

11. By definition of ternary tree, it is easy to see that maximum number of nodes at height h is 3^h .

proof: Base case, when tree is empty, # nodes = 0

$$h = -1. \quad \frac{3^{h+1} - 1}{2} = \frac{1 - 1}{2} = 0$$

$\frac{3^{h+1} - 1}{2}$ is max. # of nodes in ternary tree with height = -1.

Induction: Suppose, at height k , the max. # of nodes

$$\text{is } \frac{3^{k+1} - 1}{2}, \quad k \geq -1.$$

Let $h = k+1$, as we already know, # of nodes at $h = k+1$ is 3^{k+1} .

\therefore # of nodes in tree with $h = k+1$ is

$$\begin{aligned} \frac{3^{k+1} - 1}{2} + 3^{k+1} &= \frac{3^{k+1} - 1 + 2 \cdot 3^{k+1}}{2} = \frac{3^{k+2} - 1}{2} \\ &= \frac{3^{(k+1)+1} - 1}{2} \quad \text{for } k \geq -1 \end{aligned}$$

Therefore the statement is true.