

Assignment 10 – Simplex and Backtracking

1. N-Queens Problem:

Code:

```
print ("Enter the number of queens")
N = int(input())

#chessboard
#NxN matrix with all elements 0
board = [[0]*N for _ in range(N)]

def is_attack(i, j):
    #checking if there is a queen in row or column
    for k in range(0,N):
        if board[i][k]==1 or board[k][j]==1:
            return True
    #checking diagonals
    for k in range(0,N):
        for l in range(0,N):
            if (k+l==i+j) or (k-l==i-j):
                if board[k][l]==1:
                    return True
    return False

def N_queen(n):
    #if n is 0, solution found
    if n==0:
        return True
    for i in range(0,N):
        for j in range(0,N):
            """checking if we can place a queen here or not
            queen will not be placed if the place is being attacked
            or already occupied"""
            if (not(is_attack(i,j))) and (board[i][j]!=1):
                board[i][j] = 1
                #recursion
                #wether we can put the next queen with this arrangment or not
                if N_queen(n-1)==True:
                    return True
                board[i][j] = 0

    return False

N_queen(N)
for i in board:
    print (i)
```

Output:

```
~/DAA-Exercise9$ python3 nqueens.py
Enter the number of queens:
8
[1, 0, 0, 0, 0, 0, 0, 0]
[0, 0, 0, 0, 1, 0, 0, 0]
[0, 0, 0, 0, 0, 0, 0, 1]
[0, 0, 0, 0, 0, 1, 0, 0]
[0, 0, 1, 0, 0, 0, 0, 0]
[0, 0, 0, 0, 0, 0, 1, 0]
[0, 1, 0, 0, 0, 0, 0, 0]
[0, 0, 0, 1, 0, 0, 0, 0]
~/DAA-Exercise9$
```

2. Simplex Algorithm:

Code:

```
import numpy as np
from fractions import Fraction # so that numbers are not displayed in decimal.

print("\n****Simplex Algorithm ****\n\n")

# inputs

# A will contain the coefficients of the constraints
A = np.array([[1, 1, 1, 0], [2, 1, 0, 1]])
# b will contain the amount of resources
b = np.array([12, 16])
# c will contain coefficients of objective function Z
c = np.array([40, 30, 0, 0])

# B will contain the basic variables that make identity matrix
cb = np.array(c[3])
B = np.array([[3], [2]])
# cb contains their corresponding coefficients in Z
cb = np.vstack((cb, c[2]))
xb = np.transpose([b])
# combine matrices B and cb
table = np.hstack((B, cb))
table = np.hstack((table, xb))
# combine matrices B, cb and xb
# finally combine matrix A to form the complete simplex table
table = np.hstack((table, A))
# change the type of table to float
table = np.array(table, dtype='float')
# inputs end

# if min problem, make this var 1
MIN = 0

print("Table at itr = 0")
print("B \tCB \tXB \ty1 \ty2 \ty3 \ty4")
for row in table:
    for el in row:
        # limit the denominator under 100
        print(Fraction(str(el)).limit_denominator(100), end='\t')
    print()
print()
print("Simplex Working....")

# when optimality reached it will be made 1
```

```
reached = 0
itr = 1
unbounded = 0
alternate = 0

while reached == 0:

    print("Iteration: ", end = ' ')
    print(itr)
    print("B \tCB \tXB \ty1 \ty2 \ty3 \ty4")
    for row in table:
        for el in row:
            print(Fraction(str(el)).limit_denominator(100), end = '\t')
        print()

    # calculate Relative profits-> cj - zj for non-basics
    i = 0
    rel_prof = []
    while i < len(A[0]):
        rel_prof.append(c[i] - np.sum(table[:, 1]*table[:, 3 + i]))
        i = i + 1

    print("rel profit: ", end = " ")
    for profit in rel_prof:
        print(Fraction(str(profit)).limit_denominator(100), end = ", ")
    print()
    i = 0

    b_var = table[:, 0]
    # checking for alternate solution
    while i < len(A[0]):
        j = 0
        present = 0
        while j < len(b_var):
            if int(b_var[j]) == i:
                present = 1
                break;
            j += 1
        if present == 0:
            if rel_prof[i] == 0:
                alternate = 1
                print("Case of Alternate found")
                # print(i, end = " ")
            i += 1
        print()
        flag = 0
        for profit in rel_prof:
            if profit > 0:
                flag = 1
```

```
        break
    # if all relative profits <= 0
    if flag == 0:
        print("All profits are <= 0, optimality reached")
        reached = 1
        break

    # kth var will enter the basis
    k = rel_prof.index(max(rel_prof))
    min = 99999
    i = 0;
    r = -1
    # min ratio test (only positive values)
    while i < len(table):
        if (table[:, 2][i] > 0 and table[:, 3 + k][i] > 0):
            val = table[:, 2][i] / table[:, 3 + k][i]
            if val < min:
                min = val
                r = i    # leaving variable
            i += 1

    # if no min ratio test was performed
    if r == -1:
        unbounded = 1
        print("Case of Unbounded")
        break

    print("pivot element index:", end = ' ')
    print(np.array([r, 3 + k]))

    pivot = table[r][3 + k]
    print("pivot element: ", end = " ")
    print(Fraction(pivot).limit_denominator(100))

    # perform row operations
    # divide the pivot row with the pivot element
    table[r, 2:len(table[0])] = table[
        r, 2:len(table[0])] / pivot

    # do row operation on other rows
    i = 0
    while i < len(table):
        if i != r:
            table[i, 2:len(table[0])] = table[i, 2:len(table[0])] - table[i][3 + k] * table[r,
2:len(table[0])]
            i += 1

    # assign the new basic variable
```

```
        table[r][0] = k
        table[r][1] = c[k]

        print()
        print()
        itr+= 1

print()

print("*****")
if unbounded == 1:
    print("UNBOUNDED LPP")
    exit()
if alternate == 1:
    print("ALTERNATE Solution")

print("optimal table:")
print("B \tCB \tRS \ty1 \ty2 \ty3 \ty4")
for row in table:
    for el in row:
        print(Fraction(str(el)).limit_denominator(100), end='\t')
    print()
print()
print("value of Z at optimality: ", end=" ")

basis = []
i = 0
sum = 0
while i<len(table):
    sum += c[int(table[i][0])]*table[i][2]
    temp = "x"+str(int(table[i][0])+1)
    basis.append(temp)
    i+= 1
# if MIN problem make z negative
if MIN == 1:
    print(-Fraction(str(sum)).limit_denominator(100))
else:
    print(Fraction(str(sum)).limit_denominator(100))
print("Final Basis: ", end=" ")
print(basis)

print("Simplex Finished...")
print()
```

Output:

```
~/DAA-Exercise9$ python3 simplex.py

****Simplex Algorithm ****

Table at itr = 0
B   CB  XB  y1  y2  y3  y4
3   0   12  1   1   1   0
2   0   16  2   1   0   1

Simplex Working....
Iteration:  1
B   CB  XB  y1  y2  y3  y4
3   0   12  1   1   1   0
2   0   16  2   1   0   1
rel profit:  40, 30, 0, 0,

pivot element index: [1 2]
Iteration:  2
B   CB  XB  y1  y2  y3  y4
3   0   4   0   1/2  1  -1/2
0  40   8   1   1/2  0   1/2
rel profit:  0, 10, 0, -20,
Case of Alternate found

pivot element index: [0 4]
pivot element:  1/2

Iteration:  3
B   CB  XB  y1  y2  y3  y4
1  30   8   0   1   2  -1
0  40   4   1   0  -1   1

*****
ALTERNATE Solution
optimal table:
B   CB  RS  y1  y2  y3  y4
1  30   8   0   1   2  -1
0  40   4   1   0  -1   1

value of Z at optimality:  400
Final Basis:  ['x2', 'x1']
Simplex Finished...

~/DAA-Exercise9$
```

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