

8. Invariant  $\text{pow} = a^i$ .

Base case. At the start of 1st iteration,  $i=1$   $\text{pow}=1$ .

in the inner loop,  $\text{pow} = \text{pow} * a = 1 * a = a = a^1$

invariant hold in the Base case.

Induction hypothesis: At the start of  $k+1$  of the loop,  $i=k+1$

Assuming that  $\text{pow} = a^k$  is true for  $k=i$ .

In the inner loop.

$$\text{pow} = \text{pow} * a = a^k * a = a^{k+1}$$

therefore the invariant holds at the end of  $k+1$  of the loop.

And the invariant holds at beginning of  $k+2$  loop.

Loop termination: the loop ends after  $n$  iterations.

We were about to enter  $i=n+1$  iterations.

Therefore, by invariant, when the loops,  $\text{pow} = a^i = a^n$ .