters (2018) and Allen & Donaldson (2018) individuals consume all of the earnings made during the period, and there are no changes in working hours and preferences over time.

their results for the dynamic life cycle setting, where individuals contribute to local spillovers differently as they age. In addition, I model endogenous amenities through the entry of local establishments, rather than introducing them in a reduced form way. Consistent with the findings in the literature, I show that the presence of productivity spillovers and location preference shocks requires optimal place-based policies targeted at workers. I further show that differences between the young and the old in spatial spillovers don't require additional policies targeted at the sorting by age and location.

The paper relates to the literature that studies the determinants of the mobility flows for retirement using individual-level mobility data around the retirement age (Lu (2020), Schneider & Green (1992), Duncombe et al. (2001)). Retirees were found to be attracted to places with favourable climate and natural amenities and to places with lower taxes and lower living costs. Rosenthal & Strange (2004) show that couples near retirement age tend to move away from places with favourable business environments and towards places with high values of amenities. To the best of my knowledge, this paper is the first to document the pattern of the geographic sorting by age and location's productivity in the U.S and its changes over time. Moreover, I argue that local amenities might differ for the young and the old, and I use the aggregate data on the demographics of the U.S. CZs combined with the spatial structure of the model to recover these differences.

The remainder of the paper proceeds as follows. Section 2 describes the data and definitions used in the paper. Section 3 presents empirical analysis with the description of empirical facts. Section 4 introduces the theory and discusses its efficiency properties. Sections 5 and 6 describe the calibration of the model and its quantitative analysis. Section 7 describes counterfactual exercises. Section 8 concludes.

## 2 Data

This paper uses the 5 percent samples of the U.S. Censuses for the years 1960, 1980, 1990, 2000 and 1 percent samples of American Community Survey for the years 2012 -2016 which I aggregate into a single observation corresponding to the year 2014. The data is from Integrated Use Microdata Series (IPUMS), Ruggles et al. (2015). The IPUMS data provide detailed economic and demographic information at the individual level, including data on wages, housing costs, age, education, and geographic location of residence.

To proxy for amenities, I use establishment-level data from the County Business Patterns for year 2014 and climate and geography data from United States Department of Agriculture.<sup>8</sup> The expenditure level data come from the NBER extracts of the Consumer Expenditure Survey

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<sup>8</sup><https://www.ers.usda.gov/data-products/natural-amenities-scale>



(CEX), which includes all waves from 1980 through 2003. The CEX data provide household level observations on expenditures made in a wide set of consumption categories.

## Definitions

**Commuting Zones.** The unit of geography is a commuting zone (CZ), which is an aggregation of the U.S. counties that partitions the U.S. and is designed to proxy for the local labor markets. I use time consistent mapping between Census Pumas and 741 US commuting zones provided by [Autor & Dorn \(2013\)](#).

**Age groups.** I define by the younger age group individuals whose age is between 25 and 59 years, and by the older age group individuals older than or equal to 60. Using IPUMS data and age group definitions, I compute the young and the old population of each CZ in the U.S.

**Composition adjusted wages.** To proxy for the CZ productivity, I use the IPUMS data on the average wages earned by CZ workers.<sup>9</sup> I adjust wages for the differences in worker’s age, sex, race, nativity and highest completed education. More details are in [Appendix A](#). The resulting composition adjusted wages control for the differences in observable characteristics of the CZ workforce, and, therefore, proxy for the location-specific component of individual’s wages.

**Quality adjusted rents.** To proxy for the local prices, I use the IPUMS data on the average rents paid by the households in a given location. I adjust rents for the observed quality characteristics of the rented unit, so that to compare prices of similar units of housing across locations. More details are in [Appendix A](#).

**Amenities.** I follow [Diamond \(2016\)](#) and [Almagro & Dominguez-Ino \(2019\)](#) in measuring the availability of local amenities by using the densities of establishments in different service industries. Details on the construction of the industry groups are in [Appendix A](#). To proxy for CZ natural and climate amenities, I use the data from USDA on January hours of sun, January average temperature, July average temperature, topography and percentage of water area. This data is available only for 722 continental CZs.

## 3 Motivating empirical evidence

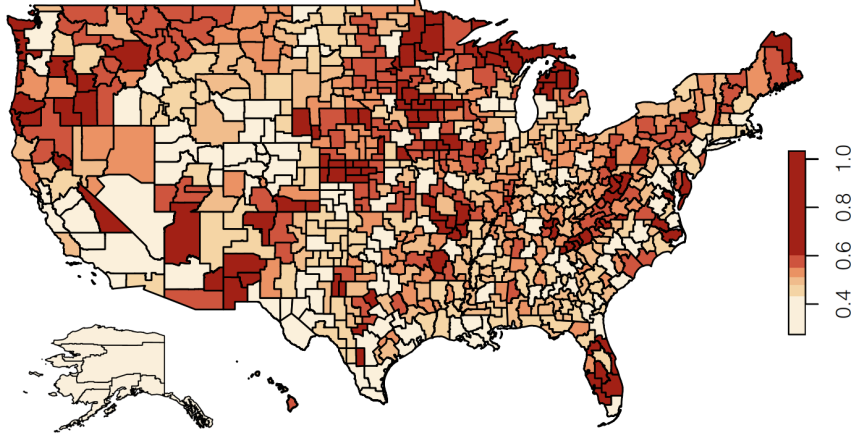
This section documents new facts on the geographic sorting by age. First, I show that there exists significant dispersion in the old-to-young ratios across U.S. CZs. Second, I document that CZ productivity is negatively related to its old-to-young ratio. I show that this cross-sectional relationship is consistent with the changes in mobility patterns with age: more productive CZs

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<sup>9</sup>By workers I define individuals of age 17-64, who work more than 44 weeks and more than 34 hours a week.



Figure 1: Demographic composition of US CZs (age 60+ to age [25,60))



The figure shows the distribution of the ratio of older residents (age 60+) to younger residents (age 25-59) across 741 U.S. CZs for the year 2014 (average across 2011-2016 ACS)

receive an inflow of individuals in the younger age cohort and an outflow of individuals in the older age cohort. Third, I show that the CZ old-to-young ratio is correlated with the composition of its establishments in a way that is related to the differences in expenditure patterns between the young and the old.

### 3.1 Geographic sorting by age across U.S. CZs

Figure 1 shows the distribution of the older age group relative to the younger age group across the U.S. CZs. There exists significant heterogeneity in the old-to-young ratios which vary from around 0.28 to almost 1. The highest ratio is in CZ Ocala in Florida, which is the home to one of the largest retirement communities in the U.S. Villages with lots of amenities specifically designed for older residents.<sup>10</sup> The lowest ratio is in CZ Kodiak in Alaska.

To evaluate the magnitude of the geographic sorting by age, I compute the average dissimilarity index for the younger and the older age groups across Census samples of 1980, 1990, 2000 and 2014.<sup>11</sup> The resulting value is 0.085, which indicates that 8.5% of older individuals need to be reallocated in order to distribute them evenly across all U.S. CZs. The same index for high and low skill workers, geographic sorting of which has been widely studied

<sup>10</sup>Villages is an age-restricted community, that legally discriminates on the basis of age, and limits residency only to individuals older than 55. The available amenities include golf and country clubs, swimming pools and other recreational activities.

<sup>11</sup>The dissimilarity index is defined as  $\frac{1}{2} \left| \frac{L_i^o}{\sum_i L_i^o} - \frac{L_i^y}{\sum_i L_i^y} \right|$  where  $L_i^o$  is the size of the older age group in the location  $i$ , and  $L_i^y$  is the size of the younger age group in  $i$

Figure 2: Sorting of the young and the old by productivity



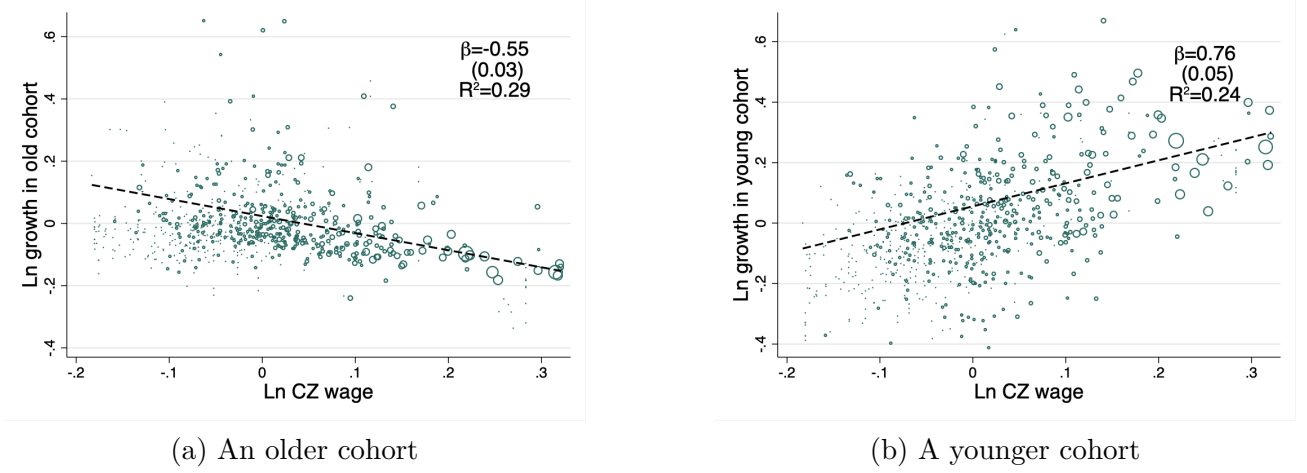
The figure plots CZ's ratio of individuals older than 60 to individuals between ages 25 and 60 against CZ's average wages earned by workers. Both variables are logs of the averages of demeaned values across 1980, 1990, 2000 and 2014 samples. CZs' wages are adjusted for the differences in CZs' demographics.  $\beta$  stands for the OLS regression coefficient and robust standard errors are in parenthesis. Regressions are weighted by location's average population across same samples. The size of each CZ circle is proportionate to its average population.

in the literature, is equal to 0.143. While the degree of geographic sorting by age is lower than the degree of geographic sorting by skill, it is still large, and its magnitude might be dampened by mobility frictions that older individuals face.

### 3.2 Sorting by age and location's productivity across the U.S. CZs

One potential reason behind the geographic sorting by age is that after retirement individuals no longer benefit from location's job opportunities. So in this section I explore whether the geographic sorting by age is systematically related to the differences in locations' productivities. For each CZ, I compute its old-to-young ratio and the average composition adjusted wages earned by its residents. As the goal is to study the long-term relationship between the location-specific productivity and its age composition, I consider the averages of both variables across Census samples of 1980, 1990, 2000 and 2014. Figure 2 shows that the CZ old-to-young ratio is significantly and negatively related to the CZ wage with the elasticity of  $-0.9$ . As shown in Appendix C, the result is robust to considering retirees instead of old, to considering different age cut-offs and to using equal weights for the CZs. I also show that the pattern of sorting remains strong even when CZ productivity is proxied by its average wages 44 years ago, suggesting that persistent component of differences in location-specific productivities is driving the sorting

Figure 3: Reallocation of young and old cohorts across CZs



The figure plots the CZ's growth in the population of a given cohort over the ten year period against the CZ's average wages earned by workers in periods  $t$  and  $t + 10$ . Both variables are logs of the averages of demeaned values across 1980-1990, 1990-2000 and 2000-2010 samples. An older cohort denotes individuals who fall into the age category 47-57 in the Census year  $t$  and a younger cohort denotes individuals who fall into the age category 15-25 in the Census year  $t$ . CZs' wages are adjusted for the differences in CZs' demographics.  $\beta$  stands for the OLS regression coefficient and robust standard errors are in parenthesis. Regressions are weighted by location's average population across same samples. The size of each CZ circle is proportionate to its average population.

pattern.<sup>12</sup>

Next, I study whether the observed cross-sectional relationship between the CZ productivity and its age composition is supported by the data on the changes in the mobility patterns with age. First, I explore the reallocation patterns of different age cohorts across U.S. CZs over a ten year period. I consider a cohort of older individuals (age 47-56) and follow them in the next decade when they potentially retire (57-66). Similarly, I consider a cohort of younger individuals (age 15-25) and follow them in the next decade when they potentially start working. Denote by  $L_{m,t}^c$  the population size of a cohort  $c$  in location  $m$  and Census year  $t$ . For each CZ  $m$ , I compute the ratio  $L_{m,t+10}^c / L_{m,t}^c$  to proxy for the reallocation patterns of the cohorts: a higher ratio implies that CZ  $m$  has a higher net inflow of individuals of cohort  $c$  over the ten year period. I use average values for 1980-1990, 1990-2000 and 2000-2010 Censuses to partially smooth the time effects for a particular cohort. Figure 3 shows that more productive CZs on average experience an outflow of individuals from the older cohort and an inflow of individuals from the younger cohort, suggesting that individuals move to more productive locations when young and then relocate to less productive locations for retirement.

Appendix C.2 provides additional details on the relocation patterns of the young and the

<sup>12</sup>In Appendix C, I show that the CZ old-to-young ratio in 2014 is significantly and negatively related to the CZ wage in 1970 with the elasticity of  $-0.6$

old cohorts. First, I show that the results are similar in all three time periods considered separately.<sup>13</sup> Second, I consider the relocation patterns of the cohorts with respect to the changes in CZ wages over the ten year period. I show that while younger individuals indeed move to CZs with growing wages, older individuals don't move to CZs with declining wages, and even tend to move to CZs with growing wages in the recent decades.<sup>14</sup> This suggests that relocation of older individuals to less productive locations is driven by the long-term differences in location-specific productivities, rather than by changes in the productivity over time.

In Appendix B, I use the data on individual's location five years ago to show that older movers have a lower probability of moving to a more productive location but a higher probability of moving to a location with a higher share of old. I also show that the largest change in mobility patterns happens around the retirement age (56-65).

### 3.3 CZ age composition and its amenities

Another potential reason behind the geographic sorting by age is that younger and older individuals value location's amenities differently. This section explores whether location's age composition is related to the observable measures of its amenities. I consider climate and natural variables from USDA and measures of the variability of local services. The latter is approximated by the number of CZ establishments in different non-tradeable industries per thousand residents. Figure 4 shows the results from the regression of the CZ old-to-young ratio on a set of its amenities controlling for CZ wages, population and prices. I find that CZs with a higher ratio of old to young residents have a significantly higher number of health care centers, nursing homes and recreational facilities (such as golf and country clubs) per capita, but lower number of clothing stores, childcare centers and bars per capita. In line with the results of previous studies (Lu (2020), Schneider & Green (1992)), CZs with a higher old-to-young ratio tend to have more favourable climate (warmer winters and cooler summers) and more favourable natural amenities (higher percentage of water area and higher topography).

### 3.4 Differences in expenditure shares by age

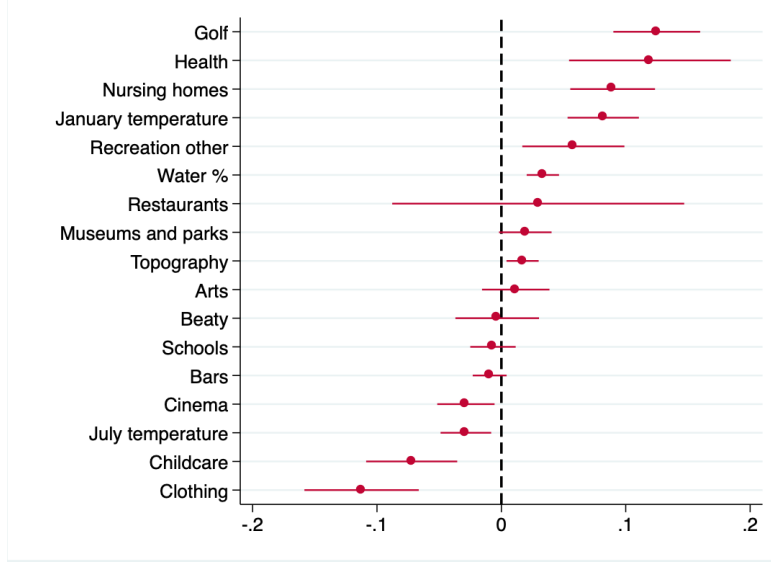
If younger and older individuals differ in their preferences for locally provided services, these differences should be reflected in their expenditure patterns. Using the consumer expenditure

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<sup>13</sup>Appendix C.2 computes the relationship between  $L_{m,t}^c$  and average wages in  $t$  and  $t + 10$  for  $t = 1980, 1990, 2000$ .

<sup>14</sup>This evidence does not contradict the suggestion that the young and the old value location's productivity differently. Appendix C.2 shows that growth in the young cohort is more strongly related to the growth in CZ wages. So it might be that CZs that experienced productivity growth also experienced the growth in amenities, which attracted both the young and the old.

Figure 4: CZ age composition and its amenities



The figure plots point estimates and 95% confidence intervals from the single regression of the log of CZ share of old (residents of  $age \geq 60$  relative to residents  $25 \leq age < 60$ ) on the set of local amenities. Logs of CZ population, wages and rents are included as controls. Standard errors are robust to heteroskedasticity. Demographics data is from 2012-2016 ACS. Establishment counts are from CBP year 2014. Data on natural amenities is from USDA. Details on the construction of establishment categories are in appendix A.4

data (CEX), I compute expenditure shares at the household level on a set of consumption categories roughly corresponding to local industries considered in the previous section. The available groups are: food outside of home, alcohol consumption outside of home, clothing, personal care services, health care services, low level education, childcare services, recreational services, and nursing home services. More details on the data construction and the composition of the categories are in the Appendix A.3. To evaluate the effect of the household's head age on the expenditure shares, I estimate the following specification for each service category:

$$\log(s_{it}^n) = \alpha + \beta \text{age}_{\geq 60} + \delta X_{it} + \psi_t + \epsilon_{it}$$

where  $s_{i,t}^n$  is the share of the consumption category  $n$  in individual's  $i$  total expenditures at year  $t$ ,  $\text{age}_{\geq 60}$  is the dummy for the age 60 or older,  $\psi_t$  is the time fixed effect and  $X_{it}$  is the set of demographic controls for race, sex, marital status and education.

Table 1 presents the estimation results. In line with the cross-sectional evidence on CZ amenities and its age composition, I find that the older demographic group spends a significantly higher share of their expenditures on health care services, nursing homes, and significantly lower share on childcare, restaurants, nightclubs and clothing. The magnitude of the differences is large: for example, older individuals spend nearly twice more on health care services and twice

TABLE 1  
AGE AND EXPENDITURE SHARES ON LOCAL SERVICES

	(1) Restaurants	(2) Bars	(3) Clothing	(4) Childcare	(5) Recreation	(6) Beauty	(7) Health	(8) NursingH
Age $\geq 60$	−0.54*** (0.015)	−0.63*** (0.02)	−0.73** (0.012)	−0.96*** (0.014)	−0.58*** (0.015)	0.23*** (0.014)	1.26*** (0.014)	0.22*** (0.008)
Obs	77842	77842	77842	77842	77842	77842	77842	77842
R squared	0.16	0.12	0.18	0.05	0.17	0.03	0.17	0.3
Controls	✓	✓	✓	✓	✓	✓	✓	✓
Time FE	✓	✓	✓	✓	✓	✓	✓	✓

$p$ -value \*\*\* $p \leq 0.01$ . Robust standard errors are given in parenthesis. Dependent variable is the log of the expenditure share on a particular spending category. For the cases when expenditure shares are zero, I bottom code the expenditure data at 1 dollar. Regressions include a set of controls for sex, race, education and marital status. Category restaurants stands for the food outside of home, nightclubs stands for the alcohol consumption outside of home, and beauty stands for personal care services. More details on the construction of spending categories are in Appendix A.3

less on childcare services. These effects can be directly related to changes in family composition and health care needs with age.

Declining expenditure shares on clothing and restaurants are in line with the findings in Aguiar & Hurst (2013), where the authors argue that these services are complementary to working hours. Similarly, expenditures on other categories, such as personal care services, might increase with age due to their complementarity with leisure time. The main discrepancy with the previous findings is that the share spend on recreation category declines with age. This result might mask significant heterogeneity in the subcomponents of the recreation consumption group in the data.<sup>15</sup>

The empirical results above are consistent with the evidence documented in Su (2019) on the frequency of visits to local amenities by different age groups. She finds that the older age group ( $\geq 40$ ) visits medical facilities and personal care facilities more often, while restaurant and bars less often as compared to the younger age group.

### 3.5 Summary of Empirical Results

To summarize, I show that there exists significant dispersion in the demographic composition of the U.S. CZs. I find that older individuals sort out of more productive locations, and that observable measures of amenities, such as climate and composition of local establishments, are correlated with demographics.

<sup>15</sup>while it includes recreational activities such as fees for sporting events and country clubs, it also includes expenditures on pets, repair of recreational equipment e.t.c.

Sorting by productivity might be driven by the decline in working hours with age and differences in exogenous location-specific productivities. However, due to the presence of productivity spillovers part of the observed sorting pattern might arise from the changes in productivity in response to the changes in demographics. Besides, locations that are more productive might also be relatively more amenable for the young. There might be two potential reasons why the composition of local establishments correlates with demographics. First, locations can differ in exogenous factors that affect the variety of some services more than the others. For example, some places can be more suitable for the entry of health care services which makes them relatively more attractive for older residents. Second, the variety of local services can adjust endogenously to local demographics through the entry of firms in response to the local expenditures.

Next, I develop a spatial model of life cycle location choices that aims to disentangle the drivers behind the observed patterns of the geographic sorting by age. I further use the model to estimate the values of U.S. locations for the young and the old, and to study the set of counterfactual questions.

## 4 Theoretical Framework

This section introduces a model to formalize how changes in working hours and preferences for location’s amenities over the life cycle affect location choices and spatial equilibrium. The setup shares many features of the models in [Allen & Arkolakis \(2014\)](#), [Allen & Donaldson \(2018\)](#) and [Monte et al. \(2018\)](#). The key new element is that individuals live for two periods: “young” and “old”, and they choose locations for both periods subject to mobility frictions for relocating when old. The model allows for the heterogeneity in individual’s preferences, in locations’ amenities for the young and the old, and in locations’ productivities. Further, I model an endogenous adjustment of locations’ amenities to expenditures of location’s residents, similar to [Almagro & Dominguez-Ino \(2019\)](#) and [Couture et al. \(2019\)](#), and endogenous adjustment of location’s productivities to local employment as in [Allen & Arkolakis \(2014\)](#). The sections below describe the model setup, how the spatial equilibrium is determined, and discuss the efficiency properties of the model.

### 4.1 Setup

The economy consists of a set of discrete locations, which are indexed by  $i = 1, \dots, J$ . Locations differ in terms of their exogenous land endowments, exogenous productivities in the tradeable sector, and exogenous amenities.



There are three types of producers in each location. First, perfectly competitive firms produce a single freely tradeable good using local labor with the production function featuring agglomeration externalities. Second, each location has construction firms who use local land endowment and a final good to produce housing with a decreasing returns to scale production technology. Finally, each location has a free entry of amenity developers who compete for local housing to produce differentiated varieties in two categories of non-tradeable services.

Economy is populated by overlapping generations of individuals. Each cohort has an initial size  $L$ , and is replaced by a new cohort after  $T$  periods. I assume that individuals can be in two states: “young” and “old”. In the young state individuals inelastically supply one unit of labor in the tradeable sector in return for the location-specific wages, and in the old state they retire and receive no labor income. Individuals in two states differ in their preferences for location-specific exogenous amenities and in their preferences for two categories of locally provided services.

Agents live for  $T = t_y + t_o$  periods in total, where the first  $t_y$  periods correspond to the young state, and the rest  $t_o$  periods to the old state. They choose a pair of locations  $(i, j)$ , where  $i$  is the location for the first  $t_y$  young periods and  $j$  is the location for the following  $t_o$  old periods. The first location choice is free of costs, but reallocation for the old period is subject to location pair specific mobility costs  $\mu_{ij}$ .

The model structure implies that in each period of time the economy is populated by  $t_y L$  young individuals and  $t_o L$  old individuals. I denote by  $\rho = t_o/t_y$  the relative length of the old period, which is also the relative number of old individuals in the economy. The model is static and aims at capturing the long-run steady state of the economy. For simplicity, there is no capital accumulation and the gross saving rate is equal to one.

#### 4.1.1 Consumer preferences

The preferences of a consumer  $\omega$  who lives in location  $i$  when young and in location  $j$  when old are determined as:

$$U_{ij\omega} = t^y \ln(u_i^y \epsilon_{i\omega}^y) + t^o \ln(u_j^o \epsilon_{j\omega}^o) - t^o \ln(\mu_{ij}) \quad (1)$$

where  $u_i^y$  and  $u_i^o$  are the common components of the per period utility of young and old residents in location  $i$ ,  $\mu_{ij}$  is the cost of moving from  $i$  to  $j$  in terms of the consumption units of the old period,  $\epsilon_{i\omega}^y$  and  $\epsilon_{j\omega}^o$  are idiosyncratic preferences of individual  $\omega$  for living in location  $i$  when young and in location  $j$  when old. This formulation implicitly assumes that the discount rate and the gross interest rate are both equal to one, so that the consumption choices within the young and the old states are the same. For more details see Appendix D.1.

Define preference shock for each location path  $\epsilon_{ij\omega}$  as  $\ln \epsilon_{ij\omega} = t^y (\ln \epsilon_{i\omega}^y + \rho \ln \epsilon_{j\omega}^o)$ . I assume

that  $\epsilon_{ij\omega}$  is drawn independently from an extreme-value (Fréchet) distribution:

$$F(\epsilon_{ij\omega}) = e^{\epsilon_{ij\omega}^{-\theta}}, \quad \theta > 1$$

where  $\theta > 1$  controls the dispersion of idiosyncratic utility. I assume that individuals learn their realisation of the preference shocks for each path  $(i, j)$  in the young state before making location choices.

The per period common utility of young and old consumers in location  $i$  is:

$$u_{it}^y = A_i^y (c_t^y)^{\delta_c} (h_t^y)^{\delta_h} (Q_{it}^y)^{\delta_b} \quad u_{it}^o = A_i^o (c_t^o)^{\delta_c} (h_t^o)^{\delta_h} (Q_{it}^o)^{\delta_b} \quad (2)$$

where  $A_i^y$  and  $A_i^o$  are the location-specific utility shifters for the young and the old,  $c$  is the consumption of the tradeable good,  $h$  is the consumption of housing, and  $Q_i$  is the consumption of the bundle of non-tradeable services in location  $i$ . I assume that  $\delta_h + \delta_c + \delta_b = 1$ .

In empirical section 3.4, I show that younger and older demographic groups systematically differ in their expenditures on local services. As argued in Aguiar & Hurst (2013) some consumption goods might be complementary to working hours (e.g. clothing, food outside of home), while others might be complementary to leisure (e.g. golf clubs). Besides, young and old might differ in their preferences health care services and childcare. To account for this, I assume that there are two categories of services  $s = 1, 2$  that enter the bundle of non-tradeables in each location. The first one ( $s = 1$ ) corresponds to the services that are valued more by the young, and the second one ( $s = 2$ ) corresponds to services that are valued more by the old :

$$Q_i^y = Q_{1i}^{\alpha_1^y} Q_{2i}^{1-\alpha_1^y} \quad Q_i^o = Q_{1i}^{\alpha_1^o} Q_{2i}^{1-\alpha_1^o}$$

where  $\alpha_1^y > \alpha_1^o$ . Within a group of services competitive amenity developers in location  $i$  offer varieties that are imperfect substitutes. Individuals have CES preferences over the varieties with the common elasticity of substitution parameter  $\sigma$ :

$$Q_{si} = \left( \int_{m=1}^{N_{si}} q_{ms}^{\frac{\sigma-1}{\sigma}} \right)^{\frac{\sigma}{\sigma-1}}$$

where  $q_{ms}$  denotes the quantity of the variety  $m$  consumed in category  $s$ , and  $N_{si}$  denotes the number of varieties in category  $s$  in location  $i$ .

#### 4.1.2 Production of the tradeable good

A continuum of firms in each location produces under perfectly competitive conditions a single homogeneous product that is freely tradeable across locations. The production function is linear

in labor with location-specific productivity level  $z_i$ :

$$y_i(\omega) = z_i l_i(\omega)$$

The productivity level  $z_i$  is determined as:

$$z_i = Z_i \left( \int l_i(\omega) d\omega \right)^{\gamma^P} = Z_i (L_i^y)^{\gamma^P} \quad (3)$$

where  $Z_i$  is the exogenous component that can vary across locations, and  $\gamma^P$  is the parameter that governs any potential agglomeration externalities operating through the size of the local production, modelled in a structural way as in [Allen & Arkolakis \(2014\)](#) and [Allen & Donaldson \(2018\)](#). As only young individuals supply labor, the agglomeration spillover is determined by the number of the young in a given location. The price of the final good is the same across all locations and is normalised to be equal to one.

#### 4.1.3 Housing sector

Producers in the construction sector in location  $i$  use intermediary input  $I_i$  and the fixed supply of land  $\bar{H}_i$  to produce housing  $H_i$  according to the following decreasing returns to scale production function:

$$H_i = \bar{H}_i I_i^{\frac{1}{1+\epsilon_h}}$$

Intermediary input is produced one to one with the final consumption good  $I_i = c_{ih}$ . Housing units are rented to location's residents and to amenity developers at the rental rate  $R_i$ . The profit maximisation problem of the producers is:

$$\max_{I_i} R_i \bar{H}_i I_i^{\frac{1}{1+\epsilon_h}} - I_i$$

I assume that construction firms are owned by local landlords who spend profits on the consumption of the tradeable good.

#### 4.1.4 Production of non-tradeable services

There is an infinite mass of potential amenity developers outside of the city who can produce a single variety in sector  $s$ . To produce  $q$  units of a variety, a developer needs to rent  $kq$  units of housing, so the marginal cost of production is location-specific and equal to  $kR_i$ . A developer in

location  $i$  producing variety  $m$  in category  $s$  solves the following profit maximisation problem:

$$\max_{p_{msi}} q_{msi}(p_{msi})(p_{msi} - kR_i)$$

Amenity developers can freely enter each category of services in each location. To produce a variety they need to pay location-service specific operating costs  $F_{si}$  in terms of the rented housing units.

## 4.2 Consumer problem

Young individuals in location  $i$  inelastically supply one unit of labor in a location of choice and earn per period location specific wage  $w_i$ . This income is spend on the consumption of the tradeable good, housing and local services during young and old periods. Consider the consumption choice problem of an individual who chose the location path  $(i, j)$ :

$$\max_{c^y, c^o, h^y, h^o, q_{ms}^y, q_{ms}^o} \ln A_i^y (c^y)^{\delta_c} (h^y)^{\delta_h} (Q_i^y)^{\delta_b} + \rho \ln A_j^o (c^o)^{\delta_c} (h^o)^{\delta_h} (Q_j^o)^{\delta_b} - \rho \ln \mu_{ij} + \ln \epsilon_{ij\omega} \quad (4)$$

s.t.

$$c^y + R_i h^y + \sum_{s=1}^2 \int_{m=1}^{N_{si}} p_{msi} q_{ms}^y + \rho (c_{ij}^o + R_j h_{ij}^o + \sum_{s=1}^2 \int_{m=1}^{N_{sj}} p_{msj} q_{ms}^o) = w_i \quad (5)$$

where  $p_{msi}$  denotes the price of variety  $m$  of category  $s$  in location  $i$ , and  $\rho = t^o/t^y$  is the relative length of the old period.

The resulting solution for the consumption of the final good and housing is:

$$c_{ij}^y = c_{ij}^o = \frac{\delta_c w_i}{1 + \rho} \quad h_{ij}^y = \frac{\delta_h w_i}{R_i(1 + \rho)} \quad h_{ij}^o = \frac{\delta_h w_i}{R_j(1 + \rho)} \quad (6)$$

The resulting demand for each variety  $m$  in categories  $s = 1, 2$  is:

$$q_{msij}^y = \alpha_s^y \delta_b \frac{w_i}{1 + \rho} \frac{1}{P_{si}} \left( \frac{P_{si}}{p_{msi}} \right)^\sigma \quad q_{msij}^o = \alpha_s^o \delta_b \frac{w_i}{1 + \rho} \frac{1}{P_{sj}} \left( \frac{P_{sj}}{p_{msj}} \right)^\sigma \quad (7)$$

where the price index is  $P_{si} = \left( \int_{m=1}^{N_{s,i}} p_{msi}^{1-\sigma} \right)^{\frac{1}{1-\sigma}}$ .

### 4.3 Endogenous amenities and consumers indirect utility

Denote by  $L_{ij}$  the number of individuals who choose location path  $(i, j)$ . Then, the total number of young and old individuals location  $i$  is:

$$L_i^y = t^y \sum_j L_{ij} \quad L_i^o = t^o \sum_j L_{ji}$$

The total demand for variety  $m$  of a group  $s$  in location  $i$  is the sum of quantities demanded by young and old residents:

$$q_{msi} = t^y \sum_j L_{ij} q_{msij}^y + t^o \sum_j L_{ji} q_{msji}^o = \frac{1}{P_{si}} \left( \frac{P_{si}}{p_{msi}} \right)^\sigma t^y \left( L_i^y \delta_b \alpha_s^y \frac{w_i}{1+\rho} + \rho \sum_j L_{ji} \delta_b \alpha_s^o \frac{w_j}{1+\rho} \right)$$

The resulting elasticity of the demand for each variety is invariant across locations and is equal to  $-\sigma$ .

Amenity developers will optimally charge constant markup over their marginal costs:

$$p_{msi} = \frac{\sigma}{\sigma - 1} k R_i \quad (8)$$

Given that all firms in the service group  $s$  in location  $i$  are symmetric, in equilibrium  $q_{msi} = q_{si}$  and  $p_{msi} = p_{si}$ . Then, the quantity demanded can be simplified as:

$$q_{si} = \frac{t^y}{N_{si} p_{si}} \left( L_i^y \delta_b \alpha_s^y \frac{w_i}{1+\rho} + \rho \sum_j L_{ji} \delta_b \alpha_s^o \frac{w_j}{1+\rho} \right) \quad (9)$$

The number of firms in each category adjusts so that the operating profit of the developer just offsets the fixed operating cost:

$$q_{si}(p_{si} - k R_i) = F_{si} R_i \quad (10)$$

Substituting the equilibrium prices (8) and quantities (9) into free entry condition (10), I can get the expression for the equilibrium number of firms:

$$N_{si} = \frac{\frac{t^y}{1+\rho} \left( L_i^y \delta_b \alpha_s^y w_i + \rho \sum_j L_{ji} \delta_b \alpha_s^o w_j \right)}{F_{si} R_i \sigma} \quad (11)$$

The number of firms in each service category is proportional to local expenditures on this service category and inversely proportional to local housing prices. As the young and the old differ in their preferences, location's demographic composition affects the composition of local establishments. Besides, the location of origin of the older residents affects the number of local firms by determining the retirees' expenditures.

Combining the solution to the consumer problem (6)-(7) and the equilibrium number of firms (11), I derive the indirect utility for each location path  $(i, j)$ <sup>16</sup>:

$$V_{ij\omega} = \ln \left( \frac{w_i a_i^y}{R_i^{(1-\delta_c)}} \right) + \rho \ln \left( \frac{w_i a_j^o}{R_j^{(1-\delta_c)}} \right) - \rho \ln(\mu_{ij}) + \ln(\epsilon_{ij\omega}) \quad (12)$$

where local amenities are determined as:

$$a_i^y = A_i^y \left( N_{1i}^{\alpha_1^y} N_{2i}^{(1-\alpha_1^y)} \right)^{\frac{\delta_b}{\sigma-1}} \quad a_i^o = A_i^o \left( N_{1i}^{\alpha_1^o} N_{2i}^{(1-\alpha_1^o)} \right)^{\frac{\delta_b}{\sigma-1}} \quad (13)$$

Endogenous number of establishments  $N_{si}$  affects consumer utility through a love of variety effect. Higher presence of individual's own demographic group in the chosen location makes this location more amenable for her: the composition of local establishment becomes more aligned with individual's preferences when the location's population shifts towards individual's demographic group.

#### 4.4 Consumer location choice problem

I will further work with the exponential transformation of the original utility function. Denote by  $W_{ij}$  the exponent of the deterministic part of the indirect utility (12) :

$$W_{ij} = \frac{w_i^{(1+\rho)} a_i^y (a_j^o)^\rho}{R_i^{1-\delta_c} R_j^{\rho(1-\delta_c)} \mu_{ij}^\rho}$$

Individuals choose a location path that maximizes their utility:

$$\max_{ij} W_{ij} \epsilon_{ij\omega}$$

Due to the Freshet assumption on the distribution of the preference shocks, the share of individuals that chooses location path  $(i, j)$  is given by:

$$\frac{L_{ij}}{L} = \frac{W_{ij}^\theta}{\sum_{k=1}^J \sum_{m=1}^J W_{km}^\theta} \quad (14)$$

The expected lifetime utility of individuals can be computed as:

$$U = E(\max_{ij} W_{ij}) = \left( \sum_{k=1}^J \sum_{m=1}^J W_{km}^\theta \right)^{\frac{1}{\theta}} \quad (15)$$

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<sup>16</sup>the results are equal up to a constant, which is a monotonic transformation that does not affect the final results

Combining optimal location choices (14), indirect utility (12), and expected utility (15), I can write bilateral migration flows for retirement as follows:

$$L_{ij} = \underbrace{\mu_{ij}^{-\theta\rho} \left( \frac{w_i^{(1+\rho)} a_i^y}{R_i^{1-\delta}} \right)^\theta}_{\text{Value of i for y}} \underbrace{\left( \frac{a_j^o}{R_j^{(1-\delta)}} \right)^{\rho\theta}}_{\text{Value of j for o}} LU^{-\theta} \quad (16)$$

Migration flows are higher into destination locations  $j$  that have better amenities for the old and lower rents, out of origin locations that are more attractive for the young, and among location pairs that have lower mobility costs.

## 4.5 Housing market

Profit maximisation problem of firms in the construction sector leads to the following housing supply function:

$$H_i = d_h \bar{H}_i (R_i)^{\frac{1}{\epsilon_h}} \quad (17)$$

where  $d_h = (1 + \epsilon_H)^{\frac{1}{\epsilon_h}}$ . Parameter  $\epsilon_h$  governs the inverse elasticity of the housing supply.

Given rental rate  $R_i$ , the amount of housing demanded by consumers is:

$$H_i^h = t^y \sum_j L_{ij} h_{ij}^y + t^o \sum_j L_{ji} h_{ji}^o = \frac{t^y}{(1 + \rho) R_i} \left( L_i^y \delta_h w_i + \rho \sum_j L_{ji} \delta_h w_j \right)$$

The amount of housing demanded by amenity developers is equal to the housing used in the production of local services including fixed entry costs:

$$H_i^d = t^y L_i^y k \sum_{s=1}^2 \int_{m=1}^{N_{si}} q_{ms,ij}^y + t^o \sum_j L_{ji} k \sum_{s=1}^2 \int_{m=1}^{N_{si}} q_{msji}^o + \sum_{s=1}^2 N_{si} F_{si}$$

The housing clearing condition is then:

$$H_i = H_i^h + H_i^d$$

Using (8) and (11), I simplify the condition to:

$$H_i = (1 - \delta_c) \frac{t^y}{(1 + \rho) R_i} \left( L_i^y w_i + \rho \sum_j L_{ji} w_j \right) \quad (18)$$

Fixed fraction  $(1 - \delta_c)$ , which is also equal to  $\delta_h + \delta_b$ , of local expenditures is spend on local housing either directly through housing consumption or indirectly through the consumption of



local services.

## 4.6 Equilibrium

**Definition 1.** For any time-invariant geography vector  $\{\bar{H}_i, Z_i, A_i^y, A_i^o, \mu_{ij}\}$  a steady-state equilibrium is a vector of endogenous variables  $\{L_i^y, L_i^o, R_i, w_i, N_{1i}, N_{2i}, a_i^y, a_i^o\}$  such that for any  $i$ :

1. Firms in the tradeable sector earn zero profits:  $w_i = z_i$ . Local productivity  $z_i$  satisfies equation (3);
2. The mobility flows between locations are consistent with individual optimal location choices (16);
3. The number of young and old in each location is determined as:

$$L_i^y = t_y \sum_j L_{ij} \quad L_i^o = t_o \sum_j L_{ji} \quad (19)$$

4. Housing supply  $H_i$  satisfies (17);
5. Housing markets clear such that equation (18) holds;
6. The number of firms in each service category is determined by the free entry condition of amenity developers such that equation (11) holds;
7. Local amenities satisfy equation (13).

From equilibrium conditions, I can express the number of the young and the old in each location as a function of location's amenities, wages and rents:

$$\frac{L_i^y}{L} = t_y \underbrace{\left( \frac{w_i^{(1+\rho)} a_i^y}{R_i^{1-\delta_c} U} \right)^\theta}_{\text{Value for young}} \underbrace{\sum_j \left( \frac{(a_j^o)^\rho}{R_j^{\rho(1-\delta_c)} \mu_{ij}^\rho} \right)^\theta}_{\text{Retirement option}} \quad (20)$$

$$\frac{L_i^o}{L} = t_o \underbrace{\left( \frac{a_i^o}{R_i^{(1-\delta_c)}} \right)^{\theta\rho}}_{\text{Value for old}} \underbrace{\sum_j \left( \frac{w_j^{(1+\rho)} a_j^y}{R_j^{1-\delta_c} \mu_{ji}^\rho U} \right)^\theta}_{\text{Proximity to young}} \quad (21)$$

The presence of mobility costs for retirement make location choices for the young and the old periods a part of the single dynamic problem. The number of young in each location depends not only on the attractiveness of this location for young, but also on how easy it is to move

from this location to locations that are valuable for retirement. Similarly, the number of old in each location depends both on the attractiveness of this location for the old, determined by its amenities for the old and rents, and on the proximity of this location to the locations valuable for the young.

As argued in the literature, the presence of spillovers might lead to the equilibria multiplicity. Unfortunately, the existence and uniqueness techniques developed in [Allen et al. \(2015\)](#) do not directly apply to the model developed in the paper. Therefore, I proceed with numerical analysis and show that for the calibrated parameter values the solution exists and is stable.

#### 4.6.1 Adjusted fundamentals

Combining equations (11) and (13), I derive the following equations for the endogenous amenities:

$$a_i^y = \frac{A_i^y}{\sigma F_{1,i}^{\alpha_1^y} F_{2,i}^{\alpha_2^y}} \left( \frac{E_{1,i}^{\alpha_1^y} E_{2,i}^{\alpha_2^y}}{R_i} \right)^{\frac{\delta_b}{\sigma-1}} \quad a_i^o = \frac{A_i^o}{\sigma F_{1,i}^{\alpha_1^o} F_{2,i}^{\alpha_2^o}} \left( \frac{E_{1,i}^{\alpha_1^o} E_{2,i}^{\alpha_2^o}}{R_i} \right)^{\frac{\delta_b}{\sigma-1}} \quad (22)$$

where  $E_{s,i}$  denotes total expenditures on category  $s$  in location  $i$  and is determined by  $E_{s,i} = t^y (L_i^y \delta_b \alpha_s^y \frac{w_i}{1+\rho} + \rho \sum_j L_{ji} \delta_b \alpha_s^o \frac{w_j}{1+\rho})$ .

Define by adjusted amenities the exogenous components of the equations 22:

$$\tilde{A}_i^y = \frac{A_i^y}{\sigma F_{1,i}^{\alpha_1^y} F_{2,i}^{\alpha_2^y}} \quad \tilde{A}_i^o = \frac{A_i^o}{\sigma F_{1,i}^{\alpha_1^o} F_{2,i}^{\alpha_2^o}} \quad (23)$$

Adjusted exogenous amenities are determined both by location's exogenous characteristics such as climate and nature ( $A_i$ ), and by location specific fixed costs of entry in non-tradable industries ( $F_{s,i}$ ). Therefore, spatial variation in the relative exogenous amenities for young and old can be rationalised not only by the differences in the valuation of climate and nature, but also by the differences in the preferences for local services. For example, if due to some exogenous reasons local entry costs into the health care industry are low, this would be reflected as a relatively higher exogenous amenity for the old.

Given the exogenous fundamentals  $\{\tilde{A}_i^y, \tilde{A}_i^o, Z_i, \bar{H}_i, \mu_{ij}\}$ , I can solve for the equilibrium set of variables  $\{L_{ij}, w_i, R_i, a_i^y, a_i^o\}$  using equations (3), (19), (16), (18), (22), and (23). Therefore, I don't need to estimate the fixed cost of entry  $F_{s,i}$  to compute the main equilibrium outcomes of the model, and also to compute the counterfactual changes in the number of firms.

## 4.7 Efficient Allocation and Policy

As argued in [Fajgelbaum & Gaubert \(2020\)](#) and [Rossi-Hansberg et al. \(2019\)](#), differences in productivity and amenity spillovers between demographic groups can lead to their inefficient

sorting across space. I explore this idea in my setting, where differences in spillovers arise due to the individual's life cycle, and where the adjustment of amenities is modelled through the entry of variety producers.<sup>17</sup>

Consider a planning problem where a planner can redistribute the final good across consumers and construction producers, and reallocate housing units between local residents and local non-tradable sectors to maximise the expected lifetime utility of the individuals. The planner can't directly choose location of consumers, so the planner is bounded by the spatial mobility constraint (16). The planner also can't condition on the realization of the individual's preference shocks for location pairs. The planner problem is defined formally in Appendix D.2.

**Proposition 1.** *In an efficient allocation the following should hold:*

$$\underbrace{x_{ij}}_{\text{consumption cost}} + \underbrace{\lambda}_{\text{opport}} = \underbrace{z_i^* + \gamma^P z_i^*}_{\text{marginal product in } i} - \frac{x_{ij}}{\theta(1+\rho)} \quad (24)$$

$$\underbrace{R_i^* N_{si} F_{si}}_{\text{housing cost}} = \underbrace{\frac{\sigma}{\sigma-1} \frac{1}{\sigma} \frac{\delta_b}{1+\rho} \left( \alpha_s^y \sum_j x_{ij} L_{ij} + \rho \alpha_s^o \sum_j x_{ji} L_{ji} \right)}_{\text{utility gain}} \quad (25)$$

for  $s = 1, 2$ , where  $x_{ij} = c_{ij}^y + \rho c_{ij}^o + R_i^* (h_{ij}^y + \sum_{s=1,2} N_{si} k q_{sij}^y) + \rho R_j^* (h_{ij}^o + \sum_{s=1,2} N_{sj} k q_{sij}^o)$  is the cost along the path,  $R_i^*$  is the multiplier under the housing constraint of the city  $i$  and  $\lambda$  is the multiplier under the labor allocation constraint

Condition (24) shows that social planner equalises the marginal cost and benefit of allocating an individual to location path  $\{i, j\}$ . The marginal cost is the consumption levels along that path, the tightening of the housing constraints and the opportunity cost of allocating the individual on a different path. The marginal benefit is the marginal productivity of the individual when she is working in location  $i$ , including the productivity spillover  $\gamma^P$ . In equilibrium, the individual's expenditures  $x_{ij}$  are equal to location  $i$  wage:  $w_i = z_i$ . So the planner's optimality condition with respect to  $L_{ij}$  differs from the equilibrium one due to the presence of productivity spillovers  $\gamma^P$ , and also due to the dispersion in the location-specific preference shocks  $\theta$ . The intuition for the latter is that the dispersion of the preference shocks leads to the variation in the marginal utilities across consumers. The planner finds it optimal to redistribute the final good away from individuals with lower marginal utility and towards the individuals with higher marginal utility. However, the planner can't condition on the preference shocks realization, so she uses that fact that more

<sup>17</sup> Rossi-Hansberg et al. (2019) consider only differences in productivity spillovers in the tradable sectors. Fajgelbaum & Gaubert (2020) consider both differences in amenity spillovers and productivity spillovers, but both are modelled in a reduced form way

productive locations attract individuals with on average worse preference draws.

Condition (25) shows that the planner chooses the optimal mass of firms in two sectors by equalising the housing costs associated with entry with the utility gains from a higher variety of services. As compared to the equilibrium outcome, the planner internalises the love of variety gains and wants to redistribute the housing away from the residential use and towards services in the same proportion across locations equal to  $\frac{\sigma}{\sigma-1}$ . Therefore, the presence of endogenous amenities does not contribute to an inefficient allocation of young and old across cities. This result differs from the findings in Fajgelbaum & Gaubert (2020), where differences in reduced-form amenity spillovers require policies targeted at the sorting of heterogeneous agents.

Overall, depending on the trade-off between productivity spillovers and distributional inefficiency due to the preference shocks, the planner either wants to increase or decrease the concentration of young individuals in more productive cities. As location choices of the young are affected by location choices of the old through housing prices, one way to affect the allocation of workers is through the reallocation of retirees. In the quantitative section, I further explore whether policies that incentivise the reallocation of retirees to less productive cities are welfare improving.

## 5 Model calibration

This section discusses the quantification of the model parameters. Section 5.1 describes the data and the mapping of the endogenous variables of the model to their empirical counterparts. Section 5.2 describes calibration of the structural parameters. Section 5.3 discusses the tree-step estimation procedure to recover the exogenous geography parameters.

### 5.1 Data

The model is calibrated to the mean outcomes across 1980, 1990, 2000 Censuses and 2012-2016 ACS. As in the empirical section, I define locations by 741 CZs in the U.S. I approximate  $L_i^o$  by the number of CZ residents older than 60.<sup>18</sup> Similarly, I approximate  $L_i^y$  by the number of CZ residents between ages 25 and 60. I use average composition adjusted wages of local workforce as my measure of  $w_i$ , and I use average quality adjusted rents paid by local residents as my measure of  $R_i$ . Therefore, for 741 commuting zones in the U.S. I observe the vector of wages, rents and location choices  $\{w_i, R_i, L_i^y, L_i^o\}$ . More details on the construction of the variables are in the Appendix A

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<sup>18</sup>the average retirement age in the US is 64, but as shown in the empirical sections individuals might decide on changing location for retirement reasons earlier than actual retirement.

TABLE 2  
CALIBRATED PARAMETERS

	Value	Description	Strategy	Source
$\gamma^P$	0.06	productivity spillover	Literature	<a href="#">Rosenthal &amp; Strange (2004)</a>
$\theta$	3.35	preference shocks shape	Calibrated	<a href="#">Hornbeck &amp; Moretti (2018)</a>
$\delta_h$	0.36	share spend on housing	Calibrated	CEX data
$\delta_b$	0.224	share spend on local goods	Calibrated	based on <a href="#">Moretti (2013)</a>
$\sigma$	5	Substitution elasticity for amenities	Literature	<a href="#">Hoelzlein (2019)</a>
$1/\epsilon_h$	1.75	elasticity of housing supply	Literature	<a href="#">Saiz (2010)</a>
$\alpha_1^y$	0.711	share spend on local good 1 by young	Calibrated	CEX data
$\alpha_1^o$	0.464	share spend on local good 1 by old	Calibrated	CEX data
$\rho$	0.5	length of old period	Calibrated	Old to young ratio

To estimate the mobility costs  $\mu_{ij}$ , I additionally need the data on location choices for each location path  $L_{ij}$ . In 2000 Census sample, I observe individual's age, current location and location five years ago. As the retirement decision is not directly observed, I assume that the reallocation for retirement reasons occurs in a 20 year window around the average retirement age of 64. So I approximate the location choices  $L_{ij}$  with  $\hat{L}_{ij} = \sum_{a=57}^{a=77} L_{ij}^5(a)$ , where  $L_{ij}^5(a)$  is the number of individuals of age  $a$  who were in location  $i$  five years ago and currently are in the location  $j$ . While  $\hat{L}_{ij}$  represents only a subsample of all moves for retirement due to the limited 5 year window, I show in Appendix E.3 that if individuals move for retirement with some constant probability for each year within the reallocation window, then this data limitation does not affect the estimation of mobility costs.

Finally, I use the consumer expenditure data (CEX) provided by NBER CEX extracts to estimate the differences in the expenditure shares on local services by age group. More details on the CEX dataset and the construction of the consumption groups are in Appendix A.3.

## 5.2 Calibrated parameters

I use CEX data for the period from 1980 to 2000 to compute the average share of housing in consumers expenditures  $\delta_h = 0.36$ <sup>19</sup>. I calibrate the expenditure share on local non-housing goods  $\delta_b$  to match the estimate from [Moretti \(2013\)](#) that 35 percent of non-housing costs varies systematically with housing prices.<sup>20</sup>

Parameters  $\alpha_1^y$  and  $\alpha_1^o$  govern the degree of heterogeneity in the expenditure shares on local goods between young and old age groups. I calibrate these parameters following the

<sup>19</sup> Total expenditures exclude savings and contributions to retirement plans. Housing costs include both housing rent (imputed rent for homeowners) and utilities

<sup>20</sup> The paper estimates the local component of non-housing costs by regressing changes in consumer price indices for individual cities (reported by BLS) on housing price changes within cities

analysis in section 3.4. In particular, I assume that expenditure patterns on local goods can be approximated by 8 consumption categories corresponding to local services in the CEX data (see Appendix A.3 for the details). Then I compute predicted expenditure shares on these categories for the younger and the older age groups. Table 3 presents the results and describes the estimation procedure. In line with the results in the section 3.4, there exists significant heterogeneity between younger and older demographic groups in their expenditure patterns: e.g. the older group spends much more on healthcare services, while the younger group spends more on clothing, restaurants and childcare. I further aggregate the expenditure categories into two broader groups. Group 1 includes categories where the younger group spends a higher share of their income than the older group: restaurants, bars, clothing, childcare services, and recreation. Other categories are included in group 2: healthcare, nursing homes and beauty services. The resulting parameters  $\alpha_1^y = 0.711$  and  $\alpha_1^o = 0.464$  are the expenditure shares on group 1 of the young and the old age groups correspondingly.

Parameter  $\sigma$  governs the elasticity of demand for consumption amenities. Dolfen et al. (2019) estimate elasticity of demand  $\sigma = 6.1$  for the offline retail stores in the U.S., Couture et al. (2019) estimate  $\sigma = 6.5$  for the U.S. restaurants, gyms, movie theaters, and outdoor amenities, Su (2019) reports values between 3.69 and 16 for disaggregated local sectors, and estimates  $\sigma \in [4.26, 7.11]$  for medical facilities. As I use aggregated sectors, I follow Hoelzlein (2019) and choose  $\sigma = 5$  which is towards the lower end of the empirical estimates.

In the model, parameter  $\theta$  governs the elasticity of the individual's location choices with respect to location fundamentals. I calibrate  $\theta$  so that the average employment response to exogenous local TFP shocks matches the estimates from Hornbeck & Moretti (2018).<sup>21</sup>

Finally, I set  $\rho = 0.5$  to match the aggregate ratio of old-to-young in the data. Parameters  $L$  and  $t_y$  are normalised, as they only affect the scaling of the model variables.

**Parameters from the Literature** I set productivity spillover  $\gamma^P = 0.06$  based on the empirical estimates of productivity spillovers summarized in Rosenthal & Strange (2004)<sup>22</sup>. Saiz (2010) estimates developed land supply elasticities for 95 metropolitan statistical areas in the United States. I set  $1/\epsilon_H$  to the population-weighted average of these elasticities equal to 1.75.

### 5.3 Mapping of the model to the data

I now describe the three step estimation procedure to recover the exogenous geography parameters  $\{\mu_{ij}, \tilde{A}_i^y, \tilde{A}_i^o, Z_i, \bar{H}_i\}$  for the U.S. CZs. First, I estimate the gravity for retirement

<sup>21</sup>Hornbeck & Moretti (2018) estimate that a 1% increase in city manufacturing TFP during the period from 1980 to 1990 is associated with an average local employment increase by 4.16%.

<sup>22</sup>the empirical estimates are found to be in the range of 3% – 8%

TABLE 3  
PREDICTED EXPENDITURE SHARES ON LOCAL SERVICES

	(1) Restaurants	(2) Bars	(3) Clothing	(4) Childcare	(5) Recreation	(6) Beauty	(7) Health	(8) NursingH
$25 \leq age < 60$	0.223	0.025	0.262	0.035	0.165	0.05	0.24	0
$age \geq 60$	0.17	0.014	0.155	0.004	0.121	0.056	0.476	0.004

Table shows the predicted expenditure shares for younger and older age groups. First, I compute the total expenditures on 8 categories and the shares corresponding to each separate group. Then, I regress the resulting shares on age dummy ( $\geq 60$ ), time fixed effects and a set of controls for sex, race, education and marital status. Finally, I compute the predicted values for the two age group dummy variables, keeping all the controls at their average values.

flows to evaluate how mobility costs vary with the distance between locations. Second, I calibrate composite amenities  $\{a_i^y, a_i^o\}$  and fixed component of mobility costs, so that the model exactly matches the data  $\{L_i^y, L_i^o, w_i, R_i\}$  and the share of the old who relocate for retirement. Finally, I decompose the model implied composite amenities, observed wages and housing prices into exogenous and endogenous components using the calibrated structural parameters described in section 5.2.

### 5.3.1 Gravity for retirement flows

I assume that mobility costs are a constant elasticity function of the physical distance between locations and a stochastic error for all pairs of CZs with positive commuting flows:

$$\ln \mu_{ij} = \begin{cases} \ln \kappa + \xi \ln dist_{ij} + \epsilon_{ij} & \text{if } i \neq j \\ 0 & \text{if } i = j \end{cases} \quad (26)$$

where  $\kappa$  is the fixed cost of reallocation,  $\xi$  is the elasticity of the mobility cost with respect to the distance, and  $\epsilon_{ij}$  is an unobserved idiosyncratic component of commuting costs specific to a CZ pair. In my baseline specification, I follow Redding & Sturm (2020) and assume prohibitive mobility costs ( $\mu_{ij} \rightarrow \infty$ ) for the pairs of commuting zones with zero retirement flows. So I restrict my sample to CZs with positive retirement flows.

Combining the specification for mobility costs (26) and the gravity equation for migration flows (16), I derive the gravity equation for the log retirement flows:

$$\ln \left( \frac{L_{ij}}{L} \right) = -\theta \rho \xi \ln dist_{ij} + \psi_i + \pi_j + e_{ij}$$

where the location of origin fixed effect includes local wage, amenities for young and rents, and



expected utility and fixed component of the mobility cost  $\psi_i = (1 + \rho)\theta \ln w_i + \theta \ln a_i^y - (1 - \delta_c)\theta \ln R_i - \theta \ln(U) - \theta \rho \ln \kappa$ , the location destination fixed effect includes amenities for old and rents  $\pi_j = \rho \theta \ln a_j^o - \rho \theta (1 - \delta_c) \ln R_j$ , and the error term represents idiosyncratic error in mobility costs between commuting zones  $e_{ij} = -\theta \epsilon_{ij}$

In my baseline specification, I estimate the composite parameter  $-\theta \xi \rho$  using OLS with origin and destination fixed effects. As described in data section 5.1, I approximate flows  $L_{ij}$  with  $\hat{L}_{ij} = \sum_{a=57}^{a=77} L_{ij}^5(a)$ , where  $L_{ij}^5(a)$  is the number of individuals of age  $a$  who were in the location  $i$  five years ago and currently are in the location  $j$  from the US Census data for the year 2000. I observe the non zero migration flows for 101445 pairs of commuting zones.<sup>23</sup>

TABLE 4  
GRAVITY EQUATION FOR RETIREMENT FLOWS

Dependent Variable	(1) $\ln \left( \frac{L_{ij}}{L} \right)$	(2) $\ln \left( \frac{L_{ij}}{L} \right)$
$\ln dist_{ij}(-\theta \rho \xi)$	-0.92*** (0.005)	-1.42*** (0.014)
Estimation	OLS	Poisson PML
Observations	101445	548340
$R^2$	0.72	-
Origin and destination fixed effects	✓	✓

Notes: The dependent variable  $\frac{L_{ij}}{L}$  is the share of individuals of age 57-77 who lives in the CZ  $i$  5 years ago and live in the CZ  $j$  in 2000. The variable  $dist_{ij}$  denotes the distance in miles between commuting zones  $i$  and  $j$ . Poisson PML is Poisson pseudo maximum likelihood estimator.  $p$ -value \*\*\* $p \leq 0.01$ . Standard errors are clustered at the commuting zone level.

Estimation results for the baseline specification are presented in table 4 column (1). The elasticity of retirees migration flows with respect to the distance is equal to  $-0.92$  and is significant at the 1% level. From the regression  $R^2$ , the gravity equation explains around 71% percent of the variation in bilateral mobility patterns, meaning that gravity framework works well for explaining the migration patterns of retirees. In column (2), I relax the assumption of infinite mobility costs for the commuting zone pairs with zero mobility flows, and estimate the gravity equation using the Poisson pseudo maximum likelihood estimator of Santos & Tenreyro (2006) on a full sample of CZ pairs. I find a similar pattern of results with a higher elasticity of  $-1.42$ .

<sup>23</sup>In the Census data I observe mobility at the PUMA level. I then redistribute the migration flows across PUMAs to migration flows across CZs using the probabilistic matching based on the Autor & Dorn (2013) crosswalk. More details are in Appendix E.2

The estimation above provide the first component of the mobility costs  $dist_{ij}^{-\theta\rho\xi}$ . In the next section, I discuss how to calibrate the fixed component of the mobility costs  $\kappa$  to match the share of the old that reallocates for retirement.

### 5.3.2 Recovering the composite amenities $a_i^y$ and $a_i^o$ and the fixed mobility cost $\kappa$

Given the estimated mobility costs  $\mu_{ij}$ , I prove that I can uniquely recover composite location amenities  $a_i^y$  and  $a_i^o$  by inverting the equilibrium conditions for the distribution of the young and the old across locations:

**Proposition 2.** *Given observed data on  $\{L_i^y, L_i^o, w_i, R_i\}$  and estimated mobility costs  $\mu_{ij}$ , there exist unique (up to scale) values of  $\{a_i^y, a_i^o\}$  that satisfy model equilibrium conditions (27) and (28):*

$$\frac{L_i^y}{L} = \left( \frac{w_i^{(1+\rho)} a_i^y}{R_i^{1-\delta_c} U} \right)^\theta \sum_j \left( \frac{(a_j^o)^\rho}{R_j^{\rho(1-\delta_c)} \mu_{ij}} \right)^\theta \quad (27)$$

$$\frac{L_i^o}{L} = \rho \left( \frac{a_i^o}{R_i^{(1-\delta_c)}} \right)^{\theta\rho} \sum_j \left( \frac{w_j^{(1+\rho)} a_j^y}{R_j^{1-\delta_c} \mu_{ji} U} \right)^\theta \quad (28)$$

*Proof.* See Appendix D.3 □

The model predicts high amenities for the young in places that have high young population despite high housing prices, low wages and a bad access to amenable places for retirement. Similarly, the model predicts high amenities for the old in places that have high old population despite a bad access to the locations valuable for young and high housing prices.

Using the results from the proposition 2, for each value of the fixed cost  $\kappa$  I can uniquely recover the composite amenities  $a_i^y$  and  $a_i^o$ . Then, I can compute the model-implied aggregate share of individuals who moves for retirement:

$$Movers = 1 - \sum_i \frac{L_{ii}}{L} = 1 - \frac{\sum_i \left( w_i^{(1+\rho)} R_i^{-(1-\delta_c)(1+\rho)} a_i^y (a_i^o)^\rho \right)^\theta}{\sum_i \sum_j \left( w_i^{(1+\rho)} R_i^{-(1-\delta_c)} a_i^y R_j^{-(1-\delta_c)\rho} (a_j^o)^\rho \mu_{ij}^\rho \right)^\theta}$$

Parameter  $\kappa$  is calibrated so that the model-implied reallocation share matches the corresponding share in the data. Using Census 2000 sample, I compute that 7.5% of individuals in the age group 60-65 moved between CZs within a 5 year period. This reallocation share misses all the moves that individuals make after the age of 65. Finkelstein et al. (2019) document that 10% of Medicare enrollees between ages 65 and 99 moved between CZs at least once over the 15 year period.<sup>24</sup> Assuming that 20% of individuals move more

<sup>24</sup>Finkelstein et al. (2019) use administrative data on Medicare enrollees for a 100% panel of Medicare

than once<sup>25</sup>, this implies that roughly 14% of individuals in the older age group move within 20 year window. Therefore, I use this reallocation share as my target in the calibration.

I find that there exists significant dispersion in the relative amenities for old  $a_o/a_y$  across the U.S. CZs. Tables 5 and 6 list CZs with lowest and highest relative amenities for the old:

CZ Name	State	$a_o/a_y$
Anchorage	Alaska	0.08
Fairbanks	Alaska	0.11
Bethel	Alaska	0.16
Unalaska	Alaska	0.17
Los Angeles	California	0.18

Table 5: CZ with lowest  $a_o/a_y$

CZ Name	State	$a_o/a_y$
Port St. Lucie	Florida	16
Sarasota	Florida	13.6
Tampa	Florida	12.6
Miami	Florida	10
Toms River	New Jersey	5.8

Table 6: CZ with highest  $a_o/a_y$

CZs with the worst relative amenities for old are Anchorage in Alaska, followed by Fairbanks in Alaska. These cities might be less attractive for older residents due to severe climate conditions. Places with the best amenities for the old are Port St. Lucie in Florida, followed by Sarasota in Florida. These cities not only have much nicer natural amenities and better climate, but also lots of recreational activities for older residents such as golf and country clubs and swimming pools.

To study whether model implied amenities are systematically related to the observable measures of amenities, I regress the ratio  $a_o/a_y$  on a set of climate and geography variables and on densities of different local establishments. Table G2 shows results. As predicted by the model, amenities are related to the composition of local establishments:  $a_o/a_y$  is significantly higher in locations with higher densities of gold and country clubs, health and nursing care services and personal care services, but lower in locations with higher density of restaurants, movie theatres and childcare services. Besides, relative amenities for old are significantly higher in locations with higher percentage of the water area and with warmer winter temperatures.

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beneficiaries (69 million enrollees) for the period 1999-2014. Over this period of time 7 million enrollees changed their CZ

<sup>25</sup>Finkelstein et al. (2019) report that 2.4 million out of 7 million movers move more than twice

## 5.4 Exogenous productivities, amenities and housing supplies

This section shows how given the structural parameters calibrated in section 5.2, composite amenities  $\{a_i^y, a_i^o\}$  recovered in section 5.3.2 and data  $\{L_i^y, R_i, w_i\}$ , I can invert the remaining exogenous fundamentals of the model  $\{\tilde{A}_i^y, \tilde{A}_i^o, Z_i, \bar{H}_i\}$ . First, I compute model-implied migration flows  $\hat{L}_{ij}$  according to equation (16). This allows me to calibrate exogenous adjusted amenities for young and old across locations using their model-based definition (23):

$$\tilde{A}_i^y = a_i^y \left( \frac{E_{1i}^{\alpha_1^y} E_{2i}^{(1-\alpha_1^y)}}{R_i} \right)^{\frac{-\delta_b}{\sigma-1}} \quad \tilde{A}_i^o = a_i^o \left( \frac{E_{1i}^{\alpha_1^o} E_{2i}^{(1-\alpha_1^o)}}{R_i} \right)^{\frac{-\delta_b}{\sigma-1}}$$

where  $E_{si}$  is the total expenditure in the city  $i$  on category  $s$  and can be approximated as:

$$\hat{E}_{s,i} = \left( L_i^y \delta_b \alpha_s^y \frac{w_i}{1+\rho} + \rho \sum_j \hat{L}_{ji} \delta_b \alpha_s^o \frac{w_j}{1+\rho} \right)$$

Given the observed wage vector  $\{w_i\}$  and calibrated productivity spillover value  $\gamma^P$ , I can invert the exogenous productivities across locations:

$$Z_i = w_i (L_i^y)^{-\gamma^P}$$

Finally, given the data  $\{R_i, w_i, L_i^y\}$  and the predicted flows  $\hat{L}_{ij}$ , I recover exogenous housing supplies  $\{\bar{H}_i\}$  using equations (17) and (18):

$$\bar{H}_i = \frac{(1-\delta_c)}{d_h(1+\rho)} R_i^{-(1+\frac{1}{\epsilon_h})} (L_i^y w_i + \rho \sum \hat{L}_{ji} w_j)$$

## 6 Quantitative Analysis of the Model

This section performs quantitative analysis of the model. Section 6.1 studies how the life cycle affects individual's location choices and the distribution of economic activity across space. Section 6.2 uses the model to analyse the drivers behind the geographic sorting by age documented in the empirical section. To summarize, I show that differences in location's exogenous amenities for the young and the old, and exogenous productivities lead to the geographic sorting by age, which is further amplified by an endogenous adjustment of productivities and amenities. I estimate that the adjustment of the number of firms to local expenditures is the key mechanism to explain the observed correlation between CZ old-to-young ratios and CZ composition of establishments. Finally, I show that the decline in working hours after retirement is driving the observed negative relationship between CZ

old-to-young ratios and the CZ wages.

Section 6.3 studies the quantitative importance of mobility frictions of moving for retirement. Section 6.4 studies the determinants of the CZ's ability to grow by attracting retirees.

## 6.1 Life cycle and spatial equilibrium

First, I study how the life cycle affects the distribution of workers across locations. Consider the equation for the distribution of young individuals (20):

$$\frac{L_i^y}{L} = t_y \underbrace{\left( \frac{w_i^{(1+\rho)} a_i^y}{R_i^{1-\delta_c} U} \right)^\theta}_{\text{Value for young}} \underbrace{\sum_j \left( \frac{(a_j^o)^\rho}{R_j^{\rho(1-\delta_c)} \mu_{ij}^\rho} \right)^\theta}_{\text{Retirement option}}$$

I compute that the  $R^2$  from the regression of the observed  $L_i^y$  on the estimated value for the young is equal to 0.7. This implies that the retirement option contributes to at least 30 percent of the variation in the CZ working age population size. This result is driven by the fact that locations that location's value for the young is different from its value for the old, and by the fact that the young anticipate the costly relocation for retirement.

To further study the importance of the life cycle for the distribution of economic activity across cities, I compare the Gini coefficients for the main endogenous local variables in the full model (as in the data) with the restricted version of the model where all individuals are young workers who make one static location choice (  $t^y = T$  and  $t^o = 0$  ). To further isolate the role of reallocating retirees, I additionally compute the Gini coefficients for the case when older individuals don't move for retirement. Table 7 presents the results. Overall, life cycle contributes to a more equal distribution of location population sizes, rents and amenities. First, some cities have an exogenous advantage in their amenities for old, and this allows them to attract both young and old residents, which contributes to a more equal distribution of economic activity across space. Moreover, older individuals move out of more expensive cities towards smaller and cheaper places. Additionally, they bring their higher earnings with them, which further contributes to a more equal distribution of prices and amenities across locations.

TABLE 7  
GINI COEFFICIENTS FOR THE MAIN LOCAL VARIABLES

	Population	Rents	Amenities young
Full model /Data	1	1	1
No mobility for retirement	1.02	1.13	1.01
No life cycle	1.21	2.17	1.04

The table shows the Gini coefficients for the local variables in the data (full model), in the model with no life cycle ( $T^y = T$  and  $t^o = 0$ ) and in the model with no mobility for retirement (I recompute local population, rents and amenities assuming that  $L_i^o = \rho L_i^y$  and keeping  $L_y$  fixed at its observed level). Coefficients are normalised by the full model levels. The sample includes 741 U.S. CZs

## 6.2 Decomposing the sorting pattern by age and location

What are the drivers of the sorting of younger and older residents across locations? From the model equilibrium conditions (20) and (21), the ratio of old-to-young in location  $i$  is determined as:

$$\ln \frac{L_i^o}{L_i^y} = \ln \rho + \rho \ln \frac{\left(a_i^o R_i^{-(1-\delta_c)}\right)^\theta}{\sum_j \left(\mu_{ij} a_j^o R_j^{-(1-\delta_c)}\right)^\theta} - \ln \frac{\left(w_i^{(1+\rho)} a_i^y R_i^{-(1-\delta_c)}\right)^\theta}{\sum_j \left(\mu_{ij} w_j^{(1+\rho)} a_j^y R_j^{-(1-\delta_c)}\right)^\theta} \quad (29)$$

Equation (29) implies that if older individuals can move across locations (mobility costs are finite), sorting of the young and the old across locations is governed by the dispersion in the differences of location values for young and old residents. This dispersion arises from three reasons. First, local wages are valued only by workers as retirees supply zero working hours. Second, the young and the old differ in their valuation of local amenities. Besides, as the relative length of the older period  $\rho$  is less than one, old are less sensitive to the variation in all location fundamentals. I further confirm that in the model with fully symmetric geography the variation in the share of the old across locations is zero.

To isolate the role of exogenous geography, I simulate the model where I shut down the endogenous responses of amenities and productivity ( $\sigma = \infty$  and  $\gamma^p = 0$ ). I find that the resulting model explains 93% of the variance of (log) ratio of old to young, implying that the remaining 7% result from the amplification of location differences through the endogenous adjustment of amenities and productivities. I further compute that of this seven percent, two percent is attributed to the endogenous adjustment of the composition of local establishments to the preferences of the young and the old.<sup>26</sup> One concern is that the aggregation procedure made in the paper might miss richer heterogeneity in young and old expenditure shares on local services. However, even in the extreme case when  $\alpha_1^y = 1$  and  $\alpha_1^o = 0$ , that is when young and

<sup>26</sup>I consider the full version of the model, where I restrict  $\alpha^y = \alpha^o$  and compute how much of the variance in the ratio of old to young this model accounts for.

old consume completely different sets of local services, the contribution of endogenous amenities to the variance in the ratio of old to young is only 6%. The reason is that amenity gains from a higher alignment of preferences with the composition of services are limited by the share spend on the local goods  $\delta_b$  and by the love of variety gains governed by  $\sigma$ .

Even though the contribution of endogenous amenities to the sorting of the young and the old is quantitatively small, I show that this mechanism can match the evidence on the correlation between the composition of location establishments and location's demographics described in section 3.3. In particular, to directly relate the empirical evidence to the model outcomes, I aggregate establishments into two broad service categories as in calibration section 5.2, and then I compute the elasticity of the composition establishments with respect to CZ demographic composition by running the following OLS regression:

$$\ln \frac{N_{2i}}{N_{1i}} = \beta_o + \beta_1 \ln \frac{L_i^o}{L_i^y} + X_i + \epsilon_i$$

where  $X_i$  include controls for log location's wages and rents. Then I run the same specification on the model simulated data, where I assume that the fixed costs of entry  $F_{s,i}$  are symmetric across locations. Figure 8 presents the results and shows that the model implied elasticity  $\beta_1 = 0.24$  is close to the OLS estimate  $\beta_1 = 0.29$  in the data. This moment was not directly targeted in the calibration. In the model, it is disciplined only through the differences in expenditure shares by age recovered from the CEX data, and through the endogenous firms' entry mechanism which was calibrated based on the estimates from the literature. Therefore, the endogenous adjustment of local firms to local expenditures is the key mechanism to explain the relationship between local amenities and demographics, but it has a limited role in explaining the sorting pattern by age and location.

Another empirical fact documented in the paper is that CZ wage is negatively correlated with CZ old-to-young ratio. The model was calibrated to fully match the distribution of the young and the old across CZs. Therefore, it fully matches the elasticity of the ratio of old-to-young with respect to the CZ productivity reported in section 3.2. To isolate the role of differences in working hours in generating this pattern, I consider a version of the model where the only change over the life cycle is retirement.<sup>27</sup> In the restricted model, the elasticity of the ratio of old to young w.r.t. CZ wages is  $-0.7$  versus  $-0.9$  in the data.<sup>28</sup> Therefore, most of the observed negative relationship between CZ wages and demographics is attributed to the decline in working hours after retirement, and the rest is attributed to relative amenities for the old being better in less productive locations.

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<sup>27</sup> I assume that  $\tilde{A}_i^o = \tilde{A}_i^y$  and that  $\alpha^o = \alpha^y$

<sup>28</sup> I run the same regression as on figure 2 using the data simulated from the restricted version of the model



TABLE 8  
COMPOSITION OF LOCAL ESTABLISHMENTS:  
MODEL VS DATA

	(1)	(2)
Dependent Variable	$N_2/N_1$ data	$N_2/N_1$ model
$L_i^o/L_i^y$	0.29* (0.15)	0.24*** (0.003)
Controls	✓	✓

$p$ -value \*\*\* $p \leq 0.01$ , \*\* $p \leq 0.05$ , \* $p \leq 0.1$ . Robust standard errors are given in parenthesis. All variables are in logs. Observations weighted by CZ sum of young and old population.  $N_1$  includes establishments in hospital, nursing care homes and beauty services.  $N_2$  includes restaurants, clothing, and childcare services. Both regressions include CZ wages and rents as controls, and include observations for 722 U.S. continental CZs.

### 6.3 The role of mobility costs of moving for retirement

In the model, young individuals are fully mobile, so their expected life time utility is equalised across space. However, this is no longer true for the utility of older residents, who face mobility costs of reallocation across cities. I find that the per period utility of older residents varies significantly across the U.S. CZs: moving from an area at the 25th percentile of the value for the old to an area at the 75th percentile is equivalent to increasing the individual's income by a factor of 2.06.<sup>29</sup> These differences are driven by the fact that locations that are most valuable for the work period are often different from locations that are best for the retirement, so a worse utility for the older residents is offset by a higher utility during the work period and vice versa.

I further show that lower mobility costs allow individuals to increasingly separate locations for work and retirement, which improves the allocation of both young and old individuals w.r.t. CZ fundamentals. In particular, I use 2 and 12 to derive the sum of the location values for young and old residents<sup>30</sup>

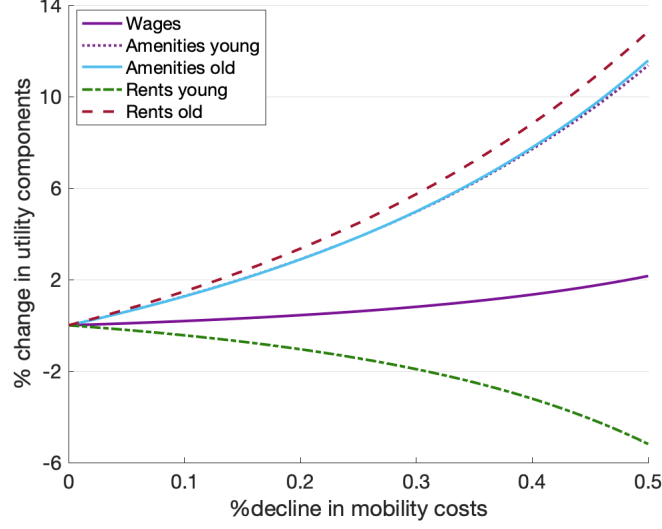
$$V = \sum_i L_i^y \left( (1 + \rho) \ln w_i + \ln a_i^i - (1 - \delta_c) \ln R_i \right) + \sum_i L_i^o \left( \ln a_j^o - (1 - \delta_c) \ln R_j \right)$$

Figure 5 shows how different components of  $V$  respond to a decline in the fixed component of mobility costs for the old  $\kappa$ . Due to lower mobility costs for retirement, young individuals are increasingly choosing locations that are more amenable for the young and more productive, and old individuals are increasingly choosing locations that are cheaper and more amenable for the

<sup>29</sup>Per period utility of older residents in a location  $i$  who lived in  $j$  when young is  $u_{ji}^o = \frac{w_j a_i^o}{R_i^{1-\delta_c}}$

<sup>30</sup>It is a sum of the common components of individual's utilities from living in a given location:  $\sum_i (L_i^y u_i^y + L_i^o u_i^o)$ .

Figure 5: Gains from lower mobility costs for retirement



This figure decomposes the changes in the sum of location values  $V$  in response to a decline the fixed component of the mobility cost for retirement  $\kappa$ . The horizontal axes shows the percentage decline change in  $\kappa$ . The vertical axes shows the resulting percentage changes in the different components of  $V$ . Wage is  $L_i^y(1 + \rho) \ln w_i$ , amenity for young is  $L_i^y \ln a_i^y$ , amenity for old is  $L_i^o \ln a_i^o$ , rent young is  $L_i^y(1 - \delta_c) \ln R_i$  and rent old is  $L_i^o(1 - \delta_c) \ln R_i$

old. The gains for the younger age group are partially offset by the higher rental prices: young residents who expect to later reallocate for retirement are more willing to pay higher prices in exchange for the location value for young.

To sum up, the results in this section suggest that there are large gains from reducing mobility frictions of moving for retirement due to the significant differences in location's value for its younger and older residents.

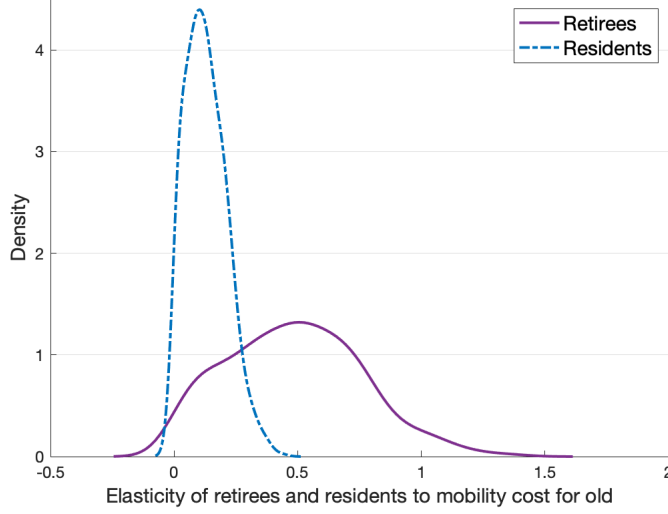
## 6.4 Local Retirement Elasticities

There exist numerous examples of cities and states trying to attract retirees to relocate there.<sup>31</sup> What determines the ability of the city to grow by attracting retirees? To answer this question, I follow the approach of Monte et al. (2018) for studying local employment elasticities. For each CZ  $i$ , I compute the response of the local retiree population to a 1 percent decline in the retiree's mobility costs of moving to a location  $i$ .<sup>32</sup> In this way, I proxy for the effects of policies that target older movers such as relocation subsidies and assistance with moving. Figure 6 shows the estimated kernel density for the distribution of the general equilibrium elasticity across 741 treated CZs. The mean estimated elasticity 0.5 is significantly lower than mean

<sup>31</sup>see Reeder (1998)

<sup>32</sup>I compute 741 counterfactuals where I shock the mobility costs of moving to CZ  $i$   $\mu_{ji}$  by the factor of 0.99 for  $j \neq i$ , keeping all other model parameters fixed

Figure 6: Local retirement elasticities



The figure plots the kernel density for the distribution of retirees and residents elasticities in response to a decline in the mobility costs for incoming retirees. Elasticities are computed from the model simulations for 741 U.S. CZs

employment elasticity to productivity shocks (around 3.9) due to the high level of mobility costs for retirement. Importantly, there exists significant heterogeneity in the predicted elasticities, which vary from as low as 0.001 to almost 1.4.

To study the determinants of this large variation in elasticities, I regress them on a set of CZ observable characteristics. Table 9 shows the results. In column 1, I include log CZ young population as the only control, and I find a strong and negative relationship between the two variables which explains a significant portion of the variation in elasticities ( $R^2$  is 0.65). Places that are less attractive for younger residents have a larger pool of potential reallocating retirees relative to their current population size, so they are more successful at increasing their retiree population. In columns 2 and 3, I add log CZ old-to-young ratio and total young population of nearby CZs as additional controls, which raises the  $R^2$  to 0.95.<sup>33</sup> Both controls capture the attractiveness of the CZ for the retirees in other locations and are positively associated with the retirement elasticity. Adding more observable controls such as wages, rents in the location and in nearby locations does not improve the regression fit.

Figure 6 shows that as compared to the retirement elasticities the predicted total population elasticities are much lower and vary from around 0 to just 0.5. The reason is that reallocating retirees increase the local housing prices which makes the location less attractive for the younger

<sup>33</sup> total young population in nearby CZs for the CZ  $i$  is the inverse mobility cost weighted sum of  $L_y$  in CZs other than  $i$

TABLE 9  
DETERMINANTS OF THE LOCAL  
RETIREMENT ELASTICITIES

	(1)	(2)	(3)
$\ln L_y$	-0.22*** (0.007)	-0.19*** (0.004)	-0.21*** (0.005)
$\ln \frac{L_o}{L_y}$		0.96*** (0.03)	0.8*** (0.04)
$\ln \bar{L}_{-i}^y$			0.91*** (0.08)
Obs.	741	741	741
R-squared	0.65	0.92	0.95

$p$ -value \*\*\* $p \leq 0.01$ . Robust standard errors are given in parenthesis. The dependent variables is the model simulated elasticity of the CZ old population w.r.t. the decline in the mobility costs for reallocating retirees.  $\bar{L}_{-i}^y$  is the inverse mobility cost weighted sum of young individuals in CZs other than  $i$ .

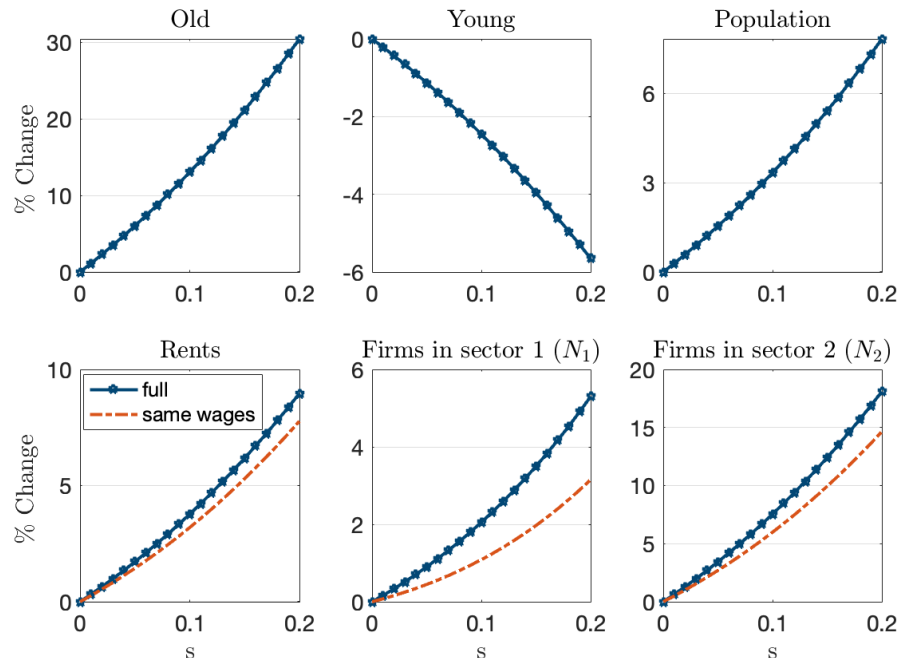
residents and dampens the response of total population to mobility costs.

Overall, the results in this section suggest that same local policies targeted at attracting retirees can have heterogeneous affects across treated cities. Locations that grow the most are the ones that are smaller, have larger share of older residents and are closer to more populated CZs. However, the total affect of such policies is significantly dampened by the high mobility costs that retirees face and by the rising local prices that drive out workers.

## 7 Counterfactual Exercises

This section describes counterfactual exercises of the model. Section 7.1 studies local and aggregate effects of place-based policies that target older individuals to relocate to less productive cities. Section 7.2 discusses the implications of the ageing shift predicted over 2020-2040 period. Section 7.3 shows that the geographic sorting by age has increased over 1960-2010 period and argues that declining mobility frictions for the old was the main factor behind these changes.

Figure 7: Local effects of the policy that subsidises the reallocation of old to less productive cities



Simulated local changes due to the introduction of a subsidy  $s$  measured as a percentage of individuals' average wages in the economy given to any old individual moving to a treated city. The policy is financed via a lump sum tax paid by all workers in the economy. Treated cities are the smallest CZs in U.S. that represent 1 percent of total population.

## 7.1 Place-based policies targeted at retirees

The previous section shows that smaller cities gain relatively more from subsidising the reallocation for retirement. Should policy promote the development of smaller/less-productive cities by this channel? Existing literature has largely focused on the affects of place-based policies that subsidize firms to locate in less developed cities or regions. This type of policies aims at reducing the spatial disparities and increasing the aggregate efficiency. However, as argued in [Kline & Moretti \(2014\)](#) positive local impacts of such policies are counterbalanced by losses in other locations and lead to the aggregate losses in the welfare and TFP. [Gaubert \(2018\)](#) further shows that such policies actually increase the spatial disparities in GDP per capita in the U.S. Related to the questions in this paper, some states indeed try to boost their less developed areas by attracting the retirees to reallocate there.<sup>34</sup> Analysis from the previous section shows that smaller cities benefit from such policies relatively more in terms of their

<sup>34</sup>For example, Alabama provides state assistance to rural communities in retiree attraction, including planning and technical assistance coordinated marketing efforts, financial assistance, and amenity development. More examples are in [Reeder \(1998\)](#).

population size. However, the efficiency of this policy depends on whether the optimal allocation features higher or lower sorting of the young and the old given the calibrated parameters.

In this section, I study quantitatively local and aggregate effects of the policies that incentivise the old to reallocate to less productive cities. I consider counterfactuals in which older individuals are given a subsidy  $s$  to move to the least productive cities in the U.S (cities in the 25th quantile by productivity). Figure 7 shows the local effects of the policy as a function of the subsidy level  $s$ . For example, a 10% subsidy in terms of the average wages in the economy which costs 0.04% of GDP (as the policy considered in Gaubert (2018)) increases the total population of treated cities by 3.2%, increases rents by 4.6% and increases the number of firms in sectors 1 and 2 by 2.01% and 9.5% respectively. The red dotted line on figure 7 shows what response of local variables would be if relocating old had same wages as the workers in the treated city. The difference between the two lines shows that local policy effects are amplified by higher earnings of relocating retirees.

The counterfactual exercise allows me to compute the general equilibrium effect of the policy on the welfare and TFP. Appendix figure H10 shows that aggregate welfare is monotonically decreasing in the subsidy level  $s$ , while the reverse holds for the aggregate TFP. While reallocation of retirees improves productive efficiency, this is achieved by very costly mobility of old, which does not offset the TFP gains. From the optimal policy perspective, it turns out that for the calibrated parameters gains from productivity spillovers are offset by a worse distributional efficiency due to the preference shocks. So higher sorting by age and productivity is not welfare improving.

I further study how the policy affects the dispersion of spatial outcomes according to the Gini coefficient for the endogenous spatial variables. I find that the type of the place-based policy that I study contributes to a more equal distribution of amenities and rents across CZs, but a more unequal distribution of wages in the tradeable sector. However, as I don't model the employment in the local service sector, the analysis might miss the additional response from employment and wages there.

## 7.2 Ageing population and changes in the city size distribution

Over the 2020-2040 period the relative size of the older age group is predicted to increase by around 36%.<sup>35</sup> Through the lens of the model, this change corresponds to an increase in the relative length of the old period  $\rho$ , which makes the older period more important for the individual's location choices and for the equilibrium outcomes.

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<sup>35</sup>The prediction is for the age groups 20-64 and 65+ from <https://www.urban.org/policy-centers/cross-center-initiatives/program-retirement-policy/projects/data-warehouse/what-future-holds/us-population-aging>

By running the counterfactual increase in  $\rho$  by 36 percent, I estimate that the ageing shift between 2030 and 2040 is expected to generate a significant shift in spatial distribution of cities: 13 percent of workers and 16 percent of retirees are expected to change their location. I find that CZs that are more attractive for old are predicted to gain both in terms their retiree and working age population, which further increases their wages and amenities.

### 7.3 Changes in geographic sorting by age, 1960-2010

Figure 8 shows that a pattern of sorting by age and location’s productivity documented in recent decades was not present in earlier Census sample of 1960.<sup>36</sup> I further compute that the dissimilarity index for the younger and the older age groups has increased by 38% over this period from around 0.06 in 1960 to around 0.08 in 2010.<sup>37</sup> These changes might be related to an increase in the mobility for retirement: the share of individuals of age 55 and older who moved between states within a 5 year window has increased by around 22% over 1960-2000.<sup>38</sup> By comparison, the share of individuals in the younger age group (25-55) who moved between states has increased only by around 4%.

This section studies the drivers behind the changes in geographic sorting by age over time. In particular, I recalibrate my model to the MSA-level data for 1960 and 2010 years, treating these two time periods as different steady states of the model. I keep all the structural parameters as in the main quantification part, except for the fixed component of the mobility cost ( $\kappa$ ) and the relative length of the old period ( $\rho$ ). I recalibrate  $\kappa$  and the exogenous location-specific parameters for year 1960 so that to match the distribution of individuals and prices in 1960 and to match the fact that the share of individuals who reallocate between states for retirement in 1960 is by 22 percent lower than in 2010.<sup>39</sup> More details on the calibration procedure are in Appendix F. I find that the mobility costs in 1960 should have been 36% lower than in 2010. One of the reasons behind this large model-implied changes in mobility costs is that in 1960 population was much more concentrated in the most productive U.S. MSAs, and most of these locations actually had old-to-young ratios above national average. So to rationalise low mobility flows for retirement in that period the model requires relatively large mobility costs.

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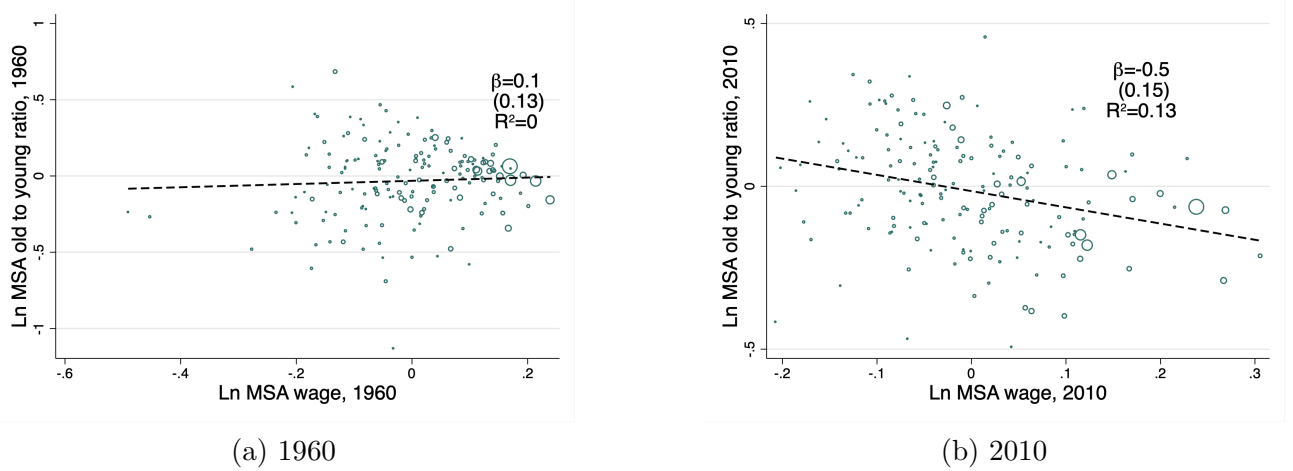
<sup>36</sup>As there is no mapping between geography units and CZs for historical samples for 1960 sample, I chose to make historical comparisons at the MSA level.

<sup>37</sup>The dissimilarity index is defined as  $\frac{1}{2} \left| \frac{L_i^o}{\sum_i L_i^o} - \frac{L_i^y}{\sum_i L_i^y} \right|$  where  $L_i^o$  is the size of the older age group in the location  $i$ , and  $L_i^y$  is the size of the younger age group in  $i$ . I include 169 common MSAs and one location corresponding to all the areas outside of the MSAs in the computation

<sup>38</sup>I compute that 3.97% of individuals older than 55 moved between U.S. states in 1960 within a five year window, while the corresponding number for 2000 is 4.83%. I choose a lower age cut-off than in the definition of the older age group as individuals might reallocate for retirement earlier than their actual retirement.

<sup>39</sup>I map each MSA to a single state and compute the share of old who relocates between states

Figure 8: Sorting by age and productivity, MSA level



Regressions weighted by the MSA total population. Older age group includes individuals of age 60+ and younger age group includes individuals of age 25 – 60. Wages are adjusted for the location’s demographics. Regressions include 169 MSAs present in both years. Wages and old-to young ratios are in logs and normalised by the MSA mean values in the corresponding year.

TABLE 10  
CHANGES IN SORTING 1960-2010

	1960	Simulation	2010
$corr(W_i, \frac{L_i^o}{L_i^y})$	0.01	−0.2	−0.27

All variables are normalized by the year means. Column two computes the correlation of the simulated  $W_i$  and  $\frac{L_i^o}{L_i^y}$  in a model that was calibrated to year 1960 at the MSA level and where mobility costs were set at 2010 level.

Next, I decompose the drivers behind the changes in the sorting by age and location’s productivity from 1960 to 2010. Table 10 shows that if I take the model calibrated to 1960 and change mobility costs alone to their calibrated 2010 level, I can explain around 73% of the increase in the correlation between MSA old-to-young ratio and MSA wages. Appendix F.1 performs the full decomposition, and shows that changes in location-specific factors explain the remaining increase in sorting, while the ageing shift actually has an opposite effect on the sorting by age and productivity. Finally, I compute that changes in mobility costs between 1960 and 2010 contributed to a 6.3 percent increase in welfare, which is equivalent to increasing an individual’s income by 4.9 percent.



## 8 Conclusion

This paper argues on the importance of the life cycle for location choices and for the distribution of economic activity across space. By building and estimating the model of location choices for work and retirement periods, I quantify the differences in locations' values for their younger and older residents. I find that these differences arise from changes in working hours and preferences for local amenities with age, and that they imply large gains from life cycle mobility. I also estimate that mobility frictions preclude retirees from moving to better places and lead to a significant dispersion in location-specific utilities of older individuals.

I document that the geographic sorting by age has increased dramatically over 1960-2010 period. Using the model structure, I argue that this increase in sorting is related to the decline in mobility frictions of relocating for retirement, which allowed individuals to increasingly separate locations for work and retirement periods. I estimate the resulting welfare gains to be equal to 6.3%. I further show that policies that target higher sorting of young and old through place-based transfers are not welfare improving. This suggests that it is important to further study the frictional components of the mobility costs that older individuals face and how and why they have changed over time.

The paper also shows that smaller cities benefit the most from local policies aimed at attracting retirees: they experience a larger increase in total population and a larger increase in the variety of local services. Therefore, such policies can be considered for the purpose of reducing spatial disparities, and they differ from similar policies targeted at workers as they do not distort production efficiency and because relocating retirees bring their savings from more productive cities with them. Another direction for the future research is to model the response of the employment in the non-traceable sector to the inflow of savings of the relocating old. This would help to better understand the scope of place-based policies targeted at the old for reducing spatial disparities and inequality.

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# Appendices

## A Data Appendix

### A.1 Composition adjusted wages

I compute individual's log hourly wages in a subsample of workers: individuals of age 17-64, who work more than 44 weeks and more than 34 hours a week. Then, for each sample year I regress log hourly wages on the set of demographic controls: age, sex, race, nativity and highest completed education:

$$\ln w_{i,t} = \alpha + \beta X_{i,t} + \epsilon_{i,t}$$

Composition adjusted wages for residents in each location  $j$  can then be constructed as:

$$\ln w_{i,j,t}^{adj} = \ln w_{i,j,t} - \sum_k \beta_t^k (X_{i,t}^k - \bar{X}_t^k)$$

where  $w_{i,j,t}$  is the individual  $i$  wage in a location  $j$  at the time  $t$ , and  $\bar{X}_t^k$  is the average of the demographic control  $k$  in year  $t$  across all individuals. CZ  $j$  composition adjusted wage is computed as the average of the composition adjusted wages of its workers.

### A.2 Quality adjusted rents

To compute a proxy for local prices, I consider rental payments reported by a subsample of households who rent housing. I use gross rent, which is monthly rental cost of the housing unit, including contract rent plus additional costs for utilities (water, electricity, gas) and fuels (oil, coal, kerosene, wood, etc.). In order to be able to compare rental prices across CZs, I adjust them for the differences in the quality of the rented housing. The observable characteristics of the housing units are the following:

- **Year build.** Six indicator variables for the year build (0-1 years, 2-5 years, 6-10 years, 11-20 years, 21-30 years, 31+)
- **Number of bedrooms.** Six indicator variables (0 bedrooms, 1, 2, 3, 4, 5+)
- **Kitchen facilities.** Indicator for the presence of the kitchen facilities
- **Plumbing facilities.** Indicator for the presence of the plumbing facilities

Then, for each sample year for the subsample of renters I regress household's log rents on the set of housing controls defined above:

$$\ln R_{i,t} = \alpha + \beta X_{i,t} + \epsilon_{i,t}$$

Quality adjusted rents for residents of each location  $j$  can then be constructed as:

$$\ln R_{i,j,t}^{adj} = \ln R_{i,j,t} - \sum_k \beta_t^k (X_{i,t}^k - \bar{X}_t^k)$$

where  $R_{i,j,t}$  is the individual  $i$  rent paid in a location  $j$  at the time  $t$ , and  $\bar{X}_t^k$  is the average of the quality control  $k$  in year  $t$  across all individuals. City  $j$  quality adjusted rents are computed as the average of the quality adjusted rents of its residents who rent housing.

### A.3 CEX data

I use data extracts from the Consumer Expenditure Surveys quarterly interview survey compiled by Ed Harris and John Sabelhaus and provided by NBER. The dataset includes households interviewed between the first quarter of 1980 and the second quarter of 2003. The interviews are conducted during five consecutive quarters: first quarter collects demographic data for each household member, and subsequent four interviews collect data on household level expenditures. The NBER extract aggregates the four interviews into a single observation per household, summing all quarterly expenditures.

As expenditure level data is provided at the household level, I restrict the sample to the single households, married couples and married couples with children under the age of 21. For each household I define a household's head using the procedure developed in [Aguiar & Hurst \(2013\)](#): a head is defined as an individual who identifies herself or himself as a household head in the survey, and if there are multiple heads, the head is identified by sex, employment, age and marital status. To match expenditure data to demographics, I use the demographic data for the identified household's head.

Harris and Sabelhaus aggregate expenditures into 47 broad categories. I compute total expenditure using all available categories, and then consider a subsample of categories that is most closely related to locally provided services:

- Food outside of home: includes food and non-alcoholic beverages at Restaurants, Cafes and fast food places, food at school and boarding places.
- Nightclubs: includes alcoholic beverages at restaurants, cafes and bars.
- Clothing: includes expenditures on clothing and shoes, jewelry and watches and tailoring.

- Personal care services: includes expenditures on barbershops, beauty parlors and health clubs.
- Health care services: includes expenditures on drugs and hospitals both out of pocket and included in medical insurance.
- Nursing Homes: includes care in Convalescent or Nursing Home
- Recreation (other recreation category in NBER extract): includes expenditures on repair and rental of recreational equipment, expenditures on pets, expenditures on country clubs, health clubs, swimming pools and other clubs, admission fees for entertainment activities and sporting event.
- Childcare services: includes expenditures on day care centers, nursery schools, elementary and secondary education.

I further restrict my subsample to households that report positive expenditures for the sum of 8 local service categories, and restrict household head to be older than 25. This leaves a sample of 77844 households.

## A.4 Amenities

I use establishments counts at the county level in the following NAICS codes as proxies for local amenities:

- Food Services and Drinking places (NAICS 722 except 7224)
- Drinking places (NAICS 7224 )
- Clothing and Accessory stores (NAICS 448)
- Golf Courses and Country clubs (NAICS 71391)
- Other recreation (NAICS 7139 except 71391).
- Performing Arts, Spectator Sports, and Related Industries (NAICS 711)
- Motion picture theatres (NAICS 512131)

I further use crosswalks from counties to pumas and from pumas to commuting zones provided by [Autor & Dorn \(2013\)](#). To compute establishment density I scale total number of establishments by commuting zone total population size to get establishment counts per 1000 residents.

Besides, I use geographic amenities data constructed by the United States Department of Agriculture<sup>40</sup>. These measures are warm winter, winter sun, temperate summer, low summer humidity, topographic variation, and water area. The data is available at the county level. I use crosswalks provided by Eckert et al. (2020) to map the data to Commuting zones. The data is available for 722 CZs out of 741.

## B Changes in the individual-level mobility patterns with age

This section studies how the direction of individual’s mobility between CZs changes with age. I use 2000 Census sample to identify the subsample of movers: individuals who changed their CZ within a 5 year window. For each mover, I compute the difference between the fundamentals of the destination and origin CZs. I study how the probability of moving up (to a commuting zone with at least 1% higher fundamental of interest) depends on individual age:

$$\text{Up}_{i,j} = \alpha + \beta X_{i,t} + \sum_{i=1}^5 \gamma_i \text{age group}_{i,t} + \psi_j + \epsilon_i$$

Where  $X_{i,t}$  is a set of demographic controls for race, sex, nativity and education and  $\psi_j$  are location fixed effects. Age groups are 25 – 35, 36 – 45, 46 – 55, 56 – 65, 66+.

Table B1 shows the results. As hypothesised, older individuals are significantly less likely to move to a more productive location as compared to young. The highest difference happens around the retirement age (age group 55-65). Older individuals are also less likely to move to a more populated and expensive location, except for the oldest group of 66+. This group does not move to cheaper places, but still moves to places with a significantly higher share of old, indicating the reallocation for amenity reasons.

## C Robustness Checks for the Empirical Results

This section provides the robustness checks for the main empirical results in the paper.

### C.1 Robustness Checks for the Results in Figure 2

First, I show that the pattern of sorting presented on Figure 2 is robust to considering retirees instead of the old. I define retirees as individuals of age 50 and older who is out of the labor force. Figure C1 shows the elasticity of retiree-to-old ratio with respect to CZ wage. The results

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<sup>40</sup><https://www.ers.usda.gov/data-products/natural-amenities-scale>



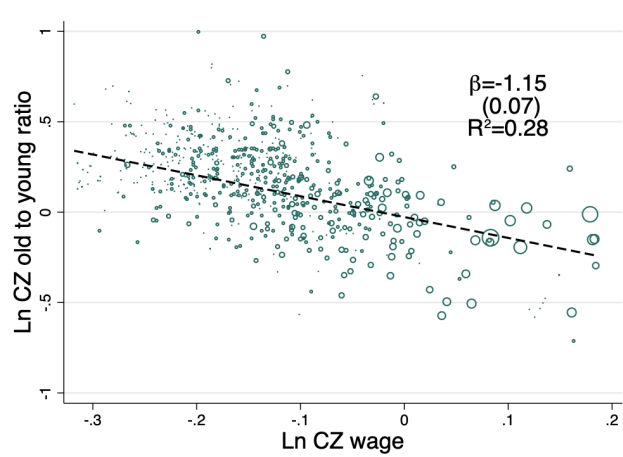
TABLE B1  
DIRECTION OF INDIVIDUAL MOBILITY BY AGE

	Higher Wage	Higher Pop.	Higher Rent	Higher old share
[36 – 45]	-0.023*** (0.002)	-0.022*** (0.002)	-0.021*** (0.002)	0.02*** (0.002)
[46 – 55]	-0.047*** (0.003)	-0.04*** (0.003)	-0.035*** (0.003)	0.043*** (0.003)
[56 – 65]	-0.088*** (0.005)	-0.066*** (0.005)	-0.047*** (0.003)	0.099*** (0.006)
66+	-0.043*** (0.005)	-0.027*** (0.004)	-0.004 (0.004)	0.084*** (0.007)
Obs.	1,091,989	1,091,989	1,091,989	1,091,989
R-squared	0.307	0.335	0.299	0.299
CZ FE	YES	YES	YES	YES
Controls	YES	YES	YES	YES

Results relative to the youngest group 25-35. Standard errors in parentheses are clustered at the CZ level

are stronger than in case of the old-to-young ratio, which might be driven by workers retiring earlier in less productive CZs

Figure C1: Sorting of retirees and workers across by productivity

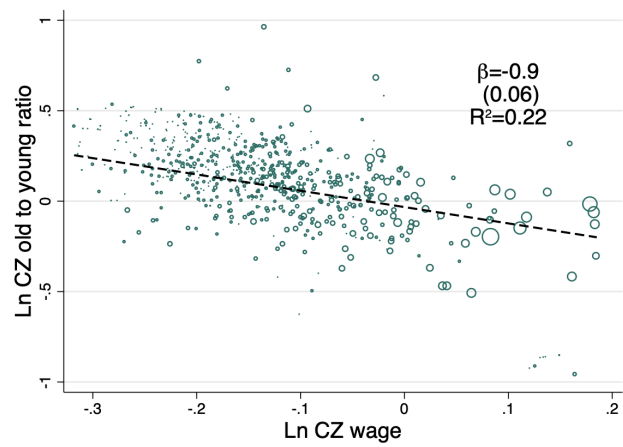


The figure plots CZ's ratio of retirees to workers against CZ's average wages earned by workers. Retirees are defined as individuals of age 50 and older who is out of the labor force. Workers are individuals between ages 17 – 64, who work more than 44 weeks and more than 34 hours a week. Both variables are logs of the averages of demeaned values across 1980, 1990, 2000 and 2014 samples. CZs' wages are adjusted for the differences in CZs' demographics.  $\beta$  stands for the OLS regression coefficient and robust standard errors are in parenthesis. Regressions are weighted by location's average population across same samples. The size of each CZ circle is proportionate to its average population.

Figure C2 shows that pattern of sorting by age and productivity is the same if we consider an age cut-off of 65+ instead of 60+. I also check if the results are robust to the weighting: the original regression uses observations weighted by the CZ population size. If observations are not weighted, the correlation between location productivity and share of old is even stronger, as shown in the figure C3.

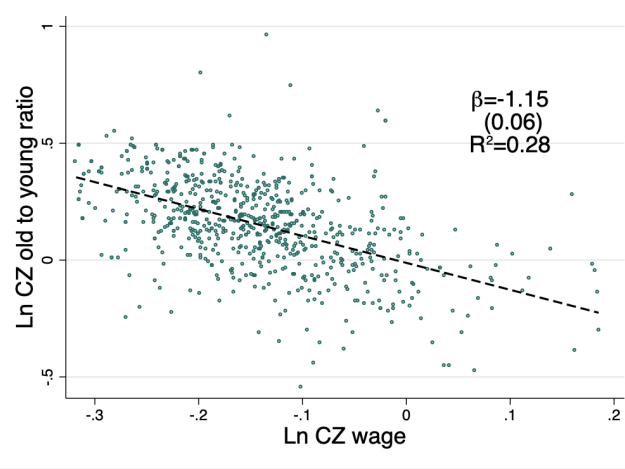
Finally, I provide an additional check that the original evidence on the sorting is mostly driven by the fact that the young and the old value locations differently, rather than by the fact that they respond to location-specific shocks in a different way. In particular, I compute whether the lagged location productivity (year 1970) is correlated with location's current old-to-young (year 2014). Figure C4 shows that the resulting sorting pattern by age and lagged productivity is strong and significant, suggesting that time persistent differences in CZ productivities are driving the sorting pattern.

Figure C2: Sorting of the young and the old (65+) by productivity



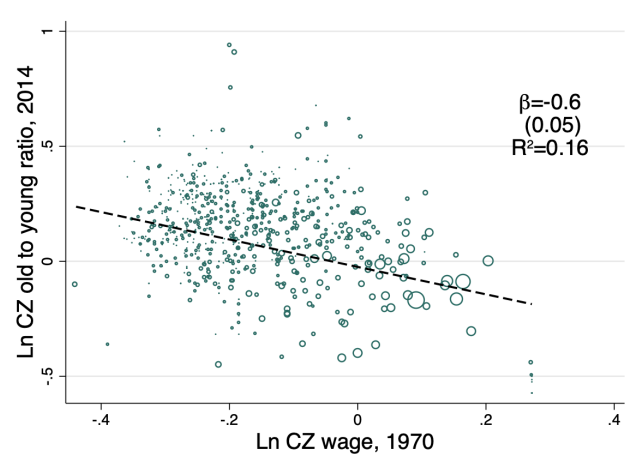
The figure plots CZ's ratio of individuals older than 65 to individuals between ages 25 and 65 against CZ's average wages earned by workers. Both variables are logs of the averages of demeaned values across 1980, 1990, 2000 and 2014 samples. CZs' wages are adjusted for the differences in CZs' demographics.  $\beta$  stands for the OLS regression coefficient and robust standard errors are in parenthesis. Regressions are weighted by location's average population across same samples. The size of each CZ circle is proportionate to its average population.

Figure C3: Sorting of the young and the old by productivity (no weights)



The figure plots CZ's ratio of individuals older than 60 to individuals between ages 25 and 60 against CZ's average wages earned by workers. Both variables are logs of the averages of demeaned values across 1980, 1990, 2000 and 2014 samples. CZs' wages are adjusted for the differences in CZs' demographics.  $\beta$  stands for the OLS regression coefficient and robust standard errors are in parenthesis.

Figure C4: Sorting of young and old across the US CZs: lagged productivity

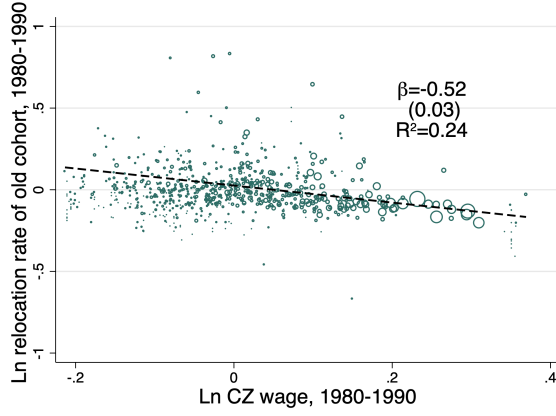


The figure plots CZ's ratio of individuals older than 60 to individuals between ages 25 and 60 in 2014 against CZ's average wages earned by workers in 1970. CZs' wages are adjusted for the differences in CZs' demographics.  $\beta$  stands for the OLS regression coefficient and robust standard errors are in parenthesis. Regressions are weighted by location's average population across same samples. The size of each CZ circle is proportionate to its average population.

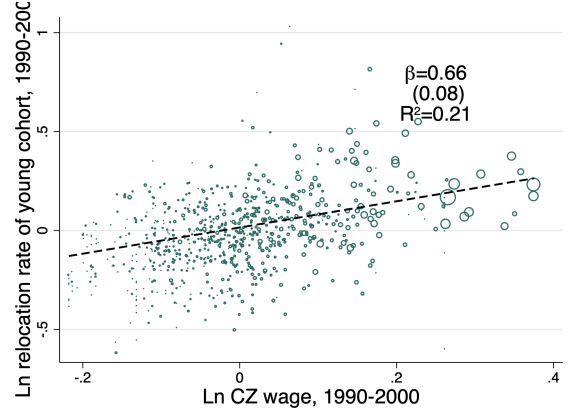


## C.2 Robustness Checks for the Results in Figure 3

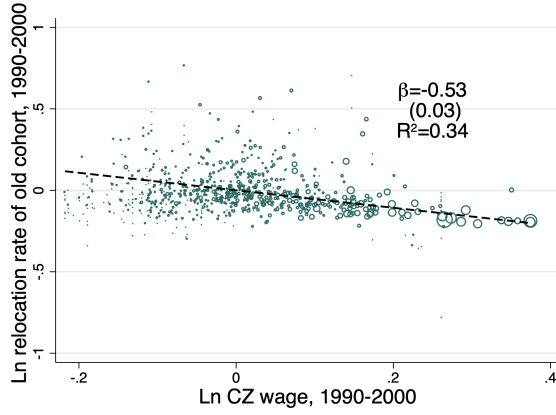
Figure C5: Reallocation of young and old cohorts across CZs, by decade



(a) An older cohort, 1980-1990



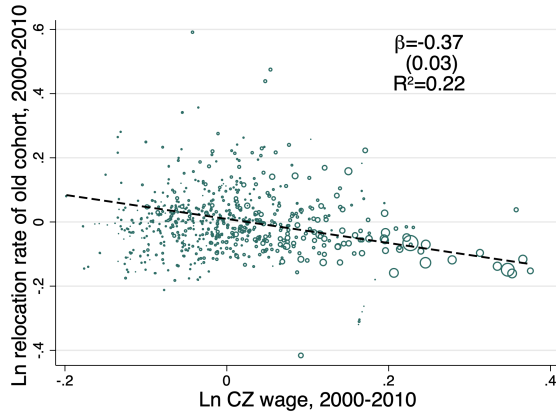
(b) A younger cohort, 1980-1990



(c) An older cohort, 1990-2000



(d) A younger cohort, 1990-2000



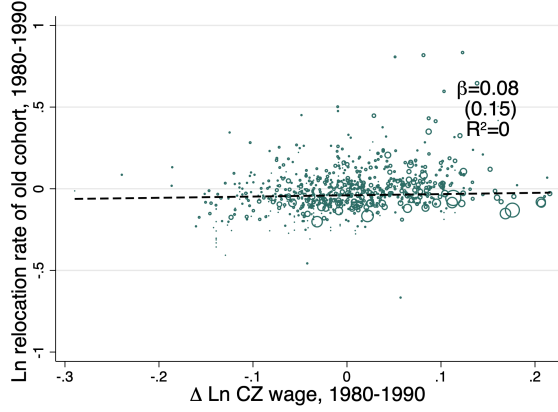
(e) An older cohort, 2000-2010



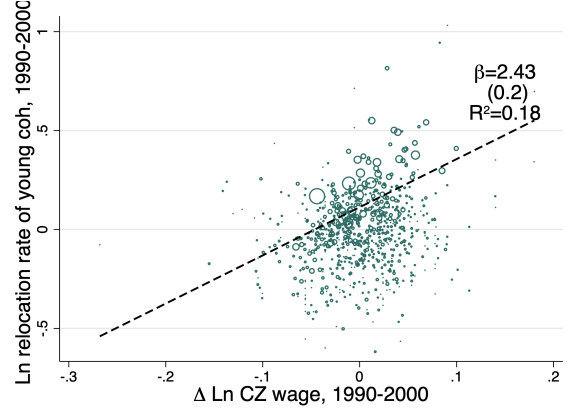
(f) A younger cohort, 2000-2010

The figure plots the CZ's growth in the population of a given cohort over the ten year period against the CZ's average wages earned by workers in periods  $t$  and  $t + 10$ . An older cohort denotes individuals who fall into the age category 47-57 in the Census year  $t$  and a younger cohort denotes individuals who fall into the age category 15-25 in the Census year  $t$ . CZs' wages are adjusted for the differences in CZs' demographics.  $\beta$  stands for the OLS regression coefficient and robust standard errors are in parenthesis. Regressions are weighted by location's average population across same samples.

Figure C6: Reallocation of young and old cohorts w.r.t wage growth



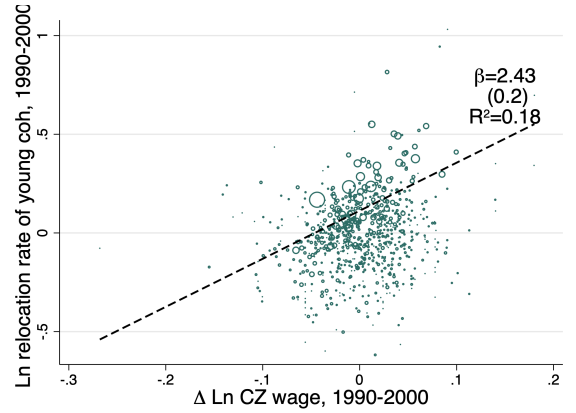
(a) An older cohort, 1980-1990



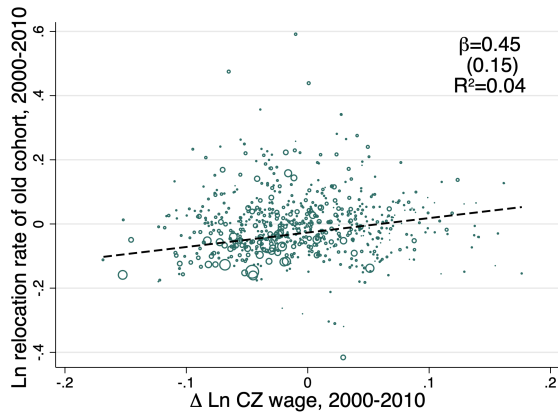
(b) A younger cohort, 1980-1990



(c) An older cohort, 1990-2000



(d) A younger cohort, 1990-2000



(e) An older cohort, 2000-2010



(f) A younger cohort, 2000-2010

The figure plots the CZ's growth in the population of a given cohort over the ten year period against the CZ's wage growth from  $t$  to  $t + 10$ . An older cohort denotes individuals who fall into the age category 47-57 in the Census year  $t$  and a younger cohort denotes individuals who fall into the age category 15-25 in the Census year  $t$ . CZs' wages are adjusted for the differences in CZs' demographics.  $\beta$  stands for the OLS regression coefficient and robust standard errors are in parenthesis. Regressions are weighted by location's average population across same samples.

## D Proofs for the Theoretical Part

### D.1 Formulation of the utility function (1

Individuals choose a pair of locations  $\{i, j\}$ , where  $i$  is where they live for the  $t^y$  young periods, and  $j$  is where they live for the  $t^o$  old periods. Conditional on the location path  $\{i, j\}$ , the individual problem is:

$$\begin{aligned} & \max_{c_t^y, c_t^o, h_t^y, h_t^o, q_{m,s,t}^y, q_{m,s,t}^o} \sum_{t=1}^{t=t^y} u(c_t^y, h_t^y, q_{m,s,t}^y) + \sum_{t=t^y+1}^{t=T} u(c_t^o, h_t^o, q_{m,s,t}^o) \\ \text{s.t.} \quad & \sum_{t=1}^{t=t^y} \left( c_t^y + R_{i,t} h_t^y + \sum_{s=1}^2 \sum_{m=1}^{N_{s,i,t}} p_{m,s,i,t} q_{m,s,t}^y \right) + \sum_{t=t^y+1}^T \left( c_t^o + R_i h_t^o + \sum_{s=1}^2 \sum_{m=1}^{N_{s,i,t}} p_{m,s,i,t} q_{m,s,t}^o \right) = \sum_{t=1}^{t=t^y} w_i \end{aligned}$$

where  $w_i$  is the wage that individual receives each period that she is young from supplying one unit of labor and where I assumed that the discount factor and the interest rate are equal to one.

As the model is stationary, in equilibrium all the prices will be constant through time. Then, in the optimal solution to this problem individuals will choose same consumption levels within young and old period:  $c_t^y = c_y$ ,  $h_t^y = h^y$ ,  $c_t^o = c^o$ ,  $h_t^o = h^o$ ,  $q_{m,s,t}^y = q_{m,s}^y$  and  $q_{m,s,t}^o = q_{m,s}^o$ . Then the problem is equivalent to:

$$\begin{aligned} & \max_{c^y, h^y, c^o, h^o} t_1 u(c^y, h^y, a_i) + t_2 u(c^o, h^o, a_j) \\ \text{s.t.} \quad & t_1 \left( c^y + R_i h^y + \sum_{m=1}^{N_{s,i}} p_{m,s,i} q_{m,s}^y \right) + t_2 \left( c^o + R_i h^o + \sum_{m=1}^{N_{s,i}} p_{m,s,i} q_{m,s}^o \right) = t_1 w_i \end{aligned}$$

Which is equivalent to the consumer problem in the main text.

### D.2 Social planner problem

**Definition 2.** Social planner chooses consumption  $\{c_{ij}^{y,o}, h_{ij}^{y,o}, q_{1ij}^{y,o}, q_{2ij}^{y,o}\}$  and a mass of firms in two non-tradeable sectors  $\{N_{1i}, N_{2i}\}$  to solve

$$\max LU$$

subject to

- *spatial mobility constraint:*

$$\ln \left( \frac{L_{ij}}{L} \right)^{\frac{1}{\theta}} = \ln \left( A_i^y (c_{ij}^y)^{\delta_c} (h_{ij}^y)^{\delta_h} (Q_i^y)^{\delta_b} \right) + \rho \ln \left( A_i^o (c_{ij}^o)^{\delta_c} (h_{ij}^o)^{\delta_h} (Q_j^o)^{\delta_b} \right) - \ln U$$

$$\text{where } Q_i^a = \left( N_{1i}^{\frac{\sigma}{\sigma-1}} q_{1ij} \right)^{\alpha_1^a} \left( N_{2i}^{\frac{\sigma}{\sigma-1}} q_{2ij} \right)^{\alpha_2^a} \text{ for } a = y, o$$

- *Housing production function*

$$H_i = \bar{H}_i I_i^{\frac{1}{1+\epsilon_h}}$$

- *Resource constraint:*

$$\sum_j \sum_i L_{ij} \left( c_{ij}^y + \rho c_{ij}^o \right) + \sum H_i I_i = \sum_j \sum_i L_{ij} Z_i (I_i^y)^{\gamma_P}$$

- *individual's allocation constraint:*

$$\sum_j \sum_i L_{ij} = L \quad (30)$$

- *Housing constraints:*

$$H_i = \sum_j L_{ij} \left( h_{ij}^y + \sum_{s=1,2} N_{s,i} k q_{sij} \right) + \rho \sum_j L_{ji} \left( h_{ji}^o + \sum_{s=1,2} N_{s,i} k q_{sji} \right) + \sum_{s=1,2} N_{s,i} F_{s,i}$$

**Proposition 3.** *In an efficient allocation the following should hold:*

$$\underbrace{x_{ij}}_{\text{consumption cost}} + \underbrace{\lambda}_{\text{opport}} = \underbrace{z_i^* + \gamma^P z_i^*}_{\text{marginal product in } i} - \frac{x_{ij}}{\theta(1+\rho)} \quad (31)$$

$$\underbrace{R_i^* N_{si} F_{si}}_{\text{housing cost}} = \underbrace{\frac{\sigma}{\sigma-1} \frac{1}{\sigma} \frac{\delta_b}{1+\rho} \left( \alpha_s^y \sum_j x_{ij} L_{ij} + \rho \alpha_s^o \sum_j x_{ji} L_{ji} \right)}_{\text{utility gain}} \quad (32)$$

for  $s = 1, 2$ , where  $x_{ij} = c_{ij}^y + \rho c_{ij}^o + R_i^* (h_{ij}^y + \sum_{s=1,2} N_{si} k q_{sij}^y) + \rho R_j^* (h_{ij}^o + \sum_{s=1,2} N_{sj} k q_{sij}^o)$  is the cost along the path,  $R_i^*$  is the multiplier under the housing constraint of the city  $i$  and  $\lambda$  is the multiplier under the labor allocation constraint

Proof. The Lagrangian of the planning problem is:



$$\begin{aligned}
L = & \ln U - \sum_{ij} \omega_{ij} \left( \ln \left( A_i^y (c_{ij}^y)^{\delta_c} (h_{ij}^y)^{\delta_h} \left( N_{1i}^{\frac{\sigma}{\sigma-1}} q_{1ij} \right)^{\delta_b \alpha_1^y} \left( N_{2i}^{\frac{\sigma}{\sigma-1}} q_{2ij} \right)^{\delta_b \alpha_2^y} \right) + \right. \\
& \rho \ln \left( A_i^o (c_{ij}^o)^{\delta_c} (h_{ij}^o)^{\delta_h} \left( N_{1j}^{\frac{\sigma}{\sigma-1}} q_{1ij} \right)^{\delta_b \alpha_1^o} \left( N_{2j}^{\frac{\sigma}{\sigma-1}} q_{2ij} \right)^{\delta_b \alpha_2^o} \right) - \ln U - \ln \left( \frac{L_{ij}}{L} \right)^{\frac{1}{\theta}} \\
& + R_i^* \left( \bar{H}_i I_i^{\frac{1}{1+\epsilon_h}} - \sum_j L_{ij} \left( h_{ij}^y + \sum_{s=1,2} N_{s,i} k q_{sij}^y \right) - \rho \sum_j L_{ji} \left( h_{ji}^o + \sum_{s=1,2} N_{s,i} k q_{sji}^o \right) - \sum_{s=1,2} N_{s,i} F_{s,i} \right) \\
& + P^* \left( \sum_j \sum_i L_{ij} Z_i \left( \sum_j L_{ij} \right)^{\gamma_P} - \sum_j \sum_i L_{ij} (c_{ij}^y + \rho c_{ij}^o) - \sum H_i I_i \right) \\
& + \lambda \left( L - \sum_j \sum_i L_{ij} \right)
\end{aligned}$$

Where  $P^*, \lambda, \omega_{ij}, R_i^*$  are Lagrangian multipliers. Normalize  $P^* = 1$ . The first order conditions are:

$$[L_{ij}] : R_i^* (h_{ij}^y + \sum_{s=1,2} N_{s,i} k q_{sij}^y) + \rho R_j^* (h_{ij}^o + \sum_{s=1,2} N_{s,j} k q_{sij}^o) + c_{ij}^y + \rho c_{ij}^o = z_i (1 + \gamma^p) - \frac{\omega_{ij}}{\theta L_{ij}} - \lambda \quad (33)$$

$$[c_{ij}^y] : \frac{\delta_c \omega_{ij}}{c_{ij}^y} = L_{ij} \quad [c_{ij}^o] : \frac{\delta_c \omega_{ij}}{c_{ij}^o} = L_{ij} \quad (34)$$

$$[h_{ij}^y] : \frac{\delta_h \omega_{ij}}{h_{ij}^y} = R_i^* L_{ij} \quad [h_{ij}^o] : \frac{\delta_h \omega_{ij}}{h_{ij}^o} = L_{ij} R_j^* \quad (35)$$

$$[q_{sij}^y] : \frac{\delta_b \alpha_s^y \omega_{ij}}{q_{sij}^y} = L_{ij} R_i^* k N_{si} \quad [q_{sij}^o] : \frac{\delta_b \alpha_s^o \omega_{ij}}{q_{sij}^o} = L_{ij} R_j^* k N_{sj} \quad (36)$$

$$[N_{si}] : \frac{\sigma}{\sigma-1} \delta_b \alpha_s^y \sum_j \omega_{ij} + \rho \frac{\sigma}{\sigma-1} \delta_b \alpha_s^o \sum_j \omega_{ji} - R_i^* \sum_j L_{ij} q_{1ij}^y k - R_i^* \rho \sum_j L_{ji} q_{1ji}^o k - R_i^* F_{1i} = 0 \quad (37)$$

$$[I_i] : R_i \frac{1}{1 + \epsilon_H} \bar{H}_i I_i^{-\frac{\epsilon_H}{1+\epsilon_H}} - H_i = 0 \quad (38)$$

Substituting 36 into 37, I get the optimality condition for the number of firms in non-tradeable sector  $s$ :

$$\frac{1}{\sigma-1} \left( \delta_b \alpha_s^y \sum_j \omega_{ij} + \rho \delta_b \alpha_s^o \sum_j \omega_{ji} \right) = R_i^* F_{si} N_{si} \quad (39)$$

Denote by  $x_{ij}$  the total cost of putting an individual on a location path  $ij$  in terms of the consumption of the final good and tightening of the housing constraints (either directly or

through consumption of non-tradeables):

$$x_{ij} = c_{ij}^y + \rho c_{ij}^o + R_i^*(h_{ij}^y + \sum_{s=1,2} N_{si} k q_{sij}^y) + \rho R_j^*(h_{ij}^o + \sum_{s=1,2} N_{sj} k q_{sij}^o)$$

From the FOCs the following holds the following holds:

$$\omega_{ij} = \frac{x_{ij} L_{ij}}{(1 + \rho)}$$

### D.3 Proof of Proposition 4

Denote  $x_i = (a_i^y)^{-\theta}$  and  $y_i = (a_i^o)^{-\beta\theta}$ . Then the system of equilibrium conditions transforms into:

$$\begin{aligned} x &= \frac{L}{U^\theta} \sum_j K_{ij} y_j^{-1} \\ y &= \frac{L}{U^\theta} \sum_j K_{ji} x_j^{-1} \end{aligned}$$

where  $K_{ij}$  are known positive values. The corresponding matrices of coefficients are:

$$B = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} \quad \Gamma = \begin{pmatrix} 0 & -1 \\ -1 & 0 \end{pmatrix}$$

Then matrix A can be found as:

$$A \equiv \Gamma B^{-1} = \begin{pmatrix} 0 & -1 \\ -1 & 0 \end{pmatrix}$$

taking the absolute value of matrix coefficients we get that:

$$A^p = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$$

The spectral radius of the matrix is equal to 1. Applying the results from [Allen et al. \(2015\)](#), I get that the solution of the system exists and is unique up to the scale. So is the solution for  $a_i^y, a_i^o$ .

## E Mobility Costs Estimation

### E.1 Distance between CZs

I use the data from the county distance database<sup>41</sup> that computes great-circle distances calculated using the Haversine formula based on internal points in the geographic area for all pairs of counties in the US. To compute the distances between the CZs, I map each 1990 county to a single 1990 CZ using the crosswalk in [Eckert et al. \(2020\)](#) based on the largest area of the intersection.<sup>42</sup> Then I compute a distance between CZs as an area weighted average distance between counties in two CZs.

### E.2 Mobility Data

For the main regression I use Census IPUMS data for the year 2000 that provides individual level data on the current location and location 5 years ago at the PUMA level. I aggregate all migration PUMAs to commuting zones and compute  $L_{ij}^5(a)$  - the number of individuals of age  $a$  who were in the CZ  $i$  five years ago and are currently in the CZ  $j$  using the crosswalk weights between migration PUMAs and CZs. As the crosswalks weights provide many to many mapping, for each PUMA to PUMA migration flows, I find all CZs corresponding to origin and destination PUMAs, and I allocate the weight of the observation to CZ flows according to the area intersection weights provided in [Autor & Dorn \(2013\)](#).

### E.3 Estimating mobility regression

In the data I observe  $L_{ij}^5(a)$ . I use five year mobility data for individuals of age  $a \in [63, 72]$ . I further assume that conditional on reallocation, the probability that it happens at age  $a$  is  $p_a$ :

$$p(a) = p\lambda^{(a-58)} \quad \frac{p(1 - \lambda^{15})}{1 - \lambda} = 1$$

That is probabilities decline with age at the rate  $\lambda$ , and the sum of probabilities between ages 60 and 75 should be equal to one.

Let  $\Pi_5$  be the probability that an individual is in the same location as 5 years ago. Then:

$$1 - \Pi_5(a) = (1 - \Pi)p_a^*$$

where  $p_a^* = p\lambda^{(a-65)}(1 + \lambda + \lambda^2 + \lambda^3 + \lambda^4)$  is the probability of reallocation within the last 5

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<sup>41</sup><https://www.nber.org/research/data/county-distance-database>

<sup>42</sup>because 1990 CZs were constructed as a collection of 1990 counties, a one to one mapping works well

years.

Given the assumptions made above, the probability that an individual of age  $a \in [63, 72]$  is in the same location as 5 years ago is:

$$\Pi_5(a) = \Pi(a) + (1 - \Pi(a))(1 - p_a^*)$$

$$\Pi(a) = \frac{1}{p_a^*}(\Pi_5 - (1 - p_a^*))$$

Given the assumptions made in the previous section:

$$\frac{L_{ij}^5(a)}{L} = \pi_{ij} p_a^*$$

$$\sum_{a=63}^{a=72} \frac{L_{ij}^5(a)}{L} = \pi_{ij} \sum_a p_a^*$$

Therefore, the share of individuals who moved from  $i$  to  $j$  within a 5 year window corresponds to the share of individuals who move from  $i$  to  $j$  up to the scale. As the scale parameter will be absorbed in the fixed effects, I can use  $\sum_{a=63}^{a=72} L_{ij}^5(a)$  as a proxy for  $L_{ij}$  in the main regression.

## F MSA calibration

Due to the data availability issues, historical comparison between 1960 and 2010 is available only at the MSA level. This section provides additional details on the mapping of the model to the MSA data for the years 1960 and 2010. I select 169 MSAs available in the Census data for both time periods.<sup>43</sup> Using the Census data I construct the vectors of wages, rents, young and old location choices  $\{W_{i,t}, R_{i,t}, L_{i,t}^y, L_{i,t}^o\}$  corresponding to 169 US MSAs for years  $t = 1960, 2010$ .<sup>44</sup> I keep all the structural parameters fixed at their calibrated values described in section 5.2, except for the relative length of the old period  $\rho$  and the fixed mobility cost  $\kappa$ . I recalibrate  $\rho_t$  for each year  $t = 1960, 2010$  so that to match the ratio of the sizes of the older and younger age groups.

I take mobility costs for year 2010 to be equal to the calibrated mobility costs for the full model (see section 5.3), where the quantification was based on the 5 year window mobility data for the year 2010. I further calibrate the mobility costs for 1960 to match the evidence on an increase in the older population mobility during 1960-2010 period. Due to the data

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<sup>43</sup>169 MSAs available in both time periods cover 58 percent of the population in 1960 and 67 percent of the population in 2010

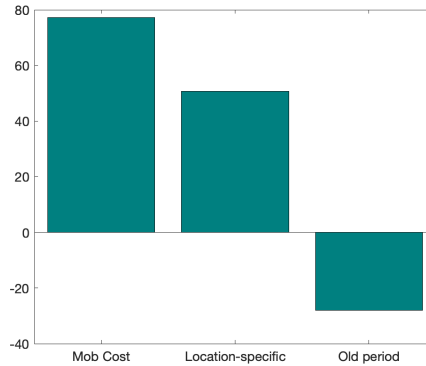
<sup>44</sup>Construction of the samples  $\{W_{i,t}, R_{i,t}, L_{i,t}^y, L_{i,t}^o\}$  follows the same steps as in the main calibration, see section A

limitations, I can only compare the individual level mobility data across U.S. states within a 5 year window. I compute that mobility around retirement age increased by around 21% over 1960-2010.<sup>45</sup> I further calibrate the fixed component of mobility costs for retirement model in 1960 together with the amenities for young and old  $\{a_{60}^y, a_{60}^o\}$  so that the share of older individuals who reallocate is 22 percent lower than in 2010.<sup>46</sup> The calibration procedure follows the same steps as in the main text of the paper. This allows me to compute that a model implied decline in mobility costs is equal to 36 percent. The following steps are the same as in the main calibration, except for the different vectors of the data.

## F.1 Decomposing changes in sorting, 1960-2010

The correlation between the MSA's old-to-young ratios and MSA's productivity changed from 0.01 in 1960 to  $-0.27$  in 2010. To determine the relative contribution of mobility costs to this change, I apply Shapley decomposition (see [Shorrocks \(2013\)](#) and [Allen & Arkolakis \(2014\)](#)). The details are the following. The model was calibrated to fully match the data for 1960 and 2010 periods. Starting from the calibration in 1960 and adding factors one by one, I compute the contribution of each factor to the total change. Then I consider the average contribution for all possible permutations of factors. The decomposition results are presented on figure F7.

Figure F7: Aggregate effects of the policy that subsidises the reallocation of old to smaller cities



The figure decomposes the changes in the correlation between MSA's old-to-young ratios and MSA's productivity from 0.01 in 1960 to  $-0.27$  in 2010. The location-specific factors include the set  $\{A_i^y, A_i^o, Z_i\}$ . The relative contribution of the factors are computed using a Shapley decomposition (see [Shorrocks \(2013\)](#))

<sup>45</sup>I compute that 3.97% of individuals older than 55 moved between U.S. states in 1960, while the corresponding number for 2010 is 4.83%. In contrast, the rise in the mobility of the younger age group (25-55) was much lower and equal to 4.4%.

<sup>46</sup>Here I implicitly assume that an increase in mobility across MSAs over the same time period is the same as across MSAs

## G Additional tables

TABLE G2  
DETERMINANTS OF MODEL IMPLIED  
AMENITIES

Dependent Variable	(1) $a_i^o/a_i^y$	(2) $a_i^o/a_i^y$
Golf and Country clubs	0.34*** (0.06)	1*** (0.12)
Hospitals	0.34*** (0.06)	1.14*** (0.31)
Personal care	0.36*** (0.06)	0.92*** (0.16)
Nursing homes	0.33*** (0.06)	0.48*** (0.17)
% Water area	0.08*** (0.023)	0.39*** (0.07)
January temperature	0.16*** (0.06)	0.05 (0.08)
Food & drinking	-0.2 (0.18)	-1.9*** (0.53)
Movie theatres	-0.4*** (0.05)	-0.53*** (0.13)
Childcare	-0.17*** (0.06)	0.12 (0.13)
Schools	-0.05 (0.03)	-0.2* (0.11)
Museums and Parks	-0.07* (0.04)	0.32*** (0.11)
Clothing	-0.06 (0.06)	0.58** (0.15)
Arts	-0.008* (0.05)	-0.34*** (0.11)
July temperature	0.16 (0.09)	0.23*** (0.08)
Topography	-0.0016 (0.02)	0.14*** (0.06)
Observations	722	722
R-squared	0.36	0.67
Weighted by CZ population		✓

$p$ -value \*\*\* $p \leq 0.01$ , \*\* $p \leq 0.05$ , \* $p \leq 0.1$ . Robust standard errors are given in parenthesis. All variables are in logs are in logs. Includes 722 mainland commuting zones.

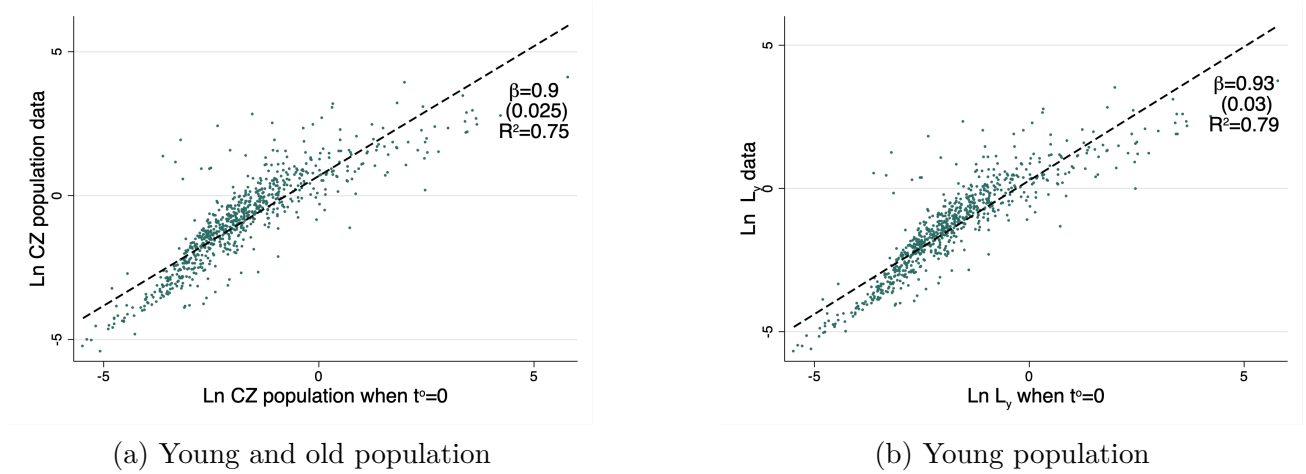
TABLE G3  
LOCAL EFFECTS OF THE PLACE-BASED  
POLICIES TARGETED AT RETIREES

$L$	$L^y$	$L^o$	$N^y$	$N^o$	$a^y$	$a^o$	$R$
5.36	-3.4	19.43	3.01	10.6	0.3	0.4	3.8

The table shows the percentage response of the corresponding local variables to a 10% subsidy for retirees for moving into a city.  $N^y$  denotes the number of firms in the non-tradeable category 1 that is valued more by young.  $N^o$  denotes the number of firms in the non-tradeable category 2 that is valued more by old.

## H Additional figures

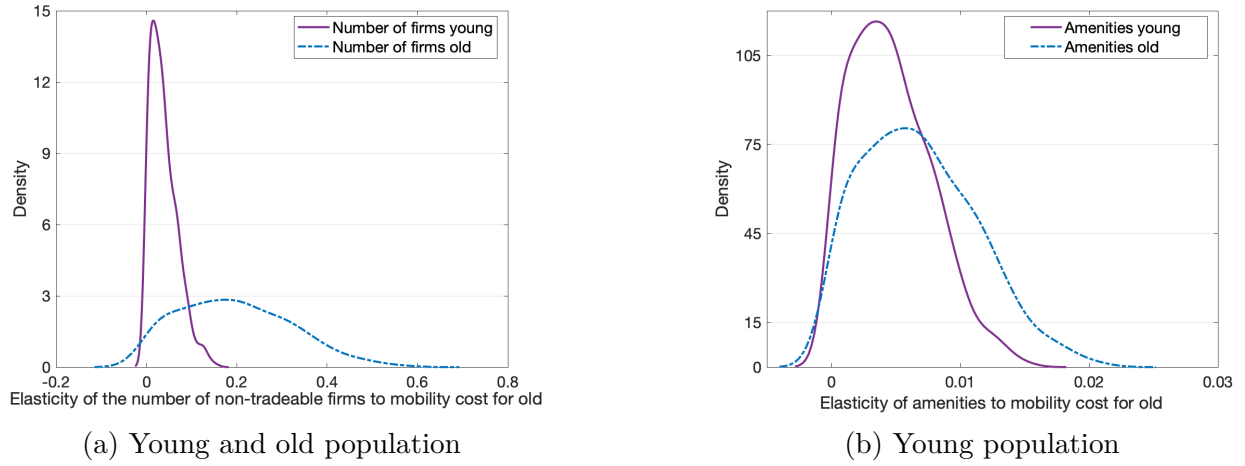
Figure H8: Fit of the model with no life cycle



The left graph shows on the vertical axes the log of the CZ population and the horizontal axes the log of the predicted CZ population in a model with no life cycle ( $t_o = 0$ ) and ( $t_y = T$ ). The right graph shows on the vertical axes the log of the number of younger rage group (age 25-60) and on the horizontal axes the log of the predicted number of younger residents in the model with no life cycle.  $\beta$  is the resulting regression coefficient. Robust standard errors are in parenthesis

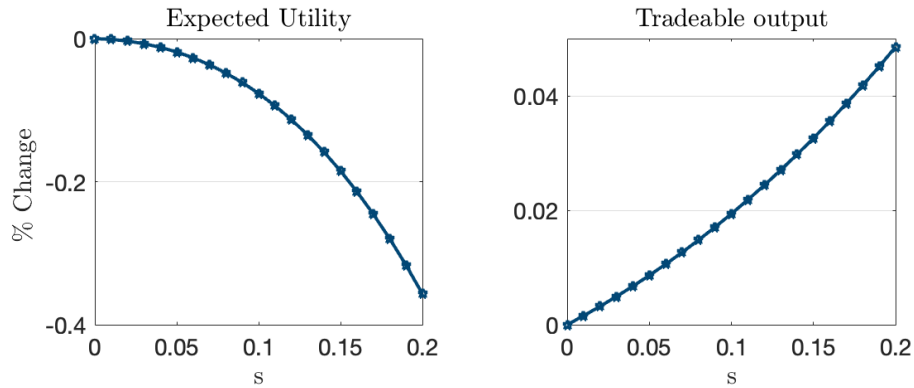


Figure H9: Elasticities of amenities and number of non-tradeable firms to the mobility of old



The left graph shows the kernel density of the distribution of the number of firms in two non-tradeable sectors (sector 1 preferred more by young and sector 2 preferred more by old in response to a decline in the mobility costs of retirees to move to a CZ. The right graph is shows same density for the amenities of young and old

Figure H10: Aggregate effects of the policy that subsidises the reallocation of old to smaller cities



Aggregate effects of the policy that introduces of a subsidy  $s$  measured as a percentage of individuals' average wages given to any old individual moving to a treated city. The policy is finances via a lump sum tax paid by all workers in the economy. Treated cities are the cities in 25th quantile by productivity